

# **Robust Control Architecture For Waste Heat Harvesting With Non-Inverting Buck-Boost Converter**

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## **Keywords**

«Four-switch Buck-Boost Converter (FSBB)», «Thermo-electric energy», «MPPT», «DSP», «Robust control»

## **Abstract**

Thermoelectric generators (TEG) can be used to harvest wasted heat. TEGs are characterized by a wide output voltage range and a considerable output resistance leading to a maximum power point dependent on the working temperature. Non-Inverting Buck-Boost converter is used to manage, from one side, the wide voltage range, and from the other a battery. This article investigates a robust control architecture to recover the maximum energy from the exhaust's heat avoiding instability issues and maximizing converter efficiency.

## **Introduction**

A Thermoelectric generator (TEG) allows to convert electrical power from a thermal power source and thus recycle the wasted power of another working system. TEGs present power characteristics that are parabola-shaped with a maximum in which their load is equal to the internal resistance for that particular input difference of temperature and in which the output voltage of the generator is equal to their open-circuit voltage [1, 2, 3]. The converter is designed to sustain the maximum power that these generators can typically deliver in an automotive application, which is usually in the order of a few hundred watts when the maximum difference of temperature occurs [4, 5, 6]. A DC-DC converter is used to convert the electrical power from the TEG and deliver it to a battery. In [7] is presented a multilevel converter to extract power from a TEG with high efficiency; however, such architecture is space consuming and not ideal to be integrated into a vehicle. [8, 9] Use a boost followed by a buck stage with coupled inductors where the MPPT is applied to the output of the TEG both using some compensator and using the minimum function to establish a smooth transition between MPPT mode and constant current or voltage modes; [11] uses a decoupled boost plus buck converter where the maximum power point tracking (MPPT) always applied on the output power of the TEG can be used as a reference for the second buck stage; [12] using the same decoupled structure employs an MPPT algorithm on the output of the TEG to control the boost stage while a buck stage regulates the output current for a battery. Here a non-inverting buck-boost topology is used, reducing the number of inductors while still allowing the harvesting with input voltages lower or higher than the battery voltage. Measuring the system output voltage and current a maximum power point tracking (MPPT) algorithm is used to track the maximum power point of the generator, maximizing the system's efficiency. To develop the controller a linearized linear model of the converter is used alongside a dual carrier modulator to simplify the control structure. The converter behavior depends on the working points, so the controller is designed to be robust enough to control the plant in all the working conditions without achieving high bandwidth since it is used to follow the relatively slow thermal dynamics.

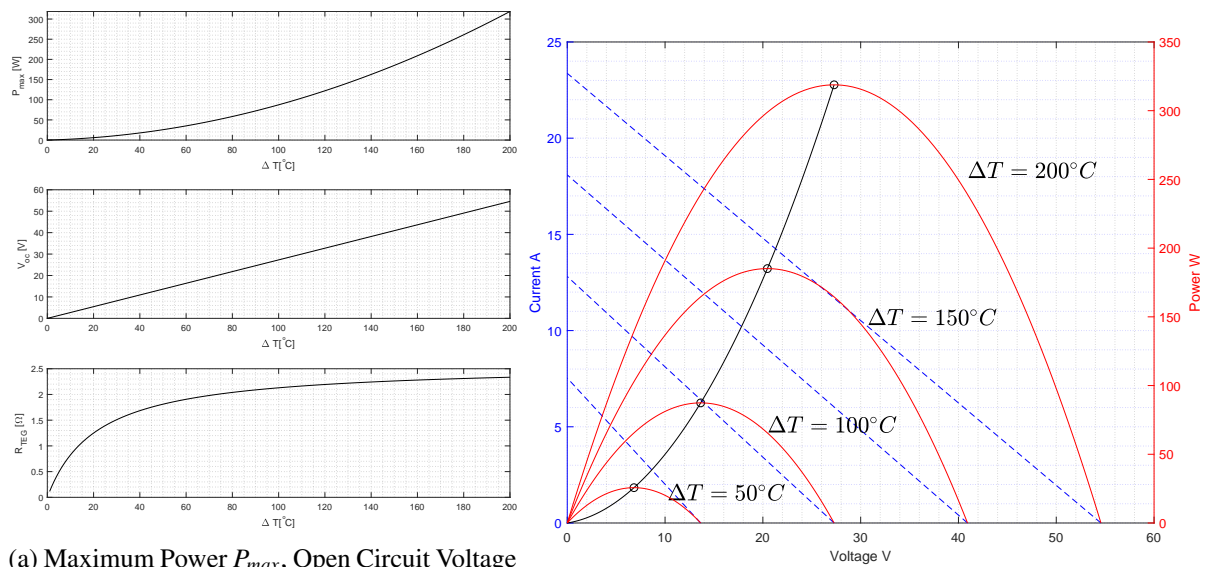
## Thermoelectric Generator

The TEG works using the Seebeck effect's physical phenomenon, exposing some thermoelectric materials to a temperature difference  $\Delta T$  they can produce an electromotive force that acts as a generator; unfortunately, these generators present a high series resistance. The characteristics of this devices are  $\Delta T$  dependent and can be represented by means of linear and quadratic equations (1 - 3), where  $V_{oc}$  is the open-circuit voltage,  $P_{max}$  is the maximum power generated and  $R_{in}$  is the internal resistance of the generator,  $a_1$ ,  $a_2$  and  $b_1$  are given constants. The typical TEG characteristics are represented in Fig. 1.

