

Effective Vs and Vp characterization from Surface Waves streamer data along river embankments

*Original*

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(Article begins on next page)

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## Effective Vs and Vp characterization from Surface Waves streamer data along river embankments. --Manuscript Draft--

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<b>Article Type:</b>	Research Paper
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<b>Keywords:</b>	river embankments.; surface waves; seismic characterization
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<b>Order of Authors:</b>	Cesare Comina Federico Vagnon Alessandro Arato Andrea Antonietti
<b>Abstract:</b>	<p>River embankments are linearly extended earth structures built for river flood protection. Their continuity and uniformity are fundamental prerequisites to ensure and maintain their protection efficiency. Weakness points usually develop in localized areas where geotechnical variability is present in the embankment body or in the underlying subsoil. Given their significant length, and the localized nature of weakness points, the characterization of river embankments cannot therefore rely on local geotechnical investigations but requires the application of efficient and economically affordable methods, able to investigate relevant lengths in a profitable way. This is even more essential when the investigations are conducted near, or in foresee of, significant flood events, when timing of the surveys is essential. In this paper the application of a procedure (W/D procedure) for the seismic characterization of river embankments, specifically designed for surface waves streamer data, is presented. The W/D procedure allows the combined definition of 2D shear (Vs) and compressional (Vp) wave velocity models and can be developed in order to be automated as a fast imaging tool. Its application to the characterization of a test site (Bormida river embankment, Piedmont Region, Italy) is presented. It is also shown that the obtained results are comparable to standard seismic processing approaches with the advantage of reduced survey time and increased efficiency, giving preliminary results directly in the field.</p>
<b>Suggested Reviewers:</b>	John Lane jwlane@usgs.gov Referenced for the use of MASW testing over embankments.  Lutz Karl lkarl@geotomographie.de Expert in MASW testing for embankment characterization.
<b>Opposed Reviewers:</b>	
<b>Response to Reviewers:</b>	

**Dear Editor and Reviewers,**

**we would like to thank you very much for your revision of our paper. We improved (in our opinion) the previous submitted manuscript according to your comments and suggestions.**

**The main point raised by both reviewers was related to the need for more explanations with respect to the adopted W/D procedure and the way in which through this procedure also the Vp information can be extracted. We have done some more effort in this respect in order to better explain the main crucial points of the W/D procedure for the presented application.**

**Nevertheless, we have not excessively extended the explanations since the W/D procedure is clearly explained in several already published papers, all referenced. Therefore, a too detailed explanation would be only a duplication of the current available literature. We hope the reviewers will be satisfied with the proposed revisions and with the added explanations given.**

**We attached two versions of the revised manuscript: a cleaned copy and a copy with underlined revisions in order to directly visualize where in the paper we have done our modifications.**

**Hereafter, we also provide a detailed, point-by-point response to your comments and questions giving indication of the corrections performed in the text or specific motivations for not making them in the few cases where we judged differently.**

**REVIEWER 1**

Hi author and editor,

I am glad to review this manuscript. This paper presents the application of a novel processing approach (W/D procedure) to surface wave streamer data. The SW field data test shows the advantage of the W/D processing method in surface wave data. This paper is well written. I recommend accepting this manuscript with a minor review.

The following is my details comments:

1. In figure 8, the vs and vp profile look similar. How can you get the Vp result? Please add the description in the main text.

**Yes, the Vs and Vp results appear indeed similar since the Vp distribution is obtained from the Vs one with the application of the Poisson's ratio calculated from the W/D procedure (reported in Figure 8c). This last is assumed constant through the whole profile and therefore the resulting Vp velocity field is a transformation of the Vs one with similar properties. A comment was added in the paper in this respect when presenting the figure. Some comments on the implications of this assumption were already present in the discussion section of the paper.**

**The way in which the Vp information can be extracted through the W/D procedure via the apparent Poisson's ratio profile was already partially contained in the previous version of the paper. Following also the above general comment some more effort was performed in order to increase the description of the W/D procedure with respect to this point, without replicating available literature.**

2. The dashed line in the inverted velocity result indicates the depict the river embankment in figure 2. So, I suggest adding the Stratigraphic log and geotechnical description of a figure in the inverted velocity profile, such as figure 8 and figure 9.

**Thank you for the observation. Following your recommendation, the DPSH Blow Count profile was added in Figure 8 at the beginning of the survey line and some comments were addressed in the text to more specifically link the geophysical observations to the survey log.**

3. This manuscript used the Monte Carlo Inversion (MCI) algorithm to invert the 1D dispersion curves. However, there are other inversion methods, such as

FWI or dispersion wave equation method. So, I suggest citing the following reference paper in the introduction section.

**Thank you for the suggested and very interesting references. These alternative inversion strategies were referenced in the introduction section of the paper.**

Jing Li, Z Feng, G Schuster. Wave-equation dispersion inversion. *Geophysical Journal International*, 2017, 208 (3), 1567-1578.

Yudi Pan, Lingli Gao, Renat Shigapov Multi-objective waveform inversion of shallow seismic wavefields *Geophysical Journal International*, 2020, 3: 1619-1631

4. There are two figure 1 in the main text. Please correct it.

**The typo was corrected.**

5. In figure 3b, the elected high energy maxima (white asterisks) is the picked fundamental dispersion curve. Because of the effect from high-order mode, how can you pick the accurate result in the high-frequency range (>30Hz). Please add some descriptions in the main text.

**Thank you for the observation. Indeed, for some of the shots, a transition of the absolute energy maxima towards higher modes was observed in the high-frequency range (>30Hz), like in the example reported in Figure 3b as you correctly observe. Nevertheless, the fundamental mode can still be followed as local maxima thank to the adopted masking that allow to isolate the correct portion of the dispersion image to be considered for the automatic research of maxima, excluding the higher modes. A paragraph was added in the text to better clarify this procedure.**

6. The horizontal label in figure 6, depth(m/s), maybe there is some mistake.

**The typo was corrected.**

7. There are two red lines in figure 7. I do not think the right side is the fitting result. Please check it.

**Yes, the two red lines are correct since they both refer to the best fitting model determined from MCI. This model is represented both in terms of layered Vs and of Vs,z (the righthand side line you were referring). A clarification was added in the figure caption. Moreover, the figure has been better commented in the text with specific references to the colors used and to the meaning of the different profiles shown.**

## **REVIEWER 2**

Generally, the authors of this manuscript applied the surface wave inversion (called W/D relationship approach) to achieve a near-surface P- and S- wave velocity model that can be used to investigate the security and geomechanical strength of river embankments.

This manuscript is more likely a case study paper. Overall, the writing is well-prepared and clear. The objective of this study is pretty interesting and reasonable. In addition, the application of their surface wave inversion W/D approach on investigating the river embankments is valuable and economically sound.

Besides lacking a detailed description on W/D approach and the validation of final inverted Vp/Vs models, the manuscript is complete. This manuscript is also well organized. All figures are well prepared.

I have two main suggestions and several minor comments in follow.

Main suggestions/comments:

1. This manuscript is about an application of surface wave inversion using W/D relationship on a field dataset. One keypoint/highlight is the W/D relationship. However, there is no detailed description of W/D approach even they cited their previous works published in Geophysics. It shall be more convenient for readers to understand the W/D approach via reading its description in this manuscript rather than referring to their previous works.

**Following the above general comment some more efforts were performed in order to increase the description of the W/D procedure, without replicating available literature. We think that the main computation steps are now better explained and clearer. Hope that the reviewer will be satisfied with that.**

2. They finally achieved 2D inverted Vs/Vp velocity profiles for this sturdy region. However, there is no validation of such results. I strongly suggest authors perform numerical elastic waveform modeling to compare the modeled surface waves using their inverted Vs/Vp models and their observed waveforms. The numerical validation could make their work more solid and complete.

**We do not agree with the reviewer that the presented velocity sections from the W/D procedure lack in validation. Comparison is specifically made in the paper, with detailed normalized differences images, to commonly adopted methods, considered as benchmarks, for Vs and Vp sections computed from seismic data. This was also specifically mentioned in the text and commented explaining eventual differences with the benchmarks. Further comments were added in the paper to specifically recall this validation approach.**

**By applying the proposed procedure to streamer data, the final aim of the paper is indeed to obtain in a fast and economically convenient way velocity sections equivalent to standard approaches. With this respect the waveform and dispersion computation suggested by the reviewer, even if interesting, is partially out of scope of the paper being strongly time demanding for the proposed application and not directly interesting for the embankment characterization. This comparison was moreover already performed, showing very reliable results, in Khosro Anjom et al. (2019) and Teodor et al. (2020) referenced in the text.**

Some mirror suggestions

1. Abstract section

It is better to mention the application of W/D approach in the surface wave inversion. This is one highlight/keypoint of this case study manuscript.

**The W/D procedure is now explicitly mentioned in the abstract of the paper.**

2. Line 82, "W/D" The abbreviation "W/D" is not defined before its first appearance even I can find its definition at line 86.

**Thank you for the observation. The meaning of the abbreviation is now explained since its first appearance in the text.**

3. Line 81, "is proposed in this paper" Because the W/D procedure is not original developed (proposed) in this manuscript. "is propose" is not accurate and suitable here. Suggest change to "is adopted in this paper".

**The statement was corrected as suggested.**

4. Line 148, figure 3b, dispersion map To form the dispersion map, you may try multiple-channel nonlinear signal comparison ((Zheng and Hu 2017, Hu et al. 2019) to achieve a higher resolution dispersion map.

**Thank you for the suggested and very interesting references on dispersion image approaches. These alternative approaches were referenced in the paper when discussing about dispersion image extraction.**

Moreover, the measurement of dispersion curve via picking the maxima at different frequencies is better to include the measurement errors or error bars.

**As explained in the text, only a single seismic shot was recorded for each position of the streamer along the embankment. Given this acquisition approach we do not have unfortunately enough information to allow for a computation of measurement error bars. No comments were added in the text in this respect. We are available to add them if the reviewer requires them mandatory.**

Hu, H., M. Senkaya, and Y. Zheng. 2019, A novel measurement of the surface wave dispersion with high and adjustable resolution: Multi-channel nonlinear signal comparison. *Journal of Applied Geophysics*, 160,236-241.

Zheng, Y., and H. Hu. 2017, Nonlinear Signal Comparison and High-Resolution Measurement of Surface-Wave Dispersion. *Bulletin of the Seismological Society of America*, 107, no. 3,1551-1556.

5. Figure 5, "Vr" What is "Vr"? The trial random velocity?

**Vr is the Rayleigh wave phase velocity. This is now explicitly referenced in the text. Modifications were also performed to the panel a) of the figure to avoid confusion.**

6. Figure 6.

I do not understand how to estimate the apparent Poisson ratio from Figure 6 and line 210 - 214. From my understanding, the W/D relationship could be directly transformed from the dispersion curve  $V_{Vss}(ff)$  at different frequencies. How to connect the Poisson ratio to W/D and  $V_{Vss}$ ? I am confused about this point.

I strongly suggest adding some mathematical descriptions on conducting the W/D relationship and Figure 6, in this section or in the appendix section, rather than just cite their previous works published in *Geophysics*, 2017.

**Please see the answer to your main comment 1.**

# 1 **Effective Vs and Vp characterization from Surface Waves streamer** 2 **data along river embankments.**

3

4 Comina C.<sup>1</sup>, Vagnon F.<sup>1</sup>, Arato A.<sup>2</sup>, Antonietti A.<sup>2</sup>5 <sup>1</sup>Dipartimento di Scienze della Terra, Università degli studi di Torino, Torino (IT)6 <sup>2</sup>Techgea S.r.l., Torino (IT).

7

8

## 9 **ABSTRACT**

10

11 River embankments are linearly extended earth structures built for river flood protection. Their  
12 continuity and uniformity are fundamental prerequisites to ensure and maintain their protection  
13 efficiency. Weakness points usually develop in localized areas where geotechnical variability is  
14 present in the embankment body or in the underlying subsoil. Given their significant length, and the  
15 localized nature of weakness points, the characterization of river embankments cannot therefore  
16 rely on local geotechnical investigations but requires the application of efficient and economically  
17 affordable methods, able to investigate relevant lengths in a profitable way. This is even more  
18 essential when the investigations are conducted near, or in foresee of, significant flood events, when  
19 timing of the surveys is essential. In this paper the application of a procedure (W/D procedure) for  
20 the seismic characterization of river embankments, specifically designed for surface waves streamer  
21 data, is presented. The W/D procedure allows the combined definition of 2D shear (Vs) and  
22 compressional (Vp) wave velocity models and can be developed in order to be automated as a fast  
23 imaging tool. Its application to the characterization of a test site (Bormida river embankment,  
24 Piedmont Region, Italy) is presented. It is also shown that the obtained results are comparable to  
25 standard seismic processing approaches with the advantage of reduced survey time and increased  
26 efficiency, giving preliminary results directly in the field.

27

## 28 **Article Highlights:**

- 29 • Effective Vs and Vp information are extracted from surface waves streamer data;
- 30 • An automated procedure for the seismic characterization of river embankments was  
31 developed;
- 32 • The procedure is demonstrated comparable to standard seismic processing approaches;
- 33 • Advantages in survey time and efficiency is highlighted.

34

35 **Keywords:** surface waves, seismic characterization, river embankments.36 **Corresponding author:** Cesare Comina, [cesare.comina@unito.it](mailto:cesare.comina@unito.it)

37

## 38 1. INTRODUCTION

39 River embankments are linearly extended earth structures constructed to serve as flood control  
40 systems during large rain events. A proper characterization of the embankment body is essential to  
41 verify its uniformity and to monitor the occurrence of possible integrity losses which could  
42 undermine its stability. In recent years, frequency and magnitude of extreme flood events have been  
43 rapidly increasing in Central America, Southern Europe, and in Italy because of climate change.

44 Moreover, the poor maintenance of hydraulic structures, ~~which~~ mostly ~~are~~ reaching their design  
45 service life, makes the adoption of specific interventions of paramount international relevance.

46 Given the significant length extension of these structures, and the localized nature of weakness  
47 points, the characterization cannot rely only on local geotechnical investigations but requires the  
48 application of efficient and economically affordable methods, able to investigate the whole  
49 embankments in a profitable way. Moreover, geotechnical investigations usually require invasive  
50 procedures (such as boreholes, penetration tests, etc) that are both expensive and time-consuming.  
51 With this respect non-invasive, rapid and cost-effective methods are desirable to identify higher  
52 potential hazard zones.

53 Among the available non-invasive geophysical methods (Chao et al., 2006; Bergamo et al., 2016;  
54 Takahashi et al., 2014; Sentenac et al., 2018), the seismic ones have peculiar advantages for the soil  
55 characterization. Seismic velocities, and particularly shear wave velocity (Vs), are directly related  
56 to the dynamic stiffness of the material, which is an important mechanical parameter for the  
57 recognition of soil layers. Moreover, in the field of geotechnical engineering, huge research effort  
58 has been spent on the correlation of Vs to parameters obtained from standard geotechnical tests. Site  
59 specific and general correlations exist to porosity, plasticity index, to the shear modulus at higher  
60 strains and to standard geotechnical in situ tests such as cone penetration, standard penetration and  
61 dilatometer tests (e.g. Kramer, 1996; Samui, 2010; Foti et al., 20014).

62 Among the seismic methods the multichannel analysis of surface waves (MASW), based on the  
63 Rayleigh wave dispersion curve (DC) analysis, is considered the most effective for the  
64 determination of Vs profiles. This method can be efficiently applied to seismic streamer data  
65 dragged along embankments and overall linear earth structures. This allows the determination of  
66 several Vs profiles to offer an almost 2D representation of the velocity field. Several literature  
67 applications of this methodology are available along embankments, river dykes and earth dams (e.g.  
68 Lutz et al., 2011; Lane et al., 2008; Min and Kim, 2006). Eventually, MASW surveys can be used  
69 in combination with geoelectrical and geotechnical methods to allow for more complete  
70 characterization (e.g. Samyn et al., 2014; Busato et al., 2016; Bièvre et al., 2017; Rahimi et al.,  
71 2018; Arato et al. 2020).

72 The main limitations of this methodology are related to the high non-linearity of the DC inversion  
73 procedure and to the lack of compressional wave velocity ( $V_p$ ) information. Several global  
74 inversion approaches have been proposed for the DC inversion (e.g. [Socco and Boiero, 2008](#)), with  
75 the aim of tackling the problem of non-uniqueness of the solution. More elaborated inversion  
76 strategies for reconstructing 2D shear wave velocity sections including waveform information (e.g.  
77 wave-equation dispersion inversion (WD), Li et al., 2017, or multi-objective waveform inversion  
78 (MOWI), Pan et al., 2020) have been also proposed. Nevertheless, all these approaches are highly  
79 time consuming, particularly for increasing number of DCs to be analysed, and can be adopted only  
80 in the post-processing stage, not allowing for an effective in situ characterization. The lack of  $V_p$   
81 information can also be a disadvantage since  $V_p$  is known to be correlated with saturation levels  
82 and related ~~Poisson's~~Poisson ratio of the materials. This last could be indeed an important  
83 parameter to be determined along river embankments, to complete the characterization.

84 To overcome these limitations, the application of a new procedure ([Socco et al., 2017; Socco and](#)  
85 [Comina, 2017](#)) for the analysis of Rayleigh wave fundamental mode DC is ~~proposed-adopted~~  
86 in this paper. This procedure is based on the relationship between Rayleigh wave wavelength and  
87 investigation depth (W/D procedure) ~~is based on~~and exploit the higher sensitivity of the DCs to  
88 time-average shear wave velocity ( $V_{s,z}$ ) than to layered velocity profiles and ~~to~~ the sensitivity of  
89 the Rayleigh wave skin depth to  $V_p$ . The W/D procedure allows the determination of both 2D  $V_s$   
90 and  $V_p$  sections from the DCs using a direct data transform approach. ~~A-The~~ relationship between  
91 the wavelength of the Rayleigh wave fundamental mode and the investigation depth (W/D  
92 relationship) is estimated through a reference  $V_s$  and  $V_{s,z}$  profile and used to directly transform all  
93 DCs into  $V_s$  profiles. The sensitivity of the W/D relationship to ~~Poisson's~~Poisson ratio is moreover  
94 exploited to obtain also  $V_p$  profiles along the studied embankment. The procedure has already  
95 demonstrated its reliability both on synthetic and real data, producing  $V_s$  and  $V_p$  models which  
96 allow a reliable waveform matching in comparison to benchmarks ([Khosro Anjom et al., 2019](#)) and  
97 effective full waveform inversion starting models (~~Khosro Anjom et al., 2019; Teodor et al., 2020~~).

98 Another significant advantage of the proposed W/D procedure is that, being a data transform  
99 approach, it does not have particular computational requirements. In principle, it could therefore be  
100 applied also during in situ measurement campaigns for a fast imaging of the seismic properties of  
101 the studied embankment. This ~~result~~products ~~in-~~ a strong reduction of survey time and increased  
102 efficiency. In this paper, the procedure is specifically implemented for surface waves streamer data  
103 and its application to the characterization of a test site (Bormida river embankment, Piedmont  
104 Region, Italy) is presented. It is shown that the obtained results are comparable to standard seismic

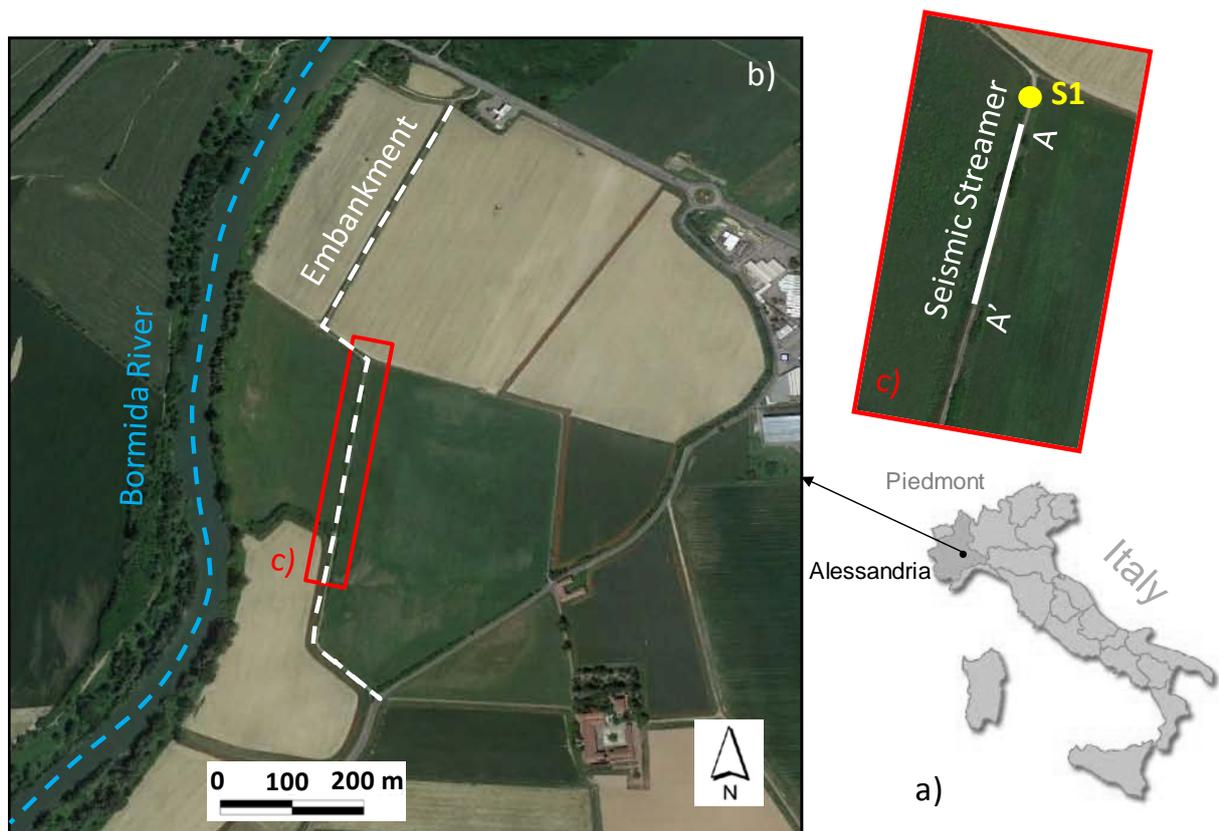
105 processing approaches with the advantage of reduced survey time and increased efficiency, and that  
106 preliminary results can be obtained directly during in situ measurements.

107

## 108 2. TEST SITE AND EXECUTED SURVEYS

109 The test site investigated in this paper is the right embankment of the Bormida river, east of the city  
110 of Alessandria, in Spinetta Marengo municipality, Piedmont Region, NW Italy (Figure 1). The  
111 embankment is separated from the river by the presence of a 200 m wide floodplain that serves as  
112 expansion area during floods (Figure 1). The top of the embankment rises about 9 m from the free  
113 surface of the river, and about 3 m from the floodplain. The soil composition of the embankment  
114 (embankment body and foundation) was obtained by available geotechnical tests: a borehole,  
115 executed on the top of the embankment in correspondence of an embankment curve (S1, in Figure 1  
116 inlet) and a dynamic penetration super heavy test (DPSH) executed in the proximity of the borehole.  
117 Both the borehole and DPSH interested ~~both~~ embankment body and foundation soil till about 16 m  
118 depth.

