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(Article begins on next page)

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Secrecy Energy Efficiency Maximization in RIS-Aided Wireless Networks with Statistical CSI

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***Abstract*—This work studies the problem of secrecy energy efficiency maximization in multi-user wireless networks aided by reconfigurable intelligent surfaces, in which an eavesdropper overhears the uplink communication. A provably convergent optimization algorithm is proposed which optimizes the user's transmit power, metasurface reflection coefficients, and base station receive filters. The complexity of the proposed method is analyzed and numerical results are provided to show the performance of the proposed optimization method.**

***Index Terms*—RIS, IRS, energy efficiency, physical layer security.**

I. Introduction

RECONFIGURABLE intelligent surfaces (RISs) have been proposed as a promising technology for 6G networks, as they provide satisfactory rate performance with lower energy consumption than traditional antenna arrays [1]–[4]. This can unlock unprecedented levels of energy efficiency (EE), a key performance indicator of 6G networks [5]. Moreover, aiming at improving their rate gains, recently it has been proposed to deploy dedicated analog amplifiers on the RIS, which led the research community to investigate the use of active RISs [6]. However, this poses a fundamental trade-off in terms of EE, since equipping the RIS with additional hardware causes larger energy consumption. Thus, the EE advantages of active RIS are not clear. In [7], active and nearly passive RISs have been compared in terms of EE, showing that active RISs do not always provide better EE. This work continues the investigation started in [7], considering another major requirement of future networks, i.e. secret communications. Several contributions have appeared that study RISs in conjunction with physical layer security techniques. However, most contributions consider the system secrecy rate, without addressing the energy efficiency of the network. A non-orthogonal multiple access (NOMA) networks that employs a simultaneous transmission and reception (STAR) RIS is considered in [8], and the system secrecy outage probability is characterized. A NOMA-based network aided by a STAR-RIS is also considered in [9], and closed-form approximations of the secrecy outage probability are derived. In [10], a STAR-aided NOMA-based network is considered and the system's worst-case secrecy capacity is maximized. In [11], the ergodic secrecy capacity of RIS-aided wireless networks is analyzed and approximated in closed form, considering flying eavesdroppers. In [12], the secrecy rate of RIS-aided networks powered by wireless power transfer is optimized. In [13] the secrecy rate of RIS-aided networks with space ground communications is optimized. In [14], the sum secrecy rate of the uplink of a multi-user RIS-aided wireless network is addressed. The SEE in RIS-aided networks has been considered in few works, such as [15] and [16]. Specifically, in [15], a deep reinforcement learning method is employed to optimize the SEE of a RIS-aided network, while in [16] a combination of alternating maximization and sequential programming is employed to maximize the SEE of a multi-user network. This work optimizes the secrecy energy efficiency (SEE) [17], in the uplink of a multi-user network in the presence of an eavesdropper. Assuming only statistical channel state information (CSI) of the eavesdropper's channel, a provably convergent algorithm is developed which optimizes the mobile users' transmit powers, the RIS coefficients, and the base station receive filters. The developed algorithm is suited to both nearly passive and active RISs, thus allowing the comparison of both approaches. Moreover, the proposed model is general enough to encompass the recently proposed use of RIS with global reflection capabilities. This new kind of RIS generalizes the use of traditional RISs since the constraint on the reflected power is not applied to each reflecting element individually, but rather to the whole surface [18].

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II. System Model and Problem Formulation

Let us consider a network consisting of K single-antenna mobile transmitters, labeled as Alices, which communicate with

their base station, labeled as Bob, equipped with N_B antennas, through a reconfigurable intelligent surface (RIS), equipped with N reflecting elements. In the same area, a single-antenna eavesdropper is present, which is labelled as Eve. Let us denote by p_k the k-th user's transmit power, by $\boldsymbol{\gamma} = (\gamma_1, \ldots, \gamma_N)$ the $N \times 1$ vector containing the RIS reflection coefficients, by $\boldsymbol{h}_k$ the $N \times 1$ channel between the k-th user and the RIS and by $\boldsymbol{G}_B$ and $\boldsymbol{g}_E$, the $N_B \times N$ and $N \times 1$ channel from the RIS to Bob and Eve, respectively. Thus, the SINRs of user k at the intended and eavesdropping receiver, upon linear reception by $\boldsymbol{c}_{k,B}$ and $\boldsymbol{c}_{k,E}$, are written as

$$\text{SINR}_{k,B} = \frac{p_k \left| \boldsymbol{c}_{k,B}^H \boldsymbol{A}_{k,B} \boldsymbol{\gamma} \right|^2}{\boldsymbol{c}_{k,B}^H \boldsymbol{W}_B \boldsymbol{c}_{k,B} + \sum_{m \neq k} p_m \left| \boldsymbol{c}_{k,B}^H \boldsymbol{A}_{m,B} \boldsymbol{\gamma} \right|^2} \tag{1}$$