$$P_{max} = a_1 \Delta T^2 + a_2 \Delta T \quad (1)$$

$$V_{oc} = b_1 \Delta T \quad (2)$$

$$R_{in} = \frac{V_{oc}^2}{4P_{max}} \quad (3)$$



(a) Maximum Power  $P_{max}$ , Open Circuit Voltage  $V_{oc}$ , Internal Resistance  $R_{teg}$  as functions of the Temperature difference.

(b) Maximum Power Point in four different working conditions

Fig. 1: TEG Characteristic

## Converter

As the output spans above and below 12 V a proper Non-Inverting Buck-Boost converter is used to recharge the battery system. A overall schematic of the converter is depicted in Fig. 2, where  $V_{in}$  and  $R_{in}$  is the modelled thermoelectric generator while  $R_{out}$  and  $V_{out}$  are the battery parameters. Switches  $T_1$  and  $T_2$  followed by the inductor can be assimilated to a buck topology. Switches  $T_3$  and  $T_4$ , after the inductor can be assimilated to a boost topology. The buck phase is commanded by the duty cycle  $d_A$ , directly for  $T_1$  and by the negated  $\bar{d}_a$  for  $T_2$  to avoid supply short circuit, it is also added a dead time. The boost phase is commanded by the duty cycle  $d_B$ , on  $T_3$  and by the negated  $\bar{d}_b$  on  $T_4$ , the dead time is added as for the buck phase. Accordingly to the switching frequency set to 30kHz the inductor value  $L$  is set to 30μH to operate in CCM. At the same time, the input and output capacitors ( $C_{in}$ ,  $C_{out}$ ) are obtained with the parallel of two 330μF electrolytic capacitors. The model can be expressed with a state-space representation as in (4) and (5), where the output is  $y = i_{out}$ , the input vector is  $u = [v_{in}, v_{out}]$ , the states

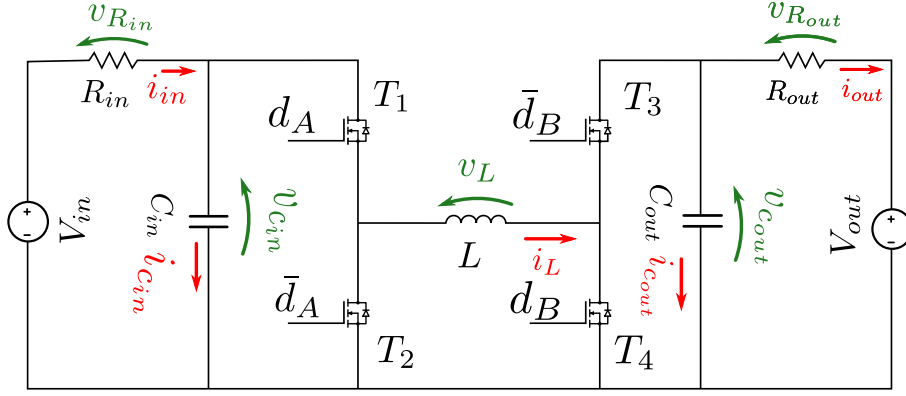


Fig. 2: Converter Schematic

vector is  $x = [v_{c_{in}}, v_{c_{out}}, i_L]$  and  $\dot{x}$  its derivative.

$$\dot{x} = Ax + Bu \quad (4)$$

$$y = Cx + Du \quad (5)$$

$$A = \begin{bmatrix} -\frac{1}{R_{in}C_{in}} & 0 & -\frac{d_A}{C_{in}} \\ 0 & -\frac{1}{R_{out}C_{out}} & \frac{d_B}{C_{out}} \\ \frac{d_A}{L} & -\frac{d_B}{L} & 0 \end{bmatrix} \quad (6)$$

$$B = \begin{bmatrix} \frac{1}{R_{in}C_{in}} & 0 \\ 0 & \frac{1}{R_{out}C_{out}} \\ 0 & 0 \end{bmatrix} \quad (7)$$

$$C = \begin{bmatrix} 0 & \frac{1}{R_{out}} & 0 \end{bmatrix} \quad (8)$$

$$D = \begin{bmatrix} 0 & -\frac{1}{R_{out}} \end{bmatrix} \quad (9)$$

Then the obtained differential equations are linearized (10 - 11) to obtain the small-signal model where the capital letters represent the DC quantities in the point in which the model is linearized. In contrast, the quantities with the "hat" are the small signals. The model built considering a non-ideal generator both as input and output produces transfer functions that are quite more accurate in describing the plant dynamics than the standard model considering only the converter [13, 14, 19] with ideal input voltage source and output load resistance.

