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High-Fidelity Meshing and Stochastic Simulation for Enhanced Surface Stress Concentration Prediction / Angelini, Davide; Cestino, Enrico; Bianco, Sergio; Mallamo, Fabio. - In: IOP CONFERENCE SERIES: MATERIALS SCIENCE AND ENGINEERING. - ISSN 1757-8981. - 1338:(2025). (45th Risoe International Symposium on Materials Science Roskilde (DK)) [10.1088/1757-899x/1338/1/012011].

Availability:

This version is available at: 11583/3004543 since: 2025-10-28T13:47:11Z

Publisher:

IOP Publishing

Published

DOI:10.1088/1757-899x/1338/1/012011

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To cite this article: Davide Angelini *et al* 2025 *IOP Conf. Ser.: Mater. Sci. Eng.* **1338** 012011

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High-Fidelity Meshing and Stochastic Simulation for Enhanced Surface Stress Concentration Prediction

Davide Angelini¹, Enrico Cestino¹, Sergio Bianco² and Fabio Mallamo²

¹DIMEAS - Department of Mechanical and Aerospace Engineering, Politecnico di Torino, Corso Duca degli Abruzzi 24, Turin, 10129, TO, Italy

²FEV Italia s.r.l., Environment Park – Parco Scientifico Tecnologico per l'Ambiente, Via Livorno, 60, Turin, 10144, TO, Italy

Contact address: davide.angelini@polito.it

Abstract. The accurate prediction of the Stress Concentration Factor (K_t) induced by surface topography is critical for the fatigue life assessment of engineering components. Existing models, such as the semi-empirical model by Arola-Ramulu, offer methods to estimate K_t , but their accuracy varies with material and roughness characteristics. This study presents a systematic evaluation of these established models using a robust stochastic simulation framework. A computational workflow is developed in Python, integrating a surrogate-based optimization algorithm with the *Gmsh* library to ensure the generation of high-fidelity Finite Element meshes for 2D dog-bone specimens. A large-scale numerical campaign is conducted on specimens made of aluminum alloy and steel, featuring statistically generated random roughness profiles. The roughness parameters for each specimen were catalogued, and the corresponding K_t is determined via linear elastic Finite Element Analysis (FEA) using Altair OptiStruct. The results from the FEA were directly compared against the predictions from Arola's rule and Zhang's Bayesian model. The analysis confirms that while Arola's rule provides reasonable estimates for low levels of roughness, it significantly underestimates K_t for more severe surface topographies. In contrast, Zhang's model demonstrated superior predictive accuracy across a wider range of roughness conditions for both materials investigated. The findings highlight that a stochastic FEA approach, underpinned by high-fidelity meshing, is an effective method for validating and comparing surface stress concentration models. The results indicate that Zhang's model is a more reliable choice for general engineering applications. Future work should extend this framework to include material plasticity, 3D surface topographies, and validation against experimentally measured surface profiles.

1 Introduction

The fatigue life of a mechanical component is fundamentally influenced by its material properties, geometric configuration, and the applied loading path. A key parameter in fatigue analysis is the theoretical Stress Concentration Factor, denoted as K_t . This factor quantifies the localized increase in stress due to geometric discontinuities, such as notches or holes, relative to the nominal stress state [1]:

$$K_t = \frac{\sigma_{\text{peak}}}{\sigma_{\text{nominal}}} \quad (1)$$

where σ_{peak} is the maximum local stress at the discontinuity and σ_{nominal} is the stress in the region unaffected by the discontinuity. The magnitude of K_t serves as a critical indicator of fatigue performance, as higher values correspond to an increased probability of crack initiation.

Numerous researchers have contributed to the compilation and calculation of K_t values for various geometries and loading conditions. Peterson's work [2] remains a comprehensive resource, providing a vast collection of stress concentration factors for metallic structures derived from both analytical and numerical methods. A classic example is the case of an infinite plate with a central circular hole under



uniaxial tension, for which the analytical solution yields $K_t = 3$. This result is independently derived by Kirsch [3] using polar coordinates and by Muskhelishvili [4] using complex variable methods, as detailed by Timoshenko [5].

Beyond macroscopic geometric features, surface roughness also introduces stress concentrations that can significantly affect fatigue life. Neuber is the first to propose a model to quantify this effect [6]:

$$K_t = 1 + n \sqrt{\lambda \frac{R_z}{\rho}} \quad (2)$$

where n is a factor dependent on the loading condition ($n = 1$ for shear, $n = 2$ for tension), ρ is the notch root radius, and λ relates the spacing to the height of the surface irregularities. Despite its age, Neuber's rule is still applied in contemporary research [7].

However, Neuber's formulation has been criticized for its applicability to certain materials, such as fiber reinforced plastics. Arola and Ramulu proposed an alternative formulation specifically for such materials [6]:

$$K_t = 1 + n \left(\frac{R_a}{\bar{\rho}} \right) \left(\frac{R_y}{R_z} \right) \quad (3)$$

This model incorporates standard surface roughness parameters, including the average roughness (R_a), peak-to-valley roughness (R_y), and ten-point mean roughness (R_z), as defined in [8]. The expression of 2D roughness parameters are the following:

$$\begin{aligned} R_a &= \frac{1}{L} \int_0^L |z| dx \\ R_y &= |z_{max} - z_{min}| \\ R_z &= \frac{1}{5} \left[\sum_{i=1}^5 (z_i)_{max} + \sum_{j=1}^5 |(z_j)_{min}| \right] \end{aligned} \quad (4)$$

where z indicates the height of the rough profile, L the evaluation length.

Subsequently, Arola extended the application of this model to metals, specifically AISI 4130 CR steel [8].

The theoretical stress concentration factor, K_t , assumes perfectly linear elastic material behavior. In reality, local plastic deformation at the notch root can mitigate the stress concentration. To account for this, the concept of the effective stress concentration factor, K_{eff} (also known as the fatigue notch factor), is introduced. This factor is related to K_t through the notch sensitivity, q , a material and geometry-dependent parameter determined experimentally [2] [9]:

$$K_{eff} = 1 + q(K_t - 1) \quad (5)$$

The utility of this relationship has been demonstrated in various studies, including by Arola for AISI 4130 CR steel [8] and by Lee et al. [10] for other materials.

