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# DDPG Performance in THz Communications over Cascaded RISs: A Machine Learning Solution to the Over-Determined System

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Abstract—THz technology is considered a key element in 6G wireless communication because it provides ultra-high bandwidths, considerable capacities, and significant gains. However, wireless systems operating at high frequencies are faced with uncertainty and highly dynamic channels. Reflecting intelligent surfaces (RISs) can increase the range of the THz communication links and boost the rate at the receiver. In contrast to the existing literature, we investigate the scenario of multiple access multi-hop (cascaded) RISs uplink THz networks in a correlated channel environment. We show that our inspected cascaded RIS system is over-determined and that the rate maximization optimization problem is non-convex. To this end, we derive a closed-form expression of the received power and derive an analytical solution based on pseudo-inverse to obtain optimum RISs' phase shifts that maximize the received signal power and hence increase the rate. In addition, we utilize deep reinforcement learning (DRL), which is capable of solving non-convex optimization problems, to obtain the optimum cascaded RISs' phase shifts at the receiver taking into account the situation of the spatially correlated channels. Simulation results demonstrate that the DRL algorithm achieves higher rates than the mathematical sub-optimal method and the case of randomized phases.

Index Terms—Wireless Communication, 5G, 6G, RIS, THz, Machine Learning, Deep Reinforcement learning.

# I. Introduction

THZ frequency bands (100 GHz - 10 THz) are considered cornerstones in the 6G communication networks. THz frequencies are favorable to support ultra-high bandwidths and significant data rates. These frequency bands can potentially provide considerable performance gains and significant capacities. Nonetheless, the transition towards the real and practical implementation of THz networks suffers from molecular losses, highly dynamic and varying channels, short-range links and communication distances, and the reliance on line-of-sight (LOS) or narrow-beam links [1], [2]. To optimize the achievable data rate at the receiver  $(R_x)$ , this research paper examines the reflecting intelligent surface (RIS) as a modern technology and promising solution. The RIS

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is a two-dimensional (2D) electromagnetic surface, precisely metasurface, that constitutes a large number of semi-passive scattering elements. Every element can be controlled via a software-defined behavior to adjust the electromagnetic properties (i.e. phase-shift) of the reflection of the incident radio frequency (RF) signals upon the RIS elements [3], [4]. Thus, the RIS can instantly amend the wireless propagation channel to improve the signal transmission, boost the received signal power, and suppress the interference at the  $R_x$ . Therefore, it improves the data rate in a cost-effective and energy-efficient behavior and provides an innovative means to attain the 6G Key performance indicators (KPIs) [5], [6].

Several research papers inspected the deployment of RIS in THz networks to investigate its power in boosting the coverage and improving the achievable data rate at the  $R_x$ [7]–[16]. However, the following research studies [7]–[14] utilized mathematical methods to solve their optimization problems, whereas the research papers in [15], [16] employed the deep reinforcement learning (DRL) method to solve the joint design of the digital beamforming at the base station (BS) and the analog beamforming at the RISs to combat the propagation attenuations and molecular absorptions in downlink broadcast THz system, which is a Base station (i.e. single source) to multi-destination (i.e. users) scenario. To the best of our knowledge, none of the studies in the literature utilized the DRL technique to determine the solution to the over-determined system of equations for the scenario of multiple access multi-hop RIS uplink THz system, which is multiple sources(i.e. users) to the same destination (i.e.  $R_x$ ).

In this study, we examine the above-mentioned gap in the literature by employing a DRL method, namely DDPG (deep deterministic policy gradient (DDPG), to jointly obtain the optimum RISs phase-shifts in the multi-hop RIS scenario to maximize the received power for user 1 at the  $R_x$ . The main challenge in our design while finding the optimum phases at RIS<sub>1</sub> and RIS<sub>2</sub> jointly lies in the non-convexity because of the constant modulus constraints of the RIS elements, and computationally intractable cascaded RIS links. Thus, the optimal solution to this optimization problem is not known, and it is not feasible to find an analytical solution using mathematical techniques. Further, employing the exhaustive search isn't practical for large-scale networks because of

it is high complexity [15], [16]. Therefore, to solve this optimization problem, we leverage a DRL method, namely the DDPG algorithm, to find out the possible solutions.