119

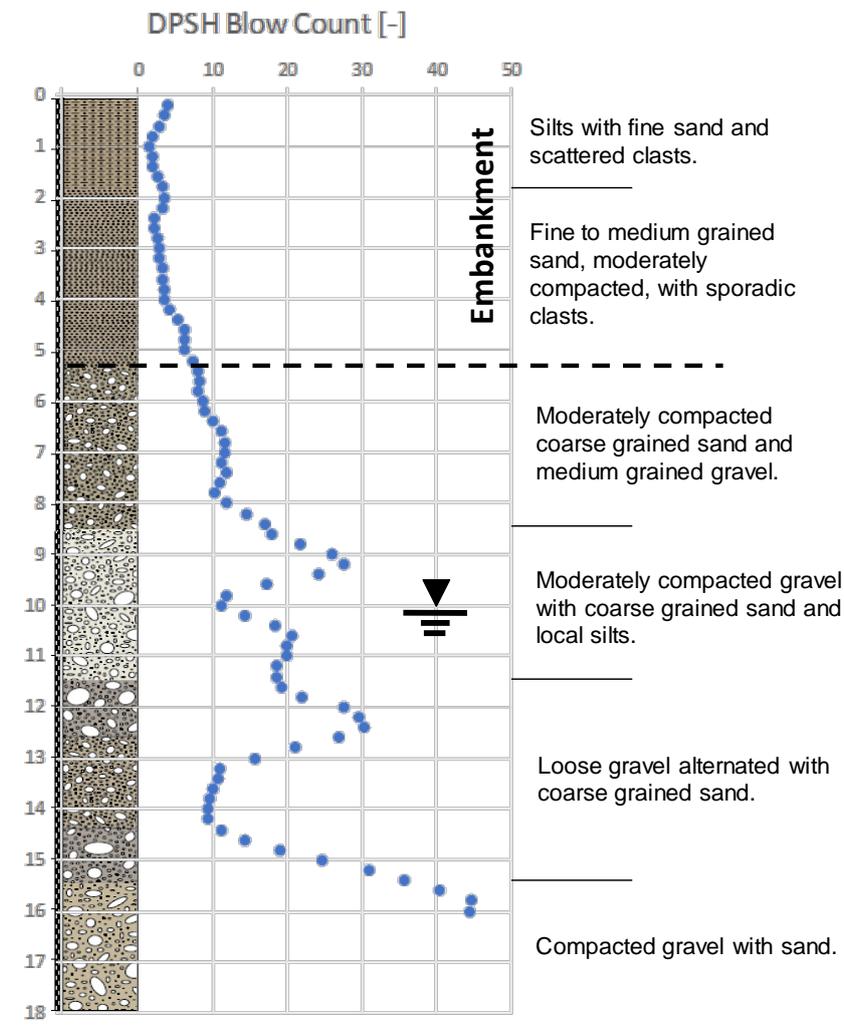


120 **Figure 1 – Location of the test site: a) north western Italian Po plain, Piedmont region, near the city of**  
121 **Alessandria, b) detail of the studied embankment and c) executed surveys.**

122 The geotechnical setting (Figure 2) can be synthesized as constituted by silts with fine sands and  
123 scattered clasts changing to fine to medium grained sands, moderately compacted, with sporadic

124 clasts, up to about 5.3 m depth (embankment body) overlaying a coarse sand and gravel formation  
 125 moderately to medium compacted with intercalated silts and local compaction reduction with depth.  
 126 At the moment of execution of the borehole (November 2007) the water table was reported at about  
 127 10 m depth from the embankment top; given the height of the river, the water table is therefore  
 128 supposed to be fed by the river and its elevation strictly dependent on the water level within the  
 129 river.

130 As it can be observed in the stratigraphic log, the transition from embankment body to natural  
 131 subsoil does not appear to be particularly sharp. This can be an indication that the construction  
 132 procedure did not involved relevant reworking of the first subsoil and that lateral differences in  
 133 depth and nature of this contact could be present along the embankment. Taking as reference the  
 134 DPSH result, local eventual differences along the embankment body will be investigated using  
 135 seismic streamer data dragged along a specific portion of the embankment (Figure 1).



136

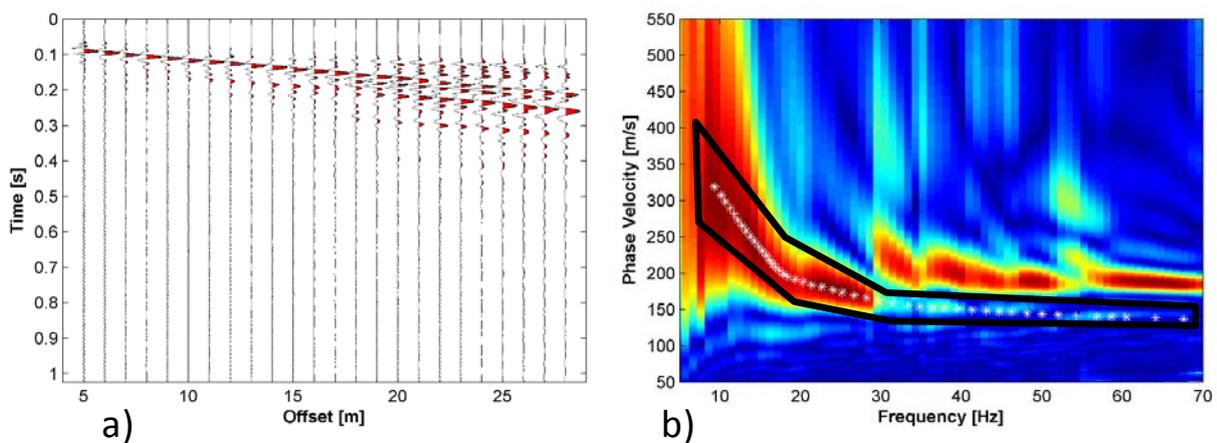
137 **Figure 1-2** – Stratigraphic log and geotechnical description of the encountered formations with  
 138 evidence of the DPSH results.

139 An embankment sector of about 90 m, south with respect to the S1 borehole (Figure 1), was  
140 investigated in May 2019 with a seismic land streamer constituted of 24, 4.5 Hz vertical geophones  
141 mounted on coupling sliders at 1 m spacing. The streamer was dragged by a pick-up truck and was  
142 moved along the studied reach at 2 m steps; for each moving step a single seismic shot was  
143 registered. The seismic source was a 40 kg accelerated mass mounted on the pick-up back; a 5 m  
144 source offset was adopted in the acquisitions. The streamer was connected to a DaQLink IV  
145 (Seismic Source, 2016) acquisition device on the pick-up truck, storing the data in a survey laptop  
146 and eventually applying pre-processing steps. Seismograms were acquired with a 0.5 ms sampling  
147 interval, -50 ms pretrig and 1.024 s total recording length. A total of 45 seismograms were therefore  
148 acquired during the survey. On these data several processing steps were applied for the definition of  
149 2D Vs and Vp models with the proposed W/D procedure.

150

### 151 3. METHODOLOGY

152 An example seismic shot is reported in Figure 3a. The used source and streamer setup allowed the  
153 acquisition of high-quality data, with clear evidence of surface waves dispersive pattern and also  
154 particularly evident first arrivals of compressional waves.



155

156 **Figure 3 – Data processing procedures on acquired seismograms: a) example seismic shot, b)**  
157 **dispersion curve extraction with evidence of the applied mask (black line) and selected high energy**  
158 **maxima (white asterisks).**

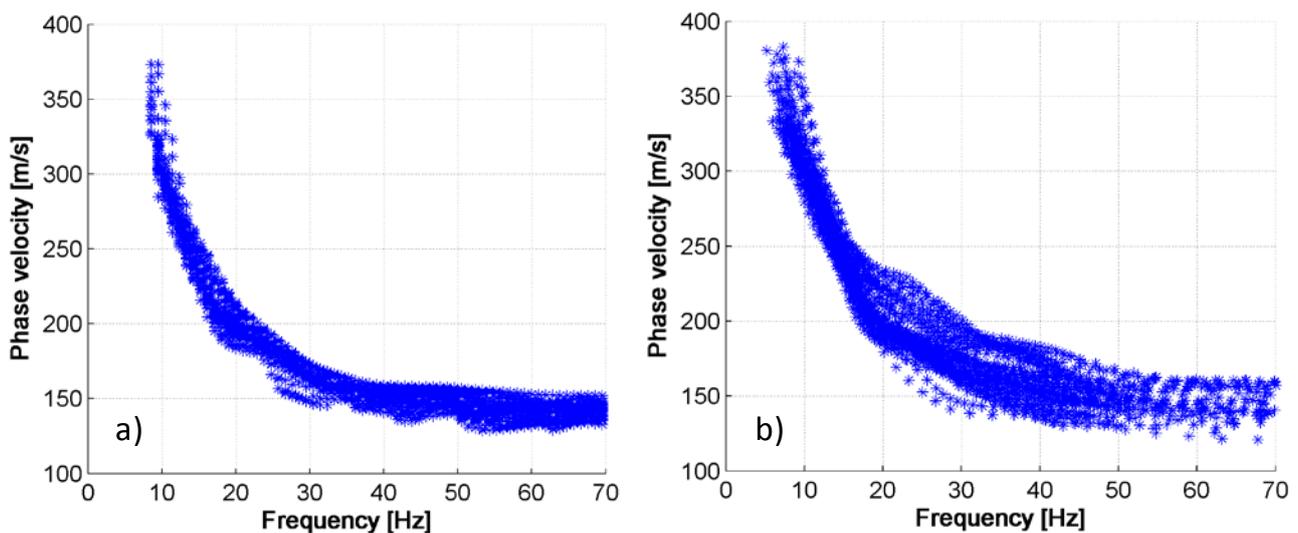
159 DCs extraction was performed with two different procedures: first, the dispersion image for each  
160 seismogram was obtained by means of a phase-shift approach (Park et al., 1998) implemented in  
161 MATLAB® routines. The phase-shift approach has demonstrated to maintain very good  
162 performances even when a limited number of traces is considered (Dal Moro et al., 2005).

163 Alternatively, to further improve the accuracy of dispersion measurement, a multi-channel

164 nonlinear signal comparison (MNLSC, Hu et al., 2019) can be adopted, producing high and  
165 adjustable resolution among a wide detected frequency range.

166 On the dispersion image this image the zone pertinent to the fundamental mode propagation was  
167 selected with a mask (black line in Figure 3b) and energy maxima were automatically searched  
168 within this area (white asterisks in Figure 3b). The mask selected for the first shot can be either  
169 automatically used for all the following shots (automatic procedure) or partially adjusted to follow  
170 eventual variations in the energy distribution (semi-automatic procedure). In the first case a rough,  
171 but fully automated, DCs selection is obtained, in the second case a more refined, but more time  
172 consuming, analysis is allowed, to better evidence eventual lateral variations. On both these selected  
173 DC groups eventual smoothing and manual outlier removal can be applied to obtain more  
174 continuous and reliable curves.

175 In Figure 4 the resulting DCs selected for all the shots from automatic and semi-automatic  
176 procedures are reported. For some of the shots a transition of the absolute energy maxima towards  
177 higher modes was observed in the high-frequency range (e.g. frequencies higher than 30Hz in  
178 Figure 3b). Nevertheless the fundamental mode can still be followed as local maxima thank to the  
179 adopted mask that allowed to isolate the correct portion of the dispersion image to be considered,  
180 excluding the higher modes from the maxima searching. It can be evidenced that the DC ranges are  
181 very similar with corresponding velocity transition. Nevertheless, the semi-automatic procedure  
182 (Figure 4b) shows higher variability for the medium-high frequency range (shallower layers) as a  
183 result of the application of a variable mask. Most of the results reported in the paper refer to the  
184 DCs selected with this approach. In the discussion section some comparisons are however presented  
185 with the results obtainable with the automatic procedure also.



186

187 **Figure 4 – DCs selected for all the shots: a) automatic procedure and b) semi-automatic procedure.**

188 The application of the W/D procedure to the extracted DCs requires the knowledge of a single  $V_s$   
189 and  $V_{s,z}$  reference profile along the seismic line together with its associated DC. This profile can be  
190 either extracted from the data themselves, by performing the inversion of a representative DC  
191 among the ones extracted, or it can be obtained by independent seismic or geotechnical data.

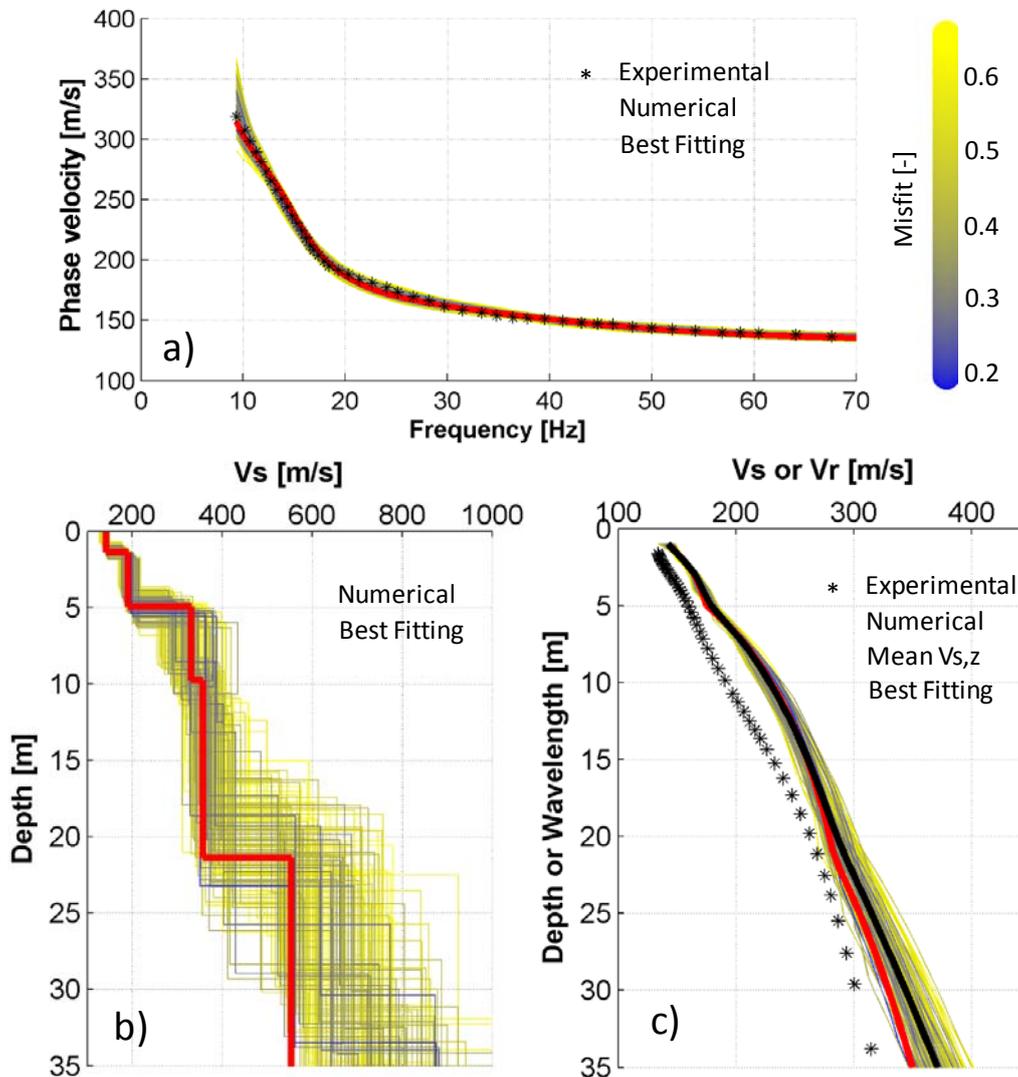
192 In this paper the first method was adopted using a Monte Carlo Inversion (MCI) algorithm (Socco  
193 and Boiero, 2008) which efficiently limits potential non-uniqueness of the solution and results in  
194 reliable  $V_s$  and  $V_{s,z}$  profiles. The inversion implies the definition of a wide model space by  
195 selecting ranges for each model parameter ( $V_s$ , thicknesses and the Poisson ratio ~~offer~~ for each layer)  
196 and performing random sampling ( $10^5$  profiles) among these ranges. Please note that, in order to  
197 allow for the W/D procedure to be applied, also Poisson ratio of each layer is considered as a model  
198 parameter, contrary to what usually performed in the inversion of DC curves.

199 Example application of the inversion process to the DC reported in Figure 3b, which was selected  
200 as reference, is reported in Figure 5. It can be observed that the set of statistical equivalent profiles  
201 selected from the MCI assess the presence of a contrast at the bottom of the embankment around 5  
202 m depth (Figure 5b). This set of profiles, and their correspondent numerical DCs, is represented in  
203 Figure 5 with a relative misfit representation based on the absolute difference between each profile  
204 misfit and the best fitting one (in red in Figure 5).

205 It can also be noted that the higher variability in terms of  $V_s$  profiles (Figure 5b) strongly reduces  
206 when the time average shear wave velocity is considered ( $V_{s,z}$ , in Figure 5c). With this respect the  
207 best selected profile (in red in Figure 5c) and the mean of the statistical set (in black in Figure 5c)  
208 almost superimpose for the top portion of the profile. Socco and Comina (2015) have already shown  
209 that the non-uniqueness of the DC inversion very slightly affects the estimation of time-average  
210 velocity, and hence, the  $V_{s,z}$  obtained from inverted profiles is very robust. Nevertheless, given the  
211 increased uncertainty at the bottom of the profile, the following analyses were limited to 20 m  
212 depth, which is enough ~~for the studied test site~~ for investigating both the embankment and a  
213 significant portion of the foundation subsoil at the studied test site.

214 Using the reference  $V_s$  and  $V_{s,z}$  profiles and all the extracted DCs, the proposed data transform  
215 procedure is then applied as following: i) the estimated  $V_{s,z}$  and its corresponding DC are used to  
216 compute the reference W/D relationship; ii) the reference W/D relationship is used to transform all  
217 DCs into  $V_{s,z}$  models; iii) an apparent Poisson ratio is estimated using the reference W/D  
218 relationship and the reference  $V_s$  model; iv) using the apparent Poisson ratio, each  $V_{s,z}$  profile is  
219 transformed into a  $V_{p,z}$  profile; v) all the reconstructed  $V_{s,z}$  and  $V_{p,z}$  profiles are ~~then~~-transformed  
220 into  $V_s$  and  $V_p$  profiles with an interval velocity analysis.

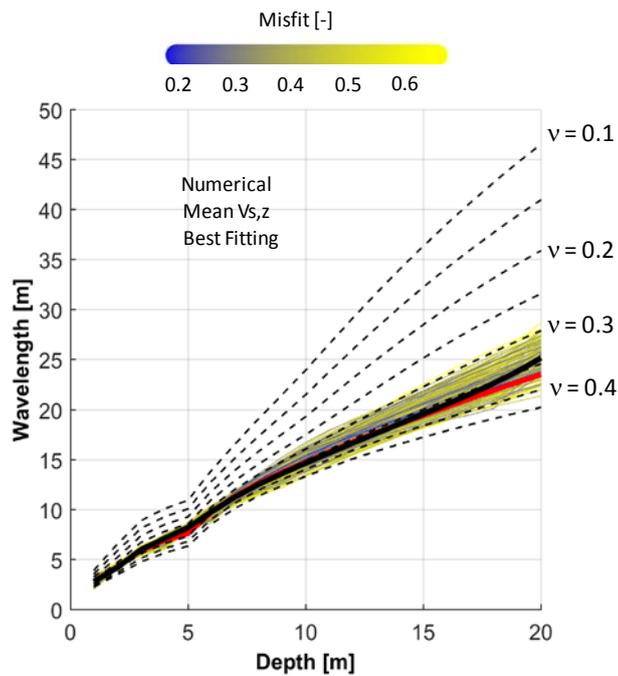
221



222

223 **Figure 5 – MCI of the reference DC curve: a) experimental and numerical dispersion curves b) best**  
 224 **fitting profile and set of statistically equivalent profiles and c) experimental dispersion curve as a**  
 225 **function of wavelength, time average velocities of best fitting profile and statistically equivalent**  
 226 **profiles with their mean.**

227 Steps i) and iii) of the procedure require more explanations. The meaning of the W/D relationship is  
 228 represented in [Figure 5c](#): for each  $V_{s,z}$  value, the wavelength (W) at which the phase velocity ( $V_r$ )  
 229 of the DC is equal to the  $V_{s,z}$  (see the arrows in [Figure 5c](#)) is searched for each depth (D). With all  
 230 the W/D pairs at which  $V_{s,z}$  and phase velocity are equal a relationship is obtained (W/D  
 231 relationship. This relationship is represented in [Figure 6](#) for the best fitting profile (in red), for the  
 232 mean of the statistically equivalent profiles (in black) and for all the statistically equivalent profiles.  
 233 Consistency of the extracted W/D relationships is evidenced.



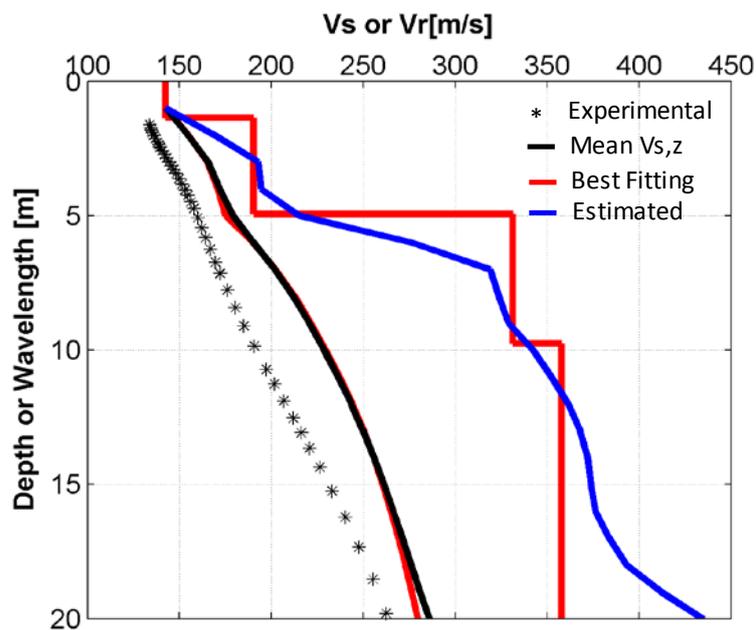
234

235 **Figure 6 – The W/D relationship for the reference DC for the best fitting profile (in red), for the mean**  
 236 **of the statistically equivalent profiles (in black) and for all the statistically equivalent profiles**  
 237 **compared with the ones obtained with different Poisson's Poisson ratio values. Some Reference**  
 238 **Poisson's Poisson ratio values are indicated on the right of the plot.**

239 This relationship represents the surface waves' skin depth for increasing wavelengths and has been  
 240 demonstrated (Socco and Comina, 2017) to be influenced by the Poisson's Poisson ratio of the  
 241 formation. With the reference  $V_s$  and  $V_{s,z}$  profiles it is therefore possible to build different  
 242 synthetic W/D relationships by changing the value of the Poisson's Poisson ratio ( $\nu$ ) of the layers  
 243 (assumed constant for all the layers). These synthetic W/D relationships are reported in Figure 6  
 244 (dashed black lines) for some example values of the Poisson ratio, dashed black lines in Figure 6).  
 245 It can be noted that Poisson ratio acts on the slope of W/D relationship. In particular, the slope  
 246 decreases when Poisson ratio increases. Therefore the slope of the experimentally determined W/D  
 247 relationship contains information on the actual Poisson ratio of the formation. -The actual apparent  
 248 Poisson's Poisson ratio profile of the formation can be therefore searched by associating to each  
 249 depth the value of Poisson's Poisson ratio that corresponds to the linear interpolation between the  
 250 upper and lower nearest synthetic constant Poisson's ratio W/D relationships. In this way an  
 251 apparent Poisson ratio profile with depth can be obtained for the reference DC. This profile can be  
 252 later used to transform all the  $V_{s,z}$  profiles into  $V_{p,z}$  profiles allowing for a 2D  $V_p$  section to be  
 253 later computed.