$$\begin{aligned} \hat{i}_{out} = & \frac{(1 + sC_{out}ESR_{C_{out}})(C_{in}R_{in}V_{c_{in}}s + \bar{D}_B(V_{c_{in}} - D_A I_L R_{in}))\hat{d}_A}{C_{in}C_{out}LR_{out}R_{in}s^3 + L(C_{out}R_{out} + C_{in}R_{in})s^2 + R_{in}R_{out}((C_{in}\bar{D}_B^2 + C_{out}D_A^2) + L)s + (R_{in}D_A^2 + R_{out}D_B^2)} \\ & + \frac{(1 + sC_{out}ESR_{C_{out}})(-C_{in}I_L LR_{in}s^2 + (C_{in}R_{in}V_{c_{out}}\bar{D}_B - I_L L)s + (-I_L R_{in}D_A^2 + V_{c_{out}}\bar{D}_B))\hat{d}_B}{C_{in}C_{out}LR_{out}R_{in}s^3 + L(C_{out}R_{out} + C_{in}R_{in})s^2 + R_{in}R_{out}((C_{in}\bar{D}_B^2 + C_{out}D_A^2) + L)s + (R_{in}D_A^2 + R_{out}D_B^2)} \end{aligned} \quad (10)$$

$$\begin{aligned} \hat{i}_{in} = & \frac{(1 + sC_{in}ESR_{C_{in}})(-C_{out}I_L LR_{out}s^2 + (I_L L - C_{out}D_A R_{out}V_{c_{in}})s - I_L R_{out}\bar{D}_B - D_A V_{c_{in}})\hat{d}_A}{C_{in}C_{out}LR_{out}R_{in}s^3 + L(C_{out}R_{out} + C_{in}R_{in})s^2 + R_{in}R_{out}((C_{in}\bar{D}_B^2 + C_{out}D_A^2) + L)s + (R_{in}D_A^2 + R_{out}D_B^2)} \\ & + \frac{(1 + sC_{in}ESR_{C_{in}})(-C_{out}D_A R_{out}V_{c_{out}}s + D_A(-I_L R_{out}\bar{D}_B - V_{c_{out}}))\hat{d}_B}{C_{in}C_{out}LR_{out}R_{in}s^3 + L(C_{out}R_{out} + C_{in}R_{in})s^2 + R_{in}R_{out}((C_{in}\bar{D}_B^2 + C_{out}D_A^2) + L)s + (R_{in}D_A^2 + R_{out}D_B^2)} \end{aligned} \quad (11)$$

and the DC relations:

$$V_{out} = \frac{D_A}{\bar{D}_B} V_{in} \quad (12)$$

$$I_{in} = \frac{D_A}{\bar{D}_B} I_{out} \quad (13)$$

## Control

### Input Current as Controlled Output

Considering the DC gains of the output current transfer function, in buck case ( $D_B = 0, I_L = I_{out}$ ):

$$\text{DC GAIN}_{\text{buck}} = \frac{\bar{D}_B(V_{in} - D_A I_L R_{in})}{R_{in} D_A^2 + R_{out} D_B^2} = \frac{V_{in} - D_A I_{out} R_{in}}{R_{in} D_A^2 + R_{out}} = \frac{V_{in} - I_{in} R_{in}}{R_{in} D_A^2 + R_{out}} \quad (14)$$

While in boost case ( $D_A = 1, I_L = I_{in}$ ):

$$\text{DC GAIN}_{\text{boost}} = \frac{V_{out} \bar{D}_B - I_L R_{in} D_A^2}{R_{in} D_A^2 + R_{out} D_B^2} = \frac{V_{out} \bar{D}_B - I_{in} R_{in}}{R_{in} + R_{out} D_B^2} = \frac{V_{in} - I_{in} R_{in}}{R_{in} + R_{out} D_B^2} \quad (15)$$

In both cases, the transfer function DC gain changes sign in the point  $V_{in} = I_{in} R_{in}$  or equivalently when the voltage drop across the input resistance is the same of the one delivered to the converter, that is the maximum power point making the system unstable because of the  $180deg$  phase loss. This type of issue is already reported as the Middlebrook criterion [17]. For this reason, it is preferable to work controlling the converter's input current instead of the output current.