Arola's formulation for K_t has been adopted in subsequent research. For instance, Suraratchai et al. [11] integrated it into the Paris' law to model fatigue crack growth, thereby linking the stress intensity factor to the surface topography. Nevertheless, the general applicability of Arola's rule is limited by the relatively small number of materials for which it has been validated.

More recently, Zhang [7] conducted a critical assessment of Arola's rule using Finite Element Analysis (FEA). By virtually generating 41 specimens with varying surface roughness, Zhang found that Neuber's equation (2) provided a better prediction of the FEM-computed K_t than Arola's original formula. Furthermore, Zhang proposed a new relationship, derived using a Bayesian learning approach, which showed a better fit to the FEM results:

$$K_t = 1.915 \left(\frac{R_a}{R_y} \right)^{-0.223} \left(\frac{R_a}{R_z} \right)^{0.122} \left(\frac{R_a}{\rho} \right)^{0.549} \quad (6)$$

The aforementioned models are primarily applicable to two-dimensional profiles. For three-dimensional surfaces, other approaches have been developed. For example, Perz et al. [12] present an analytical model based on a Fourier series decomposition of the roughness profile under plane stress conditions, with

validation against FEM simulations. Persson [13] approached the problem by deriving the probability distribution of surface stress for randomly rough surfaces, leveraging the self-affine fractal nature of most surfaces.

This paper aims to evaluate the validity of common stress concentration factor formulas through a stochastic Finite Element Analysis. To this end, a series of 2D samples with statistically defined surface roughness generated. A robust meshing strategy, employing a surrogate-based optimization algorithm [14, 15] to control the Gmsh meshing library [16, 17, 18, 19], is used to ensure high-quality meshes that meet rigorous quality criteria. Subsequently, FEA is performed using Altair OptiStruct to compute the stress concentration factors. The numerical results are compared with predictions from the literature for various materials to assess the accuracy of existing models.

Table 1: Notation used in the present work

Acronym	Meaning
K_t	Stress Concentration Factor
ρ	Local radius of curvature at the bottom of a valley
$\bar{\rho}$	Average radius of curvature at the bottom of prominent valleys of a specimen
R_a	2D average roughness
R_y	Peak-to-valley 2D roughness
R_z	10-point 2D roughness

2 Methodology

This section details the computational framework developed for the analysis, encompassing the generation of specimen geometries with realistic surface roughness, the creation of high-quality finite element meshes, and the execution of the numerical simulations to determine stress concentration factors.

2.1 Specimen and Surface Roughness Generation

A 2D dog-bone specimen is the baseline geometry of this analysis (Figure 1a). To simulate realistic surface conditions, a stochastic roughness profile is introduced onto one of the gauge section's edges. This profile is generated using a custom Python version of the 'rsgene1D.m' algorithm [20], which creates a one-dimensional random signal similar to a real roughness profile. The algorithm is specifically designed to produce a profile with a Gaussian height distribution and an exponential correlation function. The key statistical inputs controlling the generation process are:

- the Root Mean Square (RMS) height, that is the standard deviation of the surface heights, randomly set between 0 and 0.2 mm for each specimen.
- correlation length, that is the distance over which surface heights are correlated; this is fixed at 4 mm.

For each specimen, five concatenated rough segments were generated, creating a total rough edge length of 20 mm. The resulting geometry, with a detailed view of the rough profile, is illustrated in Figures 1b and 1c.

Following the generation of the rough surface, key roughness parameters (R_a , R_y , R_z) are calculated from the coordinates of the surface points according to the definitions in (4). A significant challenge in this process is the determination of the notch root radius, ρ , for the valleys in the roughness profile. Following the methodology established by Arola [6, 8] and also adopted by Lee et al. [10], the valley radius is determined by fitting a circle to at least three points within the lowest part of each valley, aiming to maximize the contact area. This graphical interpolation procedure is illustrated in Figure 2.

2.2 High-Fidelity Mesh Generation

The accuracy of Finite Element Analysis (FEA) is intrinsically dependent on the quality of the computational mesh. In this work, a robust meshing procedure is implemented to ensure high-fidelity discretization of the 2D geometries. The open-source software Gmsh [16, 17] is employed via its Python API.

Recognizing that default meshing parameters rarely yield an optimal grid, a surrogate-based optimization algorithm [14, 15] is utilized to systematically determine the best meshing parameters. The

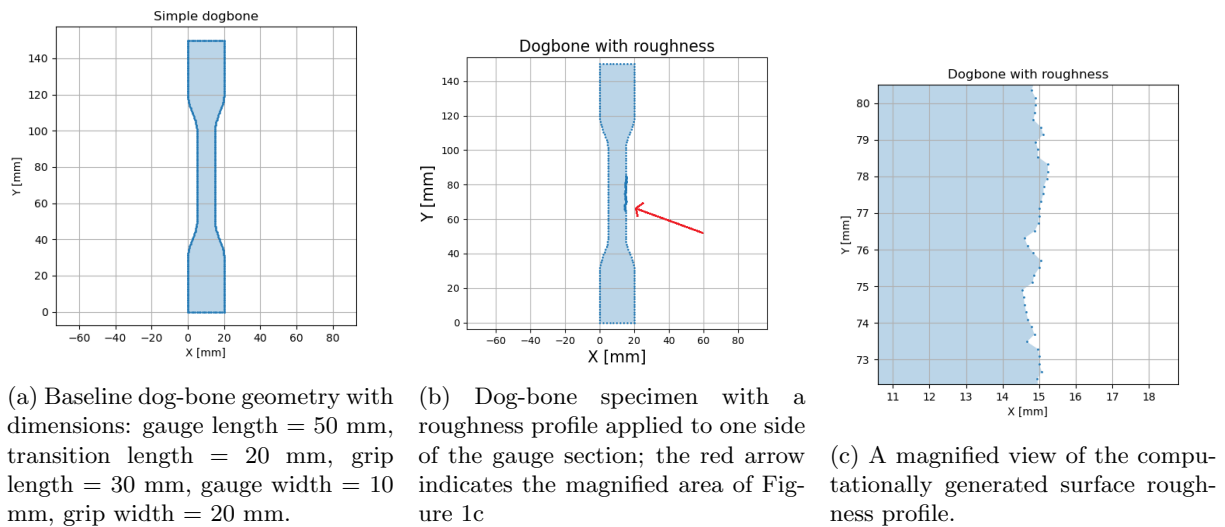
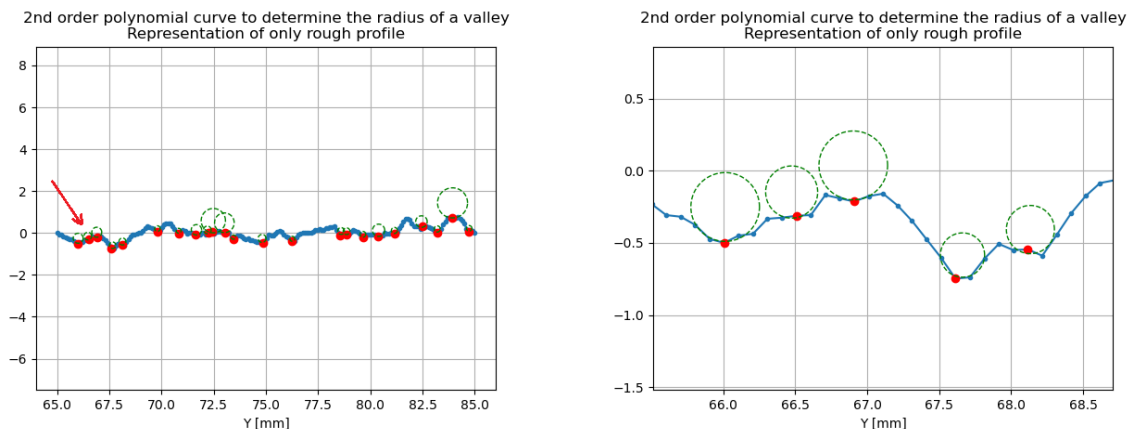