254 An example application of the W/D procedure to the reference DC is reported in Figure 7. It can be  
 255 observed that the  $V_{s,z}$  of the best fitting profile (continuous red line in Figure 7) and the mean  $V_{s,z}$

256 of the statistical set (continuous black line in Figure 7) almost superimpose for the first 20 m depth.  
 257 It can be ~~observed~~ also noted that the W/D procedure allows the estimate of a Vs model (in blue in  
 258 Figure 7) very near to the best fitting one (layered red line in Figure 7) obtained from the MCI of  
 259 the DC. The model obtained with this procedure has also the advantage of not making any  
 260 assumption with respect to the number of layers of the profile. For this reason, it can result  
 261 smoother with respect to the layered profile but also more correspondent to the actual geotechnical  
 262 situation below the embankment. Particularly, it can be observed that the transition from  
 263 embankment body to bottom layers with this estimated profile appear to be more correspondent to  
 264 what evidenced in the DPSH profile results (Figure 2) with respect to the sharp interface evidenced  
 265 by the MCI result.



266  
 267 **Figure 7 – Application of the W/D procedure to the reference DC for Vs profile determination and**  
 268 **comparison with the best fitting result (both in term of layered velocity model and Vs,z) from MCI.**

269 All the Vs and Vp profiles estimated with the W/D procedure are then interpolated along the studied  
 270 embankment to allow for a 2D visualization of the Vs and Vp velocities distributions. The data  
 271 gridding was performed in Surfer (Golden software) with an interpolation grid of 2 m in the  
 272 horizontal direction (equal to the acquisition step) and of 0.5 m in the vertical direction.

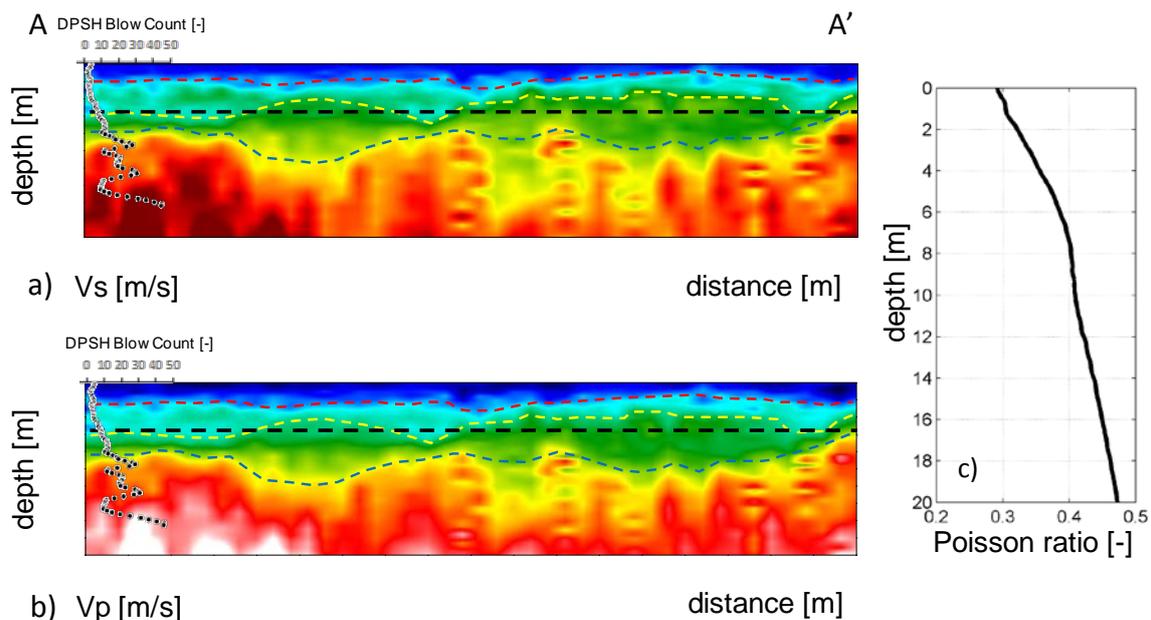
273 To validate the velocity models obtained with the application of the W/D procedure ~~the~~ the obtained  
 274 results are ~~then~~ benchmarked against standard seismic processing approaches. For Vs, all the  
 275 dispersion curves extracted were inverted with a laterally constrained inversion (LCI) approach  
 276 (Auken and Christiansen, 2004; Socco et al., 2009). For this inversion, the same number of layers of  
 277 the MCI was assumed. For Vp, processing was carried out by picking the first breaks on each

278 acquired seismogram, picked first breaks were then interpreted in tomographic approach with the  
279 use of the software Rayfract (Intelligent Resources Softwares Inc.).

280

#### 281 4. RESULTS

282 Results of the application of the W/D procedure are reported in Figure 8. Particularly, the  $V_p$  result  
283 is obtained from the  $V_s$  one with the application of the apparent Poisson ratio obtained from the  
284 W/D procedure. This last is assumed constant through the whole profile and therefore the resulting  
285  $V_p$  velocity field is a transformation of the  $V_s$  one with similar properties. Both  $V_s$  and  $V_p$  sections  
286 can discriminate the transition from the shallow silts and sands to the bottom gravels along the  
287 embankment and to delineate the embankment bottom. Coherently with the borehole results and  
288 geotechnical tests (Figure 2) this transition falls, on the left side of the sections, where the surveys  
289 are nearer to the geotechnical tests (the DPSH Blow Count profile is also reported in Figure 8a and  
290 b), around 5.3 m depth.



291

292 **Figure 8 – Results of the application of the W/D procedure to extracted DCs (section A-A’): a)  $V_s$**   
293 **section, b)  $V_p$  section and c) resulting Poisson’s ratio. On both the sections the supposed depth**  
294 **of the embankment is also reported (dashed black line) together with coloured dashed lines, derived by**  
295 **the velocity models, indicating the transition between the shallow silts and sands (in red), the thickness**  
296 **of the embankment (in yellow) and the transition to compacted gravels and sands (in blue). The DPSH**  
297 **Blow Count profile is also reported at the beginning of the sections.**

298 However, along the embankment a variation of the depth of this interface can be evidenced.  
299 Particularly, localized anomalies appear in the  $V_s$  section suggesting an increase in the depth of the

300 shallow silts and sands of the embankment (yellow dashed line in Figure 8) around 40 m  
301 progressive distance. Conversely, the depth of the interface appears to be shallower in the  
302 progressive distance range between about 50 to 80 m.

303 Seismic surveys are also able to depict the transition (red dashed line in Figure 8) from silts with  
304 fine sands and scattered clasts to fine to medium grained sands, as reported from the borehole and  
305 DPSH results, within the embankment. A deeper increase in velocity is also observed around 8 m  
306 depth on the left side of Figure 8, were the transition to more compacted gravels (blue dashed line  
307 in Figure 8) is evidenced by borehole ~~results~~ and DPSH results geotechnical tests (Figure 2). This  
308 more compacted formation appears however to increase its depth along the section moving away  
309 from the borehole and showing on average lower velocity values. Localized velocity inversions are  
310 also partially observable below 8 m in the leftmost portions of the Vs section. This evidence again  
311 well compares with what reported by the DPSH results ~~(Figure 2)~~.

312 Notwithstanding the information on the position of the water table at the site (around 10 m) the  
313 range of Vp velocities extracted by the procedure ~~depths~~ does not report, for increasing depths,  
314 velocity ranges usually attributed to saturated materials (i.e. around 1400-1500 m/s). It must be  
315 underlined that the time span between the two surveys is relevant (from November 2007 to May  
316 2019) so that eventual variations on the water table depth could be present. Nevertheless, the  
317 Poisson's Poisson ratio profile extracted with the W/D procedure (Figure 8c) shows a marked  
318 increase nearly around 10 m exceeding the 0.4 value and tending to 0.5. Poisson ratio of saturated  
319 soils is usually reported to be ~~indeed~~ in this ~~last~~ range (Boore, 2007). It must be underlined that the  
320 Poisson Poisson ratio profile here presented is the interval Poisson ratio obtained through the Vp/Vs  
321 ratio of the resulting models. This is different from the apparent Poisson ratio that is estimated in  
322 the W/D procedure (Figure 6) for the DC transformation.

323 Results of the LCI processing of the extracted dispersion curves are reported in Figure 9a. A good  
324 convergence of the inversion was obtained with LCI resulting in a final RMS error of 1.7%.

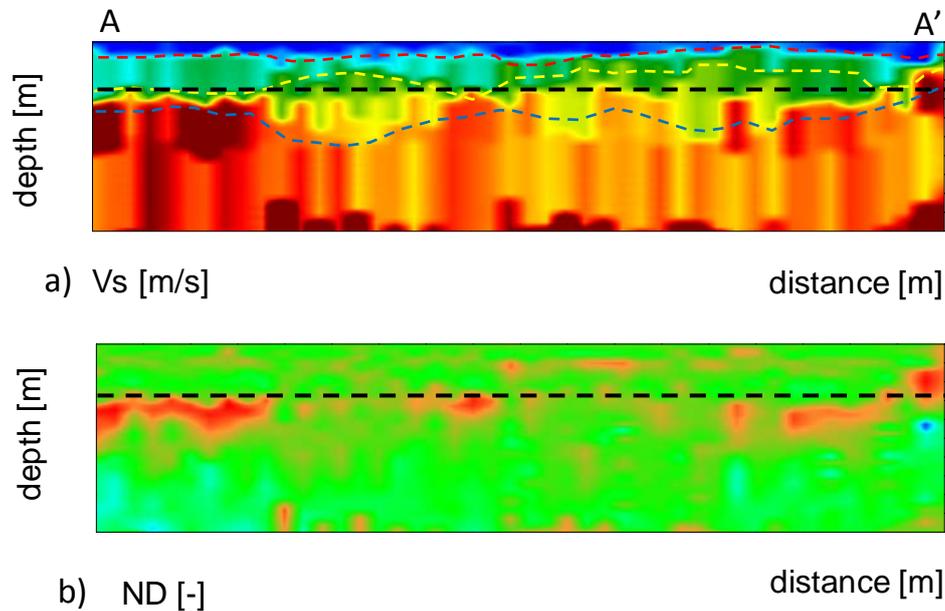
325 The comparison of the LCI result with the W/D procedure is performed in Figure 9b in term of  
326 normalized differences, taking as reference the LCI results, with the formula:

$$327 \quad ND = \frac{V_{i,LCI} - V_{i,WD}}{V_{i,LCI}} \quad (1)$$

328

329 were  $V_{i,WD}$  is the velocity value obtained from the W/D procedure and  $V_{i,LCI}$  is the velocity value  
330 obtained from the LCI in each location within the models. Therefore, positive values of the  
331 normalized difference indicate zones where the W/D procedure underestimate the velocity, negative  
332 values indicate the opposite. To allow computing the normalized differences in each point of the

333 models also layered LCI results were gridded with the same interpolation scheme of the W/D  
334 procedure results.

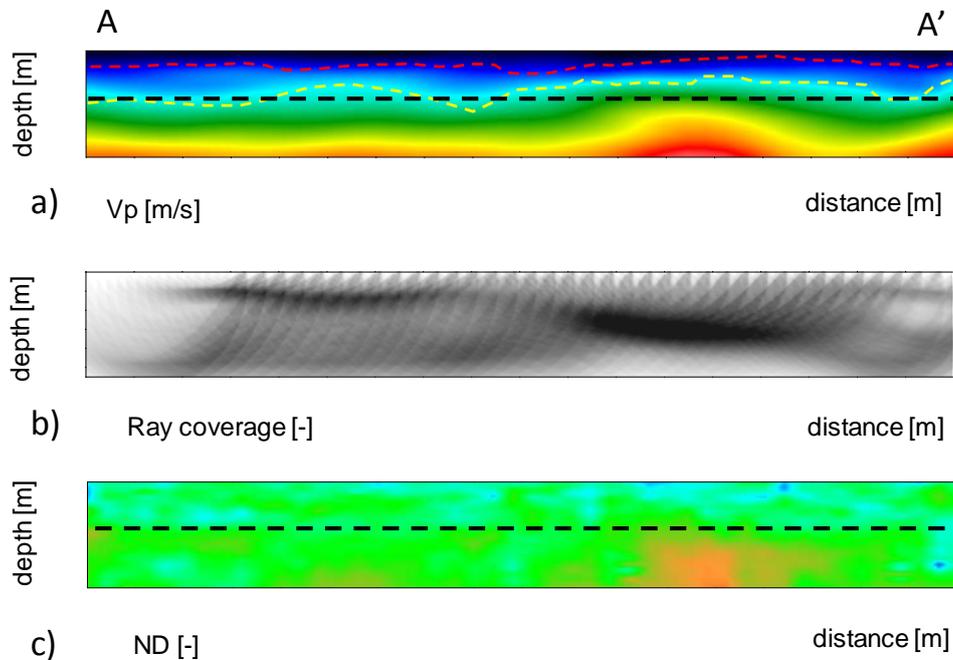


335

336 **Figure 9 – Results of the LCI of the extracted DCs (section A-A’): a) Vs section and b) Normalized**  
337 **differences with the Vs results of the W/D procedure. On both the sections the supposed depth of the**  
338 **embankment is also reported (dashed black line). Over the LCI section, the interfaces evidenced by the**  
339 **W/D procedure indicating the transition between the shallow silts and sands (in red), the thickness of**  
340 **the embankment (in yellow) and the transition to compacted gravels and sands (in blue), are**  
341 **superimposed.**

342 **Figure 9** shows that the Vs velocity range obtained using LCI inversion is comparable with that  
343 from the W/D procedure. The interfaces evidenced by the W/D procedure are reported for  
344 comparison over the resulting Vs image. Similar variability in the depth of the interfaces is noted.  
345 As an example, both the increased depth of shallower silts and sands around progressive 40 m and  
346 the shallower depth of the embankment in the progressive distance range between about 50 to 80 m  
347 are confirmed. Most of the normalized differences among the W/D and LCI models fall within a  
348  $\pm 10\%$  range indicating the good correspondence of the two results. The only portions of the section  
349 affected by higher positive normalized differences cannot be attributed to errors in the W/D  
350 procedure, but to the layering assumption in the LCI. The layered discretization adopted in the LCI  
351 can indeed result in an overestimation of the velocity near the layer boundaries (see also **Figure 7**  
352 for comparison). Most of the higher difference values fall indeed near the embankment/foundation  
353 soil interface where the layered profile results from LCI tend to give a sharper transition than the  
354 W/D result.

355 Results of the tomographic inversion of picked first arrivals are reported in Figure 10 and  
 356 compared, in term of normalized differences, with the Vp results obtained with the W/D procedure.  
 357 The same equation 1 was adopted for the computation of normalized differences with Vp values  
 358 from W/D procedure and first arrivals tomography (these last substituting the LCI values in  
 359 equation 1).



360

361 **Figure 10 – Results of the first break tomography (section A-A’): a) Vp section, b) Ray coverage along**  
 362 **the section and c) Normalized differences with the Vp results of the W/D procedure. On both the**  
 363 **sections the supposed depth of the embankment is also reported (dashed black line). Over the**  
 364 **tomography the first two interfaces evidenced by the W/D procedure, indicating the transition**  
 365 **between the shallow silts and sands (in red), the thickness of the embankment (in yellow), are**  
 366 **superimposed.**

367 From Figure 10 it can be observed that, given the reduced length of the streamer adopted, the depth  
 368 of investigation of the tomography is limited to about 10 m, or even less in some portions.  
 369 Nevertheless, within this depth, a high ray coverage is obtained in most of the section by the  
 370 combined elaboration of all the shots. A good convergence of the inversion was obtained with a  
 371 resulting RMS error of 2.7% after the final iteration.

372 Again, from Figure 10 it can be observed that the tomographic inversion depicts the same velocity  
 373 range compared to the one obtained with the W/D procedure. Given the reduced investigation depth  
 374 of the tomography only the first two interfaces evidenced by the W/D procedure are reported for  
 375 comparison over the resulting Vp image. Similar variability in the depth of these two interfaces is  
 376 noted. As an example, both the increased depth of shallower silts and sands around progressive 40

377 m and the shallower depth of the embankment in the progressive distance range between about 50  
378 to 80 m are confirmed. Being based on relatively long-path raytracing, the tomographic result  
379 shows generally a reduced lateral resolution in the identification of the velocity variations within the  
380 section.

381 Most of the normalized differences, also for  $V_p$ , fall within a  $\pm 10\%$  range indicating the good  
382 correspondence of the two results. The only portion of the section showing higher normalized  
383 differences can be attributed to a lower ray coverage zone (see [Figure 10b](#) below 7 m at about 55 to  
384 70 progressive distances) making the assumed  $V_p$  values less reliable in the tomography. Given its  
385 shallower investigation depth, also the tomography does not highlight a marked increase of  $V_p$   
386 values, at the bottom of the model, attributable to the presence of the water table.

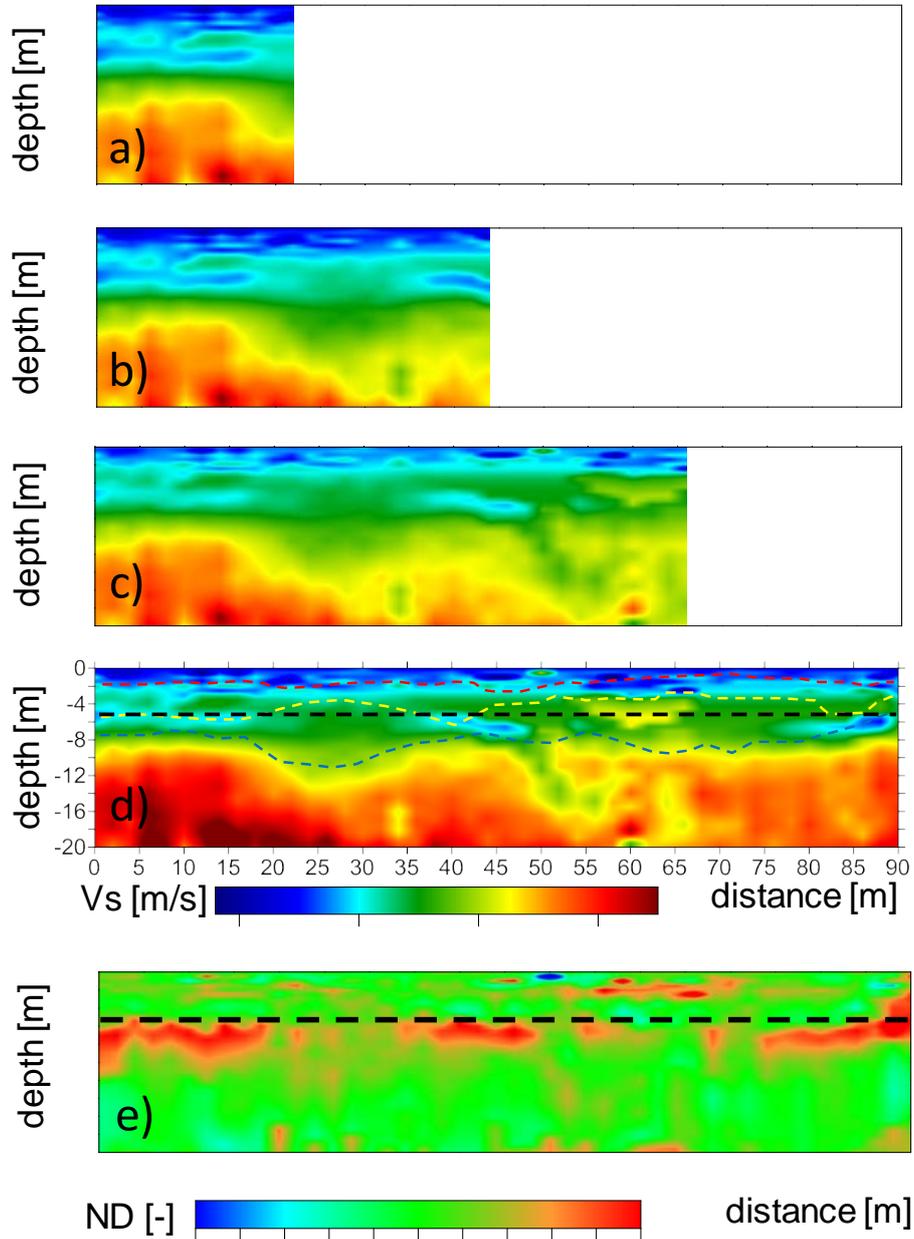
387

## 388 5. DISCUSSION

389 It was shown in the paper that the results obtainable with the W/D procedure are comparable both in  
390 terms of  $V_s$  and  $V_p$  to standard seismic processing approaches. This comparison validates therefore  
391 the application of the W/D procedure. It was observed, in the presented case study, that most of the  
392 normalized differences between the W/D procedure and both LCI and first arrivals tomography fall  
393 within a  $\pm 10\%$  range, indicating the good correspondence of the two results. Higher normalized  
394 differences along the sections can be attributed to different resolution or underlying  
395 methodological assumptions among the methods and cannot be considered as an error in the W/D  
396 procedure. Therefore, the W/D procedure can be established as a reliable alternative to the methods  
397 here compared for the characterization of embankments and overall linear earth structures.

398 The W/D procedure has also main advantages with respect to usually seismic processing  
399 approaches applied to the data obtained from similar surveys: i) being a data transform approach it  
400 does not requires relevant processing and time consuming interpretations; ii) it does not make any  
401 assumption with respect to the number of layers present along the investigated embankment and iii)  
402 allow the combined estimation of  $V_s$  and  $V_p$  for increased depths given the same acquisition setup.  
403 Particularly the first advantage is important if the speed of the surveys is considered, for example in  
404 situations in which a fast and preliminary evaluation of the state of health of an embankment is  
405 required. This can be the case of surveys conducted after, or in foresee of, significant rain and/or  
406 flood events. In these conditions the W/D procedure, applied to the fully automated extracted DCs  
407 ([Figure 4a](#)), can allow for a first, almost immediate, on site evaluation of the  $V_s$  and  $V_p$  velocity  
408 field. Both the automated DC extraction step and the conversion of DC data to  $V_s$  and  $V_p$  profiles is  
409 indeed a very fast process (few tens of seconds on a notebook), that outputs direct velocity models  
410 while the acquisition is in progress and the streamer is dragged along the embankment.

411 An example application of this direct visualization of the Vs section during data acquisition is  
 412 reported in Figure 11. It can be particularly observed that the final Vs section determined from the  
 413 fully automated extracted DCs (Figure 11d) is roughly comparable with the one determined with the  
 414 semi-automatic procedure (Figure 8a) with very similar depiction of the main interfaces.