$$\text{SINR}_{k,E} = \frac{p_k \left| \boldsymbol{g}_E^H \boldsymbol{H}_k \boldsymbol{\gamma} \right|^2}{\sigma_E^2 + \sigma_{RIS}^2 \boldsymbol{g}_E^H \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \boldsymbol{g}_E + \sum_{m \neq k} p_m \left| \boldsymbol{g}_E^H \boldsymbol{H}_m \boldsymbol{\gamma} \right|^2} \tag{2}$$

wherein $\boldsymbol{A}_{k,B} = \boldsymbol{G}_B \boldsymbol{H}_k$ and $\boldsymbol{W}_B = \sigma_B^2 \boldsymbol{I}_{N_B} + \sigma_{RIS}^2 \boldsymbol{G}_B \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \boldsymbol{G}_B^H$ is the noise covariance matrix at Bob, with $\boldsymbol{\Gamma} = \text{diag}(\boldsymbol{\gamma})$, σ_{RIS}^2 the noise variance at the RIS, while σ_{B}^2 and σ_{E}^2 are the noise variance at Bob and Eve, respectively. In this context, the goal is to optimize the system SEE, defined as the ratio of the system secrecy rate over the total power consumed in the network. As for the system secrecy rate, it is defined as $R_s = \max\{0, \sum_{k=1}^K \log_2(1 + \text{SINR}_{k,B}) - \log_2(1 + \text{SINR}_{k,E})\}$. As for the power consumption, it is obtained by summing the radiofrequency power consumed by the RIS and the users' transmit power, plus the static power consumption of the whole legitimate system, which yields $P_{tot} = P_{RIS} + \sum_{k=1}^K \mu_k p_k + P_c$ wherein μ_k denotes the inverse efficiency of the transmit amplifier associated with the k-th transmitter and $P_c = N P_{c,n} + P_0^{\text{RIS}} + P_0$, with $P_{c,n}$ the static power consumption of the n-th RIS element, P_0^{RIS} is the rest of the static power consumed by the RIS and P_0 encompasses all other sources of power consumption in the legitimate system. As for P_{RIS}, it is given by the difference between the incident power on the RIS P_{in} and the power that departs from the RIS, P_{out}, which after some elaborations [19], can be computed as;

$$\begin{aligned} P_{out} - P_{in} &= \text{tr}\left(\textstyle\sum_{k=1}^K p_k \boldsymbol{\Gamma} \boldsymbol{h}_k \boldsymbol{h}_k^H \boldsymbol{\Gamma}^H + \sigma_{\text{RIS}}^2 \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \right) \\ &\quad - \textstyle\sum_{k=1}^K p_k \left\| \boldsymbol{h}_k \right\|^2 - \sigma_{\text{RIS}}^2 N = \text{tr}\left(\left(\boldsymbol{\gamma} \boldsymbol{\gamma}^H - \boldsymbol{I}_N \right) \boldsymbol{R} \right) \end{aligned} \tag{3}$$

wherein $\boldsymbol{R} = \sum_{k=1}^K p_k \boldsymbol{H}_k^H \boldsymbol{H}_k + \sigma_{\text{RIS}}^2 \boldsymbol{I}_N$. The considered power consumption model has been developed for an active RIS, but it is general enough to be applied to a nearly passive RIS as a special case. Specifically, in the case of a nearly passive RIS, $P_{out} \leqslant P_{in}$ and thus the difference $P_{out} - P_{in}$ does not appear in the power consumption P_{tot}. Moreover, if a nearly passive RIS is employed, the terms $P_{c,n}$ and P_0^{RIS} will have a lower numerical value compared to the case of an active RIS, since simpler hardware is employed in nearly-passive RIS, i.e. no analog amplifiers are used. Similarly, the constraints that should be enforced on the RIS vector $\boldsymbol{\gamma}$ depend on whether the RIS is active or nearly passive. Specifically, if the RIS is active, then $0 \leqslant P_{out} - P_{in} \leqslant P_{R,\text{max}}$ with $P_{R,\text{max}}$ the maximum radio-frequency power that the RIS amplifier can provide. Instead, for nearly-passive RISs, the constraint $P_{out} \leqslant P_{in}$ applies, which is a special case of the constraint for the active case, obtained by relaxing the first inequality and setting $\sigma_{RIS}^2 = 0$ and $P_{R,\text{max}} = 0$ in the second inequality. In the following, the focus will be on the more general active RIS scenario. In the sequel, we assume perfect channel state information (CSI) for all channels except the channel $\boldsymbol{g}_E$ from the RIS to the eavesdropper, motivated by the fact that the eavesdropper might be a hidden node. Specifically, as for the channel $\boldsymbol{g_E}$, we follow a mean feedback model, in which we assume that the legitimate system has only access to the mean value of $\boldsymbol{g}_E$, denoted by $\widehat{\boldsymbol{g}}_E$, while the true channel is given by $\boldsymbol{g}_E = \widehat{\boldsymbol{g}}_E + \boldsymbol{\delta}$, with $\boldsymbol{\delta} \sim \mathcal{CN}(\boldsymbol{0}, \sigma_g^2 \boldsymbol{I}_{N_E})$. As a consequence, the legitimate system can not directly maximize the SEE, and an average version of the secrecy rate at the numerator of the SEE should be considered. Namely, the considered problem can be formulated as