## A. Contributions

Our contributions to this research paper can be summarized as follows:

- We formulate the multi-hop RIS correlated channel system that operates in the THz frequency range under the scenario of two transmitting users.
- We formulate user 1's rate optimization problem by jointly optimizing the phase shifts at RIS<sub>1</sub> and RIS<sub>2</sub> while the second user is considered an interferer and we show that the problem is non-convex.
- We derive a closed-form expression of the received power of the first user under the cascaded RIS correlated channel scenario and we show that the system is overdetermined.
- We find a suboptimal solution to the over-determined system to find cascaded RIS phases that maximize the received power.
- We leverage DDPG to solve the optimization problem which is non-convex and computationally intractable. Moreover, we reveal the performance of DDPG by solving the same problem with a sub-optimal mathematical method such as pseudo-inverse and comparing the performance of DDPG with the mathematical technique.
- We simulate our suboptimal and DDPG solutions and demonstrate that the DDPG algorithm is superior to the sub-optimal mathematical method, and the random generation case.

# II. COMMUNICATION SYSTEM MODEL

In our system model, we consider a static topology in Fig. 1 where there are two users, transmitter 1  $(T_{x_1})$  and transmitter  $2 (T_{x_2})$  communicating with the  $R_x$ , via two multi-hop RISs. Both users and the  $R_x$  are furnished with high parabolic directional antennas, and they are transmitting to the center of the RIS<sub>1</sub>, with diameter  $D_t$  for the two transmitters and  $D_r$  for the  $R_x$ . The distances between user 1 and RIS<sub>1</sub>, user 2 and RIS<sub>1</sub>, RIS<sub>1</sub> and RIS<sub>2</sub>, and RIS<sub>1</sub> and  $R_x$  are represented as  $r_{11}$ ,  $r_{12}$ ,  $r_{2}$ , and  $r_{3}$  respectively, whereas the horizontal distances between user 1 and RIS<sub>1</sub>, user 2 and RIS<sub>1</sub>, RIS<sub>1</sub> and RIS<sub>2</sub>, and RIS<sub>2</sub> and  $R_x$  are denoted as  $r_{11,h}$ ,  $r_{21,h}$ ,  $r_{2,h}$ , and  $r_{3,h}$  respectively. The heights of the two users  $T_{x_1}$ , and  $T_{x_2}$ , RIS<sub>1</sub>, RIS<sub>2</sub>, and  $R_x$  are represented as  $h_{T_{x_1}}$ ,  $h_{T_{x_2}}$ ,  $h_{s_1}$ ,  $h_{s_2}$ , and  $h_r$  respectively. The number of elements for RIS<sub>1</sub> and RIS<sub>2</sub> is denoted as  $V = V_x \times V_y$  and  $W = W_x \times W_y$  elements respectively. Every RIS is furnished with a controller that determines the perfect knowledge of the channel state information (CSI). The channel model between each transmitter u and RIS<sub>1</sub>, and between RIS<sub>2</sub> and the  $R_x$ , follow the rician fading model which is represented as:

$$\mathbf{h_{t,u}} = \sqrt{\frac{K1}{K1+1}} \mathbf{\tilde{h}_{t,u}} + \sqrt{\frac{1}{K1+1}} \mathbf{\tilde{h}_{t,u}}, \tag{1}$$

$$\mathbf{h_r} = \sqrt{\frac{K2}{K2+1}} \bar{\mathbf{h_r}} + \sqrt{\frac{1}{K2+1}} \tilde{\mathbf{h_r}}, \tag{2}$$