Figure 1: Geometries utilized in the Finite Element Analysis.

Figure 2: Illustration of the procedure for calculating the notch root radius (ρ) by fitting circles to the most critical valleys in the rough profile.

optimization workflow, schematically shown in Figure 3, is driven by a multi-objective function designed to maximize mesh quality according to the criteria detailed in Table [2] from [21]. The objective function prioritizes quadrilateral (QUAD) elements over triangular (TRIA) elements to mitigate potential numerical inaccuracies, penalizing the presence of TRIA elements and enforcing stringent quality checks. Any mesh failing to meet the prescribed quality thresholds for a given specimen is automatically discarded. An example of a final mesh with applied boundary conditions is shown in Figure 4. The meshing algorithm refines the boundary by introducing nodes at a higher density than the points defining the initial geometry, ensuring a high-resolution discretization of the rough profile.

2.3 Solver

The numerical simulations were performed using the commercial solver *Altair OptiStruct 2024.1*. An input file (‘.fem’) containing the mesh (CTRIA3 and CQUAD4 elements), material properties (thickness of elements 1mm), loads, and boundary conditions is generated programmatically and executed via a batch script.

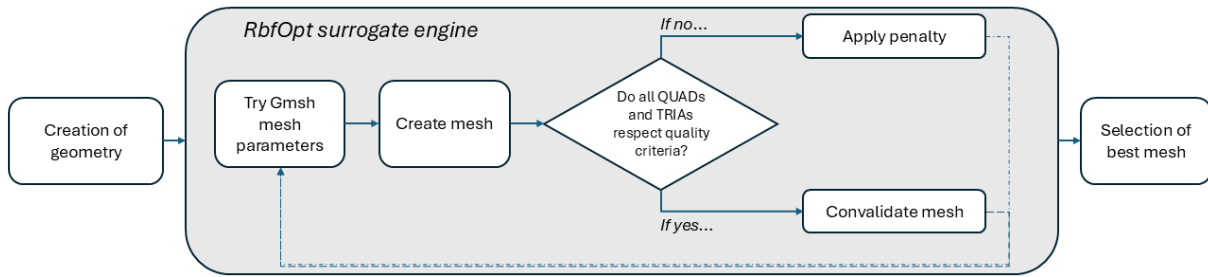


Figure 3: Schematic of the surrogate-based optimization algorithm used to find the optimal Gmsh parameters for generating a high-quality mesh.

Table 2: Quality Criteria for Triangular (TRIA) and Quadrilateral (QUAD) Elements [21].

Quality Metric	Description	Acceptance Limit	Ideal Value
Triangular (TRIA) Elements			
Minimum Angle	Smallest internal angle.	$> 20^\circ$	60°
Maximum Angle	Largest internal angle.	$< 120^\circ$	60°
Aspect Ratio	Ratio of the longest edge to the shortest altitude.	< 5	1
Jacobian	Measures deviation from an equilateral triangle.	> 0.6	1
Quadrilateral (QUAD) Elements			
Minimum Angle	Smallest internal angle.	$> 45^\circ$	90°
Maximum Angle	Largest internal angle.	$< 135^\circ$	90°
Aspect Ratio	Ratio of the longest edge to the shortest edge.	< 5	1
Jacobian	Measures distortion from a perfect square.	> 0.6	1

The analysis is configured as a 2D linear elastic simulation under plane stress conditions, assuming isotropic material behavior. As shown in Figure 4a, nodes on the bottom edge were fully constrained, while a uniform tensile load, resulting in a total force of 100 N in the vertical direction, is applied to the nodes on the top edge. The material properties for the aluminum alloy and steel used in this study are listed in Table [3].

Table 3: Isotropic linear elastic material properties used in the FEA.