### Control Structure

To reduce the two input commands (i.e.  $d_A, d_B$ ) to only one ( $u$ ) a dual carrier modulation is used [15, 16] in which the command signal  $u$ , namely the output of the controller, is split in the two duty cycles by comparing it with two triangular waves, that in a digital controller is equivalent to compute  $d_A$  and  $d_B$  as (16 - 22). The carrier waves used are two triangular waves  $W_1$  and  $W_2$  where  $V_{1H}$  and  $V_{1L}$  are the upper and lower bound of the first wave while  $V_{2H}$  and  $V_{2L}$  are the bounds for the second one, the dual carrier is set such that  $V_{2H} > V_{1H} > V_{2L} > V_{1L}$  in order to create a buck-boost region and a further constraint  $V_{1H} - V_{1L} = V_{2H} - V_{2L} = 1$  is added to have unity gain in control loop for both the buck and boost regions.

$$d_A = \text{sat}(K_1 u + K_2) \quad (16)$$

$$d_B = \text{sat}(K_3 u + K_4) \quad (17)$$

$$K_1 = \frac{1}{V_{1H} - V_{1L}} \quad (18)$$

$$K_2 = \frac{-V_{1L}}{V_{1H} - V_{1L}} \quad (19)$$

$$K_3 = \frac{1}{V_{2H} - V_{2L}} \quad (20)$$

$$K_4 = \frac{-V_{2L}}{V_{2H} - V_{2L}} \quad (21)$$

$$\text{sat}(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } 0 \leq x \leq 1 \\ 1 & \text{if } x > 1 \end{cases} \quad (22)$$

The MPPT algorithm is then used to produce a reference signal for the input current of the converter  $I_{in}$ , by sensing the output current and voltage of the converter (Fig.3) in such way to maximize the

output power deliver to the battery instead of the power sourced from the generator ensuring to take into account also the efficiency given by the voltage transformation of the converter, the same approach for photovoltaic systems is used in [20]. The MPPT algorithm used is the Incremental Conductance (IC) [26] that has shown better performance with respect of P&O, other types of MPPT designed for TEG systems can be used [25, 27, 28, 29]. On the feedback branch of the measurement a low pass filter implemented with operational amplifier is placed in order to remove the output and input ripple produced by the converter. without degrading the phase of the loop.

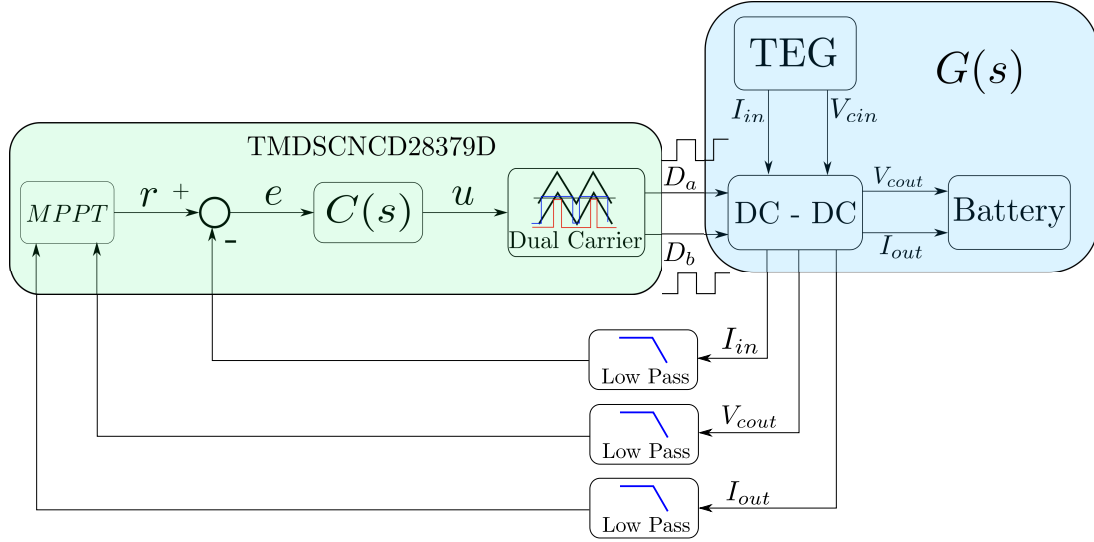


Fig. 3: Block diagram of the system

## Controller Design

In Fig. 5a is showed the transfer functions of the plant  $G(s)$  in the various operative conditions, as seen the steady-state gain varies with the working point as well as the second-order poles and the high-frequency dynamics introduced by ESRs. A robust loop-shaping controller is designed using weighting functions to solve mixed sensitivity optimization problem [23, 24]. An extensive set of plant working points are extrapolated considering the TEG equations to evaluate feasible working points, both in buck and boost; from this set a nominal transfer function  $G_n$  is selected (Fig. 4b), choosing one with the higher steady state gain to simplify the design of the controller  $C(s)$ . Some basic time domain requirements are used as reference to fix some constraints for the controller design, such as desired overshoot ( $\hat{s}$ ) and rise time ( $t_r$ ) and are converted in frequency domain requirements on the sensitivity [21],  $S(s) = 1/(1 + G(s)C(s))$  and complementary sensitivity,  $T(s) = G(s)C(s)/(1 + G(s)C(s))$ , functions such as maximum magnitude ( $S_{max}$ ,  $T_{max}$ ) and minimum crossover frequency ( $\omega_c$ ) using (23) to (27).