415  
 416 **Figure 11 – Example application of the direct visualization of the Vs section during data acquisition:**  
 417 **a), b) and c) Vs sections while dragging the streamer along the embankment; d) final Vs section and c)**  
 418 **Normalized differences with the LCI. In d) and e) the supposed depth of the embankment is also**  
 419 **reported (dashed black line). In d) the interfaces evidenced by the semi-automated W/D procedure,**  
 420 **indicating the transition between the shallow silts and sands (in red), the thickness of the embankment**  
 421 **(in yellow) and the transition to compacted gravels and sands (in blue), are superimposed.**

422

423 The presence of some artefacts can be however noted within the section and can be related to the  
424 reduced precision of the automatic picking of the DCs. A general increase in the normalized  
425 differences with the LCI (Figure 11d) is also observed, with the presence of localized anomalous  
426 local velocity values (e.g. see the shallow portion of the embankment around progressive 50 m).  
427 Nevertheless, the general imaging of the Vs structure can be considered accurate enough for a first  
428 estimation of the geotechnical variability at the site and a useful tool for a preliminary identification  
429 of anomalous portions of the examined embankments. Given the use of the same Poisson ratio  
430 profile (Figure 8c), uniform through the section, very similar considerations can be performed for  
431 what concerns the resulting Vp image.

432 This direct visualization requires the knowledge of reference Vs and Vs,z profiles over which  
433 calibrate the W/D relationship and the following Poisson ratio computation. In the present paper  
434 these reference profiles were obtained through MCI of a reference DC. The same approach can be  
435 adopted on site at the beginning of the surveys by selecting one of the clearer DCs during the first  
436 shots. Nevertheless, the MCI step can be significantly time consuming and not always applied with  
437 reliability on site. Possible alternative approaches would therefore require the execution of initial  
438 detailed tests and interpretations through which determine with accuracy the reference profiles and  
439 only later proceed with the execution of the streamer surveys. Alternatively, the reference profiles  
440 can be extracted from already available geotechnical and/or geophysical surveys along the  
441 embankment. With this respect the W/D procedure already showed comparable results also with  
442 respect to Down Hole surveys (Socco et al., 2017).

443 Limitations of the proposed W/D procedure can be related to: i) its application to only fundamental  
444 mode DC; ii) the assumption of a laterally invariable W/D relationship and Poisson ratio along the  
445 embankment. With respect to the first one, the W/D procedure has been mainly developed and  
446 applied to fundamental mode DC, but some attempts have been already made to include also higher  
447 propagation modes (e.g. Bamarouf et al., 2017). Including higher modes showed to give advantages  
448 mainly with respect to the investigation depth, even though it is a more time-consuming process.

449 However, ~~it~~ this could be a necessary step along embankments with peculiar shape dimensions,  
450 since it is well known that the shape of the embankment could influence the surface wave dispersive  
451 pattern and modes superposition (e.g. Karl et al., 2011). Pageot et al. (2016) have also shown that  
452 internal structure layering can emphasize geometrical effects and produce DCs very different from  
453 the theoretical 1D case, for both the fundamental and higher modes. In these conditions even a  
454 multi-modal inversion approach could encounter some limitations to infer accurate Vs and Vp  
455 models.

456 These effects have not been particularly noted at the site. As it can be observed in [Figure 3b](#), higher  
457 modes are indeed present in the higher frequency range, but the fundamental mode propagation is  
458 still easily recognizable as local energy maxima. This may be related to the reduced contrast  
459 between the embankment body and the underlying subsoil ([Figure 2](#)) which limits the layering  
460 effect and to the relevant width of the embankment (width to height ratio of about 5.5) which limits  
461 the presence of 3D effects.

462 Conversely the laterally invariant assumption could be easily overcome using appropriate clustering  
463 techniques on the extracted DCs that can be analysed for grouping them into subsets with  
464 homogeneous properties. The W/D procedure has then to be applied to each of the identified  
465 subsets. The application of this further processing step however increases again the computation  
466 times and prevent a direct in situ application of the procedure but has been shown to provide  
467 increased resolution in the identification of sharp lateral variations with the W/D procedure ([Khosro  
468 Anjom et al., 2019; Teodor et al., 2020](#)).

469 The clustering approach was judged to be unnecessary in the presented case study given the  
470 uniformity of the extracted DCs (see [Figure 4](#)) which suggest the presence of smooth depth  
471 variations along the embankment but the absence of particularly sharp variations. When sharp  
472 lateral variations along the embankment are the main survey target alternative identification  
473 methods based on the surface waves spectral properties (e.g. [Colombero et al., 2019](#)) could also be  
474 applied to the acquired streamer data.

475 To allow for a more complete characterization of the state of health of embankments, seismic data  
476 are usually combined with electric resistivity data. These last can indeed give important information  
477 on the variations of soil composition and water saturation, detect development of weak zones and  
478 identify local anomalies potentially related to seepage. The combined use of seismic and electrical  
479 data can indeed provide an effective geotechnical characterization of these earth structures, as  
480 shown by several research groups that are working on their integration (e.g. [Takahashi et al., 2014;  
481 Goff et al. 2015; Lorenzo et al., 2016](#)). In this respect the W/D procedure has its natural  
482 development in combination with mobile electric systems allowing also a fast and effective  
483 evaluation of resistivity properties (e.g. [Kuras et al., 2007; Comina et al., 2020](#)).

484 **6. CONCLUSION**

485 This paper presents the application of a novel processing approach (W/D procedure) to surface  
486 wave streamer data. This approach is based on the definition a wavelength/depth (W/D) relationship  
487 for surface waves and allows the combined definition of shear ( $V_s$ ) and compressional ( $V_p$ ) wave  
488 velocities. The results obtained within the paper with the W/D procedure are comparable to  
489 standard seismic processing approaches with the advantage of reduced survey time and increased  
490 efficiency. It was shown in the paper as the W/D procedure can be developed in order to be  
491 completely automated and used as a fast in situ imaging tool along embankments for preliminary  
492 evaluations on their state of life.

493 Processing of the seismic streamer data yielded to an effective characterization of the  $V_s$  and  $V_p$   
494 velocity field along the studied embankment. The origin and properties of the anomalies  
495 encountered could be better studied with the use of local geotechnical investigations to provide a  
496 more specific knowledge on the state of life of the embankment. The produced seismic sections, if  
497 properly calibrated with the few independent geotechnical tests available, can be nevertheless used  
498 for preliminary stability evaluations also in portion of the embankment non directly covered by  
499 geotechnical tests.

500 Further studies, already planned and partially executed, include the application of the W/D  
501 procedure to different embankments shapes with the eventual inclusion of higher modes in the  
502 interpretation. Moreover, the combined acquisition of electrical resistivity data, even with  
503 innovative acquisition approaches, will allow the contemporary execution of resistivity and seismic  
504 surveys with even more reduced survey time and increased knowledge on the state of health of the  
505 embankments due to the acquisition of the different complementary parameters.

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**Article Highlights:**

- Effective  $V_s$  and  $V_p$  information are extracted from surface waves streamer data;
- An automated procedure for the seismic characterization of river embankments was developed;
- The procedure is demonstrated comparable to standard seismic processing approaches;
- Advantages in survey time and efficiency is highlighted.

# 1 **Effective Vs and Vp characterization from Surface Waves streamer** 2 **data along river embankments.**

3

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7

8

## 9 **ABSTRACT**

10

11 River embankments are linearly extended earth structures built for river flood protection. Their  
12 continuity and uniformity are fundamental prerequisites to ensure and maintain their protection  
13 efficiency. Weakness points usually develop in localized areas where geotechnical variability is  
14 present in the embankment body or in the underlying subsoil. Given their significant length, and the  
15 localized nature of weakness points, the characterization of river embankments cannot therefore  
16 rely on local geotechnical investigations but requires the application of efficient and economically  
17 affordable methods, able to investigate relevant lengths in a profitable way. This is even more  
18 essential when the investigations are conducted near, or in foresee of, significant flood events, when  
19 timing of the surveys is essential. In this paper the application of a procedure (W/D procedure) for  
20 the seismic characterization of river embankments, specifically designed for surface waves streamer  
21 data, is presented. The W/D procedure allows the combined definition of 2D shear (Vs) and  
22 compressional (Vp) wave velocity models and can be developed in order to be automated as a fast  
23 imaging tool. Its application to the characterization of a test site (Bormida river embankment,  
24 Piedmont Region, Italy) is presented. It is also shown that the obtained results are comparable to  
25 standard seismic processing approaches with the advantage of reduced survey time and increased  
26 efficiency, giving preliminary results directly in the field.

27

## 28 **Article Highlights:**

- 29 • Effective Vs and Vp information are extracted from surface waves streamer data;
- 30 • An automated procedure for the seismic characterization of river embankments was  
31 developed;
- 32 • The procedure is demonstrated comparable to standard seismic processing approaches;
- 33 • Advantages in survey time and efficiency is highlighted.

34

35 **Keywords:** surface waves, seismic characterization, river embankments.36 **Corresponding author:** Cesare Comina, [cesare.comina@unito.it](mailto:cesare.comina@unito.it)

37

38 **1. INTRODUCTION**

39 River embankments are linearly extended earth structures constructed to serve as flood control  
40 systems during large rain events. A proper characterization of the embankment body is essential to  
41 verify its uniformity and to monitor the occurrence of possible integrity losses which could  
42 undermine its stability. In recent years, frequency and magnitude of extreme flood events have been  
43 rapidly increasing in Central America, Southern Europe, and in Italy because of climate change.  
44 Moreover, the poor maintenance of hydraulic structures, mostly reaching their design service life,  
45 makes the adoption of specific interventions of paramount international relevance.

46 Given the significant length extension of these structures, and the localized nature of weakness  
47 points, the characterization cannot rely only on local geotechnical investigations but requires the  
48 application of efficient and economically affordable methods, able to investigate the whole  
49 embankments in a profitable way. Moreover, geotechnical investigations usually require invasive  
50 procedures (such as boreholes, penetration tests, etc) that are both expensive and time-consuming.  
51 With this respect non-invasive, rapid and cost-effective methods are desirable to identify higher  
52 potential hazard zones.

53 Among the available non-invasive geophysical methods (Chao et al., 2006; Bergamo et al., 2016;  
54 Takahashi et al., 2014; Sentenac et al., 2018), the seismic ones have peculiar advantages for the soil  
55 characterization. Seismic velocities, and particularly shear wave velocity ( $V_s$ ), are directly related  
56 to the dynamic stiffness of the material, which is an important mechanical parameter for the  
57 recognition of soil layers. Moreover, in the field of geotechnical engineering, huge research effort  
58 has been spent on the correlation of  $V_s$  to parameters obtained from standard geotechnical tests. Site  
59 specific and general correlations exist to porosity, plasticity index, to the shear modulus at higher  
60 strains and to standard geotechnical in situ tests such as cone penetration, standard penetration and  
61 dilatometer tests (e.g. Kramer, 1996; Samui, 2010; Foti et al., 20014).

62 Among the seismic methods the multichannel analysis of surface waves (MASW), based on the  
63 Rayleigh wave dispersion curve (DC) analysis, is considered the most effective for the  
64 determination of  $V_s$  profiles. This method can be efficiently applied to seismic streamer data  
65 dragged along embankments and overall linear earth structures. This allows the determination of  
66 several  $V_s$  profiles to offer an almost 2D representation of the velocity field. Several literature  
67 applications of this methodology are available along embankments, river dykes and earth dams (e.g.  
68 Lutz et al., 2011; Lane et al., 2008; Min and Kim, 2006). Eventually, MASW surveys can be used  
69 in combination with geoelectrical and geotechnical methods to allow for more complete  
70 characterization (e.g. Samyn et al., 2014; Busato et al., 2016; Bièvre et al., 2017; Rahimi et al.,  
71 2018; Arato et al. 2020).

72 The main limitations of this methodology are related to the high non-linearity of the DC inversion  
73 procedure and to the lack of compressional wave velocity ( $V_p$ ) information. Several global  
74 inversion approaches have been proposed for the DC inversion (e.g. [Socco and Boiero, 2008](#)), with  
75 the aim of tackling the problem of non-uniqueness of the solution. More elaborated inversion  
76 strategies for reconstructing 2D shear wave velocity sections including waveform information (e.g.  
77 wave-equation dispersion inversion (WD), [Li et al., 2017](#), or multi-objective waveform inversion  
78 (MOWI), [Pan et al., 2020](#)) have been also proposed. Nevertheless, all these approaches are highly  
79 time consuming, particularly for increasing number of DCs to be analysed, and can be adopted only  
80 in the post-processing stage, not allowing for an effective in situ characterization. The lack of  $V_p$   
81 information can also be a disadvantage since  $V_p$  is known to be correlated with saturation levels  
82 and related Poisson ratio of the materials. This last could be indeed an important parameter to be  
83 determined along river embankments, to complete the characterization.

84 To overcome these limitations, the application of a new procedure ([Socco et al., 2017](#); [Socco and](#)  
85 [Comina, 2017](#)) for the analysis of Rayleigh wave fundamental mode DC is adopted in this paper.  
86 This procedure is based on the relationship between Rayleigh wave wavelength and investigation  
87 depth (W/D procedure) and exploit the higher sensitivity of the DCs to time-average shear wave  
88 velocity ( $V_{s,z}$ ) than to layered velocity profiles and the sensitivity of the Rayleigh wave skin depth  
89 to  $V_p$ . The W/D procedure allows the determination of both 2D  $V_s$  and  $V_p$  sections from the DCs  
90 using a direct data transform approach. The relationship between the wavelength of the Rayleigh  
91 wave fundamental mode and the investigation depth (W/D relationship) is estimated through a  
92 reference  $V_s$  and  $V_{s,z}$  profile and used to directly transform all DCs into  $V_s$  profiles. The sensitivity  
93 of the W/D relationship to Poisson ratio is moreover exploited to obtain also  $V_p$  profiles along the  
94 studied embankment. The procedure has already demonstrated its reliability both on synthetic and  
95 real data, producing  $V_s$  and  $V_p$  models which allow a reliable waveform matching in comparison to  
96 benchmarks ([Khosro Anjom et al., 2019](#)) and effective full waveform inversion starting models  
97 ([Teodor et al., 2020](#)).

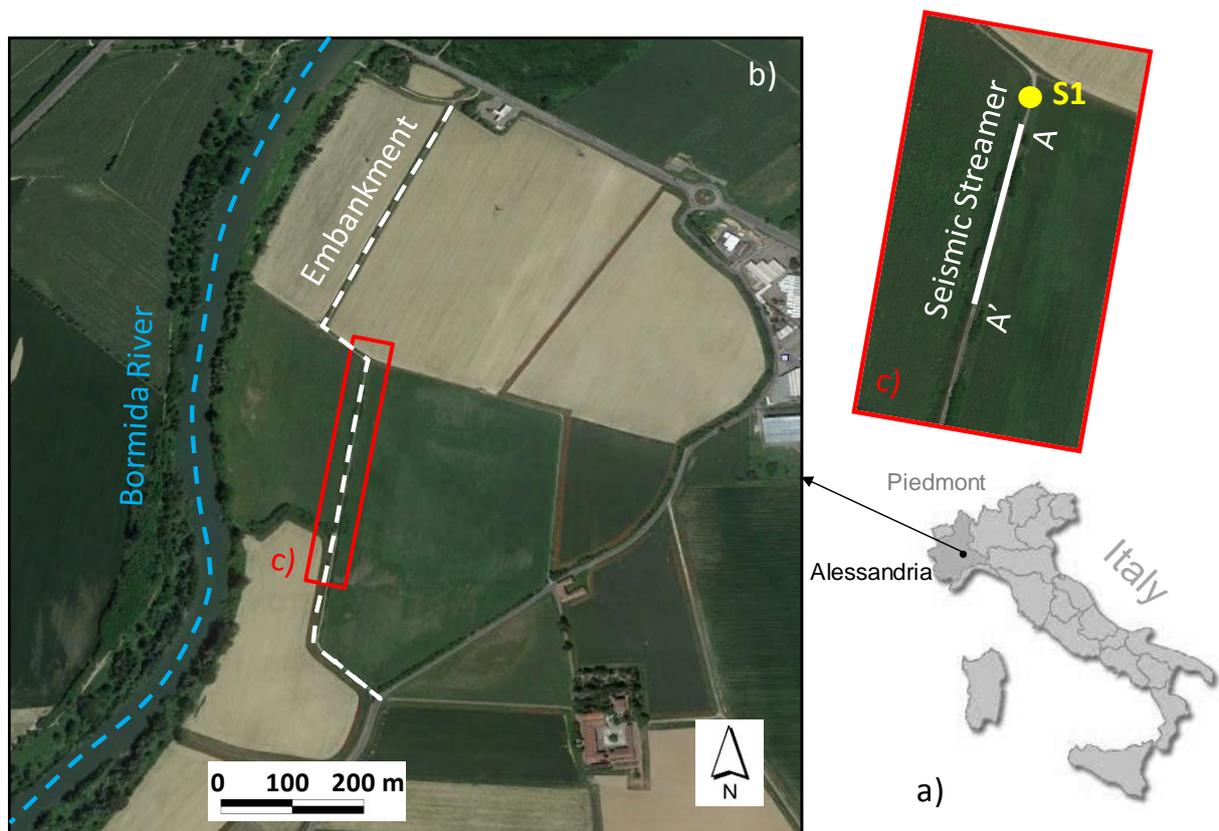
98 Another significant advantage of the proposed W/D procedure is that, being a data transform  
99 approach, it does not have particular computational requirements. In principle, it could therefore be  
100 applied also during in situ measurement campaigns for a fast imaging of the seismic properties of  
101 the studied embankment. This products a strong reduction of survey time and increased efficiency.  
102 In this paper, the procedure is specifically implemented for surface waves streamer data and its  
103 application to the characterization of a test site (Bormida river embankment, Piedmont Region,  
104 Italy) is presented. It is shown that the obtained results are comparable to standard seismic

105 processing approaches with the advantage of reduced survey time and increased efficiency, and that  
106 preliminary results can be obtained directly during in situ measurements.

107

## 108 2. TEST SITE AND EXECUTED SURVEYS

109 The test site investigated in this paper is the right embankment of the Bormida river, east of the city  
110 of Alessandria, in Spinetta Marengo municipality, Piedmont Region, NW Italy (Figure 1). The  
111 embankment is separated from the river by the presence of a 200 m wide floodplain that serves as  
112 expansion area during floods (Figure 1). The top of the embankment rises about 9 m from the free  
113 surface of the river, and about 3 m from the floodplain. The soil composition of the embankment  
114 (embankment body and foundation) was obtained by available geotechnical tests: a borehole,  
115 executed on the top of the embankment in correspondence of an embankment curve (S1, in Figure 1  
116 inlet) and a dynamic penetration super heavy test (DPSH) executed in the proximity of the borehole.  
117 Both the borehole and DPSH interested embankment body and foundation soil till about 16 m  
118 depth.



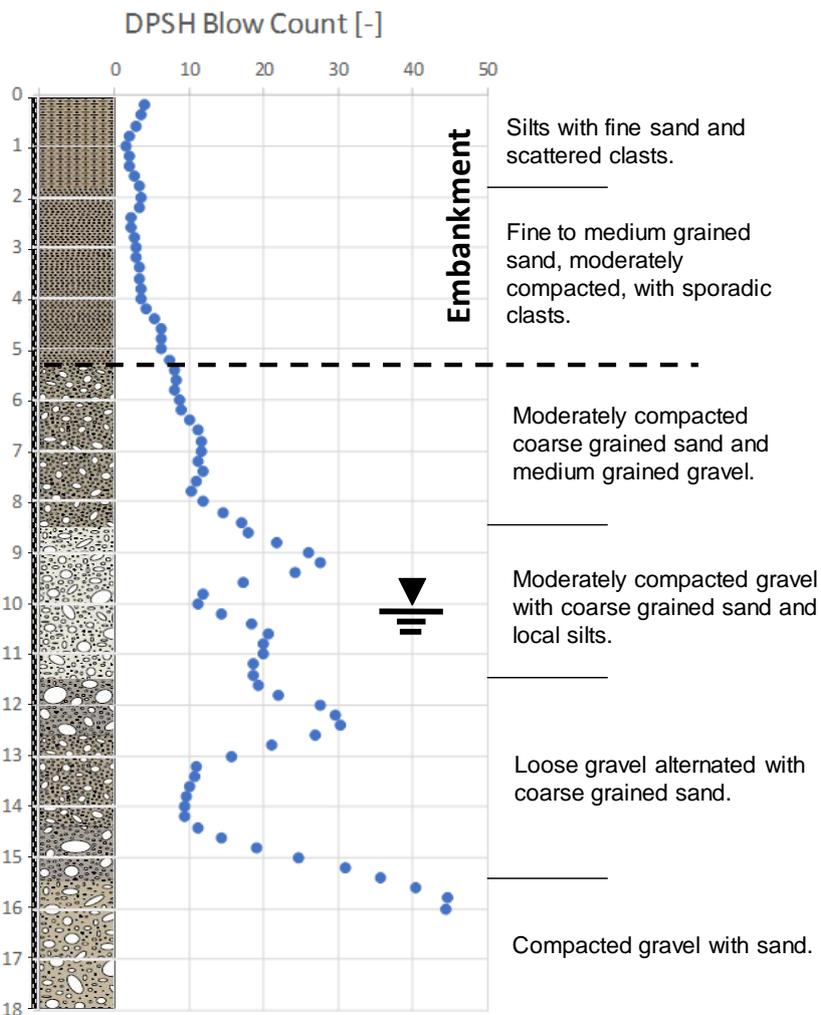
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120 **Figure 1 – Location of the test site: a) north western Italian Po plain, Piedmont region, near the city of**  
121 **Alessandria, b) detail of the studied embankment and c) executed surveys.**

122 The geotechnical setting (Figure 2) can be synthesized as constituted by silts with fine sands and  
123 scattered clasts changing to fine to medium grained sands, moderately compacted, with sporadic

124 clasts, up to about 5.3 m depth (embankment body) overlaying a coarse sand and gravel formation  
 125 moderately to medium compacted with intercalated silts and local compaction reduction with depth.  
 126 At the moment of execution of the borehole (November 2007) the water table was reported at about  
 127 10 m depth from the embankment top; given the height of the river, the water table is therefore  
 128 supposed to be fed by the river and its elevation strictly dependent on the water level within the  
 129 river.

130 As it can be observed in the stratigraphic log, the transition from embankment body to natural  
 131 subsoil does not appear to be particularly sharp. This can be an indication that the construction  
 132 procedure did not involved relevant reworking of the first subsoil and that lateral differences in  
 133 depth and nature of this contact could be present along the embankment. Taking as reference the  
 134 DPSH result, local eventual differences along the embankment body will be investigated using  
 135 seismic streamer data dragged along a specific portion of the embankment (Figure 1).



