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Original
Design of Digital OTAs With Operation Down to 0.3 V and nW Power for Direct Harvesting / Pedro, Toledo; Crovetti, PAOLO STEFANO; Aiello, Orazio; Alioto, Massimo. - In: IEEE TRANSACTIONS ON CIRCUITS AND SYSTEMS. I, REGULAR PAPERS. - ISSN 1549-8328. - STAMPA. - 68:9(2021), pp. 3693-3706. [10.1109/TCSI.2021.3089339]

## Availability:

This version is available at: 11583/2909432 since: 2021-06-25T12:32:22Z

Publisher:
IEEE

Published
DOI:10.1109/TCSI.2021.3089339

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# Design of Digital OTAs with Operation down to 0.3 V and nW Power for Direct Harvesting 

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#### Abstract

In this paper, passive-less fully-digital operational transconductance amplifiers (DIGOTA) for energy- and areaconstrained systems are modeled and analyzed from a design viewpoint. The digital behavior of DIGOTAs is modeled as an equivalent small-signal differential-mode circuit with zero bias current, and a common-mode feedback loop operating as a selfoscillating threshold sampler. Such continuous-time equivalent circuits are used to derive an explicit model of the main performance parameters that are generally adopted to characterize OTAs. This provides an insight into circuit operation and allows to derive practical guidelines to achieve a given design target. Among the others, an explicit model is derived for the DC gain, the frequency response, the gain-bandwidth product, the input-referred noise, and the input offset voltage. The models are validated via direct comparison with multi-die measurement results in CMOS 180 nm .

From an application viewpoint, the voltage (power) reduction down to 0.25 V (sub-nW) uniquely enable direct harvesting (e.g., with solar cells), suppressing any intermediate DC-DC conversion stage. This further enhances the area efficiency advantage of DIGOTA stemming from its fully-digital nature, making it well suited for cost-sensitive and purely-harvested systems.


Index Terms- Operational transconductance amplifier (OTA), digital OTA, low voltage, low power, Internet of Things (IoT)

## I. Introduction

OPERATIONAL transconductance amplifiers (OTAs) are fundamental building blocks in today's integrated systems. Battery-less sensor nodes are particularly well suited for tightly power- and cost-constrained systems, thanks to the elimination of energy storage. In such constrained systems, devising suitable OTA architectures is challenging in view of the very limited power budget (from nWs to few tens of nWs ) and available area [1], [2] (e.g., few tens of thousands of $\mathrm{F}^{2}$, where $\mathrm{F}=$ minimum feature size of the process). Also, traditional OTAs based on analog techniques typically cannot operate below $0.5-\mathrm{V}$ supply voltage, although required by lightlyregulated or unregulated harvesting [1], [2]. Indeed, state-of-the-art analog OTAs operate above 1 V , their power consumption is lower bounded by the bias currents, and their area is several tens to hundreds of thousands of $\mathrm{F}^{2}$ (see, e.g., [3]-[5]). Power efficiency is further degraded at heavier capacitive loads, and their frequency compensation for closedloop stability requires complex schemes (e.g., as in multi-stage OTAs) and area-hungry passive components [3]-[4].

Manuscript received March 22, 2021.
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Sub-0.5 V operation was demonstrated in OTAs with bulkdriven input stage, dynamic body biasing, and inverter-based gain stages at degraded energy efficiency, larger area (hundreds to thousands of squared feature-size, $\mathrm{F}^{2}$ ), and increased design complexity [6]-[8]. Also, VCO-based [9], ring amplifiers [10] and digital OTAs [11]-[14] were proposed to overcome such limitations, reduce the design and system integration effort, and allow seamless integration with harvesters [15]-[22]. In detail, VCO-based OTAs [9] have the highest gain-bandwidth product at degraded energy efficiency, ring amplifiers disallow continuous-time operation and require the generation of an additional explicit clock [10]. Mostly-digital OTAs are not competitive in terms of performance and require passives and calibration [11]-[14].

Recently, fully-digital OTAs (DIGOTA) were introduced for sub-0.3 V and nW-power operation [23]. DIGOTAs employ time-domain processing, digital architectures with zero bias current, and passive-less self-oscillating common-mode compensation. Digital standard cell design enables digital-like area scaling, very low design effort, and portability across technologies. In this paper, a detailed analysis of DIGOTA amplifiers is presented to gain an insight into the main performance parameters and the underlying design tradeoffs. The resulting circuit models are validated through silicon measurements across multiple dice.

The paper is structured as follows. In Section II, a qualitative analysis of DIGOTA is presented. A quantitative circuit analysis under common-mode and differential inputs is presented in Sections III-IV. The DIGOTA frequency response is modeled in Section V, whereas non-idealities and power are modeled in Section VI. Design considerations and testchip demonstration are discussed in Section VII. In Section VIII, the models are validated against simulations and multi-die measurements, and are compared to state-of-the-art OTAs. Conclusions are drawn in Section IX. Two appendices detail the calculations of circuit parameters.