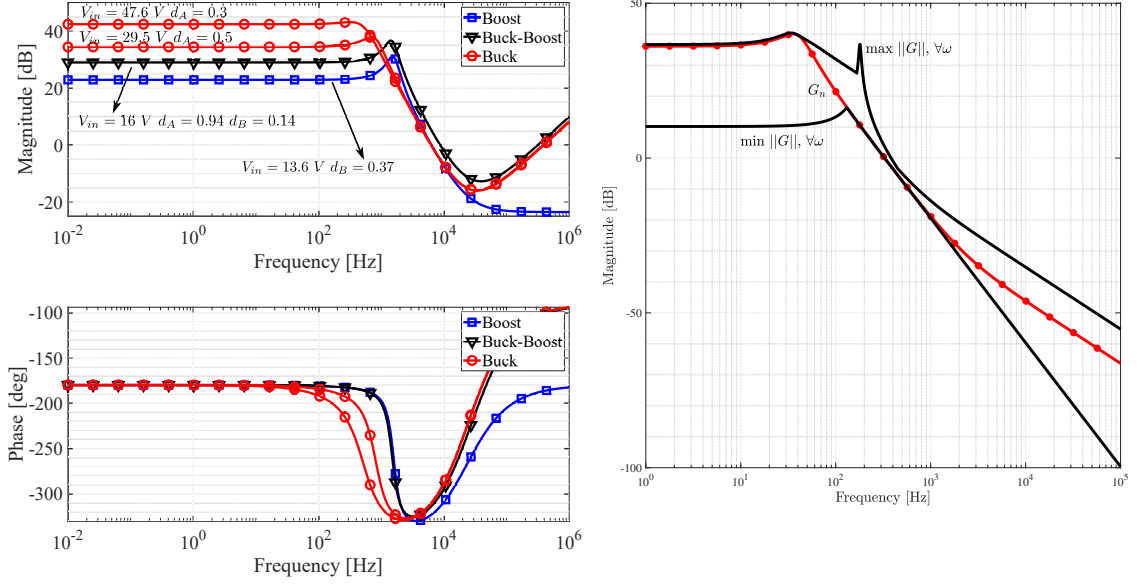
$$\zeta = \frac{|\ln(\hat{s})|}{\sqrt{\pi^2 + (\ln(\hat{s}))^2}} \quad (23)$$

$$\omega_n = \frac{\pi - \arccos(\zeta)}{t_r \sqrt{1 - \zeta^2}} \quad (24)$$

$$\omega_c = \omega_n \sqrt{\sqrt{1 + 4\zeta^4} - 2\zeta^2} \quad (25)$$

$$S_{max} = \sqrt{\frac{8\zeta^2 + 1 + (4\zeta^2 + 1)\sqrt{(8\zeta + 1)}}{8\zeta^2 + 1 + (4\zeta^2 - 1)\sqrt{(8\zeta + 1)}}} \quad (26)$$

$$T_{max} = \frac{1}{2\zeta\sqrt{1 - \zeta^2}} \quad (27)$$



(a) Plant transfer functions  $G(s)$  in four different working conditions (b) Maximum and minimum ranges of the possible transfer functions and nominal transfer function

Fig. 4: Plant Transfer Functions

The plant uncertainties are modelled with unstructured multiplicative structure (28), the robust stability condition for this type of uncertainty is then given by (29) where  $S_n(s)$  and  $T_n(s)$  are the sensitivity functions computed using the nominal plant transfer function  $G_n(s)$ . Considering the initial set of transfer functions an additional weighting function is computed as  $W_u(s)^{-1} = \max_{\forall \omega} \left( \frac{G(s)}{G_n(s)} - 1 \right)$ , and it is used to shape the mask for the complementary sensitivity function as  $\|W_t(s)\| \leq \|W_u(s)\| \quad \forall \omega$  accordingly to the robust stability condition (29).

$$M_G = \{G(s) = G_n(s)(1 + W_u^{-1}(s)\Delta s(s)) \quad , \quad \|\Delta s(s)\|_{\infty} \leq 1\} \quad (28)$$