$$\max_{\boldsymbol{\gamma}, \boldsymbol{p}, \boldsymbol{C}_B} \frac{\sum_{k=1}^K \log_2(1 + \text{SINR}_{k,B}) - \mathbb{E}_{\boldsymbol{\delta}} \left[\log_2(1 + \text{SINR}_{k,E}) \right]}{P_{tot}} \tag{4a}$$

$$\text{s.t. } \text{tr}(\boldsymbol{R}) \leqslant \text{tr}(\boldsymbol{R} \boldsymbol{\gamma} \boldsymbol{\gamma}^H) \leqslant P_{R,max} + \text{tr}(\boldsymbol{R}) \tag{4b}$$

$$0 \leqslant p_k \leqslant P_{max,k} \; \forall \; k = 1, \ldots, K \, , \tag{4c}$$

with $\boldsymbol{C}_B = [\boldsymbol{c}_{1,B}, \ldots, \boldsymbol{c}_{K,B}]$, and we have dropped the positive operator $^+$, since we assume that the maximum of the secrecy rate is positive[1]. We also observe that Problem (4b) is always feasible, since setting $|\gamma_n| = 1$ for all n fulfills all constraints.

III. Proposed Optimization Method

The considered problem (4) is challenging due to the non-convexity of the objective function and constraints, and also due to the presence of the statistical expectation in the numerator of the objective. Let us first deal with the statistical expectation. Unfortunately, a closed-form expression of the term $\mathbb{E}_{\boldsymbol{\delta}} \left[\log_2(1 + \text{SINR}_{k,E}) \right]$ is not available. Thus, in order to simplify the problem, we resort to the popular approach of approximating the objective by taking the statistical expectation inside the logarithm, which yields

$$\begin{aligned} &\mathbb{E}_{\boldsymbol{\delta}} \left[\log_2(1 + \text{SINR}_{k,E}) \right] \\ &= \mathbb{E}_{\boldsymbol{\delta}} \left[\log_2 \left(\sigma_E^2 + \sigma_{RIS}^2 \boldsymbol{g}_E^H \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \boldsymbol{g}_E + \sum_{m=1}^K p_m \left| \boldsymbol{g}_E^H \boldsymbol{H}_m \boldsymbol{\gamma} \right|^2 \right) \right] \\ &- \mathbb{E}_{\boldsymbol{\delta}} \left[\log_2 \left(\sigma_E^2 + \sigma_{RIS}^2 \boldsymbol{g}_E^H \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \boldsymbol{g}_E + \sum_{m \neq k} p_m \left| \boldsymbol{g}_E^H \boldsymbol{H}_m \boldsymbol{\gamma} \right|^2 \right) \right] \\ &\approx \log_2 \left(\sigma_E^2 + \mathbb{E}_{\boldsymbol{\delta}} \left[\sigma_{RIS}^2 \boldsymbol{g}_E^H \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \boldsymbol{g}_E + \sum_{m=1}^K p_m \left| \boldsymbol{g}_E^H \boldsymbol{H}_m \boldsymbol{\gamma} \right|^2 \right] \right) \\ &- \log_2 \left(\sigma_E^2 + \mathbb{E}_{\boldsymbol{\delta}} \left[\sigma_{RIS}^2 \boldsymbol{g}_E^H \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H \boldsymbol{g}_E + \sum_{m \neq k} p_m \left| \boldsymbol{g}_E^H \boldsymbol{H}_m \boldsymbol{\gamma} \right|^2 \right] \right) \end{aligned} \tag{5}$$

[1]The case in which the maximum of the secrecy rate is not positive is of no practical interest since it would imply that no secret communication is possible.