## II. DIGOTA ARCHITECTURE AND QUALITATIVE ANALYSIS

## A. Operating Principle of DIGOTAs

DIGOTAs aim to achieve the behavior of conventional analog OTAs, while using fully-digital circuit approaches based on digital standard cells [23]. Like any OTA (Fig. 1a), DIGOTAs amplify the differential input $v_{D}=v_{I N+}-v_{I N-}$ defined by the input voltages $v_{I N+}$ and $v_{I N-}$, while ideally

[^0]

Fig. 1. In-principle schematic of a) analog OTA, b) digital OTA (DIGOTA). rejecting its common-mode component $v_{C M}=\left(v_{I N+}+v_{I N-}\right) /$ 2. The reliance of DIGOTA on logic gates inherently reduces the power floor imposed by bias currents and reference circuits necessary in conventional analog OTAs [11]-[14], [23], enabling power savings well beyond their analog counterparts.

To introduce the operating principle of DIGOTA, let us consider a simple pair of digital inverters INV + and INV- as in Fig. 1b. This pair generates a high (low) output differential voltage when $v_{D}>0\left(v_{D}<0\right)$ as in Fig. 1b, when the input common-mode component $v_{C M}$ is close to the inverter trip point $V_{\text {trip }}$ [11]-[14] (more specifically, such that $\left|v_{C M}-V_{\text {trip }}\right|<$ $v_{D} / 2$ [14]). For large-signal $v_{D}$, the output saturates at the supply voltage $V_{D D}$ (ground) as in Fig. 1b, as expected from any high-gain OTA. If $v_{C M}$ is instead farther away from $V_{\text {trip }}$ (see Fig. 1b), the digital outputs of the inverters are equal and hence cannot discriminate whether $v_{D}>0$ or $v_{D}<0$. However, their digital output still provides useful information on whether $v_{C M}<V_{\text {trip }}$ or $v_{C M}>V_{\text {trip }}$. This information can be exploited to correct the common-mode input signal and enforce the condition $v_{C M}=V_{\text {trip }}$ via negative-feedback compensation. In this case, a common-mode compensation signal needs to be added to the primary inputs to suppress its effect on the output.

In prior digital-based OTAs, a common-mode compensation signal was added to the primary inputs via a passive summing network based on on-chip resistors, pseudo-resistors, or quasifloating gate transistors, at the cost of substantial area overhead (e.g., 45\%) and voltage gain degradation (-6dB) [11]-[14]. In [23], the summing network was suppressed by introducing an input stage based on the Muller C-element in Fig. 2a. The output of this logic gate is well-known to be 0 when its inputs are $(0,0), 1$ when they are $(1,1)$ and held at the previous value when they are $(0,1)$ or $(1,0)$ as in Fig. 2a [24].

(b)

Fig. 2. a) DIGOTA schematic, b) logic states and state transition graph.
The two Muller-C elements are driven by the two input voltages $v_{I N+}$ and $v_{I N-}$, and their remaining input is driven by the digital common-mode compensation signal $P D$.
From Fig. 2a, $P D=1(P D=0)$ activates the pull-down (pullup) network of the Muller C-elements, and hence leads to a monotonically decreasing (increasing) waveform in their output voltages $v_{M U L+}$ and $v_{M U L-}$. In turn, these voltages respectively drive the inverters INV+ and INV-, whose digital outputs $\overline{M U L_{+}}$and $\overline{M U L_{-}}$determine the output $P D$ of the swapping circuit MCswap to close the common-mode compensation loop.

## B. Qualitative Circuit Analysis of DIGOTAs

When a common-mode input is applied (i.e., $v_{D}=0$ ), MCswap in Fig. 2a detects the conditions $(0,0)$ and $(1,1)$ described in Fig. 1 b . Then, it dynamically compensates the common-mode at nodes $v_{M U L+}$ and $v_{M U L-}$ to maintain it around the trip point voltage $V_{\text {trip }}$ of the inverter gates INV+ and INV-, as needed in Fig. 1b. In detail, the conditions ( $\overline{M U L_{+}}, \overline{M U L_{-}}$) equal to $(0,0)$ and $(1,1)$ alternatively enable the pull-up and the pull-down networks of the Muller C-elements via $P D$, based on the state transition diagram in Fig. 2b. When $v_{M U L+}$ and $v_{M U L-}$ are both lower than $V_{\text {trip }}$ (i.e., $\left.\left(\overline{M U L_{+}}, \overline{M U L_{-}}\right)=(1,1)\right)$, DIGOTA operates in state A in Fig. 2b, and MCswap sets $P D=0$ to activate the pull-up networks of the Muller C-elements as in


Fig. 3. DIGOTA circuit details vs logic state under $v_{D}>0$ (reverse all directions for $v_{D}<0$ ). The state sequence follows the transition graph in Fig. 2 b : a) A , b) $\mathrm{B}+$, c) C and d) $\mathrm{D}+$. The subscript $+(-)$ refers to the case $v_{D}>0\left(v_{D}<0\right)$.