where  $\mathbf{h_{t,u}}$  is the channel between each user u and RIS<sub>1</sub>, K1 is the rician factor of  $\mathbf{h_{t,u}}$ . Further, the LOS component for the channel  $\mathbf{h_{t,u}}$  is represented as  $\mathbf{\bar{h}_{t,u}} \in C^{1\times V}$ , and the non-LOS (NLOS) component is represented as  $\mathbf{\tilde{h}_{t,u}} \in C^{1\times V}$ . Similarly, for the  $R_x$  channel  $\mathbf{h_r}$ ,  $K_2$  is the rician factor, the LOS component is represented as  $\mathbf{\bar{h}_r} \in C^{W\times 1}$ , and the NLOS component is represented as  $\mathbf{\bar{h}_r} \in C^{W\times 1}$ .

Moreover, the channel between RIS<sub>1</sub> and RIS<sub>2</sub>,  $\mathbf{h}_{v,w} \sim \mathcal{CN}(0,\mathbf{R})$ , is spatially correlated and it follows the Rayleigh fading model, where  $\mathbf{R}$  represents the covariance matrix, which is obtained based on the model of the exponential spatial correlation. This is controlled by the correlation factor among the adjacent reflecting units  $\rho \in [0,1]$ , which is represented as:

$$[\mathbf{R}]_{v,w} = \rho^{|v-w|} e^{|v-w|\xi} \tag{3}$$

where  $\xi$  denotes the angle of arrival. Increasing values of  $\rho$  enhances the correlation among the elements of the channel  $\mathbf{h_{w,v}}$ . In practical cases, the value of the correlation factor  $\rho$  is less than 1, and thus, the correlations happen among the adjacent elements with considerably reduced correlation at huge distances.

### III. END-TO-END RATE DERIVATION

In our scenario, the two users are sending their signals at  $RIS_1$  from different distances and angles covering all the elements of  $RIS_1$ . The reflected power from the  $v_{th}$  reflecting element of the at  $RIS_1$  can be expressed as [17].

$$P_{r,v}^{u} = \left(\frac{\lambda}{4\pi}\right)^{2} \frac{G_{t,u}G(\theta_{i1,u})G(\theta_{r,1})}{r_{tu}^{2}} \times |h_{t,uv}|^{2} |\gamma_{v}|^{2} P_{t}, \quad (4)$$

where  $G_{t,u}$  represents the Tx antenna gain of transmitter  $T_{x_u}$ ;  $G(\theta_{i1,u})$  and  $G(\theta_{r,1})$  denote the gain of the reflecting element from the incident and reflection angles respectively;  $\gamma_v = \gamma e^{-j\alpha_v}$  symbolizes the reflection coefficient of the  $v^{th}$  reflecting element of RIS<sub>1</sub>; and  $r_{t,u}$  denotes the distance between user u and the RIS<sub>1</sub> reflecting element v. Similarly, the reflected power from the  $w^{th}$  reflecting element of RIS<sub>2</sub> due to being illuminated by the signal reflected by the  $v^{th}$  reflecting element of RIS<sub>1</sub> is

$$P_{r,vw}^{u} = \left(\frac{\lambda}{4\pi}\right)^{4} \frac{G_{t,u}G(\theta_{i1,u})G(\theta_{r,1})G(\theta_{i,2})G(\theta_{r,2})}{r_{tu}^{2}r_{2}^{2}} \times |h_{t,uv}|^{2}|\gamma_{v}|^{2}|h_{vw}|^{2}|\gamma_{w}|^{2}P_{t},$$
(5)

where  $h_{vw}$  represents the (v,w) element of the RIS<sub>1</sub>-RIS<sub>2</sub> channel matrix  $\mathbf{H}$ ,  $\gamma_w = \gamma e^{-j\varphi_w}$  symbolizes the reflection coefficient of the  $w^{th}$  reflecting element RIS<sub>2</sub>. Finally, the