Since $\boldsymbol{g}_E = \widehat{\boldsymbol{g}}_E + \boldsymbol{\delta}$, elaborating we obtain, for all $m = 1, \ldots, K$

$$\mathbb{E}_{\boldsymbol{\Delta}}\left[\left|\boldsymbol{g}_E^H \boldsymbol{H}_m \boldsymbol{\gamma}\right|^2\right] = \widehat{\boldsymbol{g}}_E^H \boldsymbol{H}_m \boldsymbol{\gamma}\boldsymbol{\gamma}^H \boldsymbol{H}_m^H \widehat{\boldsymbol{g}}_E + \sigma_g^2 \|\boldsymbol{H}_m \boldsymbol{\gamma}\|^2$$
$$= \boldsymbol{\gamma}^H \boldsymbol{H}_m^H \left(\widehat{\boldsymbol{g}}_E \widehat{\boldsymbol{g}}_E^H + \sigma_g^2 \boldsymbol{I}_N\right) \boldsymbol{H}_m \boldsymbol{\gamma} = \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_m \boldsymbol{\gamma}\|^2 \quad (6)$$

$$\mathbb{E}_{\boldsymbol{\Delta}}\left[\boldsymbol{g}_E^H \boldsymbol{\Gamma}\boldsymbol{\Gamma}^H \boldsymbol{g}_E\right] = \boldsymbol{\gamma}^H \left(\widehat{\boldsymbol{g}}_E \widehat{\boldsymbol{g}}_E^H + \sigma_g^2 \boldsymbol{I}_N\right) \boldsymbol{\gamma} = \|\boldsymbol{R}_E^{1/2} \boldsymbol{\gamma}\|^2, \quad (7)$$

wherein $\boldsymbol{R}_E = \widehat{\boldsymbol{g}}_E \widehat{\boldsymbol{g}}_E^H + \sigma_g^2 \boldsymbol{I}_N$ Then, (5) becomes

$$\mathbb{E}_{\boldsymbol{\delta}}\left[\log_2(1 + \mathrm{SINR}_{k,E})\right] \approx \log_2\left(1 + \widetilde{\mathrm{SINR}}_{k,E}\right), \quad (8)$$

with $\widetilde{\mathrm{SINR}}_{k,E}$ given by

$$\widetilde{\mathrm{SINR}}_{k,E} = \frac{p_k \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_k \boldsymbol{\gamma}\|^2}{\sum_{m \neq k} p_m \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_m \boldsymbol{\gamma}\|^2 + \sigma_{RIS}^2 \|\boldsymbol{R}_E^{1/2} \boldsymbol{\gamma}\|^2 + \sigma_E^2} \quad (9)$$

Thus, the objective (4a) can be approximated as

$$\widetilde{\mathrm{SEE}} = \frac{\sum_{k=1}^K \log_2(1 + \mathrm{SINR}_{k,B}) - \log_2(1 + \widetilde{\mathrm{SINR}}_{k,E})}{P_{tot}} \quad (10)$$

The next challenge is to deal with the non-convexity of the optimization problem. To this end, $\boldsymbol{\gamma}$, $\boldsymbol{p}$, and $\boldsymbol{C}_B$ will be optimized alternatively, as shown in the next three subsections.

A. RIS optimization

With respect to the RIS vector $\boldsymbol{\gamma}$, the problem is expressed as:

$$\max_{\boldsymbol{\gamma}} B \frac{\sum_{k=1}^K \log_2(1 + \mathrm{SINR}_{k,B}) - \log_2\left(1 + \widetilde{\mathrm{SINR}}_{k,E}\right)}{\mathrm{tr}\left(\boldsymbol{R}\boldsymbol{\gamma}\boldsymbol{\gamma}^H\right) + P_{c,eq}} \quad (11a)$$

$$\text{s.t. } \mathrm{tr}\left(\boldsymbol{R}\right) \leqslant \mathrm{tr}(\boldsymbol{R}\boldsymbol{\gamma}\boldsymbol{\gamma}^H) \leqslant P_{R,max} + \mathrm{tr}\left(\boldsymbol{R}\right) \quad (11b)$$

wherein $P_{c,eq} = \sum_k p_k \mu_k + P_c - \mathrm{tr}(\boldsymbol{R})$. Problem (11) is challenging since the objective is neither concave nor pseudo-concave, which prevents the direct use of fractional programming [20], and (11b) is a non-convex constraint. To circumvent this challenge, we employ the sequential fractional programming method. To this end, we express the term $\boldsymbol{c}_{k,B}^H \boldsymbol{W}_B \boldsymbol{c}_{k,B}$, in terms of the vector $\boldsymbol{\gamma}$, instead of the matrix $\boldsymbol{\Gamma}$. To achieve this, we define $\boldsymbol{u}_k = \boldsymbol{G}_B^H \boldsymbol{c}_{k,B}$ and $\widetilde{\boldsymbol{U}}_{k,B} = \mathrm{diag}\left(|u_{1,B}|^2, \ldots, |u_{N,B}|^2\right)$. Subsequently, by incorporating the expression of $\boldsymbol{W}_B$, we obtain $\boldsymbol{c}_{k,B}^H \boldsymbol{W}_B \boldsymbol{c}_{k,B} = \sigma^2 \|\boldsymbol{c}_{k,B}\|^2 + \sigma_{\mathrm{RIS}}^2 \|\widetilde{\boldsymbol{U}}_{k,B}^{1/2} \boldsymbol{\gamma}\|^2$. For the sequential fractional programming method, a concave lower-bound of the numerator in (11a) is needed. Then, let us define