Fig. 3a. This increases $v_{M U L+}$ and $v_{M U L-}$, bringing their common-mode closer to $V_{\text {trip }}$ as desired. Conversely, when $v_{M U L+}$ and $v_{M U L-}$ are higher than $V_{\text {trip }}$ (i.e., $\overline{M U L_{+}}$, $\left.\overline{M U L_{-}}\right)=(0,0)$ ), DIGOTA operates in state C (Fig. 2b), MCswap sets $P D=1$, and the pull-down networks of the Muller Celements are activated (Fig. 3c). This brings the common mode of $v_{M U L+}$ and $v_{M U L-}$ again closer to $V_{\text {trip }}$, as desired. Hence, the MCswap circuit implements a passive-less selfoscillating loop (see Figs. 3a-c) dynamically tracking the effect of the common-mode input on $v_{M U L+}$ and $v_{M U L-}$, as needed by INV+ and INV- to sense the differential input (Fig. 1b).
When a non-zero differential input $v_{D}=v_{I N+}-v_{I N_{-}}$is applied, the two input voltages $v_{I N+}$ and $v_{I N-}$ driving the Muller C-elements determine the currents $i_{\text {MUL+ }}$ and $i_{\text {MUL- }}$ charging (discharging) the capacitance $C_{M U L}$ at their output, as in Fig. 2a. Starting from state A as discussed above, a smallsignal differential input $v_{D}>0$ makes $i_{M U L+}<i_{M U L-}$, generating a proportional differential voltage at their outputs $v_{M U L+}$ and $v_{M U L-}$ as in Fig. 3b, while moving to state $\mathrm{B}+$ in Fig. 2 b (all is reversed if $v_{D}<0$, moving to state B-). Once the common-mode of these two voltages is brought close to $V_{\text {trip }}$ (i.e., within $V_{\text {trip }} \pm v_{D} / 2$ as in Fig. 2b) by the above selfoscillating loop, their difference can be discriminated by INV + and INV- as in Fig. 1b. In this case, the inverter digital outputs (MUL+,$\left.\overline{M U L_{-}}\right)$become $(1,0)$ for $v_{D}>0\left((0,1)\right.$ for $\left.v_{D}<0\right)$, triggering operation in state $\mathrm{B}+(\mathrm{B}-)$. The same considerations
hold when starting from state C in Fig. 2b, which then moves to state $\mathrm{D}+$ for $v_{D}>0$ ( $\mathrm{D}-$ for $v_{D}<0$ ). The overall DIGOTA state transition graph is summarized in Fig. 2b [23].
Finally, the inverter outputs ( $\left.\overline{M U L_{+}}, \overline{M U L_{-}}\right)$defining the DIGOTA state in Fig. 2 b drive the output stage, and hence determine the output voltage $v_{\text {out }}$. When operating in states $\mathrm{B}+/ \mathrm{D}+$ in Fig. 2 b (i.e., $v_{D}>0$ ), $\left(\overline{M U L_{+}}, \overline{M U L_{-}}\right)=(1,0)$ turns on the pull-up transistor MPO as in Fig. 2a, and correctly raises $v_{\text {OUT }}$ as depicted in Figs. 3b and 3d. The opposite happens in states B-/D- (i.e., $v_{D}<0$ ), which turns on the pull-down MNO transistor to lower $v_{\text {out }}$. In practical cases where the DIGOTA is used in a negative-feedback loop configuration (e.g., voltage buffer), $v_{\text {OUT }}$ ultimately settles to the value that makes $v_{D} \simeq 0$, as in any OTA as exemplified in Section VIII. Finally, no change in $v_{\text {OUT }}$ is observed in states A and C where commonmode compensation is solely performed, from Figs. 3a and 3c.

## III. Circuit Analysis under Common-Mode Inputs

In this section, a model of the DIGOTA circuit is introduced to quantitatively model the common-mode behavior. Under a pure common-mode input $v_{I N}^{+}=v_{I N}^{-}=v_{C M}$, only the transitions between state A and C are allowed from Fig. 2b.
Assuming the initial state A and the initial condition $v_{M U L+}=v_{\text {MUL- }}=V_{\text {min }}$, the output voltages of the Muller C elements $v_{M U L+}$ and $v_{M U L-}$ equally increase due to circuit symmetry (see Figs. 2a, 3a and 4). In particular, transistors

MN2+ and MN2- in Fig. 2a are OFF, MP2+ and MP2- are ON, and MP1- and MP1+ are in weak inversion (see Figs. 2a and 3a). Since $v_{I N}^{+}=v_{I N}^{-}=v_{C M}$, the drain current $i_{M U L+}\left(i_{M U L-}\right)$ of MP1 + (MP1-) charging the capacitance $C_{M U L}$ in Fig. 2a is [2]

$$
\begin{equation*}
i_{D}=I_{P, 0} e^{\frac{v_{S G}-\left(\left|v_{T H, O P}\right|-\lambda_{D I B L} v_{S D}\right)}{n k T / q}}\left(1-e^{-\frac{v_{S D}}{k T / q}}\right) \approx I_{P, 0} \frac{\frac{v_{S G}}{n_{S T} / q}}{} \tag{1}
\end{equation*}
$$

where $v_{S G}\left(v_{S D}\right)$ is the PMOS source-gate (source-drain) voltage, $I_{P, 0}$ is the leakage current (i.e., with $v_{S G}=0$ ), $n$ is the transistor slope factor, $V_{T H, 0 P}$ is the transistor threshold voltage, $\lambda_{D I B L}$ is the drain induced barrier lowering (DIBL) coefficient, and $v_{S D}$ was assumed to be at least 3-4 thermal voltages $k T / q$.