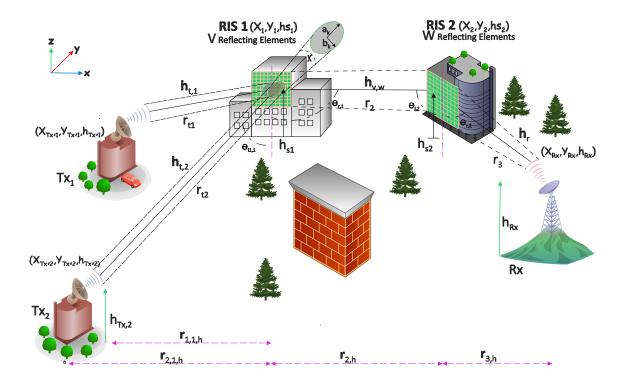


Figure 1: Communication System Model.

received captured power at the  $R_x$  through channel  $h_{vw}$  can be written as follows:

$$P_{rx,vw}^{u} = \left(\frac{\lambda}{4\pi}\right)^{2} \frac{P_{r,vw}^{u}}{r_{3}^{2}} G_{r} |h_{rw}|^{2}.$$
 (6)

$$P_{rx,vw}^{u} = \left(\frac{\lambda}{4\pi}\right)^{6} \frac{G_{t,u}G(\theta_{i1,u})G(\theta_{r,1})G(\theta_{i,2})G(\theta_{r,2})G_{r}}{r_{tu}^{2}r_{2}^{2}r_{3}^{2}} \times |h_{t,uv}|^{2}|\gamma_{v}|^{2}|h_{vw}|^{2}|\gamma_{w}|^{2}|h_{rw}|^{2}P_{t},$$
(7)

Further, user u's total received power at the  $R_x$  is expressed as [17]

$$P_{Rx}^{u} = |\sqrt{L_{\tau,u}} \sum_{v=1}^{V} \sum_{w=1}^{W} |h_{t,uv}| |\gamma| |h_{vw}| |\gamma| |h_{rw}|$$

$$e^{-j(\psi_{t_{u_v}} + \alpha_v + \psi_{vw} + \varphi_w + \psi_{r_w} + \beta_U + \beta_3))} |^2 P_t,$$
(8)

where  $\psi_{tu_v}$  is the phase for the transmitter channel for user u and  $v^{th}$  reflecting element,  $\psi_{vw}$  is the phase for the  $\mathbf{h}_{v,w}$  channel for  $v^{th}$  and  $w^{th}$  reflecting element,  $\psi_{r_w}$  is the phase for the  $R_x$  channel for  $w^{th}$  reflecting element,  $|\gamma|$  is assumed to equal 1.

 $eta_U$  and  $eta_3$  designate the deterministic phases corresponding to the traveled distance between each user u to RIS $_1$  over the first hop, and the traveled distance between RIS $_2$  and the  $R_x$  over the third hop. These phases are designated as follows:

$$\beta_u = 2\pi \times r_{t_u}/\lambda.$$

$$\beta_3 = 2\pi \times r_3/\lambda.$$
(9)

$$L_{\tau, u} = L_{\text{FSPL}, u} \times L_{\text{absorption}} \tag{10}$$

 $L_{
m absorption}$  designates the absorption losses according to [18], and  $L_{
m FSPL,u}$  represents the free space path loss for each user u, and it is written as:

(8) 
$$L_{FSPL,\tau,u} = \left(\frac{\lambda}{4\pi}\right)^6 \frac{G_{t,u}G(\theta_{i1,u})G(\theta_{r,1})G(\theta_{i,2})G(\theta_{r,2})G_r}{r_{tu}^2 r_2^2 r_3^2}$$
(11)

Therefore, equation (8) can be expressed as below:

$$P_{Rx}^{u} = |\sqrt{L_{\tau,u}} \sum_{v=1}^{V} \sum_{w=1}^{W} |h_{t,uv}| |h_{vw}| |h_{rw}|$$

$$e^{-j(\psi_{t_{u_v}} + \alpha_v + \psi_{vw} + \varphi_w + \psi_{r_w} + \beta_U + \beta_3)})|^2 P_t,$$
(12)