$$x_B = p_k \left|\boldsymbol{c}_{k,B}^H \boldsymbol{A}_{k,B} \boldsymbol{\gamma}\right|^2, \; x_E = p_k \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_k \boldsymbol{\gamma}\|^2 \quad (12)$$

$$y_B = \sigma^2 \|\boldsymbol{c}_{k,B}\|^2 + \sigma_{\mathrm{RIS}}^2 \|\widetilde{\boldsymbol{U}}_{k,B}^{1/2} \boldsymbol{\gamma}\|^2 + \sum_{m \neq k} p_m \left|\boldsymbol{c}_{k,B}^H \boldsymbol{A}_{m,B} \boldsymbol{\gamma}\right|^2 \quad (13)$$

$$y_E = \sum_{m \neq k} p_m \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_m \boldsymbol{\gamma}\|^2 + \sigma_{RIS}^2 \|\boldsymbol{R}_E^{1/2} \boldsymbol{\gamma}\|^2, \quad (14)$$

and observe that the numerator of (11a) can be written as

$$R_s = \log_2\left(1 + \frac{x_B}{y_B}\right) - \log_2\left(1 + \frac{x_E}{y_E + \sigma_E^2}\right) = \log_2\left(1 + \frac{x_B}{y_B}\right)$$
$$+ \log_2\left(1 + \frac{y_E}{\sigma_E^2}\right) + \log_2\left(\sigma_E^2\right) - \log_2(\sigma_E^2 + x_E + y_E) \quad (15)$$

Then, in order to lower-bound (15), we leverage the bounds

$$\log_2\left(1 + \frac{x}{y}\right) \geqslant \log_2\left(1 + \frac{\bar{x}}{\bar{y}}\right) + \frac{\bar{x}}{\bar{y}}\left(\frac{2\sqrt{x}}{\sqrt{\bar{x}}} - \frac{x + y}{\bar{x} + \bar{y}} - 1\right) \quad (16)$$

$$\log_2(\sigma_E^2 + x + y) \leqslant \log(\sigma_E^2 + \bar{x} + \bar{y}) + \frac{x + y - \bar{x} - \bar{y}}{\sigma_E^2 + \bar{x} + \bar{y}} \quad (17)$$

which hold for any x, y, $\bar{x}$ and $\bar{y}$, with equality whenever $x = \bar{x}$ and $y = \bar{y}$. For any feasible vector $\bar{\boldsymbol{\gamma}}$ of RIS reflection coefficients, we also define

$$\bar{x}_B = p_k \left|\boldsymbol{c}_{k,B}^H \boldsymbol{A}_{k,B} \bar{\boldsymbol{\gamma}}\right|^2, \bar{x}_E = p_k \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_k \bar{\boldsymbol{\gamma}}\|^2 \quad (18)$$

$$\bar{y}_B = \sigma^2 \|\boldsymbol{c}_{k,B}\|^2 + \sigma_{\mathrm{RIS}}^2 \|\widetilde{\boldsymbol{U}}_{k,B}^{1/2} \bar{\boldsymbol{\gamma}}\|^2 + \sum_{m \neq k} p_m \left|\boldsymbol{c}_{k,B}^H \boldsymbol{A}_{m,B} \bar{\boldsymbol{\gamma}}\right|^2 \quad (19)$$

$$\bar{y}_E = \sum_{m \neq k} p_m \|\boldsymbol{R}_E^{1/2} \boldsymbol{H}_m \bar{\boldsymbol{\gamma}}\|^2 + \sigma_{RIS}^2 \|\boldsymbol{R}_E^{1/2} \bar{\boldsymbol{\gamma}}\|^2 \quad (20)$$

Then, the following lower-bound holds

$$R_s(\boldsymbol{\gamma}) \geqslant \log_2\left(1 + \frac{\bar{x}_B}{\bar{y}_B}\right) + \frac{\bar{x}_B}{\bar{y}_B}\left(\frac{2\sqrt{x_B}}{\sqrt{\bar{x}_B}} - \frac{x_B + y_B}{\bar{x}_B + \bar{y}_B} - 1\right)$$
$$+ \log_2\left(1 + \frac{\bar{y}_E}{\sigma_E^2}\right) + \frac{\bar{y}_E}{\sigma_E^2}\left(\frac{2\sqrt{y_E}}{\sqrt{\bar{y}_E}} - \frac{y_E + \sigma_E^2}{\bar{y}_E + \sigma_E^2} - 1\right)$$
$$+ \log_2\left(\frac{\sigma_E^2}{\sigma_E^2 + \bar{x}_E + \bar{y}_E}\right) - \frac{x_E + y_E - \bar{x}_E - \bar{y}_E}{\sigma_E^2 + \bar{x}_E + \bar{y}_E} \quad (21)$$