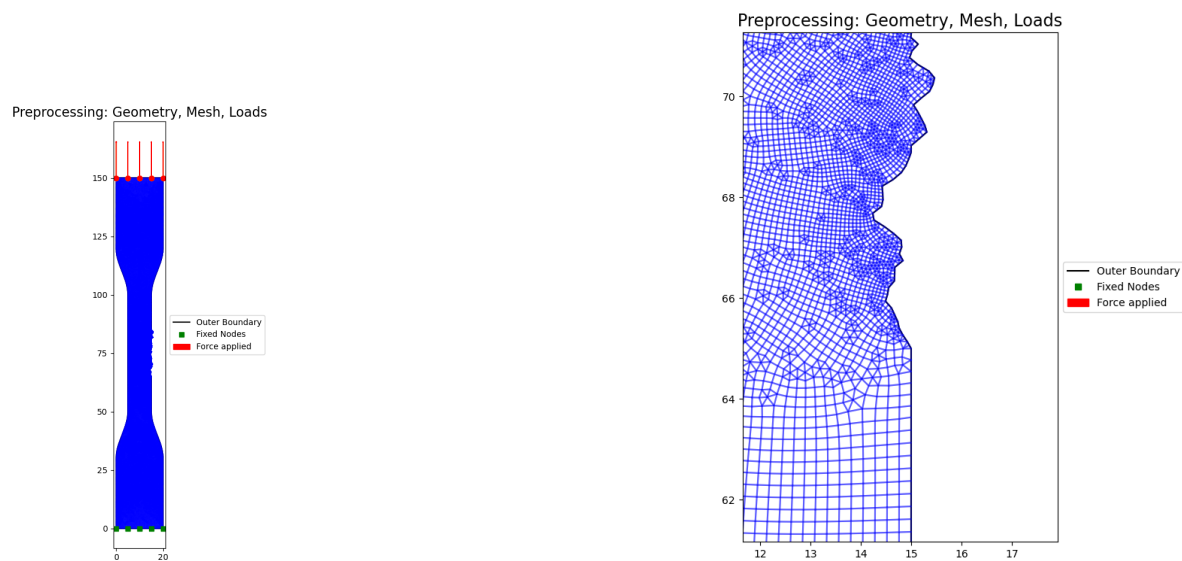
Material	Young's Modulus, E (MPa)	Poisson's Ratio, ν	Source
Aluminum Alloy	72,000	0.33	[7]
AISI 4130 CR Steel	205,000	0.29	[22]

After the simulation run, the maximum Von Mises stress along the rough surface is extracted. The theoretical stress concentration factor, K_t , is then calculated by dividing this maximum stress by the nominal stress. The nominal stress is computed as the applied force (100 N) divided by the cross-sectional area of the gauge section ($10 \text{ mm} \times 1 \text{ mm} = 10 \text{ mm}^2$), resulting in a nominal stress of 10 MPa. This procedure is consistent with the method used by Zhang [7] for calculating K_t from FEM results.

Figure 5 presents a typical Von Mises stress contour plot from the analysis.

3 Results

This section presents the results of the Finite Element Analysis, beginning with a mesh convergence study to establish the numerical stability of the proposed methodology. Subsequently, the stress concentration



(a) Overview of the mesh and applied boundary conditions. (b) A magnified view of the fine mesh along the rough boundary.

Figure 4: Example of a quality-approved mesh used for the FEA.

factors (K_t) computed from the simulations are compared against established analytical and empirical models from the literature for both aluminum and steel specimens.

3.1 Mesh Convergence Study

A mesh sensitivity analysis is conducted to ensure that the numerical results are independent of the mesh discretization. 20 meshes are generated for the same geometry. Table [4] reports number of nodes in the rough border, average, maximum and minimum mesh size per each sample, where the size of one elements is estimated as the square root of the area. Figure 6 shows that the Stress Concentration Factor is constant and tends to an asymptotic value as the number of nodes on rough border increases, confirming the reliability of the numerical results obtained with the surrogate Gmsh procedure.

3.2 Analysis of Aluminum Specimens

A set of 50 aluminum specimens with statistically varying surface roughness profiles is generated and analyzed. The FEM-computed K_t values were then compared with the predictions from Arola's model [6] and Zhang's model [7], as illustrated in Figure 7.

The comparison reveals that for low stress concentration factors (approximately $K_t < 1.1$), Arola's rule shows good agreement with the FEM results. However, as the severity of the surface roughness increases, leading to higher K_t values, Arola's model significantly underestimates the stress concentration observed in the simulations. This finding is consistent with the observations reported by Zhang [7]. In contrast, the Bayesian model proposed by Zhang, given by equation (6), demonstrates a much better correlation with the FEM results across the entire range of tested geometries. Nevertheless, a divergence in the trend is noticeable for higher K_t values, which may be attributable to differences in the numerical methodologies or the specific roughness characteristics generated.

3.3 Analysis of Steel Specimens

A similar analysis is performed for steel specimens. The computed K_t values were compared against Arola's original rule and Zhang's rule. The results are presented in Figure 8.

For low K_t values, a reasonable agreement is observed among the FEM results and the predictions from all three models. This aligns with the findings of Arola [8], where the model is validated in this low- K_t regime. However, for more pronounced surface features corresponding to higher stress concentrations, both Arola's rule fails to accurately predict the FEM data. Notably, Zhang's rule, despite being originally developed for an aluminum alloy, provides a better prediction for the steel specimens over a wider range