136

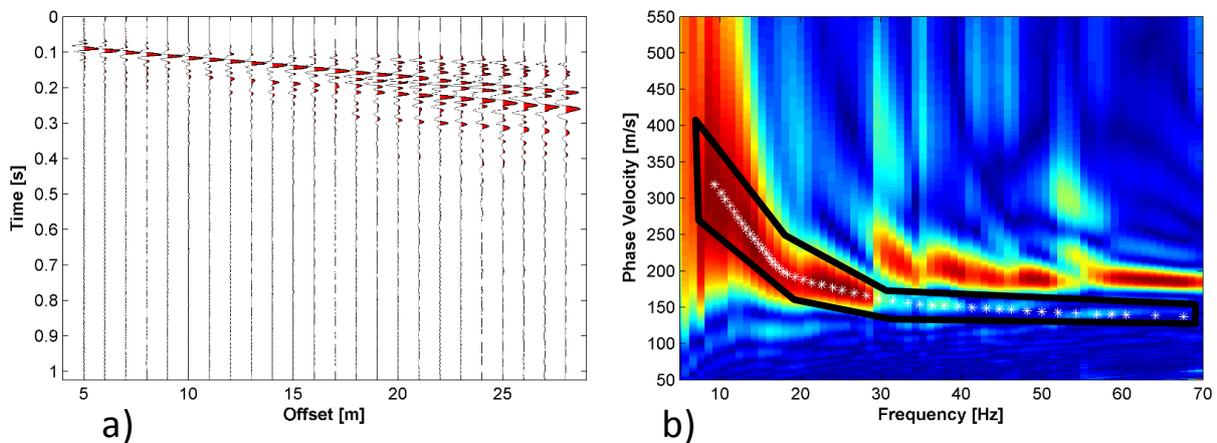
137 **Figure 2 – Stratigraphic log and geotechnical description of the encountered formations with evidence**  
 138 **of the DPSH results.**

139 An embankment sector of about 90 m, south with respect to the S1 borehole (Figure 1), was  
140 investigated in May 2019 with a seismic land streamer constituted of 24, 4.5 Hz vertical geophones  
141 mounted on coupling sliders at 1 m spacing. The streamer was dragged by a pick-up truck and was  
142 moved along the studied reach at 2 m steps; for each moving step a single seismic shot was  
143 registered. The seismic source was a 40 kg accelerated mass mounted on the pick-up back; a 5 m  
144 source offset was adopted in the acquisitions. The streamer was connected to a DaQLink IV  
145 (Seismic Source, 2016) acquisition device on the pick-up truck, storing the data in a survey laptop  
146 and eventually applying pre-processing steps. Seismograms were acquired with a 0.5 ms sampling  
147 interval, -50 ms pretrig and 1.024 s total recording length. A total of 45 seismograms were therefore  
148 acquired during the survey. On these data several processing steps were applied for the definition of  
149 2D Vs and Vp models with the proposed W/D procedure.

150

### 151 3. METHODOLOGY

152 An example seismic shot is reported in Figure 3a. The used source and streamer setup allowed the  
153 acquisition of high-quality data, with clear evidence of surface waves dispersive pattern and also  
154 particularly evident first arrivals of compressional waves.



155

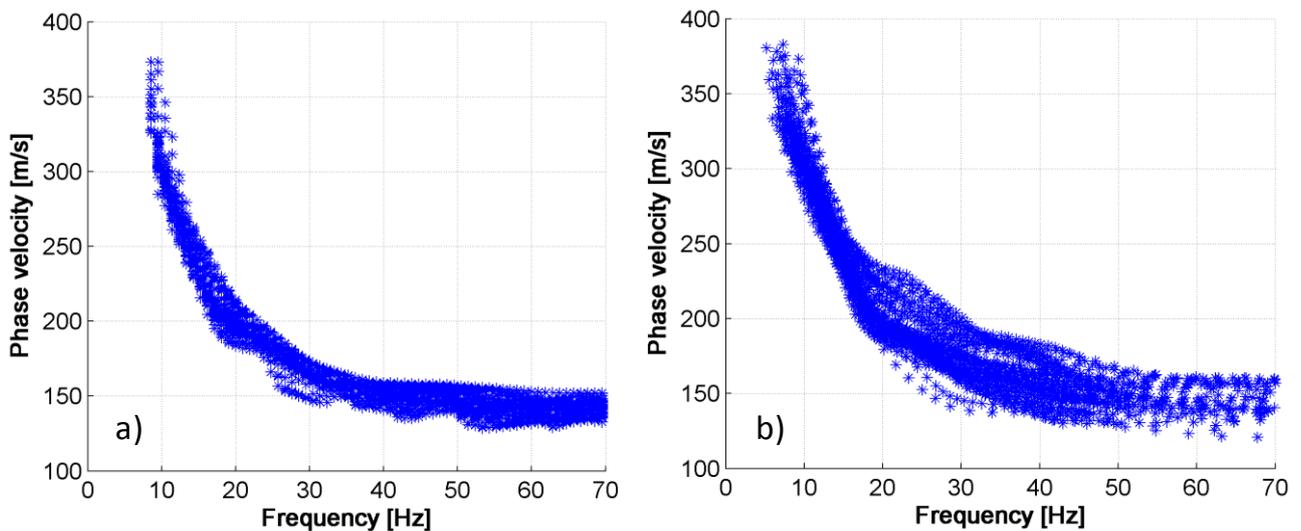
156 **Figure 3 – Data processing procedures on acquired seismograms: a) example seismic shot, b)**  
157 **dispersion curve extraction with evidence of the applied mask (black line) and selected high energy**  
158 **maxima (white asterisks).**

159 DCs extraction was performed with two different procedures: first, the dispersion image for each  
160 seismogram was obtained by means of a phase-shift approach (Park et al., 1998) implemented in  
161 MATLAB® routines. The phase-shift approach has demonstrated to maintain very good  
162 performances even when a limited number of traces is considered (Dal Moro et al., 2005).  
163 Alternatively, to further improve the accuracy of dispersion measurement, a multi-channel

164 nonlinear signal comparison (MNLSC, [Hu et al., 2019](#)) can be adopted, producing high and  
165 adjustable resolution among a wide detected frequency range.

166 On the dispersion image the zone pertinent to the fundamental mode propagation was selected with  
167 a mask (black line in [Figure 3b](#)) and energy maxima were automatically searched within this area  
168 (white asterisks in [Figure 3b](#)). The mask selected for the first shot can be either automatically used  
169 for all the following shots (automatic procedure) or partially adjusted to follow eventual variations  
170 in the energy distribution (semi-automatic procedure). In the first case a rough, but fully automated,  
171 DCs selection is obtained, in the second case a more refined, but more time consuming, analysis is  
172 allowed, to better evidence eventual lateral variations. On both these selected DC groups eventual  
173 smoothing and manual outlier removal can be applied to obtain more continuous and reliable  
174 curves.

175 In [Figure 4](#) the resulting DCs selected for all the shots from automatic and semi-automatic  
176 procedures are reported. For some of the shots a transition of the absolute energy maxima towards  
177 higher modes was observed in the high-frequency range (e.g. frequencies higher than 30Hz in  
178 [Figure 3b](#)). Nevertheless the fundamental mode can still be followed as local maxima thank to the  
179 adopted mask that allowed to isolate the correct portion of the dispersion image to be considered,  
180 excluding the higher modes from the maxima searching. It can be evidenced that the DC ranges are  
181 very similar with corresponding velocity transition. Nevertheless, the semi-automatic procedure  
182 ([Figure 4b](#)) shows higher variability for the medium-high frequency range (shallower layers) as a  
183 result of the application of a variable mask. Most of the results reported in the paper refer to the  
184 DCs selected with this approach. In the discussion section some comparisons are however presented  
185 with the results obtainable with the automatic procedure also.



186

187 **Figure 4 – DCs selected for all the shots: a) automatic procedure and b) semi-automatic procedure.**

188 The application of the W/D procedure to the extracted DCs requires the knowledge of a single  $V_s$   
189 and  $V_{s,z}$  reference profile along the seismic line together with its associated DC. This profile can be  
190 either extracted from the data themselves, by performing the inversion of a representative DC  
191 among the ones extracted, or it can be obtained by independent seismic or geotechnical data.

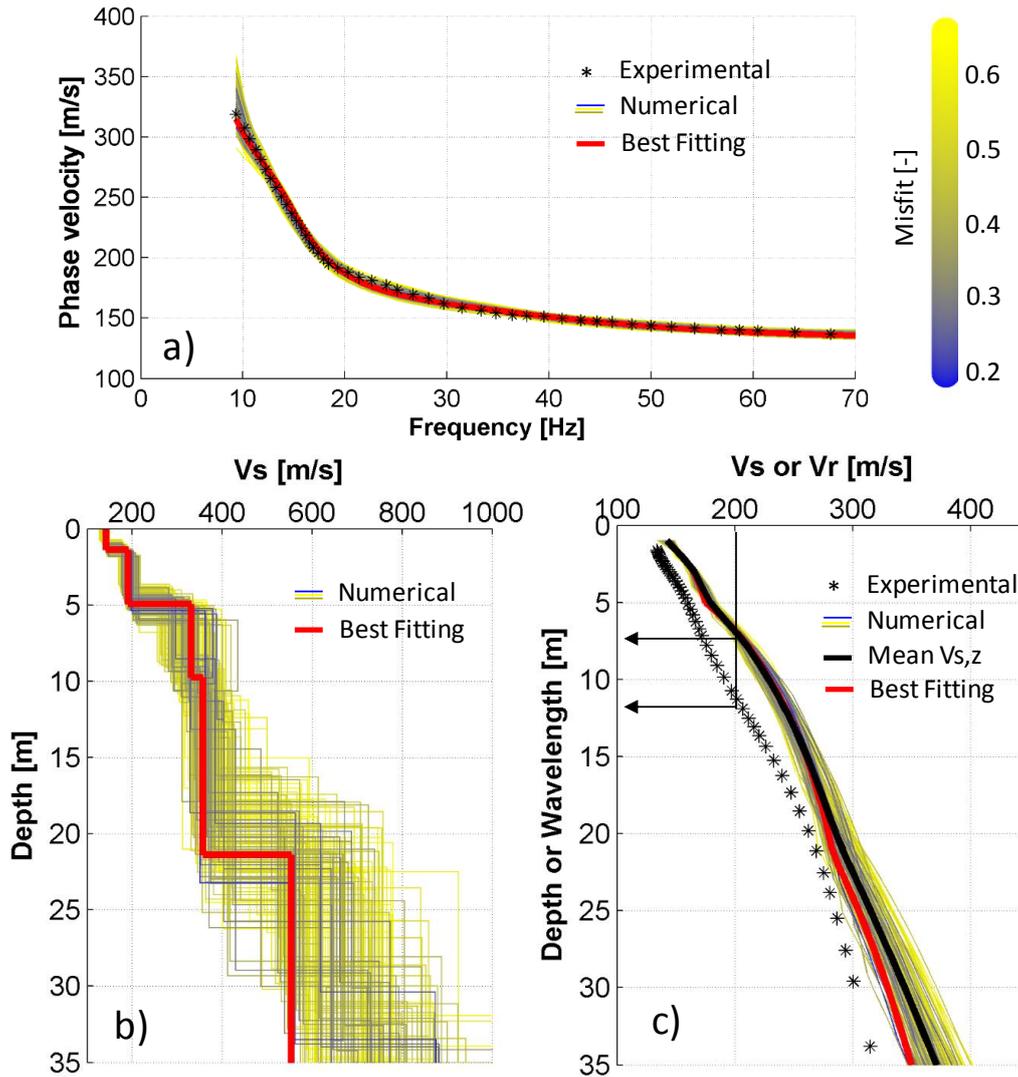
192 In this paper the first method was adopted using a Monte Carlo Inversion (MCI) algorithm (Socco  
193 and Boiero, 2008) which efficiently limits potential non-uniqueness of the solution and results in  
194 reliable  $V_s$  and  $V_{s,z}$  profiles. The inversion implies the definition of a wide model space by  
195 selecting ranges for each model parameter ( $V_s$ , thicknesses and the Poisson ratio of each layer) and  
196 performing random sampling ( $10^5$  profiles) among these ranges. Please note that, in order to allow  
197 for the W/D procedure to be applied, also Poisson ratio of each layer is considered as a model  
198 parameter, contrary to what usually performed in the inversion of DC curves.

199 Example application of the inversion process to the DC reported in Figure 3b, which was selected  
200 as reference, is reported in Figure 5. It can be observed that the set of statistical equivalent profiles  
201 selected from the MCI assess the presence of a contrast at the bottom of the embankment around 5  
202 m depth (Figure 5b). This set of profiles, and their correspondent numerical DCs, is represented in  
203 Figure 5 with a relative misfit representation based on the absolute difference between each profile  
204 misfit and the best fitting one (in red in Figure 5).

205 It can also be noted that the higher variability in terms of  $V_s$  profiles (Figure 5b) strongly reduces  
206 when the time average shear wave velocity is considered ( $V_{s,z}$ , in Figure 5c). With this respect the  
207 best selected profile (in red in Figure 5c) and the mean of the statistical set (in black in Figure 5c)  
208 almost superimpose for the top portion of the profile. Socco and Comina (2015) have already shown  
209 that the non-uniqueness of the DC inversion very slightly affects the estimation of time-average  
210 velocity, and hence, the  $V_{s,z}$  obtained from inverted profiles is very robust. Nevertheless, given the  
211 increased uncertainty at the bottom of the profile, the following analyses were limited to 20 m  
212 depth, which is enough for investigating both the embankment and a significant portion of the  
213 foundation subsoil at the studied test site.

214 Using the reference  $V_s$  and  $V_{s,z}$  profiles and all the extracted DCs, the proposed data transform  
215 procedure is then applied as following: i) the estimated  $V_{s,z}$  and its corresponding DC are used to  
216 compute the reference W/D relationship; ii) the reference W/D relationship is used to transform all  
217 DCs into  $V_{s,z}$  models; iii) an apparent Poisson ratio is estimated using the reference W/D  
218 relationship and the reference  $V_s$  model; iv) using the apparent Poisson ratio, each  $V_{s,z}$  profile is  
219 transformed into a  $V_{p,z}$  profile; v) all the reconstructed  $V_{s,z}$  and  $V_{p,z}$  profiles are transformed into  
220  $V_s$  and  $V_p$  profiles with an interval velocity analysis.

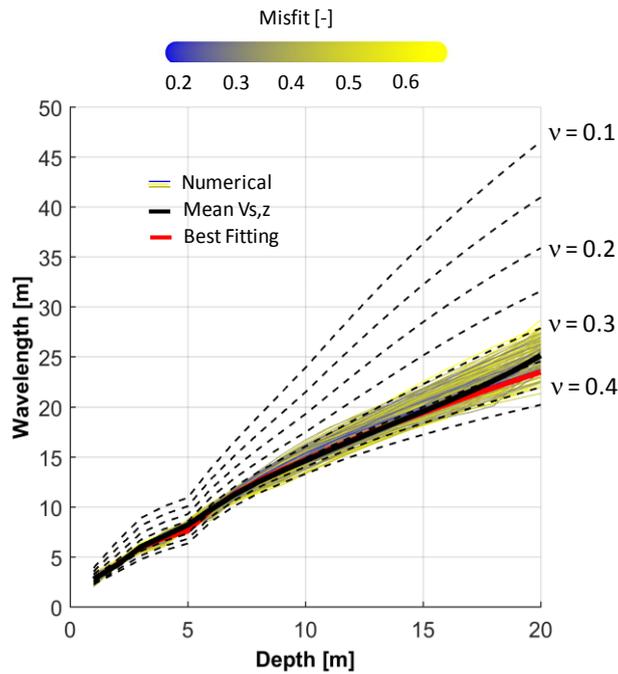
221



222

223 **Figure 5 – MCI of the reference DC curve: a) experimental and numerical dispersion curves b) best**  
 224 **fitting profile and set of statistically equivalent profiles and c) experimental dispersion curve as a**  
 225 **function of wavelength, time average velocities of best fitting profile and statistically equivalent**  
 226 **profiles with their mean.**

227 Steps i) and iii) of the procedure require more explanations. The meaning of the W/D relationship is  
 228 represented in [Figure 5c](#): for each  $V_{s,z}$  value, the wavelength (W) at which the phase velocity ( $V_r$ )  
 229 of the DC is equal to the  $V_{s,z}$  (see the arrows in [Figure 5c](#)) is searched for each depth (D). With all  
 230 the W/D pairs at which  $V_{s,z}$  and phase velocity are equal a relationship is obtained (W/D  
 231 relationship). This relationship is represented in [Figure 6](#) for the best fitting profile (in red), for the  
 232 mean of the statistically equivalent profiles (in black) and for all the statistically equivalent profiles.  
 233 Consistency of the extracted W/D relationships is evidenced.



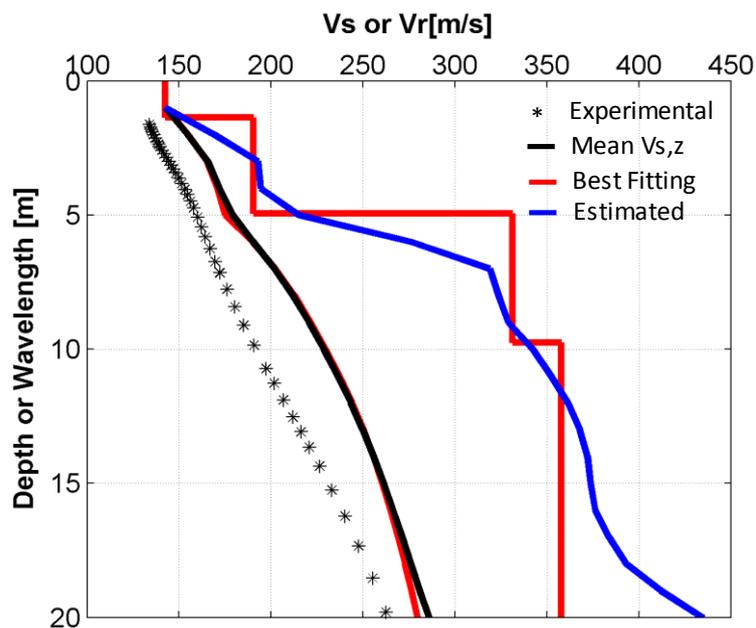
234

235 **Figure 6 – The W/D relationship for the reference DC for the best fitting profile (in red), for the mean**  
 236 **of the statistically equivalent profiles (in black) and for all the statistically equivalent profiles**  
 237 **compared with the ones obtained with different Poisson ratio values. Reference Poisson ratio values**  
 238 **are indicated on the right of the plot.**

239 This relationship represents the surface waves' skin depth for increasing wavelengths and has been  
 240 demonstrated (Socco and Comina, 2017) to be influenced by the Poisson ratio of the formation.  
 241 With the reference  $V_s$  and  $V_{s,z}$  profiles it is therefore possible to build different synthetic W/D  
 242 relationships by changing the value of the Poisson ratio ( $\nu$ ) of the layers (assumed constant for all  
 243 the layers). These synthetic W/D relationships are reported in Figure 6 (dashed black lines) for  
 244 some example values of the Poisson ratio. It can be noted that Poisson ratio acts on the slope of  
 245 W/D relationship. In particular, the slope decreases when Poisson ratio increases. Therefore the  
 246 slope of the experimentally determined W/D relationship contains information on the actual Poisson  
 247 ratio of the formation. The actual apparent Poisson ratio profile of the formation can be therefore  
 248 searched by associating to each depth the value of Poisson ratio that corresponds to the linear  
 249 interpolation between the upper and lower nearest synthetic W/D relationships. In this way an  
 250 apparent Poisson ratio profile with depth can be obtained for the reference DC. This profile can be  
 251 later used to transform all the  $V_{s,z}$  profiles into  $V_{p,z}$  profiles allowing for a 2D  $V_p$  section to be  
 252 later computed.

253 An example application of the W/D procedure to the reference DC is reported in Figure 7. It can be  
 254 observed that the  $V_{s,z}$  of the best fitting profile (continuous red line in Figure 7) and the mean  $V_{s,z}$   
 255 of the statistical set (continuous black line in Figure 7) almost superimpose for the first 20 m depth.

256 It can be also noted that the W/D procedure allows the estimate of a  $V_s$  model (in blue in Figure 7)  
 257 very near to the best fitting one (layered red line in Figure 7) obtained from the MCI of the DC. The  
 258 model obtained with this procedure has also the advantage of not making any assumption with  
 259 respect to the number of layers of the profile. For this reason, it can result smoother with respect to  
 260 the layered profile but also more correspondent to the actual geotechnical situation below the  
 261 embankment. Particularly, it can be observed that the transition from embankment body to bottom  
 262 layers with this estimated profile appear to be more correspondent to what evidenced in the DPSH  
 263 results (Figure 2) with respect to the sharp interface evidenced by the MCI result.



264  
 265 **Figure 7 – Application of the W/D procedure to the reference DC for  $V_s$  profile determination and**  
 266 **comparison with the best fitting result (both in term of layered velocity model and  $V_{s,z}$ ) from MCI.**

267 All the  $V_s$  and  $V_p$  profiles estimated with the W/D procedure are then interpolated along the studied  
 268 embankment to allow for a 2D visualization of the  $V_s$  and  $V_p$  velocities distributions. The data  
 269 gridding was performed in Surfer (Golden software) with an interpolation grid of 2 m in the  
 270 horizontal direction (equal to the acquisition step) and of 0.5 m in the vertical direction.

271 To validate the velocity models obtained with the application of the W/D procedure the obtained  
 272 results are benchmarked against standard seismic processing approaches. For  $V_s$ , all the dispersion  
 273 curves extracted were inverted with a laterally constrained inversion (LCI) approach (Auken and  
 274 Christiansen, 2004; Socco et al., 2009). For this inversion, the same number of layers of the MCI  
 275 was assumed. For  $V_p$ , processing was carried out by picking the first breaks on each acquired  
 276 seismogram, picked first breaks were then interpreted in tomographic approach with the use of the  
 277 software Rayfract (Intelligent Resources Softwares Inc.).

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#### 4. RESULTS

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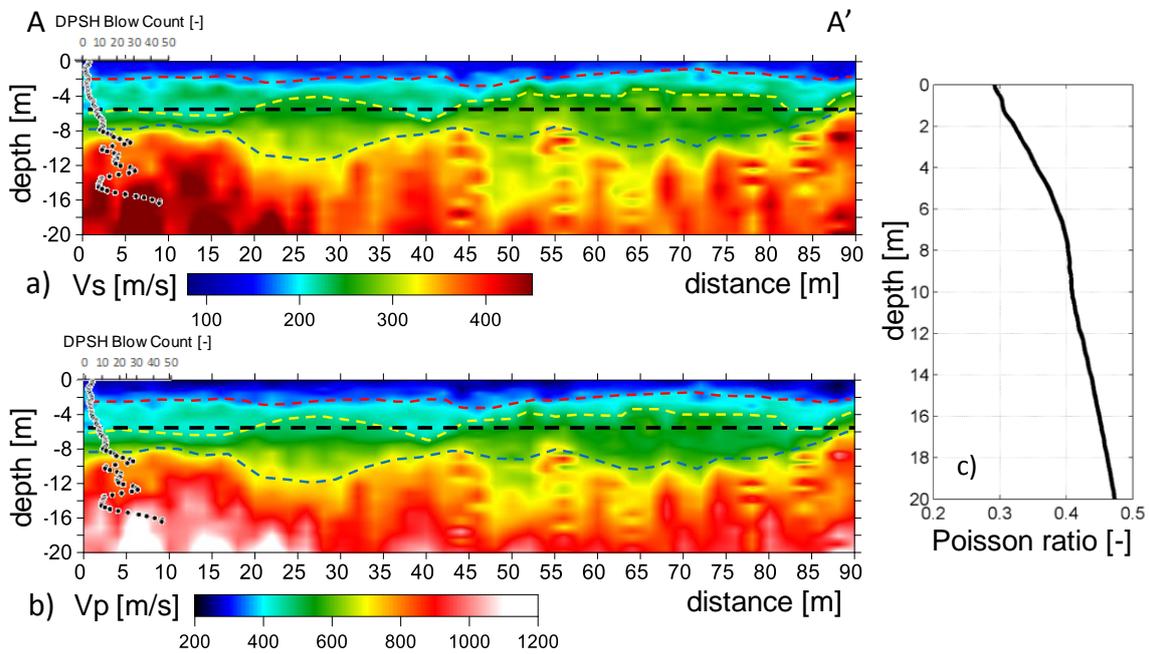
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Results of the application of the W/D procedure are reported in Figure 8. Particularly, the  $V_p$  result is obtained from the  $V_s$  one with the application of the apparent Poisson ratio obtained from the W/D procedure. This last is assumed constant through the whole profile and therefore the resulting  $V_p$  velocity field is a transformation of the  $V_s$  one with similar properties. Both  $V_s$  and  $V_p$  sections can discriminate the transition from the shallow silts and sands to the bottom gravels along the embankment and delineate the embankment bottom. Coherently with the borehole results and geotechnical tests this transition falls, on the left side of the sections, where the surveys are nearer to the geotechnical tests (the DPSH Blow Count profile is also reported in Figure 8a and b), around 5.3 m depth.