It can be seen that all terms in (21) that depend on $\boldsymbol{\gamma}$ are concave, except for $\sqrt{x_B}$ and $\sqrt{y_E}$. However, these terms are convex in $\boldsymbol{\gamma}$, and thus they can be lower-bounded by a first-order Taylor expansion around $\bar{\boldsymbol{\gamma}}$. Let us denote by $\widetilde{R}_s(\boldsymbol{\gamma})$, the resulting lower-bound. Lastly, as for the left-hand side of (11b), since $\mathrm{tr}\left(\boldsymbol{R}\boldsymbol{\gamma}\boldsymbol{\gamma}^H\right)$ is convex in $\boldsymbol{\gamma}$, its first-order Taylor expansion around any point $\bar{\boldsymbol{\gamma}}$ provides the lower-bound $\mathrm{tr}\left(\boldsymbol{R}\boldsymbol{\gamma}\boldsymbol{\gamma}^H\right) = \boldsymbol{\gamma}\boldsymbol{R}\boldsymbol{\gamma}^H \geqslant \bar{\boldsymbol{\gamma}}\boldsymbol{R}\bar{\boldsymbol{\gamma}}^H + 2\Re\left\{\bar{\boldsymbol{\gamma}}^H \boldsymbol{R}\left(\boldsymbol{\gamma} - \bar{\boldsymbol{\gamma}}\right)\right\}$. Consequently, each iteration of the sequential method solves:

$$\max_{\boldsymbol{\gamma}} \frac{\sum_{k=1}^K \widetilde{SR}_k}{\mathrm{tr}\left(\boldsymbol{R}\boldsymbol{\gamma}\boldsymbol{\gamma}^H\right) + P_{c,eq}^{(a)}} \quad (22a)$$

$$\text{s.t. } \boldsymbol{\gamma}\boldsymbol{R}\boldsymbol{\gamma}^H \leqslant P_{R,max} + \mathrm{tr}\left(\boldsymbol{R}\right) \quad (22b)$$

$$\bar{\boldsymbol{\gamma}}\boldsymbol{R}\bar{\boldsymbol{\gamma}}^H + 2\Re\left\{\bar{\boldsymbol{\gamma}}^H \boldsymbol{R}\left(\boldsymbol{\gamma} - \bar{\boldsymbol{\gamma}}\right)\right\} \geqslant \mathrm{tr}\left(\boldsymbol{R}\right) \quad (22c)$$

The numerator and denominator of (22a) are concave and convex, respectively, and thus (22) can be solved by fractional programming. The procedure is in Algorithm (1), which enjoys the convergence properties of sequential programming.

Algorithm 1 RIS optimization

$\epsilon > 0$, $\bar{\boldsymbol{\gamma}} = \boldsymbol{\gamma}_0$ `with` $\boldsymbol{\gamma}_0$ `any feasible vector;`
repeat
`Let` $\boldsymbol{\gamma}_0$ `be the solution of` (22); `Set` $\bar{\boldsymbol{\gamma}} = \boldsymbol{\gamma}_0$;
until $\|\bar{\boldsymbol{\gamma}} - \boldsymbol{\gamma}_0\| < \epsilon$

Proposition 1: *Algorithm 1 monotonically improves the value of the objective and converges to a first-order optimal point of* (11).

$$\max_{\{p_k\in[0,P_{max,k}]\}_{k=1}^K} \frac{\sum_{k=1}^K \log_2\left(1+\frac{p_k a_{k,k}^{(B)}}{d_{k,B}+\sum_{m\neq k} p_m a_{k,m}^{(B)}}\right)-\log_2\left(1+\frac{p_k a_k^{(E)}}{d_E+\sum_{m\neq k} p_m a_m^{(E)}}\right)}{\sum_{k=1}^K \mu_{k,eq} p_k + P_{c,eq}} \tag{23}$$

B. Transmit Power Optimization

Let us define, for all m and k, $a_{k,m}^{(B)} = |\boldsymbol{c}_{k,B}^H \boldsymbol{A}_{m,i}\boldsymbol{\gamma}|^2$, $d_{k,B} = \boldsymbol{c}_{k,B}^H \boldsymbol{W}_B \boldsymbol{c}_{k,B}$, $a_m^{(E)} = \|\boldsymbol{R}_E^{1/2}\boldsymbol{H}_m\boldsymbol{\gamma}\|^2$, $d_E = \sigma_{RIS}^2\|\boldsymbol{R}_E^{1/2}\boldsymbol{\gamma}\|^2 + \sigma_E^2$, $P_{c,eq} = \sigma_{\text{RIS}}^2\left(\|\boldsymbol{\gamma}\|^2 - N\right) + P_c$ and $\mu_{k,eq} = \mu_k - \|\boldsymbol{h}_k\|^2 + \|\boldsymbol{H}_k\boldsymbol{\gamma}\|^2$. Then, the power optimization problem is formulated as in (23). Problem (23) can be addressed again by sequential fractional programming, observing that the secrecy rate at the numerator of (23) can be written as the difference of two concave functions of $\boldsymbol{p}$ as