Assuming that the input is nearly constant during state A (see Section IV), from Fig. $4 C_{M U L}$ is charged at the constant current $I_{C M, A}$ given by (1) with $v_{S G}=V_{D D}-v_{C M}$, leading to a ramplike increase in $v_{M U L+}$ and $v_{M U L-}$ from $V_{\text {min }}$ to $V_{\text {trip }}$ over the period of time $\tau_{M U L}$ in (2)

$$
\begin{equation*}
\tau_{M U L}=\left(V_{\text {trip }}-V_{\min }\right) \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, A}}=\left(V_{\text {trip }}-V_{\min }\right) \cdot \frac{C_{\mathrm{MUL}}}{I_{P, 0} e^{\frac{V_{D D^{-v} C M}}{n k T / q}}} \tag{2}
\end{equation*}
$$

Once $v_{M U L+}=v_{M U L-}=V_{\text {trip }}$, the subsequent inverters INV + and INV- switch their output from 1 to 0 after a gate delay $\tau_{I N V}$, as in Fig. 4. Then, the $P D$ signal is updated and makes a $0 \rightarrow 1$ transition after an MCswap gate delay $\tau_{\text {MCswap }}$, thus moving from state A to C as in Fig. 4.

From the above considerations and Fig. 4, the resulting overall duration $T_{A}$ of state A is hence equal to

$$
\begin{equation*}
T_{A}=\left(V_{\text {trip }}-V_{\min }\right) \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, A}}+\tau_{I N V}+\tau_{M C s w a p} \tag{3}
\end{equation*}
$$

at the end of which $v_{M U L+}$ and $v_{M U L-}$ have kept increasing to their maximum value $V_{\max }$ due to the uninterrupted charge of $C_{M U L}$ during the inverter and the MCswap delay (see the evaluation of $V_{\text {max }}$ in Appendix A). The above analysis can be repeated for state C by considering that $v_{M U L+}$ and $v_{M U L-}$ will now decrease from $V_{\max }$ down to $V_{\text {trip }}$ due to the discharge of $C_{M U L}$ through the Muller C-element NMOS current $I_{C M, C}$ in state C (instead of PMOS, see Fig. 3c), trigger the transition of INV+ and INV- after $\tau_{I N V}$, and the $0 \rightarrow 1$ transition of $P D$ after $\tau_{M C \text { swap }}$ to return to state A. Hence, the overall duration $T_{C}$ of state C results to

$$
\begin{equation*}
T_{C}=\left(V_{\max }-V_{t r i p}\right) \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, C}}+\tau_{I N V}+\tau_{M C s w a p} \tag{4}
\end{equation*}
$$



Fig. 4. Timing analysis of the self-oscillating loop timing under pure common-mode inputs, and evaluation of the time $T_{A}$ spent in state A.


Fig. 5. Self-oscillation period $T_{0}$ and $T_{0} \cdot I_{C M}$ vs. $v_{C M}\left(V_{D D}=300 \mathrm{mV}\right)$, as evaluated from transistor-level transient simulations.

From the detailed calculations in Appendix A and equations (3)-(4), the overall self-oscillation period $T_{0}=T_{A}+T_{C}$ is approximately given by

$$
\begin{align*}
& T_{0} \approx V_{D D} \cdot \frac{C_{M U L}}{I_{C M}}+2\left(\tau_{I N V}+\tau_{M C s w a p}\right)  \tag{5a}\\
& I_{C M}=\frac{2}{\frac{1}{I_{C M, A}}+\frac{1}{I_{C M, C}}} \tag{5b}
\end{align*}
$$

where $I_{C M}$ averages the $C_{M U L}$ (dis) charge currents in state A and C as in (5b) (see Appendix A). Fig. 5 shows the relatively weak dependence of the self-oscillation period $T_{0}$ on $v_{C M}$, as evaluated with transistor-level simulations under $V_{D D}=0.3 \mathrm{~V}$. Such a weak common-mode dependence is due to the opposite dependence of $I_{C M, A}$ and $I_{C M, C}$ on $v_{C M}$. Fig. 5 (y-axis on the right) also shows that the product of $(5 \mathrm{a})-(5 \mathrm{~b}) T_{0} \cdot I_{C M}$ is even less dependent on $v_{C M}$, which is useful for other circuit considerations in the following.

From (5b), $T_{0}$ is set by the sum of the (typically dominant) delay associated with the Muller C-element, the inverters INV+ and INV-, and the MCswap gate delay. The dominance of the first term in (5a) due to the Muller C-element also explains the above-discussed independence of $T_{0} \cdot I_{C M}$ on $v_{C M}$. In summary, the self-oscillation period has the well-understood digital logiclike dependence on voltage, temperature, and gate sizing [2].