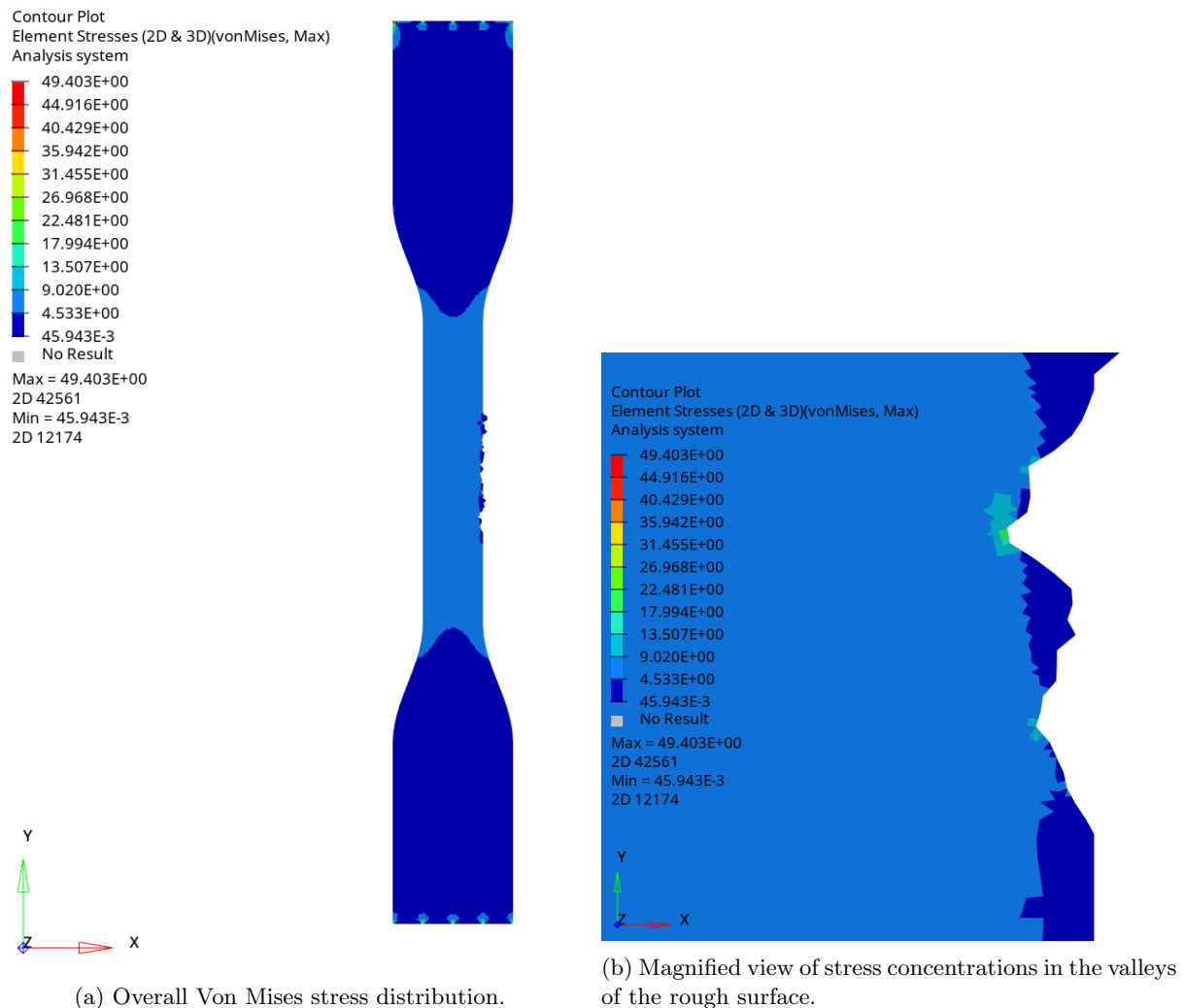


Figure 5: Example of Von Mises stress results for an Aluminium specimen under tensile load.

of K_t values than the other models. This suggests that Zhang's formulation may capture the geometric effects of roughness more robustly, although its applicability should be further investigated for different material classes.

4 Discussion

This section discusses the methodological choices, interprets the observed trends, and contextualizes the findings within the existing literature.

4.1 Methodological Considerations

In contrast to the rectangular geometry used by Zhang [7], this study employed a dog-bone specimen shape. This choice ensures a state of ideal uniaxial tension in the gauge section, by isolating the effect of surface roughness on the stress concentration factor, K_t , more effectively.

For mesh generation, the combination of a surrogate-based optimization algorithm with the Gmsh library proved to be highly efficient. It consistently produced high-quality meshes satisfying the criteria in Table [2] within a maximum of 50 iterations per sample. Alternative meshing tools like DistMesh [23] were considered but ultimately discarded. DistMesh is limited to generating triangular elements in 2D, which contradicts our goal of creating meshes dominated by higher-quality quadrilateral elements. Furthermore, preliminary tests indicated that Gmsh is computationally less expensive.

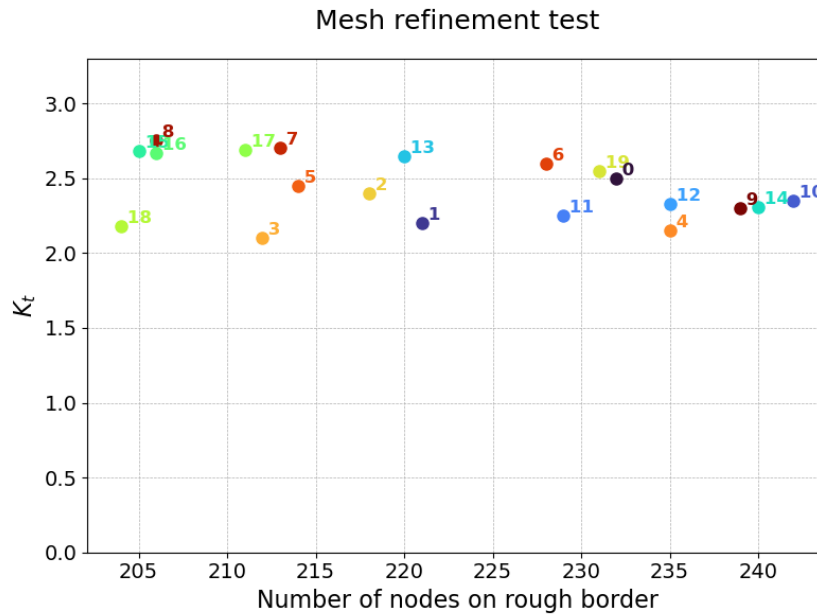
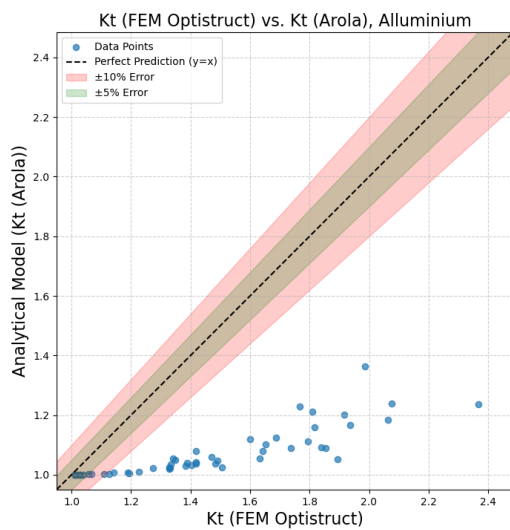
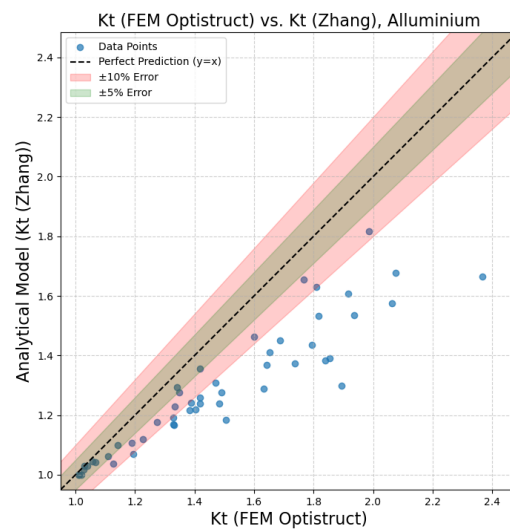


Figure 6: Number of nodes in rough border VS K_t



(a) Comparison with Arola’s rule [6].