$$R_s(\boldsymbol{p}) = \underbrace{\sum_{k=1}^K \log\left(d_{k,B}+\sum_{m=1}^K p_m a_{k,m}^{(B)}\right)+\log\left(d_E+\sum_{m\neq k} p_m a_m^{(E)}\right)}_{g_1(\boldsymbol{p})}$$
$$-\underbrace{\left(\sum_{k=1}^K \log\left(d_{k,B}+\sum_{m\neq k} p_m a_{k,m}^{(B)}\right)+\log\left(d_E+\sum_{m=1}^K p_m a_m^{(E)}\right)\right)}_{g_2(\boldsymbol{p})} \tag{24}$$

Then a concave lower-bound of $R_s(\boldsymbol{p})$, can be obtained by linearizing $g_2(\boldsymbol{p})$ around any feasible point $\bar{\boldsymbol{p}}$, namely $R_s(\boldsymbol{p}) \geqslant g_1(\boldsymbol{p}) - g_2(\bar{\boldsymbol{p}}) - \nabla g_2(\bar{\boldsymbol{p}}))^T(\boldsymbol{p}-\bar{\boldsymbol{p}}) = \widetilde{R}_s(\boldsymbol{p})$ Then, a surrogate problem that fits the assumptions of sequential fractional programming can be formulated as

$$\max_{\{p_k\in[0,P_{max,k}]\}_{k=1}^K} \frac{\widetilde{R}_s(\boldsymbol{p})}{\sum_{k=1}^K \mu_{k,eq} p_k + P_{c,eq}} \tag{25}$$

which can be solved by standard fractional programming methods. Then, the power allocation subroutine is stated as in Algorithm 2, which is guaranteed to converge to a point fulfilling the first-order optimality conditions of (23).

Algorithm 2 Power optimization

$\epsilon > 0$, $\bar{\boldsymbol{p}} = \boldsymbol{p}_0$ with $\boldsymbol{p}_0$ any feasible vector;
repeat
  Let $\boldsymbol{p}_0$ be the solution of (25); Set $\bar{\boldsymbol{p}} = \boldsymbol{p}_0$;
until $\|\bar{\boldsymbol{p}} - \boldsymbol{p}_0\| < \epsilon$

Proposition 2: *Algorithm 2 monotonically improves the value of the objective and converges to a point fulfilling the KKT optimality conditions of (23).*

C. Receive Filter Optimization

The optimization of $\boldsymbol{C}_B$, exclusively influences the legitimate rate at the numerator of the SEE, and it can be decoupled across users, boiling down to maximizing the users' individual legitimate rates. This yields the linear MMSE receiver, which, for the considered case, is $\boldsymbol{c}_{k,B} = \sqrt{p}_k \boldsymbol{M}_{k,B}^{-1}\boldsymbol{A}_{k,B}\boldsymbol{\gamma}$ where $\boldsymbol{M}_{k,B} = \sum_{m\neq k} p_m \boldsymbol{A}_{m,i}\boldsymbol{\gamma}\boldsymbol{\gamma}^H\boldsymbol{A}_{m,B}^H + \boldsymbol{W}_B$ represents the interference-plus-noise covariance matrix of user k.

D. Overall Algorithm, Convergence, and Complexity

The overall alternating maximization algorithm can be stated as in Algorithm 3.

Algorithm 3 Solution algorithm for Problem (4)

Set $\epsilon > 0$, initialize $\tilde{\boldsymbol{p}}$, $\tilde{\boldsymbol{\gamma}}$ to feasible values
Compute $\boldsymbol{c}_k = \sqrt{p}_k \boldsymbol{M}_k^{-1}\boldsymbol{A}_k$ for all k;
repeat
  Compute $\text{SEE}_{in} = \text{SEE}(\tilde{\boldsymbol{p}}, \tilde{\boldsymbol{\gamma}}, \boldsymbol{C})$;
  Given $\tilde{\boldsymbol{p}}$ run Algorithm 1 with output $\tilde{\boldsymbol{\gamma}}$;
  Given $\tilde{\boldsymbol{\gamma}}$ run Algorithm 2 with output $\tilde{\boldsymbol{p}}$;
  Compute $\boldsymbol{c}_k = \sqrt{p}_k \boldsymbol{M}_k^{-1}\boldsymbol{A}_k$ and $\text{SEE}_{out} = \text{SEE}(\tilde{\boldsymbol{p}}, \tilde{\boldsymbol{\gamma}}, \boldsymbol{C})$;
until $|\text{SEE}_{out} - \text{SEE}_{in}| < \epsilon$

Proposition 3: *Algorithm 3 monotonically increases the SEE value and converges in the value of the objective.*