## IV. Circuit Analysis under Differential Inputs

When a small-signal differential input voltage $v_{D}=v_{I N}^{+}-$ $v_{I N}^{-}$is added to the common-mode component $v_{C M}$, its effect can be analyzed as a perturbation to the self-oscillatory circuit behavior [25] (e.g., as commonly adopted to analyze phase noise in oscillators). The assumption of slow-varying signals compared to the self-oscillation frequency allows to average out the fluctuations of small-signal parameters during each period. As detailed in Appendix B, this allows to rely on straightforward small-signal analysis, as in the following.

## A. Circuit Analysis of the Input Stage

Under a differential input, the circuit in Fig. 2a can be linearized as in Fig. 6. The first stage models the equal smallsignal currents $i_{+}=i_{-}$with opposite directions coming from the Muller C-elements, as determined by the opposite smallsignal components of $v_{I N}^{+}=v_{D} / 2$ and $v_{I N}^{-}=-v_{D} / 2$. Being small-signal components, these currents are superimposed to the common-mode discussed in Section III. In Fig. 6, $g_{m}$ is the effective small-signal transconductance of the input stage (i.e., Muller C-elements) and $r_{o}$ is the small-signal output resistance, which are both evaluated in Appendix B.

Qualitatively, from Fig. 6 the opposite small-signal currents $i_{M U L+}$ and $i_{M U L-}$ at the outputs of the Muller C-elements lead to different slopes in voltages $v_{M U L+}$ and $v_{M U L-}$, during state A (same for C). As discussed in Subsection B, this leads to a small-signal difference of the time when $v_{M U L+}$ and $v_{M U L-}$ reach $V_{\text {trip }}$, and hence to the signed difference $\Delta t$ between the switching of the INV+ and the INV- output. Under small-signal analysis, such time difference $\Delta t$ is inherently proportional to $v_{D}$. As discussed in Subsection C and exemplified in Fig. 7, during states B and D the time difference $\Delta t$ activates the output stage transistor ${ }^{1}$ MPO if $v_{D} \geq 0$ (MNO if $v_{D}<0$ ), which charges (discharges) the capacitive load $C_{L}$. This translates into a small-signal change in $v_{O U T}$ that is proportional to $v_{D}$, and has the same sign, as expected from an OTA (see Fig. 7).

From the small-signal circuit in Fig. 6, the transfer function from $v_{D}$ to the differential output at the Muller C-elements is

$$
\begin{equation*}
\frac{v_{M U L, D}(s)}{v_{D}(s)}=\frac{v_{M U L+}(s)-v_{M U L-}(s)}{v_{D}(s)}=\frac{g_{m} r_{o}}{1+s \cdot r_{o} C_{M U L}} . \tag{6}
\end{equation*}
$$

From (6), the input stage has a first-order transfer function whose gain is equal to the transistor intrinsic gain $g_{m} r_{o}$, which is approximately independent of the common-mode input as discussed in Appendix B. Analogous considerations hold for $r_{o}$, which defines the pole in (6).

## B. Intermediate Voltage-to-Time Conversion

The impact of $v_{D}$ on the differential output of the Muller Celements determines a difference $\Delta t$ in the point of time when $V_{\text {trip }}$ of INV+ and INV- are crossed by $v_{M U L+}$ and $v_{M U L-}$, as shown in Fig. 6 and exemplified in Fig. 7. The difference $\Delta t_{k}$ at a given cycle $k$ of the common-mode self-oscillation with the period $T_{C M, k}$ in (5a) stems from the voltage-to-time conversion performed by the INV+ and INV-, and is crucial for the DIGOTA circuit operation. In detail, the DIGOTA circuit operates in state $\mathrm{B}(\mathrm{D})$ during the time interval $\left(T_{C M, k}-\right.$
$\left.\frac{\Delta t_{k}}{2}, T_{C M, k}+\frac{\Delta t_{k}}{2}\right)$ right after being in state $\mathrm{A}(\mathrm{C})$, thus enabling the output stage as in Fig. 7. During this interval, the load capacitance $C_{L}$ is charged (discharged) for a time proportional to $\Delta t_{k}$ if $v_{D}>0\left(v_{D}<0\right)$ [23].

Assuming again that the input varies slowly and is nearly constant during $T_{0}, v_{M U L+}$ and $v_{M U L-}$ around $V_{\text {trip }}$ can be expressed through linear interpolation, thus yielding

$$
\begin{gather*}
v_{M U L+}\left(T_{C M, k}-\frac{\Delta t_{k}}{2}\right)=v_{M U L, C M}\left(T_{C M, k}-\frac{\Delta t_{k}}{2}\right)+\frac{v_{M U L, D}\left(T_{C M, k}\right)}{2} \\
=v_{M U L, C M}\left(T_{C M, k}\right)-\left.\frac{\partial v_{M U L, C M}}{\partial t}\right|_{T_{C M, k}} \frac{\Delta t_{k}}{2}+\frac{v_{M U L, D}\left(T_{C M, k}\right)}{2}  \tag{7a}\\
\begin{array}{c}
v_{M U L-} \\
\left(T_{C M, k}+\frac{\Delta t_{k}}{2}\right)=v_{M U L, C M}\left(T_{C M, k}+\frac{\Delta t_{k}}{2}\right)-\frac{v_{M U L, D}\left(T_{C M, k}\right)}{2} \\
=v_{M U L, C M}\left(T_{C M, k}\right)+\left.\frac{\partial v_{M U L, C M}}{\partial t}\right|_{T_{C M, k}} \frac{\Delta t_{k}}{2}-\frac{v_{M U L, D}\left(T_{C M, k}\right)}{2}
\end{array}
\end{gather*}
$$