(b) Comparison with Zhang’s rule [7].

Figure 7: Comparison of the stress concentration factor (K_t) computed via FEM with predictions from Arola’s and Zhang’s models for the 50 aluminum specimens.

It is important to note that the present analysis is strictly linear elastic. The applied load of 100N is deliberately kept low to ensure that even with stress concentrations, the peak local stress remained below the typical yield strength (σ_y) of both materials. With higher stress levels is necessary to perform a plastic analysis and use the correction for the effective stress concentration factor, K_{eff} . Future work should take into consideration that.

Table 4: Results of mesh sensitivity test

Sample	Number of nodes in rough border	Avg. mesh size [mm]	Min mesh size [mm]	Max mesh size [mm]	Number of TRIAs	Number of QUADS
0	232	0.335	0.053	0.558	3182	17279
1	221	0.181	0.052	0.292	4392	65542
2	218	0.234	0.053	0.386	3098	38883
3	212	0.147	0.052	0.237	2834	103380
4	235	0.148	0.047	0.244	7212	98475
5	214	0.236	0.054	0.374	1936	39410
6	228	0.326	0.051	0.521	2868	18775
7	213	0.341	0.052	0.622	1796	17971
8	206	0.343	0.052	0.576	1444	18127
9	239	0.232	0.054	0.363	4490	38125
10	242	0.237	0.052	0.391	4950	36130
11	229	0.180	0.048	0.305	6482	64601
12	235	0.232	0.054	0.378	4416	38158
13	220	0.337	0.052	0.619	2652	17594
14	240	0.232	0.055	0.351	4568	38057
15	205	0.334	0.050	0.626	1556	19058
16	206	0.334	0.051	0.624	1470	19106
17	211	0.334	0.052	0.625	1482	19107
18	204	0.172	0.051	0.255	1316	75990
19	231	0.327	0.053	0.514	3334	18202

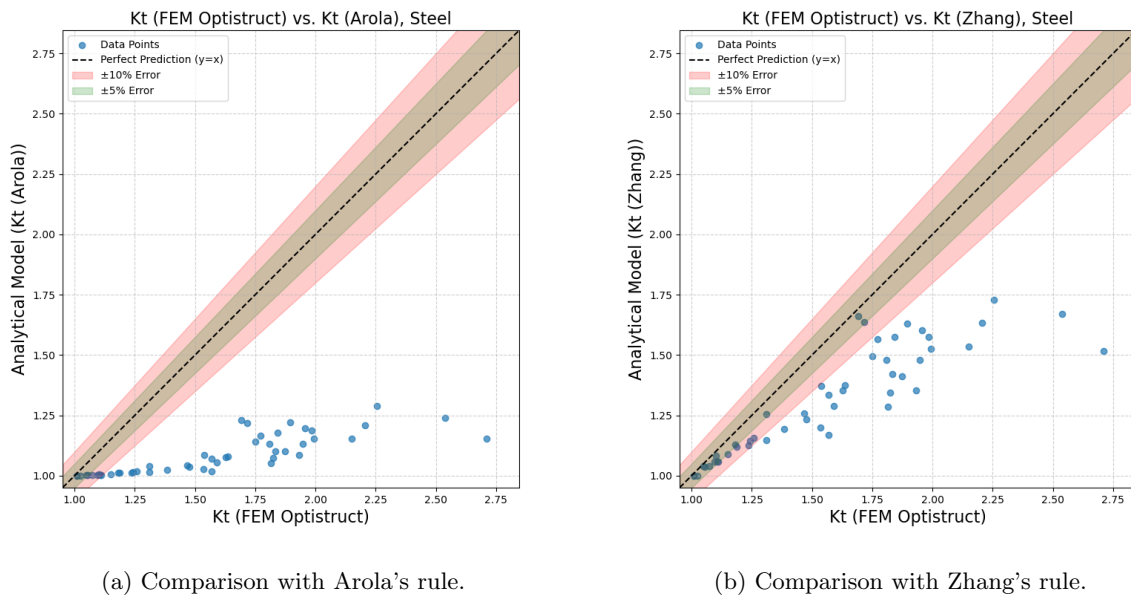


Figure 8: Comparison of the stress concentration factor computed via FEM with predictions from Arola's rule and Zhang's rule for the steel specimens.

4.2 Influence of Roughness Parameters on K_t

To understand the underlying mechanics, the influence of individual roughness parameters on the FEM-computed K_t is investigated. The analysis included roughness values that exceeded those typically found in as-built components to explore a wider design space.

As depicted in Figures 9 and 10, a clear positive correlation exists between K_t and the roughness height parameters (R_a , R_y , and R_z) for both steel and aluminum. This aligns with established engineering principles, where smoother surfaces are specified to enhance fatigue resistance. Conversely, an inverse relationship is observed between K_t and the average valley radius, $\bar{\rho}$. This is physically intuitive, as a smaller radius corresponds to a sharper notch, which produces a more severe stress concentration.

Second-order polynomial and reciprocal models were fitted to these relationships, with the resulting equations and coefficients of determination (R^2) summarized in Tables [5] and [6]. These tables provide quantitative models describing the sensitivity of K_t to each geometric parameter for both the FEM results and the literature models.

4.3 Evaluation of Predictive Models

In applications where surface roughness is minimal, leading to low stress concentration factors, the results suggest that most of the evaluated models, including Arola's rule, provide reasonable predictions. Given that many industrial components operate in this low- K_t regime, the continued use of Arola's rule can be justified for its simplicity.

However, for components with higher surface roughness, Arola's rule shows significant deviation from the FEM results. Zhang's empirical model [7] demonstrates superior predictive accuracy across a broader range of roughness parameters for both materials investigated. Therefore, for applications where a more accurate prediction of K_t is critical, Zhang's rule is recommended.