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**Figure 8 – Results of the application of the W/D procedure to extracted DCs (section A-A’): a)  $V_s$  section, b)  $V_p$  section and c) resulting Poisson ratio. On both the sections the supposed depth of the embankment is also reported (dashed black line) together with coloured dashed lines, derived by the velocity models, indicating the transition between the shallow silts and sands (in red), the thickness of the embankment (in yellow) and the transition to compacted gravels and sands (in blue). The DPSH Blow Count profile is also reported at the beginning of the sections.**

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However, along the embankment a variation of the depth of this interface can be evidenced. Particularly, localized anomalies appear in the  $V_s$  section suggesting an increase in the depth of the shallow silts and sands of the embankment (yellow dashed line in Figure 8) around 40 m progressive distance. Conversely, the depth of the interface appears to be shallower in the progressive distance range between about 50 to 80 m.

300 Seismic surveys are also able to depict the transition (red dashed line in Figure 8) from silts with  
301 fine sands and scattered clasts to fine to medium grained sands, as reported from the borehole and  
302 DPSH results, within the embankment. A deeper increase in velocity is also observed around 8 m  
303 depth on the left side of Figure 8, were the transition to more compacted gravels (blue dashed line  
304 in Figure 8) is evidenced by borehole and DPSH results . This more compacted formation appears  
305 however to increase its depth along the section moving away from the borehole and showing on  
306 average lower velocity values. Localized velocity inversions are also partially observable below 8 m  
307 in the leftmost portions of the Vs section. This evidence again well compares with what reported by  
308 the DPSH results.

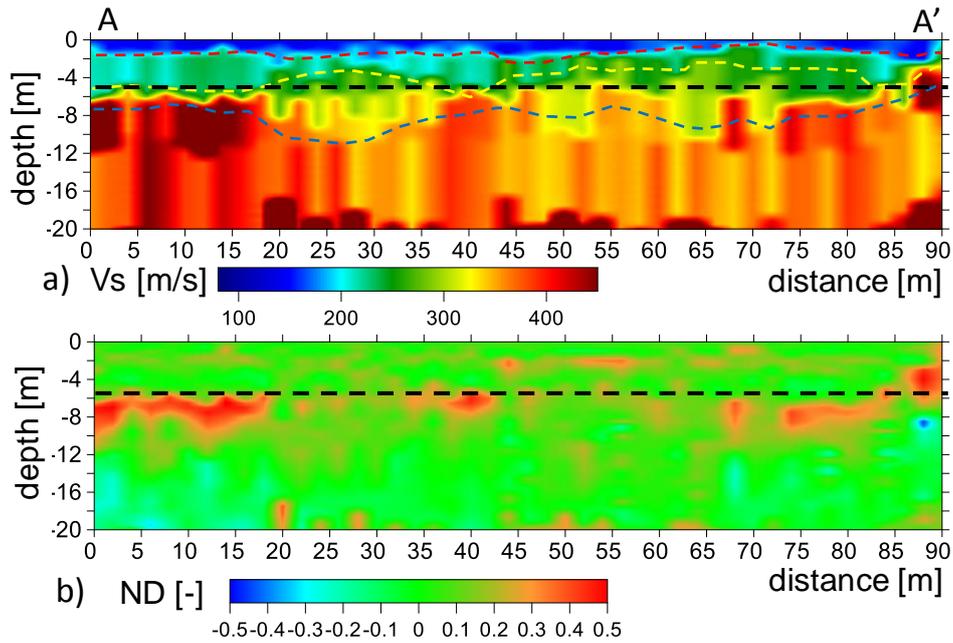
309 Notwithstanding the information on the position of the water table at the site (around 10 m) the  
310 range of Vp velocities extracted by the procedure does not report, for increasing depths, velocity  
311 ranges usually attributed to saturated materials (i.e. around 1400-1500 m/s). It must be underlined  
312 that the time span between the two surveys is relevant (from November 2007 to May 2019) so that  
313 eventual variations on the water table depth could be present. Nevertheless, the Poisson ratio profile  
314 extracted with the W/D procedure (Figure 8c) shows a marked increase nearly around 10 m  
315 exceeding the 0.4 value and tending to 0.5. Poisson ratio of saturated soils is usually reported to be  
316 in this range (Boore, 2007). It must be underlined that the Poisson ratio profile here presented is the  
317 interval Poisson ratio obtained through the Vp/Vs ratio of the resulting models. This is different  
318 from the apparent Poisson ratio that is estimated in the W/D procedure (Figure 6) for the DC  
319 transformation.

320 Results of the LCI processing of the extracted dispersion curves are reported in Figure 9a. A good  
321 convergence of the inversion was obtained with LCI resulting in a final RMS error of 1.7%.

322 The comparison of the LCI result with the W/D procedure is performed in Figure 9b in term of  
323 normalized differences, taking as reference the LCI results, with the formula:

$$324 \quad ND = \frac{V_{i,LCI} - V_{i,W/D}}{V_{i,LCI}} \quad (1)$$

325  
326 were  $V_{i,W/D}$  is the velocity value obtained from the W/D procedure and  $V_{i,LCI}$  is the velocity value  
327 obtained from the LCI in each location within the models. Therefore, positive values of the  
328 normalized difference indicate zones where the W/D procedure underestimate the velocity, negative  
329 values indicate the opposite. To allow computing the normalized differences in each point of the  
330 models also layered LCI results were gridded with the same interpolation scheme of the W/D  
331 procedure results.



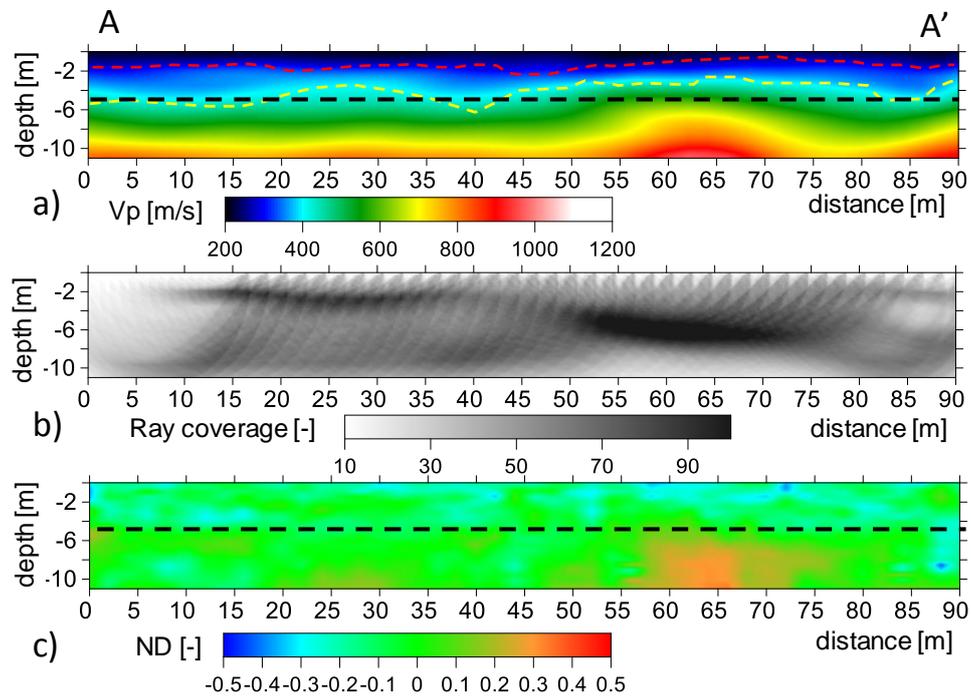
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333 **Figure 9 – Results of the LCI of the extracted DCs (section A-A’): a) Vs section and b) Normalized**  
 334 **differences with the Vs results of the W/D procedure. On both the sections the supposed depth of the**  
 335 **embankment is also reported (dashed black line). Over the LCI section, the interfaces evidenced by the**  
 336 **W/D procedure indicating the transition between the shallow silts and sands (in red), the thickness of**  
 337 **the embankment (in yellow) and the transition to compacted gravels and sands (in blue), are**  
 338 **superimposed.**

339 **Figure 9** shows that the Vs velocity range obtained using LCI inversion is comparable with that  
 340 from the W/D procedure. The interfaces evidenced by the W/D procedure are reported for  
 341 comparison over the resulting Vs image. Similar variability in the depth of the interfaces is noted.  
 342 As an example, both the increased depth of shallower silts and sands around progressive 40 m and  
 343 the shallower depth of the embankment in the progressive distance range between about 50 to 80 m  
 344 are confirmed. Most of the normalized differences among the W/D and LCI models fall within a  
 345  $\pm 10\%$  range indicating the good correspondence of the two results. The only portions of the section  
 346 affected by higher positive normalized differences cannot be attributed to errors in the W/D  
 347 procedure, but to the layering assumption in the LCI. The layered discretization adopted in the LCI  
 348 can indeed result in an overestimation of the velocity near the layer boundaries (see also **Figure 7**  
 349 for comparison). Most of the higher difference values fall indeed near the embankment/foundation  
 350 soil interface where the layered profile results from LCI tend to give a sharper transition than the  
 351 W/D result.

352 Results of the tomographic inversion of picked first arrivals are reported in **Figure 10** and  
 353 compared, in term of normalized differences, with the Vp results obtained with the W/D procedure.  
 354 The same equation 1 was adopted for the computation of normalized differences with Vp values

355 from W/D procedure and first arrivals tomography (these last substituting the LCI values in  
356 equation 1).



357

358 **Figure 10 – Results of the first break tomography (section A-A’): a) Vp section, b) Ray coverage along**  
359 **the section and c) Normalized differences with the Vp results of the W/D procedure. On both the**  
360 **sections the supposed depth of the embankment is also reported (dashed black line). Over the**  
361 **tomography the first two interfaces evidenced by the W/D procedure, indicating the transition**  
362 **between the shallow silts and sands (in red), the thickness of the embankment (in yellow), are**  
363 **superimposed.**

364 From Figure 10 it can be observed that, given the reduced length of the streamer adopted, the depth  
365 of investigation of the tomography is limited to about 10 m, or even less in some portions.  
366 Nevertheless, within this depth, a high ray coverage is obtained in most of the section by the  
367 combined elaboration of all the shots. A good convergence of the inversion was obtained with a  
368 resulting RMS error of 2.7% after the final iteration.

369 Again, from Figure 10 it can be observed that the tomographic inversion depicts the same velocity  
370 range compared to the one obtained with the W/D procedure. Given the reduced investigation depth  
371 of the tomography only the first two interfaces evidenced by the W/D procedure are reported for  
372 comparison over the resulting Vp image. Similar variability in the depth of these two interfaces is  
373 noted. As an example, both the increased depth of shallower silts and sands around progressive 40  
374 m and the shallower depth of the embankment in the progressive distance range between about 50  
375 to 80 m are confirmed. Being based on relatively long-path raytracing, the tomographic result

376 shows generally a reduced lateral resolution in the identification of the velocity variations within the  
377 section.

378 Most of the normalized differences, also for  $V_p$ , fall within a  $\pm 10\%$  range indicating the good  
379 correspondence of the two results. The only portion of the section showing higher normalized  
380 differences can be attributed to a lower ray coverage zone (see [Figure 10b](#) below 7 m at about 55 to  
381 70 progressive distances) making the assumed  $V_p$  values less reliable in the tomography. Given its  
382 shallower investigation depth, also the tomography does not highlight a marked increase of  $V_p$   
383 values, at the bottom of the model, attributable to the presence of the water table.

384

## 385 **5. DISCUSSION**

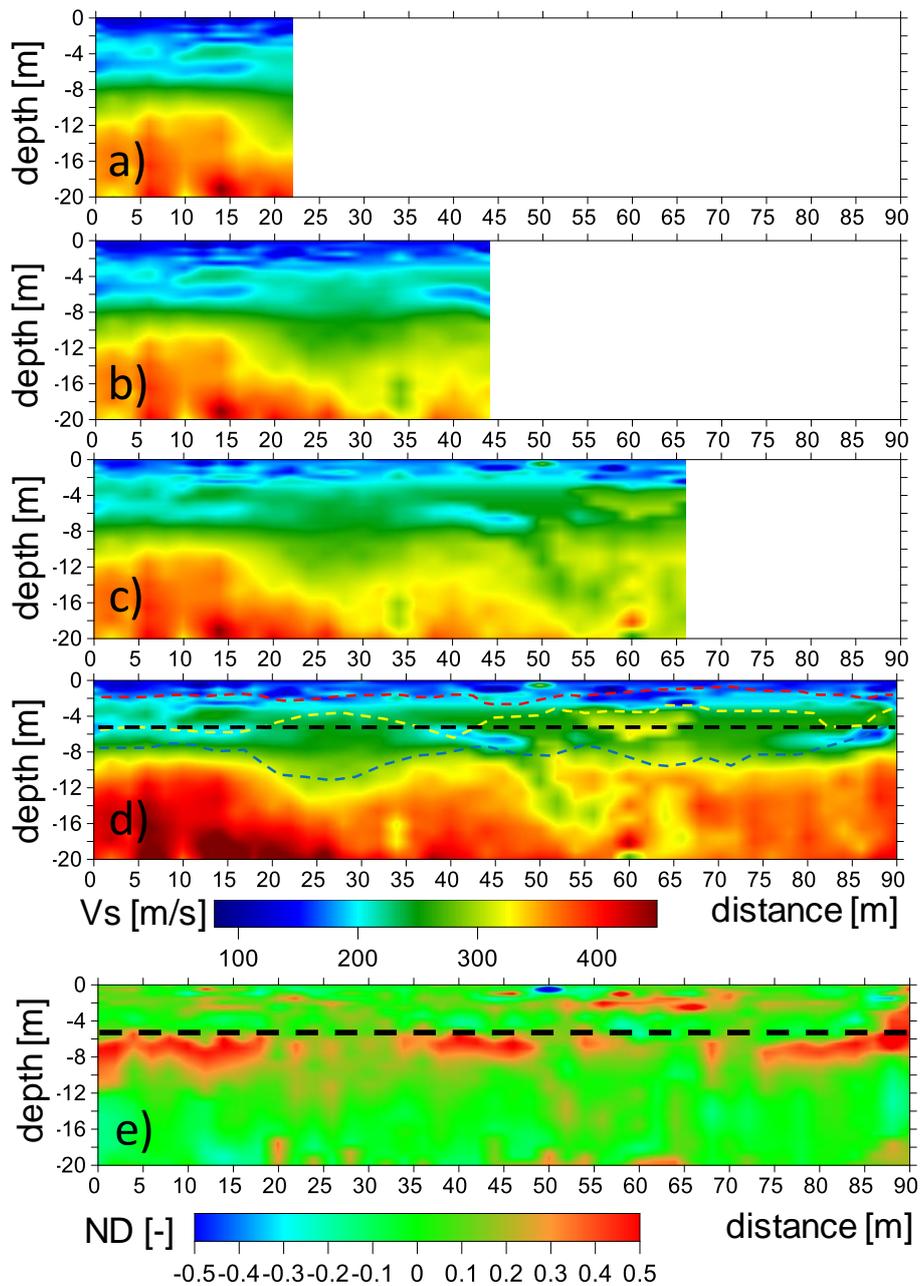
386 It was shown in the paper that the results obtainable with the W/D procedure are comparable both in  
387 terms of  $V_s$  and  $V_p$  to standard seismic processing approaches. This comparison validates therefore  
388 the application of the W/D procedure. It was observed, in the presented case study, that most of the  
389 normalized differences between the W/D procedure and both LCI and first arrivals tomography fall  
390 within a  $\pm 10\%$  range, indicating the good correspondence of the two results. Higher normalized  
391 differences along the sections can be attributed to different resolution or underlying  
392 methodological assumptions among the methods and cannot be considered as an error in the W/D  
393 procedure. Therefore, the W/D procedure can be established as a reliable alternative to the methods  
394 here compared for the characterization of embankments and overall linear earth structures.

395 The W/D procedure has also main advantages with respect to usually seismic processing  
396 approaches applied to the data obtained from similar surveys: i) being a data transform approach it  
397 does not requires relevant processing and time consuming interpretations; ii) it does not make any  
398 assumption with respect to the number of layers present along the investigated embankment and iii)  
399 allow the combined estimation of  $V_s$  and  $V_p$  for increased depths given the same acquisition setup.

400 Particularly the first advantage is important if the speed of the surveys is considered, for example in  
401 situations in which a fast and preliminary evaluation of the state of health of an embankment is  
402 required. This can be the case of surveys conducted after, or in foresee of, significant rain and/or  
403 flood events. In these conditions the W/D procedure, applied to the fully automated extracted DCs  
404 ([Figure 4a](#)), can allow for a first, almost immediate, on site evaluation of the  $V_s$  and  $V_p$  velocity  
405 field. Both the automated DC extraction step and the conversion of DC data to  $V_s$  and  $V_p$  profiles is  
406 indeed a very fast process (few tens of seconds on a notebook), that outputs direct velocity models  
407 while the acquisition is in progress and the streamer is dragged along the embankment.

408 An example application of this direct visualization of the  $V_s$  section during data acquisition is  
409 reported in [Figure 11](#). It can be particularly observed that the final  $V_s$  section determined from the

410 fully automated extracted DCs (Figure 11d) is roughly comparable with the one determined with the  
 411 semi-automatic procedure (Figure 8a) with very similar depiction of the main interfaces.



412  
 413 **Figure 11 – Example application of the direct visualization of the Vs section during data acquisition:**  
 414 **a), b) and c) Vs sections while dragging the streamer along the embankment; d) final Vs section and c)**  
 415 **Normalized differences with the LCI. In d) and e) the supposed depth of the embankment is also**  
 416 **reported (dashed black line). In d) the interfaces evidenced by the semi-automated W/D procedure,**  
 417 **indicating the transition between the shallow silts and sands (in red), the thickness of the embankment**  
 418 **(in yellow) and the transition to compacted gravels and sands (in blue), are superimposed.**

419  
 420 The presence of some artefacts can be however noted within the section and can be related to the  
 421 reduced precision of the automatic picking of the DCs. A general increase in the normalized

422 differences with the LCI (Figure 11d) is also observed, with the presence of localized anomalous  
423 local velocity values (e.g. see the shallow portion of the embankment around progressive 50 m).  
424 Nevertheless, the general imaging of the Vs structure can be considered accurate enough for a first  
425 estimation of the geotechnical variability at the site and a useful tool for a preliminary identification  
426 of anomalous portions of the examined embankments. Given the use of the same Poisson ratio  
427 profile (Figure 8c), uniform through the section, very similar considerations can be performed for  
428 what concerns the resulting Vp image.

429 This direct visualization requires the knowledge of reference Vs and Vs,z profiles over which  
430 calibrate the W/D relationship and the following Poisson ratio computation. In the present paper  
431 these reference profiles were obtained through MCI of a reference DC. The same approach can be  
432 adopted on site at the beginning of the surveys by selecting one of the clearer DCs during the first  
433 shots. Nevertheless, the MCI step can be significantly time consuming and not always applied with  
434 reliability on site. Possible alternative approaches would therefore require the execution of initial  
435 detailed tests and interpretations through which determine with accuracy the reference profiles and  
436 only later proceed with the execution of the streamer surveys. Alternatively, the reference profiles  
437 can be extracted from already available geotechnical and/or geophysical surveys along the  
438 embankment. With this respect the W/D procedure already showed comparable results also with  
439 respect to Down Hole surveys (Socco et al., 2017).

440 Limitations of the proposed W/D procedure can be related to: i) its application to only fundamental  
441 mode DC; ii) the assumption of a laterally invariable W/D relationship and Poisson ratio along the  
442 embankment. With respect to the first one, the W/D procedure has been mainly developed and  
443 applied to fundamental mode DC, but some attempts have been already made to include also higher  
444 propagation modes (e.g. Bamarouf et al., 2017). Including higher modes showed to give advantages  
445 mainly with respect to the investigation depth, even though it is a more time-consuming process.

446 However, this could be a necessary step along embankments with peculiar shape dimensions, since  
447 it is well known that the shape of the embankment could influence the surface wave dispersive  
448 pattern and modes superposition (e.g. Karl et al., 2011). Pageot et al. (2016) have also shown that  
449 internal structure layering can emphasize geometrical effects and produce DCs very different from  
450 the theoretical 1D case, for both the fundamental and higher modes. In these conditions even a  
451 multi-modal inversion approach could encounter some limitations to infer accurate Vs and Vp  
452 models.

453 These effects have not been particularly noted at the site. As it can be observed in Figure 3b, higher  
454 modes are indeed present in the higher frequency range, but the fundamental mode propagation is  
455 still easily recognizable as local energy maxima. This may be related to the reduced contrast

456 between the embankment body and the underlying subsoil (Figure 2) which limits the layering  
457 effect and to the relevant width of the embankment (width to height ratio of about 5.5) which limits  
458 the presence of 3D effects.

459 Conversely the laterally invariant assumption could be easily overcome using appropriate clustering  
460 techniques on the extracted DCs that can be analysed for grouping them into subsets with  
461 homogeneous properties. The W/D procedure has then to be applied to each of the identified  
462 subsets. The application of this further processing step however increases again the computation  
463 times and prevent a direct in situ application of the procedure but has been shown to provide  
464 increased resolution in the identification of sharp lateral variations with the W/D procedure (Khosro  
465 Anjom et al., 2019; Teodor et al., 2020).

466 The clustering approach was judged to be unnecessary in the presented case study given the  
467 uniformity of the extracted DCs (see Figure 4) which suggest the presence of smooth depth  
468 variations along the embankment but the absence of particularly sharp variations. When sharp  
469 lateral variations along the embankment are the main survey target alternative identification  
470 methods based on the surface waves spectral properties (e.g. Colombero et al., 2019) could also be  
471 applied to the acquired streamer data.

472 To allow for a more complete characterization of the state of health of embankments, seismic data  
473 are usually combined with electric resistivity data. These last can indeed give important information  
474 on the variations of soil composition and water saturation, detect development of weak zones and  
475 identify local anomalies potentially related to seepage. The combined use of seismic and electrical  
476 data can indeed provide an effective geotechnical characterization of these earth structures, as  
477 shown by several research groups that are working on their integration (e.g. Takahashi et al., 2014;  
478 Goff et al. 2015; Lorenzo et al., 2016). In this respect the W/D procedure has its natural  
479 development in combination with mobile electric systems allowing also a fast and effective  
480 evaluation of resistivity properties (e.g. Kuras et al., 2007; Comina et al., 2020).

481        **6. CONCLUSION**

482        This paper presents the application of a novel processing approach (W/D procedure) to surface  
483        wave streamer data. This approach is based on the definition a wavelength/depth (W/D) relationship  
484        for surface waves and allows the combined definition of shear ( $V_s$ ) and compressional ( $V_p$ ) wave  
485        velocities. The results obtained within the paper with the W/D procedure are comparable to  
486        standard seismic processing approaches with the advantage of reduced survey time and increased  
487        efficiency. It was shown in the paper as the W/D procedure can be developed in order to be  
488        completely automated and used as a fast in situ imaging tool along embankments for preliminary  
489        evaluations on their state of life.