The common-mode voltage contribution $v_{M U L+}=v_{M U L-}=$ $v_{M U L, C M}$ in (7a-b) is due to the discharge of capacitors through the common-mode current $I_{C M}$ in (5b) at the constant rate $I_{C M} / C_{\text {MUL }}$. This makes $\partial v_{M U L, C M} /\left.\partial t\right|_{T C M, k}$ equal to $I_{C M} / C_{\text {MUL }}$ in (7a-b). Also, $v_{M U L, C M}\left(T_{C M, k}\right)=V_{\text {trip }}$ since $T_{C M, k}$ is defined as the time at which $v_{M U L, C M}$ crosses $V_{\text {trip }}$. Accordingly, (7a-b) lead to the following $\Delta t_{k} / v_{M U L, D}$ transfer function

$$
\begin{equation*}
\frac{\Delta t_{k}}{v_{M U L, D}\left(T_{C M, k}\right)}=\frac{C_{\mathrm{MUL}}}{I_{C M}} \tag{8}
\end{equation*}
$$

which quantifies the small-signal voltage-to-time conversion performed by INV+ and INV- in Fig. 6.

Since zero crossings occur every half period, voltage-to-time conversion takes place every $T_{0} / 2$ and leads to the generation of a signed time difference $\Delta t_{k}$ whose sign is the same as $v_{D}$ [26], and its width is proportional to $v_{M U L, D}$ evaluated at $k T_{0} / 2$. In other words, the input is effectively sampled with a sampling period $T_{0} / 2$, where $T_{0}$ is expressed in (5a). Hence, the loop in DIGOTA through the MCswap circuit acts such as a self-


Fig. 6. DIGOTA equivalent circuit and transfer function under differential input $v_{D}$.

[^1]kept to a minimum, and in particular such that $\tau_{\text {out }} \ll \tau_{\text {MCswap }}$. Accordingly, the delay $\tau_{\text {out }}$ is not further considered in the analysis.


Fig. 7. Operation of DIGOTA under positive and negative input differential voltages.
oscillating threshold sampler [27]-[28] with a natural sampling frequency of $2 / T_{0}$.

## C. Output Stage and Overall Transfer Function

In the output stage in Fig. 6, the pulses $\Delta t_{k}$ turn on the MPO $(\mathrm{MNO})$ if $v_{D}>0\left(v_{D}<0\right)$ for a duration $\Delta t_{k}$. When the time difference $\Delta t_{k}$ is non-zero, MPO (MNO) generates a current $I_{O N}\left(-I_{O N}\right)$ driving the capacitive load, as MPO and MNO are sized to deliver the same current to $C_{L}$. Since time pulses $\Delta t_{k}$ take place every $T_{0} / 2$, the output stage current $i_{\text {OUT }}(t)$ driving $C_{L}$ can be written as

$$
\begin{equation*}
i_{O U T}(t)=\sum_{k=0}^{+\infty} I_{O N} \Delta t_{k} \delta\left(t-\frac{k T_{0}}{2}\right) \tag{9}
\end{equation*}
$$

where the sign of the output current was incorporated in $\Delta t_{k}$, from the above considerations. The Laplace transform of (9) can be evaluated as in [26] from the $z$ transform of $\Delta t_{k}$ evaluated in $z=e^{s T_{0} / 2}$. Assuming as usual that the input signal frequency is lower than the self-oscillation frequency $2 / T_{0}$ (e.g., by at least an order of magnitude), the output current $I_{\text {out }}(s)$ is evaluated by substituting (6)-(8) in (9). Straightforward calculations reveal that $I_{o u t}(s)$ is related to the input differential voltage $V_{D}(s)$ as in a first-order continuoustime linear circuit.

More specifically, considering that $I_{\text {out }}$ flows through the impedance defined by $r_{O U T}$ in parallel with $C_{L}$ from Fig. 6, the differential voltage gain transfer function of DIGOTA is

$$
\begin{equation*}
A_{D}(s)=\frac{V_{O U T}(s)}{V_{D}(s)}=\frac{2 g_{m} r_{o} \cdot \frac{I_{O N}}{I_{C M}} \cdot \frac{r_{O U T} C_{\mathrm{MUL}}}{T_{0}}}{\left(1+s \cdot r_{O U T} C_{L}\right) \cdot\left(1+s \cdot r_{o} C_{M U L}\right)} \tag{10}
\end{equation*}
$$

From (10), DIGOTA has a second-order transfer function when a differential input is applied. Its dependence on design and process parameters is discussed in the next section.