The total received power for the first user can be maximized by solving the following system of equations:

$$\alpha_v + \varphi_w + \psi_{t_{1_v}} + \psi_{vw} + \psi_{r_w} + \beta_1 + \beta_3 = \mathbf{C}, \quad \forall v, w.$$
 (13)

where  ${\bf C}$  designates any constant value. This means that the power  $P^u_{Rx}$  is maximum when  ${\bf C}$  is equal to constant  $\forall v,w$ . In this research paper, we will select  ${\bf C}=0$ . Hence, equation (13) represents an over-determined system of equations with V+W unknowns, and  $V\times W$  equations. This problem is almost always inconsistent and it has no solution. Nonetheless, we will solve this problem using machine learning (ML) and specifically the DRL method to obtain the unknowns  $\alpha_v$  and  $\varphi_w$ , calculate the received power for the first user, and then compare the results to the sub-optimal solution obtained from the mathematical technique pseudo inverse.

1) Moore-Penrose Pseudo Inverse Method: The Moore-Penrose pseudo-inverse solution for the over-determined system is expressed as follows:

$$\mathbf{M}\mathbf{\Phi} = \mathbf{K},\tag{14}$$

where  $\Phi$  with dimensions  $(V+W)\times 1$  is the matrix that represents RIS<sub>1</sub> and RIS<sub>2</sub> phase shifts,  $\mathbf{M}$  with dimensions  $(V\times W)\times (V+W)$  represents the binary matrix, and  $\mathbf{K}$  with dimensions  $(V\times W)\times 1$  represents the matrix containing constant values such as the phase shifts of the transmitter channel  $\mathbf{h}_{t,u}$ , the phase shifts of the channel between RIS<sub>1</sub> and RIS<sub>2</sub>  $\mathbf{h}_{\mathbf{v},\mathbf{w}}$ , and the phase shifts of the  $R_x$  channel  $\mathbf{h}_r$ .

$$\mathbf{M}^{+} = (\mathbf{M}^{\mathbf{T}}\mathbf{M})^{-1}\mathbf{M}^{\mathbf{T}},\tag{15}$$

where  $\mathbf{M}^+$  is pseudo-inverse of a matrix  $\mathbf{M}$ . Thus, the pseudo-inverse solution  $\Phi$  is expressed as

$$\mathbf{\Phi} = \mathbf{M}^{+} \mathbf{K} \tag{16}$$

Moreover, the received signal-to-noise ratio (SINR for)  $T_{x_u}$  at the  $R_x$  can be written as::

$$\Omega_u = \frac{P_{Rx}^u}{\sum_{\substack{i=1\\i \neq u}}^{U} P_{Rx}^i + \sigma^2}.$$
 (17)

Therefore, the data rate of user u is designated as:

$$R_u = \log_2(1 + \Omega_u). \tag{18}$$

Our goal in this work is to obtain the values of the RIS<sub>1</sub> and RIS<sub>2</sub> phase shifts that maximize the rate for user 1. Accordingly, the formulated problem at RIS<sub>1</sub> and RIS<sub>2</sub> is to obtain the phase shift matrices  $\alpha_v$  and  $\varphi_w$   $\forall v, w$  that maximizes  $R_1$ , and it is written as:

$$\max_{\alpha, \varphi} \sum_{u=1}^{U} \log_2 (1 + \Omega_1),$$

$$s.t.$$

$$C1 : |\gamma_v|^2 = 1, \forall v \in \{1, 2, ..., V\},$$

$$C2 : |\gamma_w|^2 = 1, \forall w \in \{1, 2, ..., W\},$$

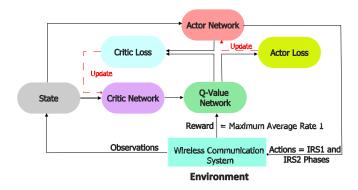


Figure 2: DDPG Model.