490        Processing of the seismic streamer data yielded to an effective characterization of the  $V_s$  and  $V_p$   
491        velocity field along the studied embankment. The origin and properties of the anomalies  
492        encountered could be better studied with the use of local geotechnical investigations to provide a  
493        more specific knowledge on the state of life of the embankment. The produced seismic sections, if  
494        properly calibrated with the few independent geotechnical tests available, can be nevertheless used  
495        for preliminary stability evaluations also in portion of the embankment non directly covered by  
496        geotechnical tests.

497        Further studies, already planned and partially executed, include the application of the W/D  
498        procedure to different embankments shapes with the eventual inclusion of higher modes in the  
499        interpretation. Moreover, the combined acquisition of electrical resistivity data, even with  
500        innovative acquisition approaches, will allow the contemporary execution of resistivity and seismic  
501        surveys with even more reduced survey time and increased knowledge on the state of health of the  
502        embankments due to the acquisition of the different complementary parameters.

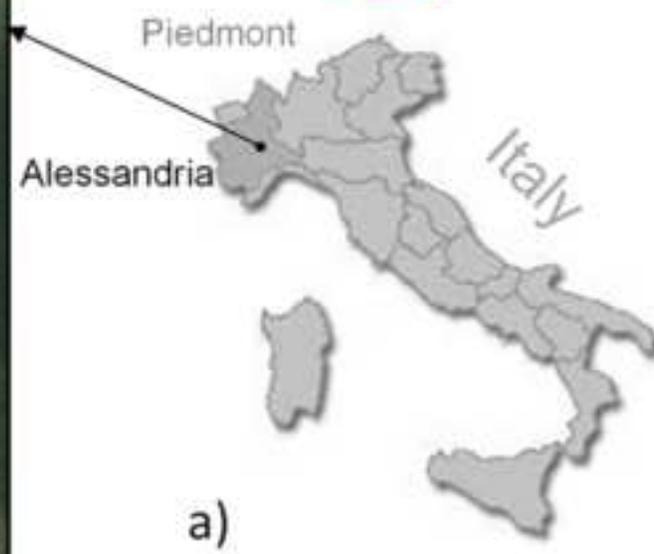
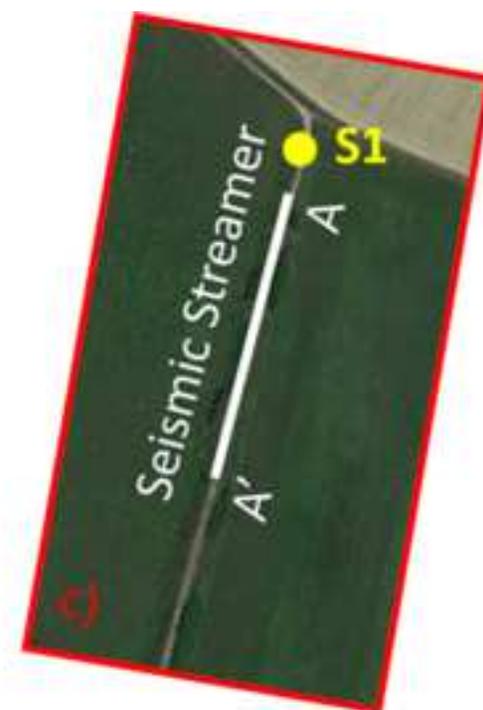
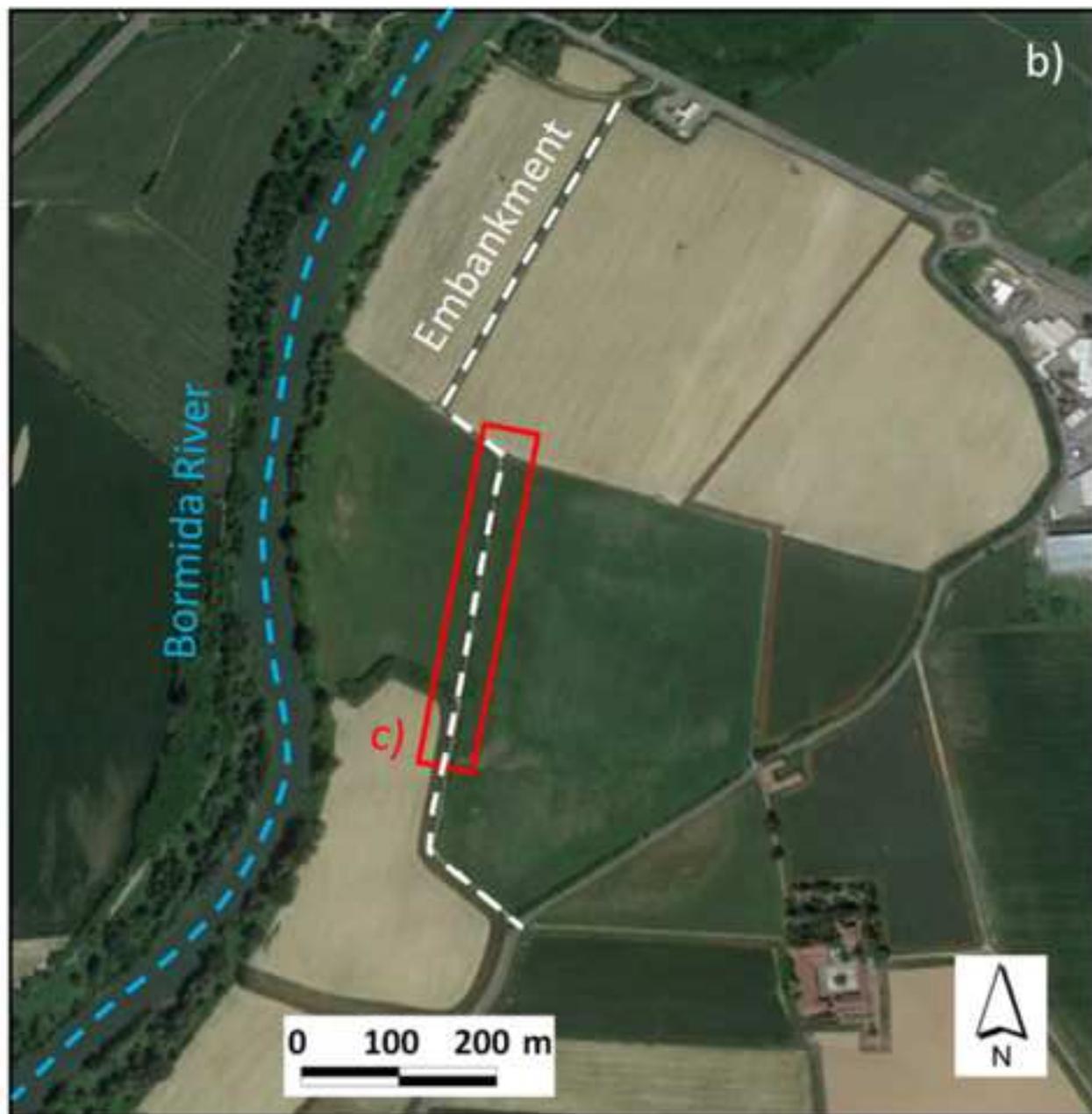
503 **ACKNOWLEDGMENTS**

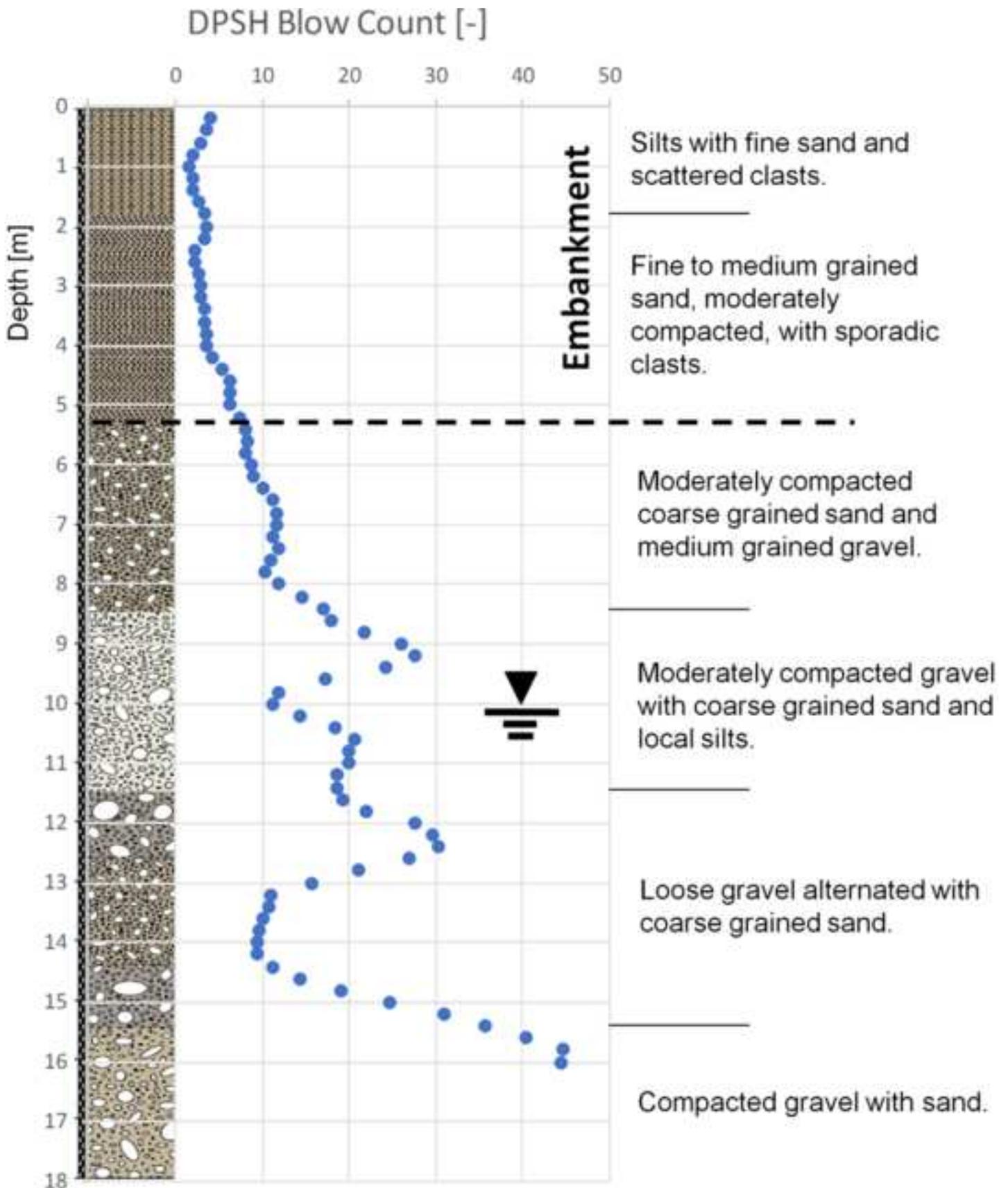
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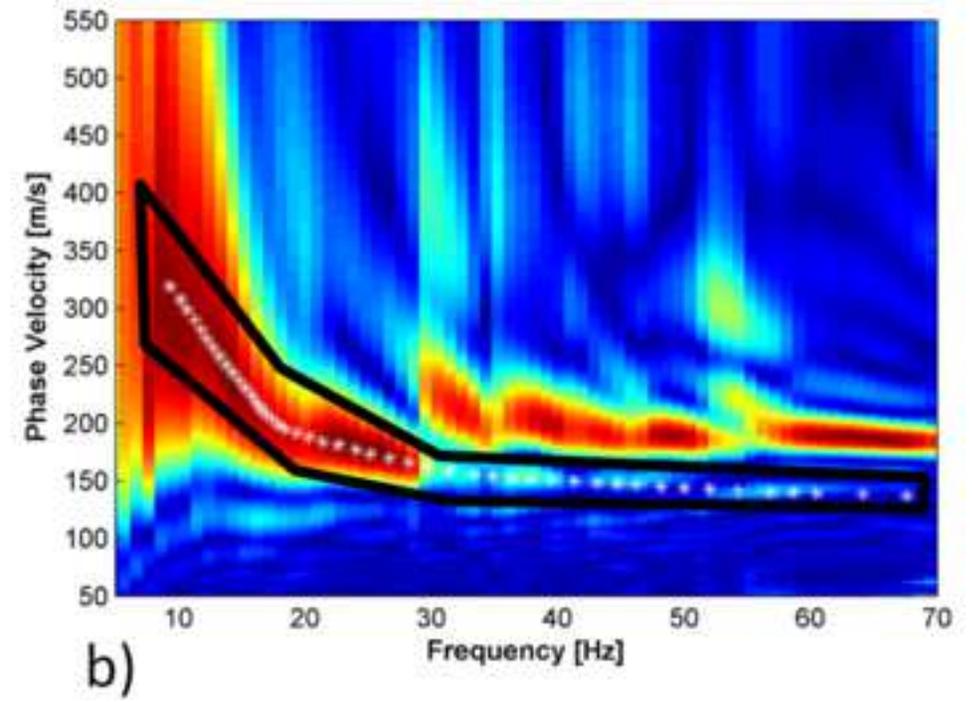
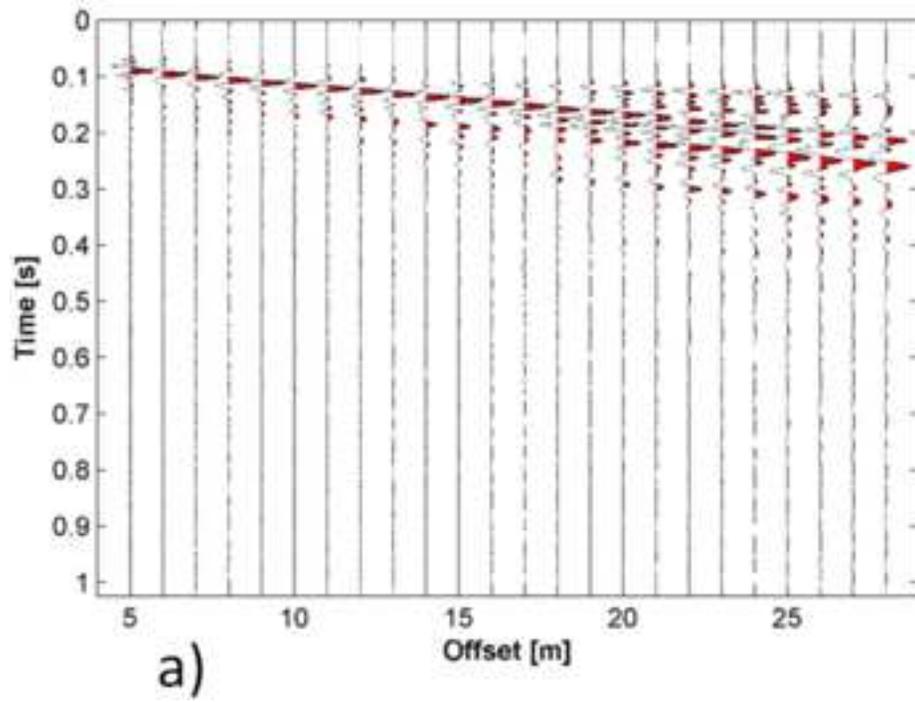
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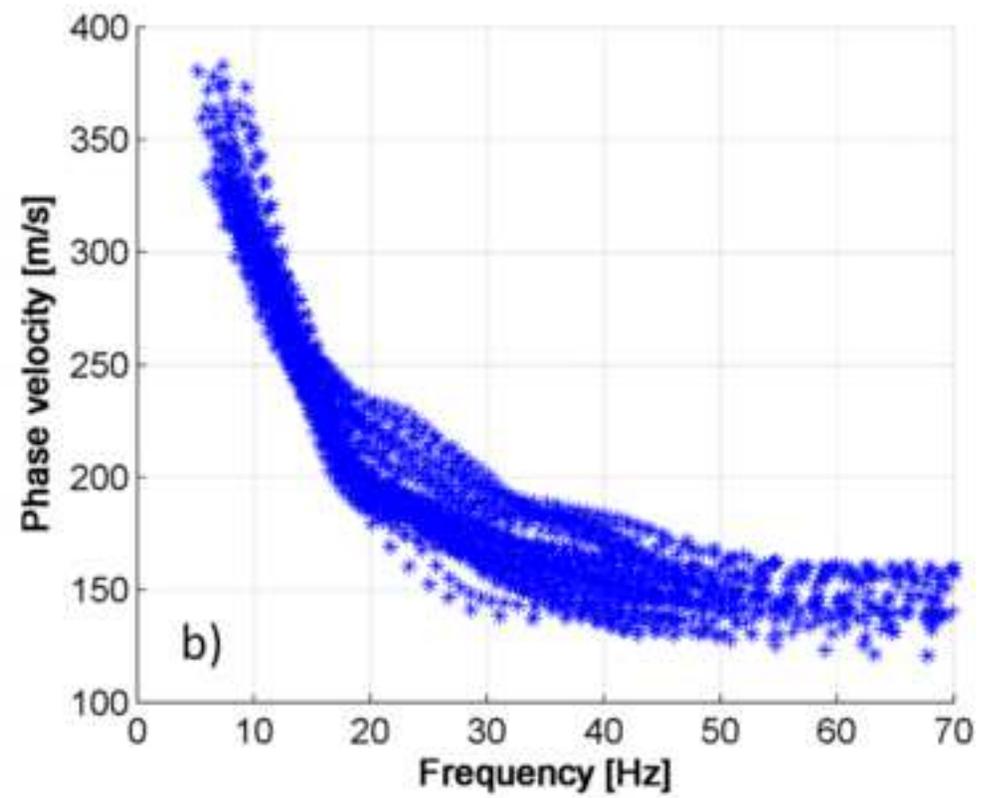
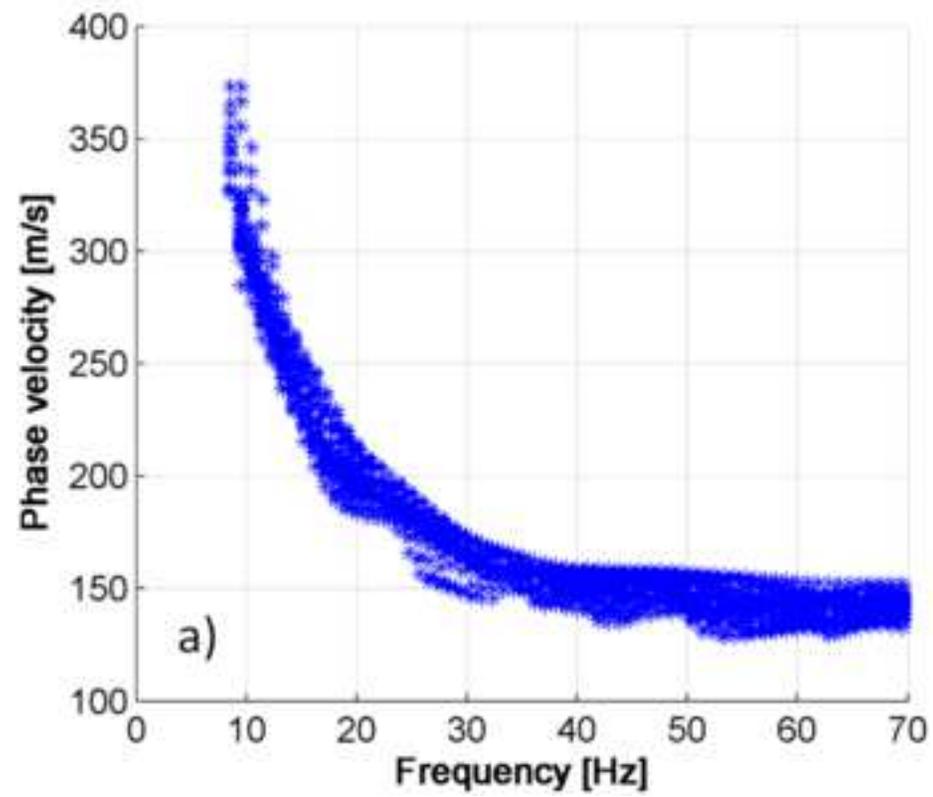
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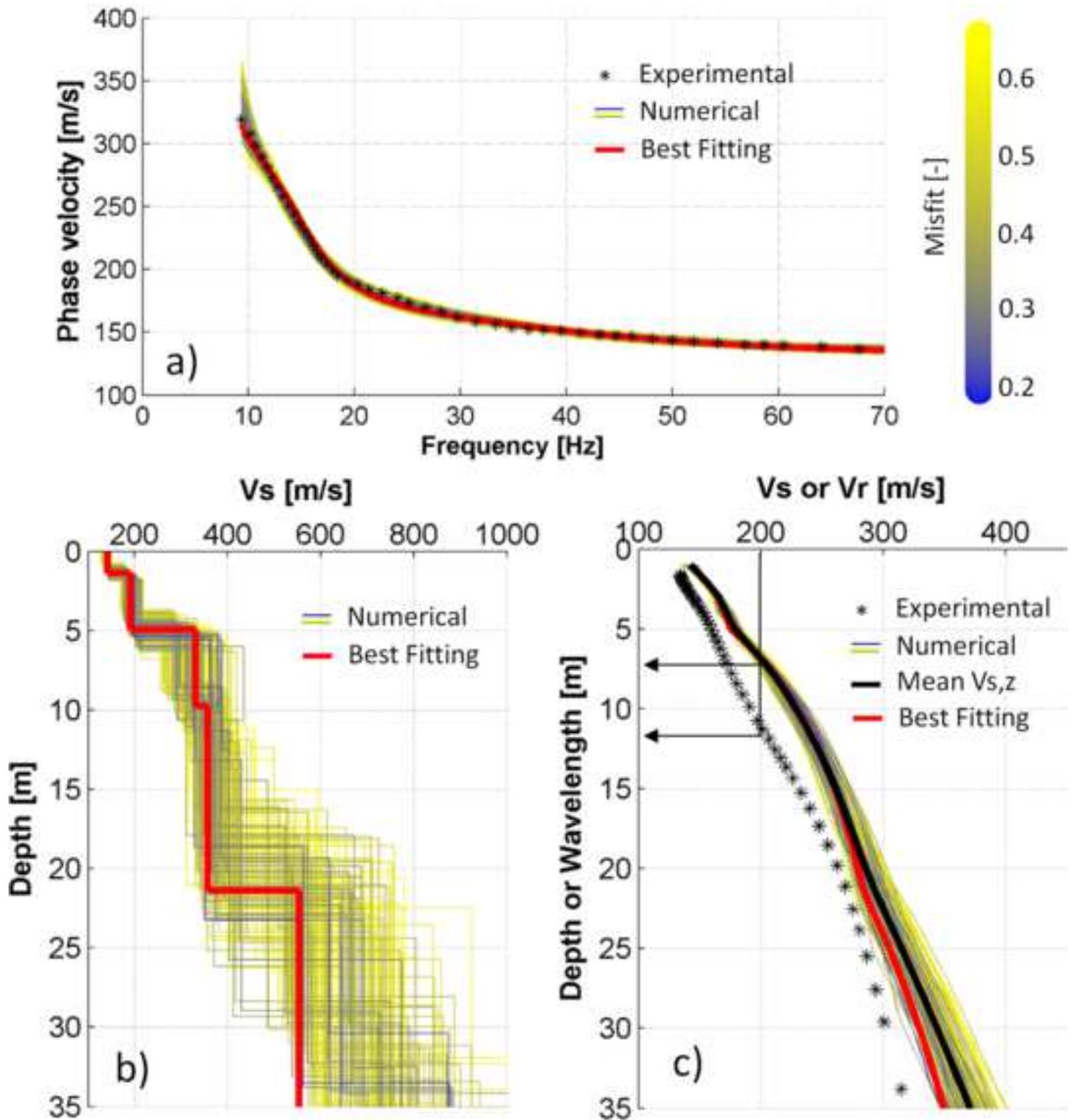
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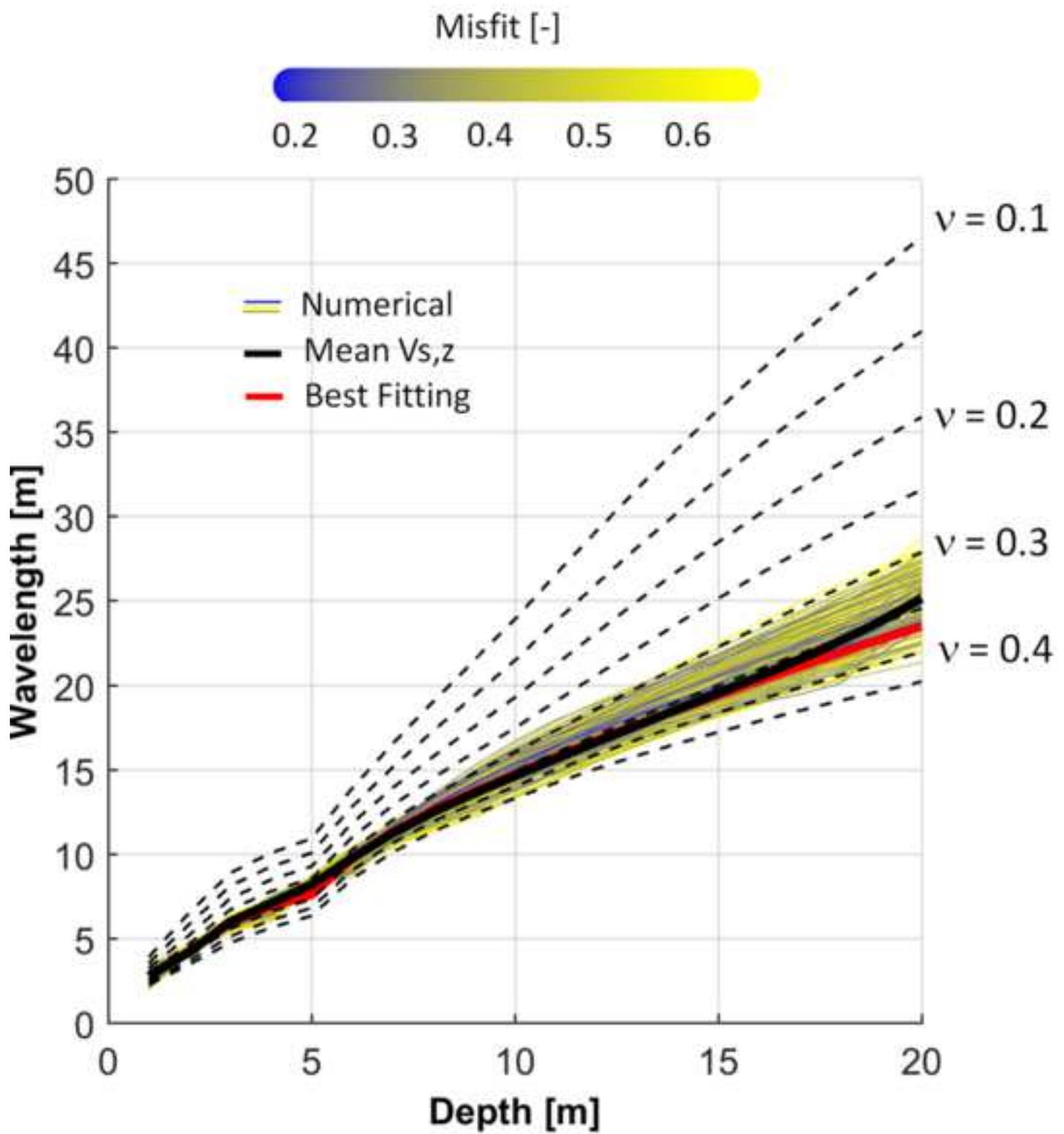