## V. Frequency Response and Gain-Bandwidth Product

From (10), the DIGOTA DC gain is

$$
\begin{equation*}
A_{V 0}=2 g_{m} r_{o} \cdot I_{O N} \cdot \frac{r_{O U T} C_{\mathrm{MUL}}}{T_{0} \cdot I_{C M}} \tag{11}
\end{equation*}
$$

and is much higher than one. Indeed, $g_{m} r_{o} \gg 1$ since it is the intrinsic transistor gain, whereas $I_{O N} / I_{C M} \gg 1$ since the output stage always sees a full-swing input and is hence fully ON, whereas $I_{C M}$ in (5b) is much lower than the transistor ON current (see (A.3) in Appendix A). As exemplified by the parameters in Table I, the ratio $r_{\text {OUT }} C_{\mathrm{MUL}} / T_{0}$ is always larger than 0.07 and the DC gain in (11) is 29.83 dB . This agrees well with the measured result of 29.28 dB (see Section VIII).

The frequency response in (10) has two real negative poles:

$$
\begin{equation*}
s_{p 1}=-\frac{1}{r_{O U T} C_{\mathrm{L}}} \quad s_{p 2}=-\frac{1}{r_{o} C_{\mathrm{MUL}}} \tag{12}
\end{equation*}
$$

where $s_{p 1}$ is dominant, since the load capacitance $C_{L}$ is orders of magnitude larger than the transistor parasitic capacitance $C_{M U L}$, whereas $r_{O U T}$ and $r_{O}$ are small-signal transistor output resistances and are hence much closer to each other. The resulting gain-bandwidth product $f_{G B W}$ is
$f_{G B W}=\frac{1}{2 \pi} \cdot \frac{A_{V 0}}{r_{O U T} C_{L}}=\frac{1}{2 \pi} \cdot \frac{2}{T_{0}} \cdot \frac{I_{O N}}{I_{C M}} \cdot g_{m} r_{o} \cdot \frac{C_{M U L}}{C_{L}} \approx \frac{1}{\pi} \cdot \frac{I_{O N}}{\lambda_{D I B L} V_{D D} C_{L}}$
where the expression of $g_{m} r_{o}$ in Appendix B was used, and (5a) was simplified to $V_{D D} \cdot \frac{C_{\mathrm{MUL}}}{I_{C M}}$, due to its dominance over the other delays (see detailed considerations in Section III. As an
example, $f_{G B W}$ in (13) results in 257 Hz at $V_{D D}=0.3 \mathrm{~V}$, which is in good agreement with the measured value of 250 Hz (see Table II). From (13), $f_{G B W}$ is independent of the common-mode input. From the same equation, $f_{G B W}$ benefits from temperature increases, due to the monotonically increasing $I_{O N} / \lambda_{D I B L}$ ratio ( $3 \% /{ }^{\circ} \mathrm{C}$ ).

From (13), the gain-bandwidth product expectedly decreases at heavier loads $C_{L}$ and increases when the output stage transistors can deliver higher on-current, as expected by the resulting improvement in the load driving capability. In particular, an increase in the supply voltage in the sub-threshold region leads to an exponential increase in the output stage current $I_{O N}$, and hence on the gain-bandwidth product. As an example, $f_{G B W}$ increases to 41.3 kHz at $V_{D D}=0.5 \mathrm{~V}$, which is in agreement with the measured value of 57.5 kHz in Table II.

## VI. ANALYSIS OF DIGOTA NON-IDEALITIES AND POWER

## A. Input Offset and Input-Referred Noise

The input offset voltage of DIGOTA is determined by the mismatch in the two signal paths in Fig. 6 starting from the Muller C-elements in the first stage. In particular, the offset $V_{\text {OS }}$ is determined by the mismatch in the ON currents of transistors MN1+ and MN1-, as well as MP1+ and MP1-. Other contributions come from the mismatch between the capacitances at the output of the Muller C-elements $C_{M U L}$, and the mismatch $\Delta V_{\text {trip }}$ between the trip points of the inverter gates INV- and INV+. Considering such mismatch terms as independent random variables with standard deviation $\sigma_{x}$, the overall input-referred offset voltage standard deviation is readily found to be:

$$
\begin{equation*}
\sigma_{V_{\mathrm{OS}}}=\sqrt{\frac{\sigma_{\mathrm{I}_{\mathrm{N}}}^{2}}{g_{m}^{2}}+\frac{\sigma_{\mathrm{I}_{\mathrm{P}}}^{2}}{g_{m}^{2}}+\frac{\sigma_{C_{M U L}}^{2} \cdot I_{C M, T P}^{2}}{\left(g_{m} C_{M U L}\right)^{2}}+\frac{\sigma_{V_{\text {trip }}}^{2}}{\left(g_{m} r_{o}\right)^{2}}} \tag{14}
\end{equation*}
$$

As an example, $\sigma_{V_{O S}}$ in (14) results to 5 mV under the design parameters in Table I, which is in good agreement with the 4.7mV offset standard deviation measured across twelve dice.

The noise performance of DIGOTA is dominated by the shot noise in the input devices MN1+, MN1-, MP1+, and MP1- in Fig. 2a since all devices operate in the subthreshold region.