The solution to the optimization problem is non-trivial, it is an NP-hard problem, because of constant modulus constraints of RIS<sub>1</sub> and RIS<sub>2</sub> reflecting elements that make the problem non-convex. Thus, it is nearly not possible to find out a mathematical solution for the cascaded RIS optimization problem. To solve it, we utilize the DRL method, namely DDPG, rather than solving the challenging problem mathematically. The proposed DDPG scheme details are given in section IV.

# IV. PROPOSED DDPG SCHEME BASED RISS'PHASES CONTROL

DDPG is a model-free RL method that merges the merits of both the policy gradients and Q-learning algorithms. Taking into consideration that the states in our scenario are dependent on the output sum rate and channel gains, while the actions are the RIS phase shifts, we are considering a continuous action and a continuous state system. Thus, we chose to use DDPG since its main advantage arises from the fact that it utilizes both the continuous state and action spaces.

The DDPG algorithm consists of several vital elements. These elements include the agents operating in our communication system model which are the RIS<sub>1</sub> and RIS<sub>2</sub>, the states  $\mathbf{s}^{(T)}$  represented by  $\mathbf{h}_{t,u}^{(T)}$ ,  $\mathbf{h}_{v,w}^{(T)}$ ,  $\mathbf{h}_{r}^{(T)}$ , and the rate for user 1 of the previous state  $R_{1}^{(T-1)}$ , the reward  $\mathbf{r}^{(t)}$  which is the rate for user 1  $R_{1}^{(T)}$  at the current state, the action  $\mathbf{a}^{(t)}$  which is represented by the phases of the RIS<sub>1</sub> and RIS<sub>2</sub>, the policy function  $\mu$ , and the Q-value function  $Q(\mathbf{s}, \mathbf{a}|\theta^Q)$  which measures how good is the action. The goal of this research paper is to improve the average rewards including the instant and future rewards. The DDPG algorithm consists of four neural networks that include the actor-network, the critic network, the target critic network, and the target actor-network to increase stability in the system.

# A. DDPG Algorithm Framework

The goal of the DDPG scheme is to train the agents RIS<sub>1</sub> and RIS<sub>2</sub> to take actions that maximize the long-term average reward, which is in our system the rate of user 1 via the environment changes as shown in Fig. 2 taking into consideration the constant modulus constraints mentioned

# Algorithm 1 DDPG Algorithm-based Framework

- 1: Algorithm Initialization: Set the timestep T=0 and initialize the reply buffer of the DDPG agent  $\mathcal{D}$  with capacity M.
- 2: Initialize the weights of the critic networks  $\theta^Q$ , and actor networks  $\theta^{\mu}$  randomly.
- 3: Initialize target network parameters:  $\theta^{Q'} \leftarrow \theta^{Q}$ , and  $\theta^{\mu'} \leftarrow \theta^{\mu}$ .
- 4: for T=1 to  $\infty$  do
- Observe the state  $\mathbf{s}^{(T)}$  and select an action with exploration OU noise  $\mathbf{a}^{(T)} = \mu(\mathbf{s}^{(T)}|\theta^{\mu}) + \mathbf{n}_T$ .
- Execute the action  $\mathbf{a}^{(T)}$  at RIS<sub>1</sub> and RIS<sub>2</sub>.
- Receive the immediate reward  $r^{(T)}$ , observe the next state  $s^{(T+1)}$ , and store the transition  $(\mathbf{a}^{(T)}, \mathbf{s}^{(T)}, r^{(T)}, \mathbf{s}^{(T+1)})$  in the replay memory D.
- Sample the mini-batch transitions from  $\mathcal{D}$  randomly:  $B \leftarrow$  $\{(\mathbf{s}^{(i)}, \mathbf{a}^{(i)}, r^{(i)}, \mathbf{s}^{(i+1)})\} \in \mathcal{D}.$
- Calculate the target Q-value:  $\tilde{Q}(\mathbf{s}^{(i)},\mathbf{a}^{(i)}|\theta^{Q'}) = r^{(i)} +$  $\Gamma Q(\mathbf{s}^{(i+1)}, \mu(\mathbf{s}^{(i)}|\theta^{\mu'})|\theta^{Q'})$  where  $\Gamma$  is the discount factor.
- Update the parameters  $\theta^Q$  in the critic network by minimizing the loss using the obtained target Q-value. L= $\frac{1}{|B|} \sum_{i=1}^{|B|} (\tilde{Q}(\mathbf{s}^{(i)}, \mathbf{a}^{(i)} | \theta^{Q'}) - Q(\mathbf{s}^{(i)}, \mathbf{a}^{(i)} | \theta^{Q}))$
- Update the parameters  $\theta^{\mu}$  in actor-network based on the