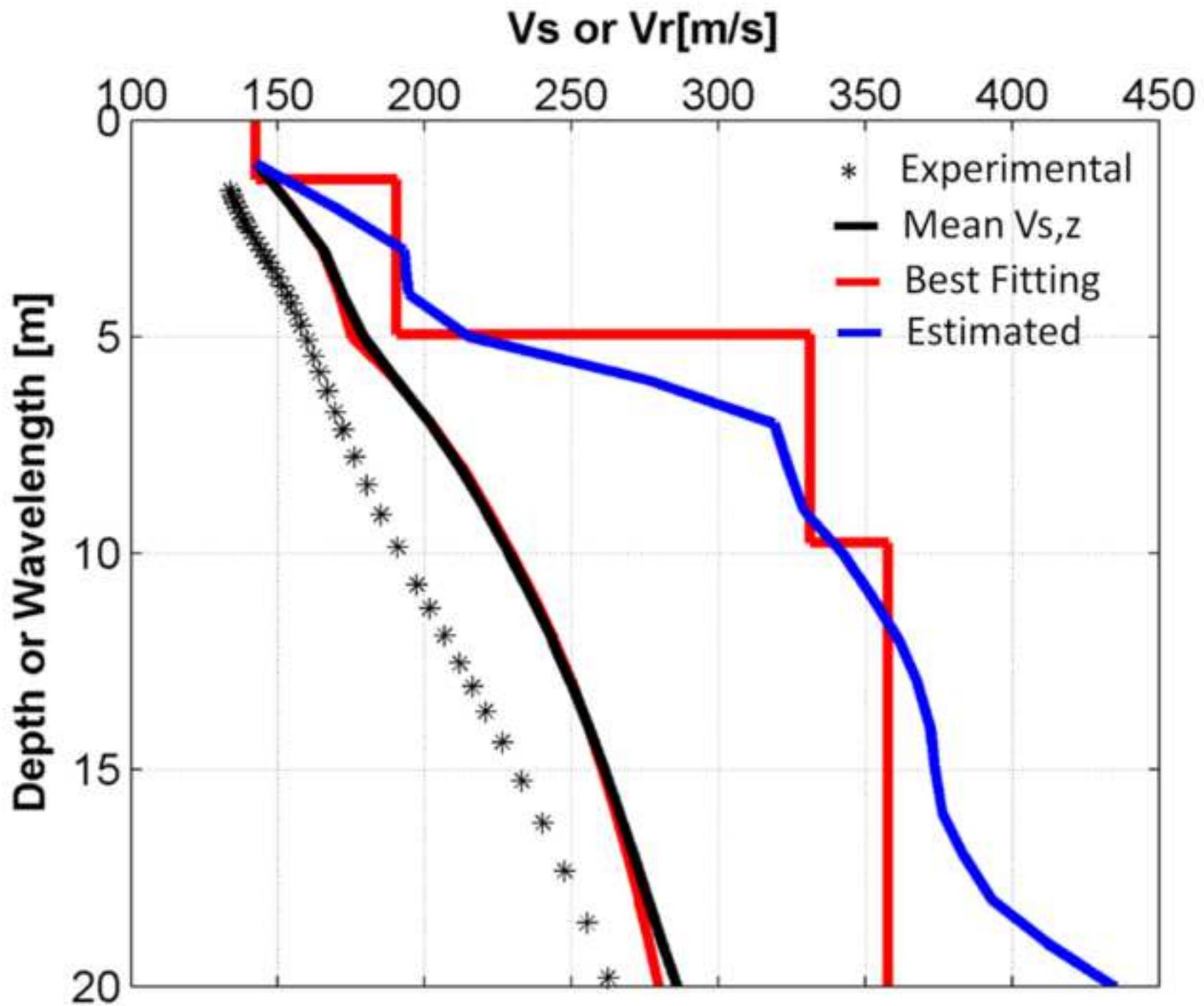


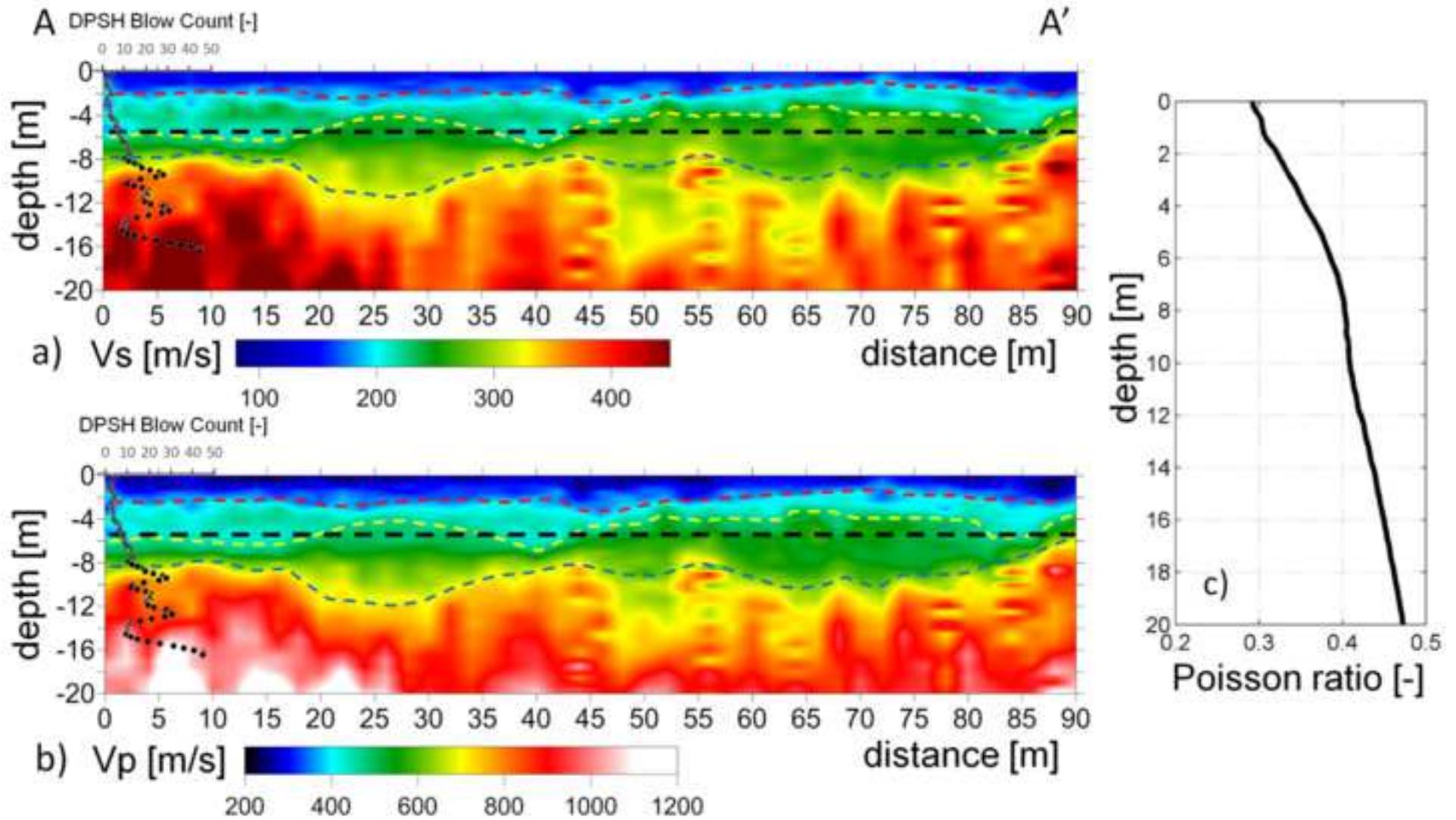


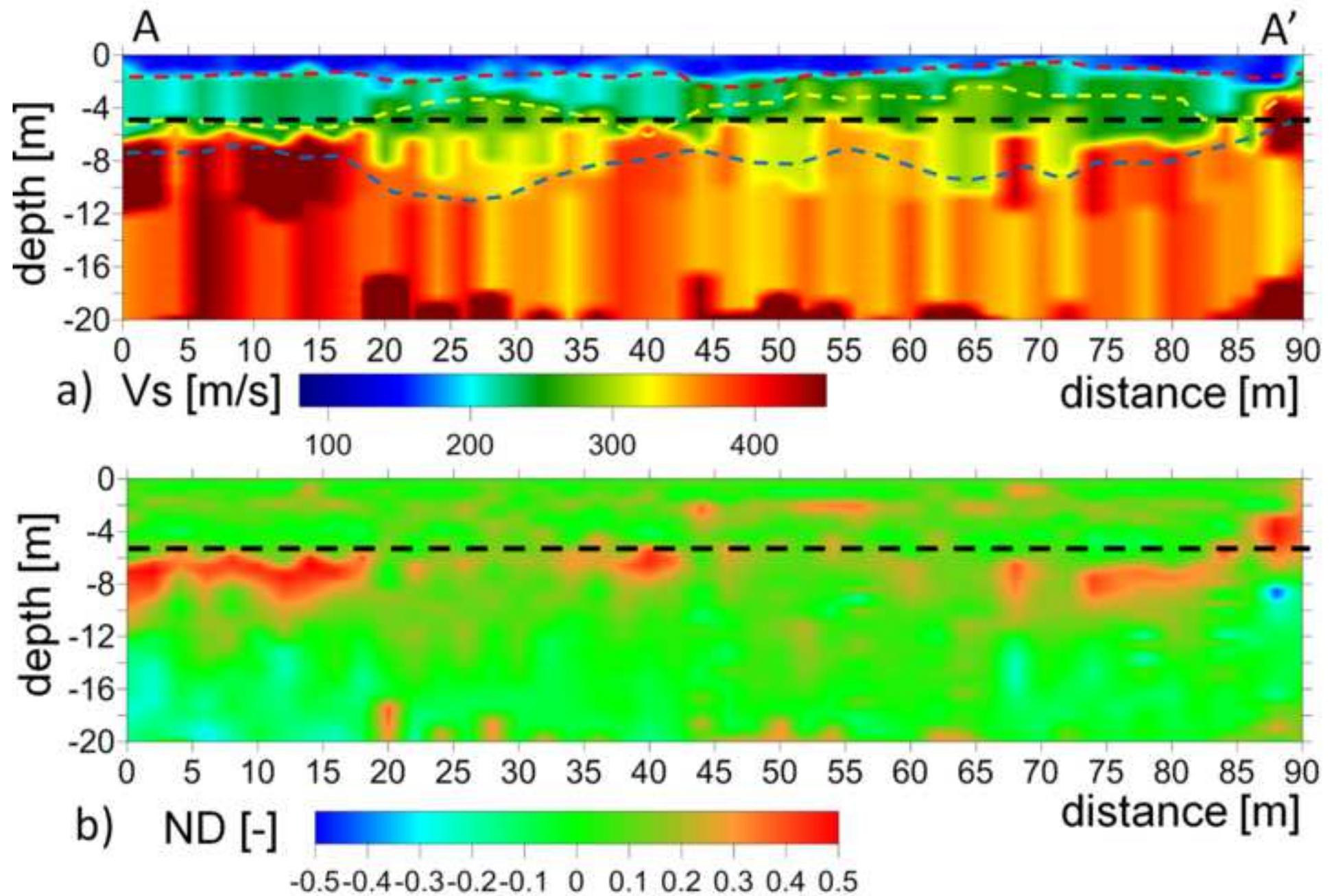


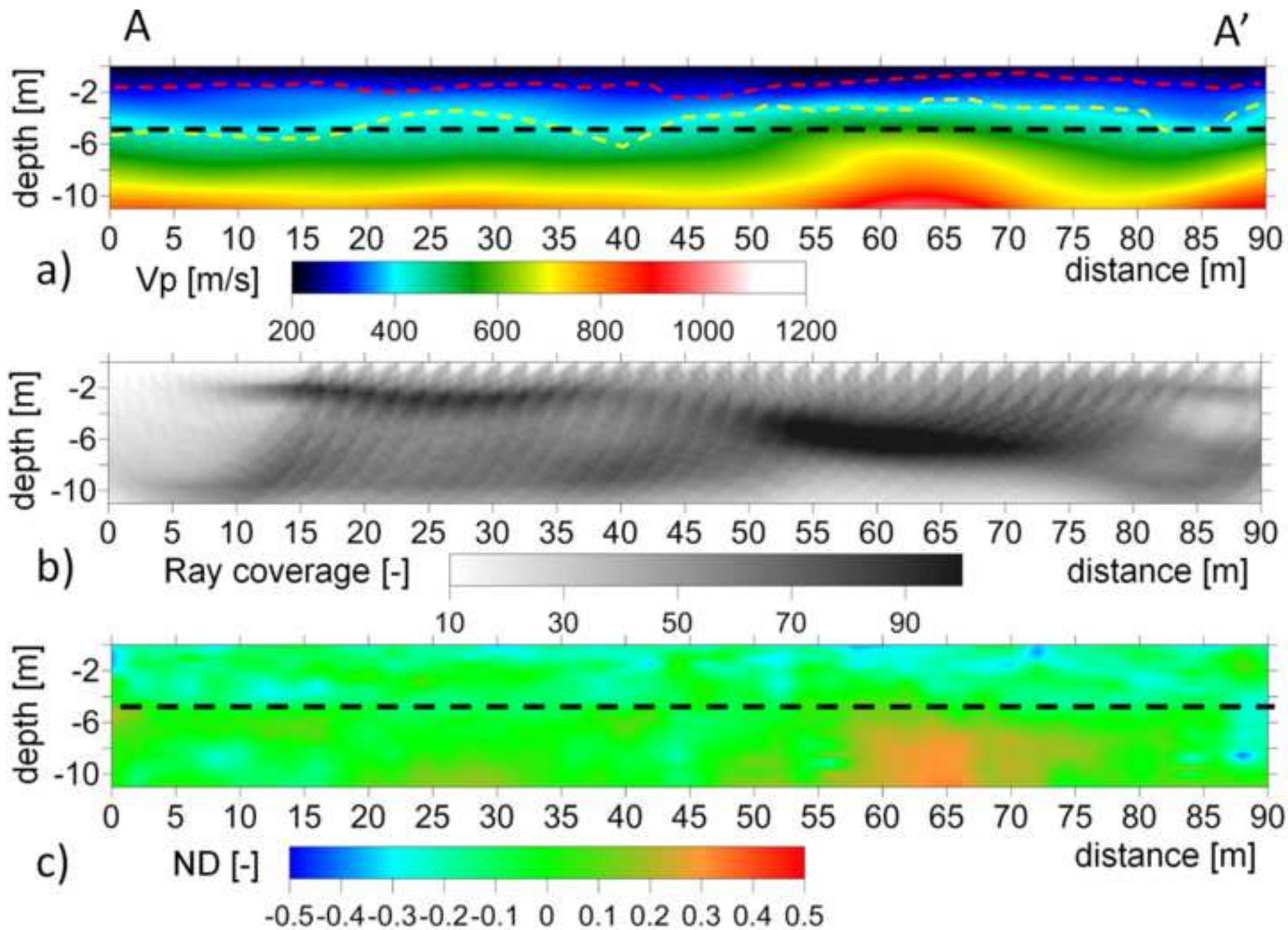


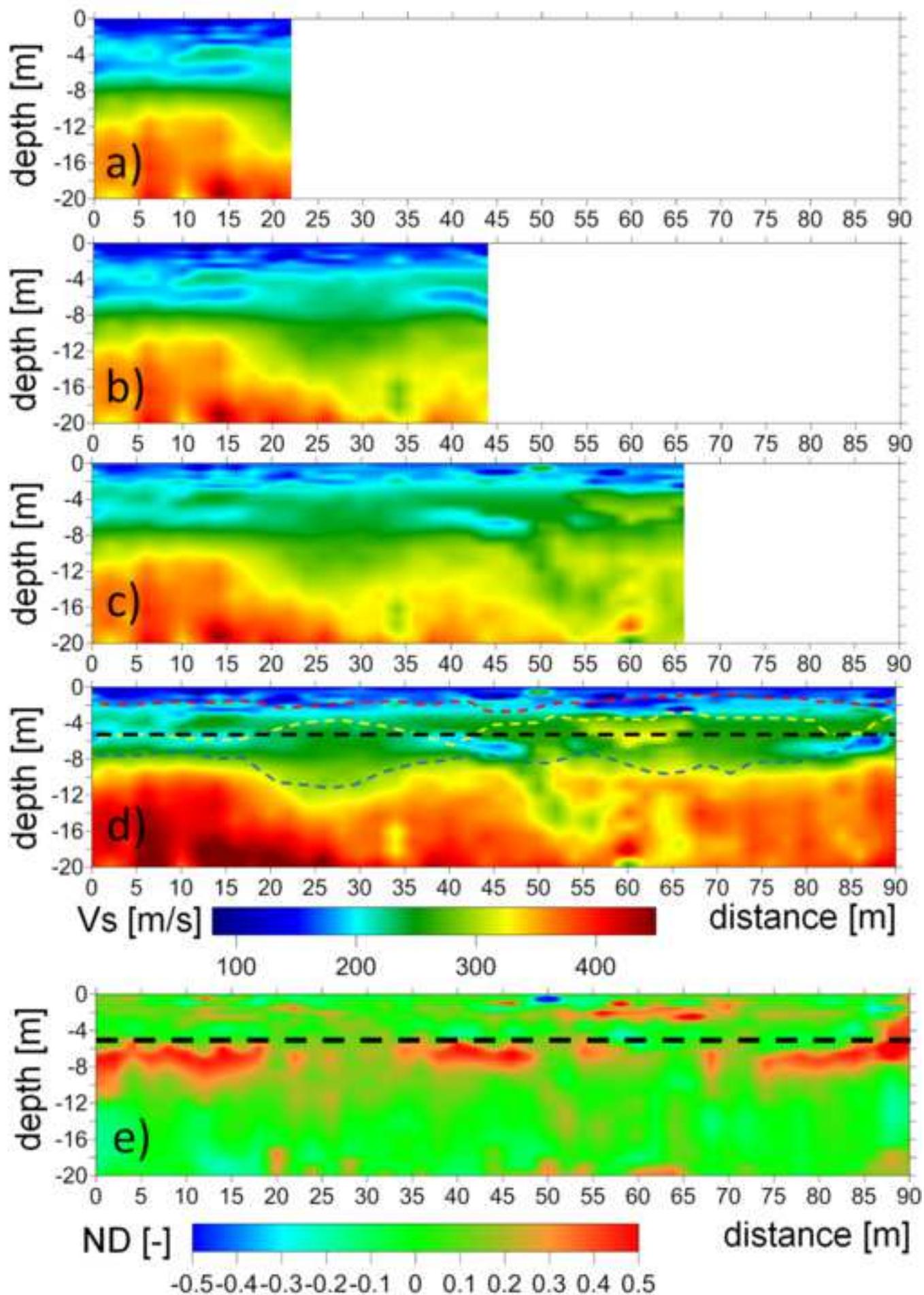






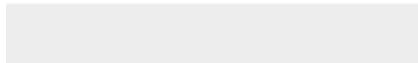
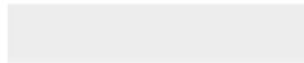








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**Declaration of interests**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

Title: **Effective  $V_s$  and  $V_p$  characterization from Surface Waves streamer data along river embankments.**

Authors: **Comina C.** Writing - Original Draft, Conceptualization, Methodology, Investigation, Data Curation, Visualization

**Vagnon F.** Writing - Review & Editing, Conceptualization, Investigation, Data Curation, Visualization

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