Proof: Based on Propositions 1 and 2, we can infer that Algorithm 3 increases the SEE function in each step. Thus, since the SEE function has a finite maximizer, Algorithm 3 eventually converges in the value of the objective. ■

Computational Complexity: Neglecting the complexity of computing the closed-form receive filters in $\boldsymbol{C}$, the complexity of Algorithm 3 is obtained recalling that pseudo-concave maximizations with n variables can be restated as concave maximization with $n+1$ variables and thus their complexity is polynomial in $n+1$ [20]. So, RIS and power optimization have complexity $(N+1)^\alpha$ and $(K+1)^\beta$, respectively[2], and thus the complexity of Algorithm 3 is $\mathcal{C}_1 = \mathcal{O}\left(I_1\left(I_{\gamma,1}(N+1)^\alpha + I_{p,1}(K+1)^\beta\right)\right)$ with $I_{\gamma,1}$, $I_{p,1}$ and I_1 the number of iteration for Algorithms 1, 2, 3 to converge.

IV. Numerical Analysis

For the numerical analysis, we set $K = 4$, $N_B = 4$, $N = 100$, $B = 20\,\text{MHz}$, $P_0 = 30\,\text{dBm}$, $P_{0,RIS}^{(a)} = 20\,\text{dBm}$, and $P_{c,n}^{(p)} = 0\,\text{dBm}$. The noise spectral density is $-174\,\text{dBm/Hz}$ with a receive noise figure of 5 dB. Mobile users are distributed within a 30 m radius, maintaining a minimum distance of $R_n = 20\,\text{m}$ from the RIS. Bob is positioned 20 m away from the RIS, while Eve represents any potential eavesdropping node within a 30 m radius from Bob. Mobile users are paced at a height from 0 to 2.5 m, whereas both the RIS and BS are 10 m from the ground. The power decay exponents are $n_h = 4$ and $n_g =$

[2]The exponents α and β are not known, but for generic convex problems they can be bounded between 1 and 4 [21]

2. The channels undergo Rician fading, with factors $K_t = 4$ for the RIS-to-BS link and $K_r = 2$ for the user-to-RIS and RIS-to-Eve links. The RIS-to-BS channel is allocated a higher Rician factor due to its static positioning, which bolsters the Line of Sight (LOS) component. Fig. 1 shows the achieved SEE versus $P_{t,max}$, comparing the optimal SEE with statistical CSI (SEE Max - sCSI) and perfect CSI (SEE Max - pCSI), the SEE obtained by the resource allocation which maximizes the secrecy rate with statistical CSI (SEE with SSR Max - sCSI) and perfect CSI (SEE with SSR Max - pCSI), and the SEE obtained with random power and RIS allocation with statistical CSI (w/o Opt - sCSI) and perfect CSI (w/o Opt - sCSI). It is seen that the proposed scheme largely outperforms the case in which no resource allocation is performed and that the lack of CSI does not cause detrimental SEE degradation. A similar scenario is shown in Fig. 2, with the difference that the secrecy rate is shown. Similar remarks as for Fig. 1 hold, except that, for high P_{max}, not optimizing the RIS coefficients provides a higher secrecy rate than optimizing the RIS with statistical CSI.

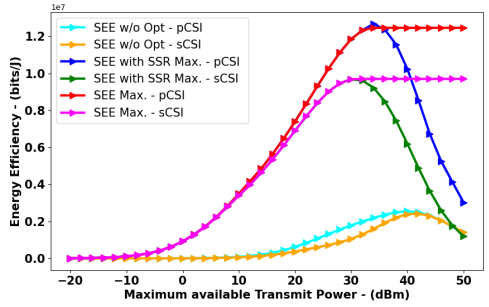

Fig. 1. SEE versus $P_{t,max}$. $K = 4$, $N_B = 4$, $N_E = 1$, $N = 100$, $n_h = 4, n_g = 2$.

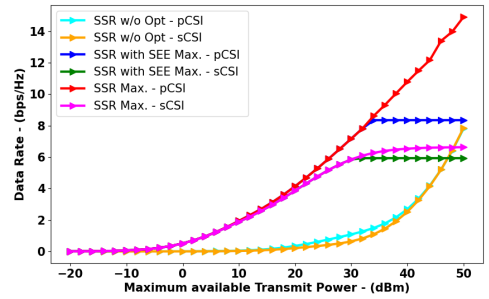

Fig. 2. Secrecy Sum Rate versus $P_{t,max}$. $K = 4$, $N_B = 4$, $N_E = 1$, $N = 100$, $n_h = 4, n_g = 2$.

V. Conclusion

This work has proposed a provably convergent and low complexity optimization algorithm for the maximization of the SEE in the uplink of a wireless network aided by an RIS. The analysis has shown that the lack of perfect CSI as to the eavesdropper's channel from the RIS does not cause significant SEE degradation.

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