sampled policy gradient:  $\nabla_{\theta\mu} \boldsymbol{J} \approx \frac{1}{|B|} \sum_{i=1}^{|B|} \nabla_a Q(\mathbf{s}^{(i)}, \mathbf{a}^{(i)} | \theta^Q) \nabla_{\theta\mu} \mu(\mathbf{s}^{(i)} | \theta^\mu)$  Update the target actor and critic networks using the soft updates  $\tau$  to increase the learning stability:  $\theta^{Q'}_{\phantom{Q'}}\leftarrow \tau\theta^Q+(1-\tau)\theta^{Q'}_{\phantom{Q'}}$ 

$$\theta^{Q'} \leftarrow \tau \theta^{Q} + (1 - \tau)\theta^{Q}$$
$$\theta^{\mu'} \leftarrow \tau \theta^{\mu} + (1 - \tau)\theta^{\mu'}$$

13: **end for** 

in eq 19. The agents modify the randomized phase shift matrices, and the policy in a way that copes with the random environmental statistical behavior to maintain a long-term average reward, instead of an immediate response to the channel random changes. The DDPG algorithm-based framework is shown in algorithm 1.

# V. NUMERICAL RESULTS

In this section, we assess the performance of the DRL-based multi-hop RIS in THz networks. To demonstrate the performance of the DDPG algorithm in our system, we compare the results generated by DDPG with the pseudo inverse solution, and with those generated by using random phases. The default simulation parameters in our system are revealed in Table I. We define the term distance ratio as the ratio between the distance between user 1 and RIS<sub>1</sub>  $r_{t1}$ , and the distance between user 2 and RIS<sub>1</sub>  $r_{t2}$ . Numerical results for the data rates are calculated for 2 users and 1000 Monte-Carlo simulations.

We reveal the results for maximizing the received power for the first user at the  $R_x$  by plotting the rate for the first user versus the distance ratio between the two users using DDPG, and pseudo-inverse methods. Fig. 3 shows a comparison between the results generated by DDPG, pseudo-inverse, and the case of randomized phases (i.e. without optimization) for a correlation factor equal to 0.9. It is clear from the figure that as the distance ratio increases the rate decreases because the interference between user 1