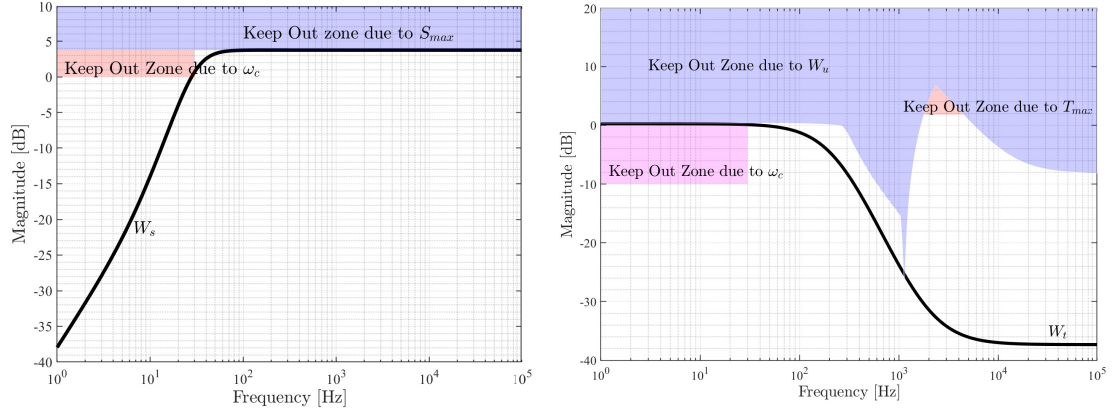
$$\|W_u(s)^{-1}T_n(s)\|_{\infty} \leq 1 \quad (29)$$

With the given frequency requirements the masks for the sensitivity (30) and complementary sensitivity (31) functions are obtained. For the sensitivity function a Butterworth polynomial is used as second order denominator, a zero in the origin is added to guarantee zero tracking error,  $\omega_2$  is computed such that the maximum magnitude of the sensitivity function  $S_{max}$  that has been previously computed is respected, moreover to ensure that the sensitivity function crossover frequency is at least greater than  $\omega_c$  an additional low frequency zero in  $\omega_1$  and a steady state gain  $c_1$  as additional tunable parameter for the mask are added. For the complementary sensitivity function the same constraints are considered with the additional maximum magnitude shape introduced by  $\|W_t(s)\| \leq \|W_u(s)\| \quad \forall \omega$  (Fig. 5).

$$W_s(s) = \frac{c_1 s(1 + \frac{s}{\omega_1})}{1 + \frac{1.414}{\omega_2} s + (\frac{s}{\omega_2})^2} \quad (30)$$

$$W_t(s) = \frac{c_2(1 + \frac{s}{\omega_4})(1 + \frac{s}{\omega_4})}{(1 + \frac{s}{\omega_3})(1 + \frac{s}{\omega_3})} \quad (31)$$

Solving the optimization problem (32) the controller is designed. The computation of the controller is performed by using the "linmod()" command to obtain the generalized plant from a Simulink block diagram and "hinflmi()" to solve the optimization problem in the Matlab environment. The obtained controller is simplified by cancelling undesired high frequency dynamics until is achieved a third-order controller after some tweaking of the weight  $W_1(s)$  and  $W_2(s)$  starting from  $W_1(s) = W_s(s)$  and  $W_2(s) =$



(a)  $W_s$  and its constraints

(b)  $W_t$  and its constraints

Fig. 5: Masks and Weighting functions of the sensitivity and complementary sensitivity

$W_t(s)$ .

$$G_c = \arg \min_{G_c \in G_{stable}} \left( \begin{bmatrix} S_n W_1^{-1} \\ T_n W_2^{-1} \end{bmatrix} \right) \quad (32)$$

The robust stability constraint is not always met, the  $W_t^{-1}T_n$  transfer function exceed  $0dB$  for some points (Fig. 6) but only slightly and since the model with unstructured uncertainty is quite conservative when imposing the perturbation to compute  $W_u$  this do not represent a problem at all: as shown in (Fig. 7) the loop transfer functions with the given controller, are all stable and do not met the Nyquist point.