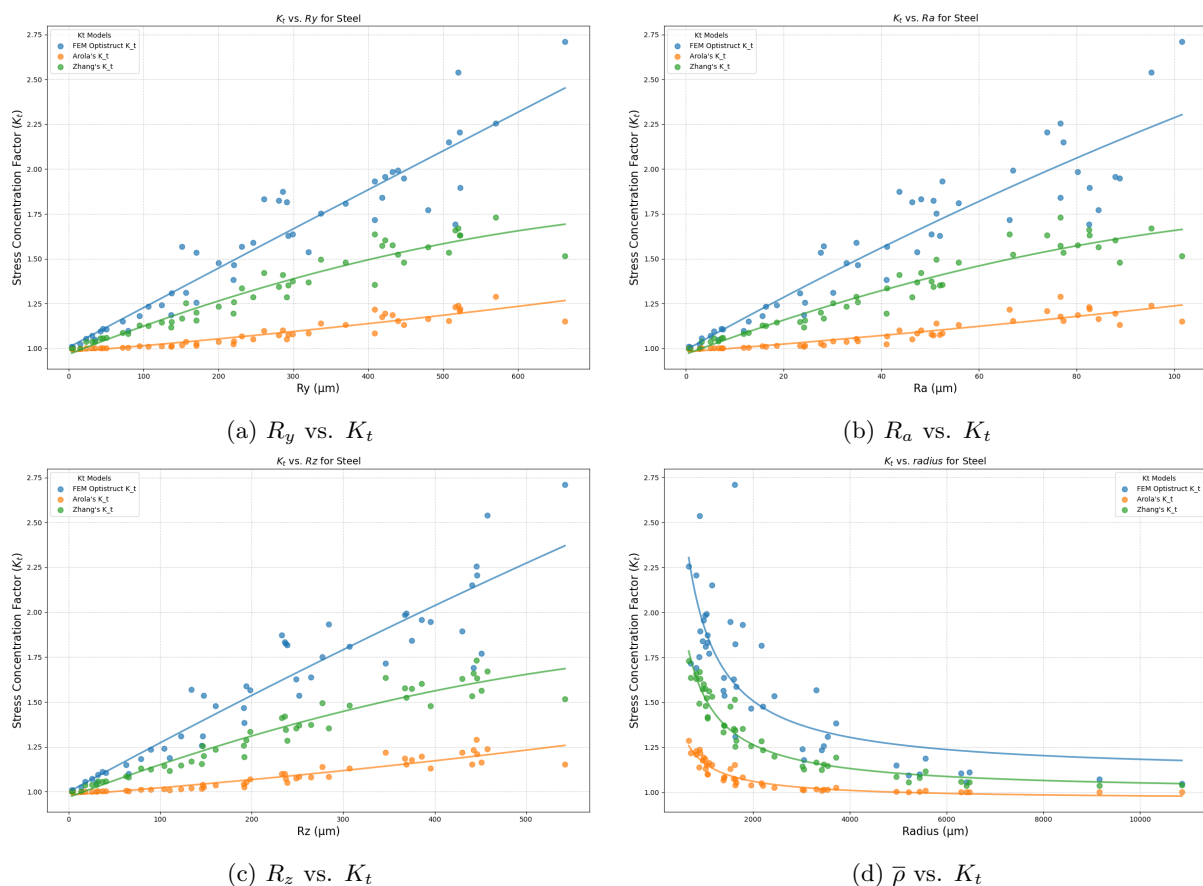


Figure 9: Relationship between individual roughness parameters and the computed Stress Concentration Factor (K_t) for the steel specimens.

5 Conclusion

This study performed a systematic evaluation of common analytical and empirical models for the stress concentration factor (K_t) induced by surface roughness, using stochastic Finite Element Analysis. The