Table I: Parameters Used in Simulation

Simulation Parameters	Values
Number of Users $(U)$	2
The Speed of light c	$3 \times 10^{8}$
Carrier Frequency f	$300 \times 10^{9}$
Number of antennas per transmitter $N_t$	1
Number of antennas at the $R_x N_r$	1
Wavelength $(\lambda)$	$1 \times 10^{-3}$
Number of RIS 1 Reflecting Elements (V)	18
Number of RIS <sub>2</sub> Reflecting Elements (W)	18
X-axis of RIS <sub>1</sub> $x_{r1}$	5
Y-axis of RIS <sub>1</sub> $y_{r1}$	10
height of RIS <sub>1</sub> $h_{r1}$	12
X-axis of RIS <sub>2</sub> $x_{r2}$	10
Y-axis of RIS <sub>2</sub> $y_{r2}$	10
height of RIS $_2$ $h_{r2}$	12
Distance between User 1 and RIS <sub>1</sub>	3 to 15
Distance between User 2 and RIS <sub>1</sub>	15
Heights of User 1 and User 2 $h_t$	5
RIS <sub>1</sub> and RIS <sub>2</sub> Reflection Coefficients $\alpha$	1
RIS <sub>1</sub> and RIS <sub>2</sub> half-power Spacing $d_x$	$\lambda/2$
$RIS_1$ and $RIS_2$ Element Spacing $d_y$	$\lambda/2$
Antenna diameter in meters $D_t$	0.12
X-axis of Rx $x_{rx}$	20
Y-axis of Rx $y_{rx}$	0
height of Rx $h_r$	5
Bandwidth	$2 \times 10^9 \text{ MHz}$
Noise power spectral density $N_{PSD}$	−174 dB/Hz
Noise figure at the $R_X$ $F_{dB}$	10
Average Noise power in dB N0	-174 dB/Hz
Noise power in linear scale no	$7.9621 \times 10^{-11}$
Transmitters to RIS <sub>1</sub> Path loss exponent	2 2
RIS <sub>2</sub> to $R_x$ Path loss exponent	_
Rician Factor	10
Coefficient of Soft Updates $ au$	$1 \times 10^{-3}$
Batch size	$\frac{128}{10^5}$
Replay Buffer Capacity C	
Number of episodes	10000
Critic-Network learning rate	$3 \times 10^{-4}$
Actor-Network learning rate	$1 \times 10^{-4}$
Target Critic-Network learning rate	$3 \times 10^{-4}$
Target Actor-Network learning rate	$1 \times 10^{-4}$
Discount factor of the future reward $\Gamma$	0.99

and user 2 increases. Further, DDPG achieves higher rates than that of the pseudo-inverse, and randomized phases case. Moreover, Fig. 4 reveals the rates for the DDPG scheme versus the distance ratio for different correlation factors. It is obvious that when the correlation factor  $\rho$ increases, the data rates for the DDPG scheme increase. The reason for that, increasing the correlation factor value, will increase the learning efficiency of the DDPG scheme. Therefore, the DDPG algorithm attains higher data rates than other methods especially when the correlation factor  $\rho$  is high.

# VI. CONCLUSION

In this research paper, a multiple access scenario with a multi-hop RIS uplink system is considered to overcome the short-range communications issues in THz networks, to maximize the received power for the first user. The maximization problem for the multi-hop RIS network is over-determined because it consists of a number of equations greater than the number of unknowns. Further, it is non-convex

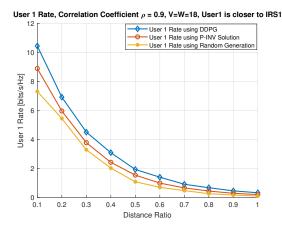


Figure 3: Rate of user 1 vs Distance ratio for correlation factor  $\rho$  equal to 0.9. V = W = 18.

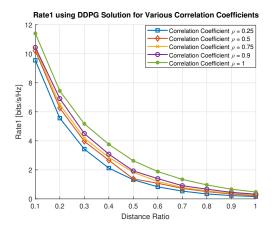


Figure 4: Rate of user 1 vs Distance ratio for various correlation factors  $\rho$ . V = W = 18.

due to the constant modulus constraints at RIS<sub>1</sub> and RIS<sub>2</sub>. To solve this problem, we utilized the DDPG scheme which possesses the ability to deal with over-determined systems and non-convex optimization problems. DDPG finds out the optimal RIS phases which in turn maximizes the received power for the first user. Numerical results reveal that DDPG attains rates higher than that of the pseudo-inverse solution and randomized phases. Furthermore, DDPG shows the importance of the correlation in the channels to optimize the learning process and attain higher data rates.

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