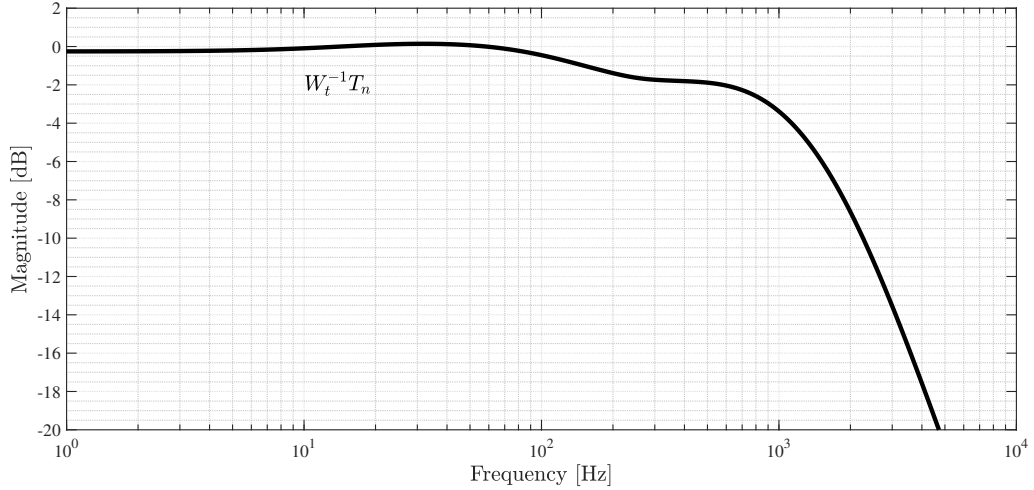


Fig. 6: Robust Stability Condition

Simulation and experimental (Fig. 8) tests, while running the same discrete controller, are performed in various points, here is reported in Fig 9, as a comparison between a simulation and experimental results, a step from 2A to 7A of input current to change also the operating condition of the converter from buck  $u < V_{2L}$  to buck-boost  $V_{2L} < u < V_{1H}$ , recalling that  $V_{2L} = -0.1$  and  $V_{1H} = 0.1$ ; in both cases, the controller exhibits the same behavior except a slight offset in the DC value of the control variable  $u$  and input and output voltages  $V_{cin}$  and  $V_{cout}$ , these differences are imputed to the uncertainties in the input and output resistances values and the parasitic of the converter. The resulting rise time and settling time, both for experimental and simulated results, are  $9.8ms$  and  $40ms$  while the overshoot is  $6.57\%$ . The



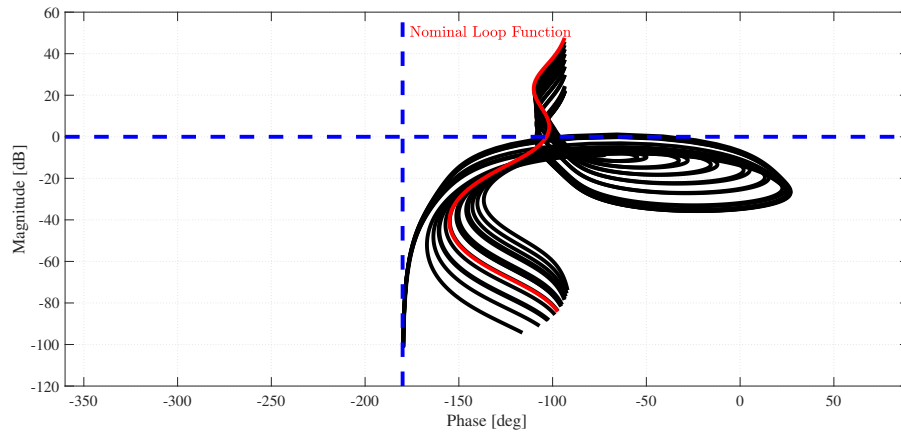


Fig. 7: Nicholas chart of the various loop functions

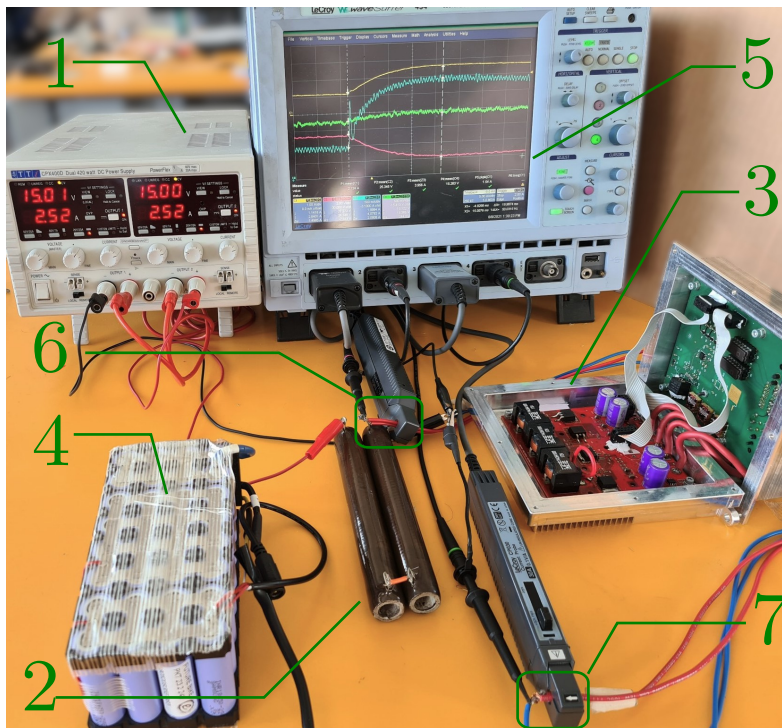


Fig. 8: Testbench: 1) Input Voltage Generator, 2) Input Resistance  $2\Omega$ , 3) Custom Non Inverting Buck Boost converter and DSP prototype, 4) Output Battery pack (8P4S with INR18650-29E cells), 5) Oscilloscope Lecroy, 6) Input Measurements, 7) Output Measurements