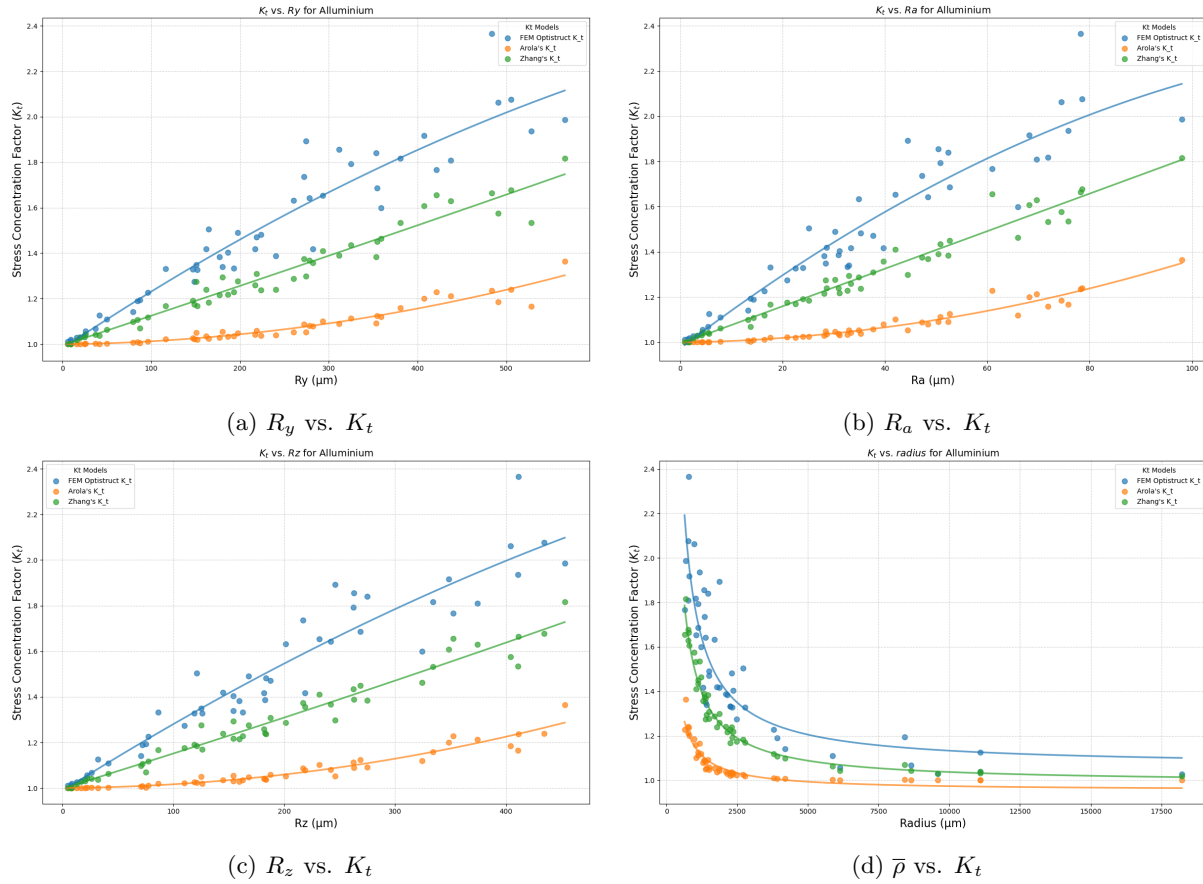


Figure 10: Relationship between individual roughness parameters and the computed Stress Concentration Factor (K_t) for the aluminum specimens.

Table 5: Summary of regression models for Stress Concentration Factor (K_t) based on roughness parameters for Steel.

Parameter	Data Source	Fit Type	Equation	R^2
R_a (μm)	FEM OptiStruct	Polynomial	$K_t = -2.13 \times 10^{-5} R_a^2 + 0.0151 R_a + 0.9915$	0.855
	Arola's Model	Polynomial	$K_t = 4.65 \times 10^{-6} R_a^2 + 0.0021 R_a + 0.9803$	0.835
	Zhang's Model	Polynomial	$K_t = -3.26 \times 10^{-5} R_a^2 + 0.0102 R_a + 0.9678$	0.923
R_y (μm)	FEM OptiStruct	Polynomial	$K_t = -5.69 \times 10^{-8} R_y^2 + 0.0022 R_y + 1.007$	0.884
	Arola's Model	Polynomial	$K_t = 1.42 \times 10^{-7} R_y^2 + 3.39 \times 10^{-4} R_y + 0.9802$	0.853
	Zhang's Model	Polynomial	$K_t = -8.50 \times 10^{-7} R_y^2 + 0.0017 R_y + 0.9676$	0.929
R_z (μm)	FEM OptiStruct	Polynomial	$K_t = -4.58 \times 10^{-7} R_z^2 + 0.0028 R_z + 0.9998$	0.870
	Arola's Model	Polynomial	$K_t = 2.30 \times 10^{-7} R_z^2 + 3.86 \times 10^{-4} R_z + 0.9812$	0.860
	Zhang's Model	Polynomial	$K_t = -1.13 \times 10^{-6} R_z^2 + 0.0019 R_z + 0.9693$	0.937
$\bar{\rho}$ (μm)	FEM OptiStruct	Reciprocal	$K_t = 814.74/\bar{\rho} + 1.1024$	0.592
	Arola's Model	Reciprocal	$K_t = 202.40/\bar{\rho} + 0.9606$	0.895
	Zhang's Model	Reciprocal	$K_t = 532.56/\bar{\rho} + 0.9996$	0.925

key findings are as follows:

1. Arola's rule provides acceptable predictions for K_t only in cases of low surface roughness. As

Table 6: Summary of regression models for Stress Concentration Factor (K_t) based on roughness parameters for Aluminum.

Parameter	Data Source	Fit Type	Equation	R^2
R_a (μm)	FEM OptiStruct	Polynomial	$K_t = -5.79 \times 10^{-5} R_a^2 + 0.0177 R_a + 0.9639$	0.888
	Arola's Model	Polynomial	$K_t = 3.27 \times 10^{-5} R_a^2 + 3.79 \times 10^{-4} R_a + 0.9982$	0.939
	Zhang's Model	Polynomial	$K_t = 7.65 \times 10^{-7} R_a^2 + 0.0082 R_a + 0.9946$	0.960
R_y (μm)	FEM OptiStruct	Polynomial	$K_t = -1.14 \times 10^{-6} R_y^2 + 0.0027 R_y + 0.9746$	0.896
	Arola's Model	Polynomial	$K_t = 8.60 \times 10^{-7} R_y^2 + 5.07 \times 10^{-5} R_y + 0.9985$	0.917
	Zhang's Model	Polynomial	$K_t = 8.52 \times 10^{-8} R_y^2 + 0.0013 R_y + 0.9969$	0.950
R_z (μm)	FEM OptiStruct	Polynomial	$K_t = -1.39 \times 10^{-6} R_z^2 + 0.0031 R_z + 0.9853$	0.900
	Arola's Model	Polynomial	$K_t = 1.35 \times 10^{-6} R_z^2 + 2.12 \times 10^{-5} R_z + 1.001$	0.926
	Zhang's Model	Polynomial	$K_t = 2.95 \times 10^{-7} R_z^2 + 0.0015 R_z + 1.003$	0.958
$\bar{\rho}$ (μm)	FEM OptiStruct	Reciprocal	$K_t = 721.35/\bar{\rho} + 1.0609$	0.750
	Arola's Model	Reciprocal	$K_t = 197.64/\bar{\rho} + 0.9537$	0.882
	Zhang's Model	Reciprocal	$K_t = 510.36/\bar{\rho} + 0.9860$	0.960

roughness increases, its accuracy diminishes significantly.

2. The Bayesian model proposed by Zhang demonstrated superior predictive capability over a wider range of roughness conditions for both aluminum and steel, making it a more robust choice for general engineering applications.

The present work has several limitations. The analysis is confined to a linear elastic material model and investigated only two materials. Furthermore, the roughness profiles were synthetically generated, without new experimental results.

Future research should be directed towards addressing these limitations. The inclusion of material plasticity in the FEM models would allow for a more rigorous investigation, also it could be compared to the value of the effective stress concentration factor, K_{eff} . Expanding the study to include a wider range of engineering alloys and incorporating experimentally measured surface profiles from real components would enhance the industrial relevance of the findings. Additionally, extending the framework to 3D analysis and investigating the influence of residual stresses and microstructural features would represent valuable contributions to the field. Finally, integrating these improved K_t models into fatigue life prediction frameworks would be a logical next step.

6 Declarations

This publication is part of the project PNRR-NGEU which has received funding from the MUR-DM 117/2023



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