controller is converted in discrete with a Tustin discretization for digital implementation and executed with a sampling frequency of  $30\text{KHz}$  in the DSP. The MPPT must runs sufficiently slower than the given bandwidth of the system so that from one step to another, the reference change is correctly followed by the plant, for this reason the MPPT loop is implemented with a frequency of  $5 - 15\text{Hz}$  more than enough for thermal dynamics of an exhaust system. Implementation wise the control logic is implemented in a TMS320F28379D by Texas Instruments [18].



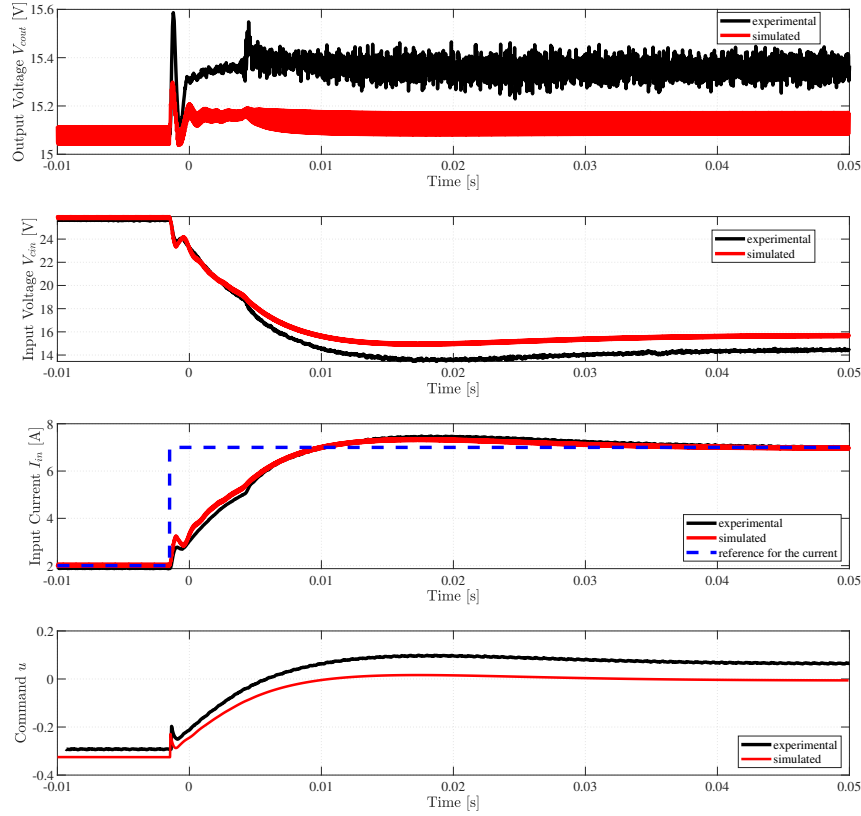


Fig. 9: Experimental And simulated results, step from 2 to 7A with an input voltage  $V_{in}$  of 30V and an input resistance of  $2\Omega$  transition from buck to buck-boost

## Conclusion

The proposed converted presents high efficiency compared to other solutions in which a higher number of passive components are used, and thus the losses are inevitably higher; in our tests the efficiency obtained ranged between 0.88 to 0.96 depending on the working point and the current sourced by the TEG, even if there is always a bit of uncertainty due to efficiency measurements complexity moreover the efficiency of the system is higher when the MPPT is applied to the output of the convert. The converter non-linearity when spanning such different working conditions is another source of problems, for this reason a robust controller design is proposed that shows to be stable in all the tests performed; this type of controller suits well the given control problem especially if the bandwidth required is not too high but the working conditions can vary drastically in terms of plant transfer function's shape. To improve the boost's performance, which is reduced by the lower initial gain provided by the plant transfer function, the gain of the boost carrier can be raised by reducing the distance between  $V_{2h}$  and  $V_{2l}$  in the dual-carrier setup, increasing performance in the boost region, however a too high gain can increase the constraints given by  $W_i$  due to the resonance peak in the boost transfer functions. Simulation and experimental comparison are provided, resulting in a good match between the two, and showing the capability of the dual-carrier to be an effective way to implement a unique controller to drive both the boost and buck phases of the converter.

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