Table I. Parameters from Simulations, Transistor Sizes ( $V_{D D}=0.3 \mathrm{~V}$ )

| transistor | $\mathbf{W}(\boldsymbol{\mu m})$ | $\mathbf{L}(\boldsymbol{\mu m})$ | Transistor | $\mathbf{W}(\boldsymbol{\mu m})$ | $\mathbf{L}(\boldsymbol{\mu m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{MN} 1 \pm$ | 3.9 | 0.18 | $\mathrm{MP} 1 \pm$ | 9 | 0.18 |
| $\mathrm{MN} 2 \pm$ | 5 | 0.18 | $\mathrm{MP} 2 \pm$ | 6.85 | 0.18 |
| MNMC | 1 | 0.18 | MPMC | 2.5 | 0.18 |
| MNO | 1 | 0.18 | MPO | 8.48 | 0.18 |
|  | strength |  |  | strength |  |
| $\mathrm{INV} \pm$ | 5 X |  | $\mathrm{AND} / \mathrm{OR}$ | 4 X |  |
| NegNOR | 5 X |  | NegAND | 5 X |  |
| parameter | value | unit | parameter | value | unit |
| $T_{0}$ | 13 | $\mu \mathrm{~s}$ | $r_{\text {OUT }}$ | 7.8 | nS |
| $g_{m}$ | 27 | nS | $C_{M U L}$ | 8 | fF |
| $g_{0}$ | 1.35 | nS | $C_{\text {int }}$ | 170 | fF |
| $I_{C M}$ | 930 | pA | $C_{L}$ | 150 | pF |
| $I_{O N}$ | 9.15 | nA |  |  |  |

[^2]Accordingly, the in-band equivalent input noise power can be expressed as [1]

$$
\begin{equation*}
\bar{v}_{n}^{2} \approx 2 \pi \frac{2 q I_{C M}}{g_{m}^{2}} f_{G B W}=2 r_{0} n k T \frac{I_{O N}}{T_{0} \cdot I_{C M}} \frac{C_{\mathrm{MUL}}}{C_{L}} \tag{15}
\end{equation*}
$$

which is independent of the input common-mode, as $T_{0} \cdot I_{C M}$ is independent of it (see Section III and Fig. 5). As an example, the values in Table I lead to an RMS in-band input-referred noise of $18.16 \mu \mathrm{~V}$ from (15) at $V_{D D}=0.3 \mathrm{~V}$, which is in agreement with the measured one of $21 \mu \mathrm{~V}$ in Table II. This corresponds to less than one LSB in a sensor interface based on 12-bit analog-digital conversion, which exceeds the range required by the vast majority of IoT applications [2].

## B. Power Consumption

The power consumption of the DIGOTA circuit is the sum of the power consumption of the active power $P_{\text {gates }}$ of the logic gates involved in the self-oscillating loop (i.e., Muller Celements, inverter gates, MCswap), the contribution $P_{\text {out }}$ of the output stage, and the overall leakage power $P_{l k g}$

$$
\begin{equation*}
P_{\text {DIGOTA }}=P_{\text {gates }}+P_{\text {out }}+P_{l k g} . \tag{16}
\end{equation*}
$$

In (16), $P_{\text {gates }}$ is given by the dynamic power of the internal logic gates with overall switched capacitance $C_{i n t}$ operating at frequency $2 / T_{0}$, which can be expressed as

$$
\begin{equation*}
P_{\text {gates }}=\frac{2}{T_{0}} C_{i n t} V_{D D}^{2} . \tag{17}
\end{equation*}
$$

$P_{\text {out }}$ is the power needed to (dis)charge the load capacitance $C_{L}$, which can be expressed as

$$
\begin{equation*}
P_{o u t}=f_{S} C_{L} V_{\text {out }}^{2} \tag{18}
\end{equation*}
$$

where a sinewave output with peak-to-peak amplitude $V_{O U T}$ at frequency $f_{S}$ has been assumed.

The leakage power in (16) is equal to the product of the supply voltage $V_{D D}$ and the total DIGOTA leakage current $I_{l k g}$, which is negligible in practical cases in 180 nm . At $V_{D D}=0.3 \mathrm{~V}$, based on simulations, the power $P_{\text {out }}$ drawn by the output stage accounts for $39 \%$ of the total power, whereas $P_{\text {gates }}$ accounts for $\sim 59.7 \%$, and $P_{l k g}$ is $1.3 \%$. Interestingly, DIGOTA is inherently more power-efficient than a conventional commonsource (CS) amplifier biased in weak inversion [1] to keep the same gain-bandwidth product. This is shown by comparing the DIGOTA power in (16)-(18) while neglecting leakage, and the power $P_{C S}$ of the common-source stage in (19)

$$
\begin{equation*}
P_{C S}=\left.V_{D D} I_{Q}\right|_{f_{G B W}}=2 \pi f_{G B W} C_{L} \frac{n k T}{q} V_{D D} \tag{19}
\end{equation*}
$$

which was evaluated as the product of the supply voltage and the quiescent current $I_{Q}$ required $^{2}$ to match the same $f_{G B W}$. The resulting power ratio leads to

$$
\begin{align*}
& \frac{P_{D I G O T A}}{P_{C S}}=\frac{1}{4 \pi g_{m} r_{o}} \frac{C_{i n t}}{C_{M U L}} \frac{I_{C M}}{I_{O N}} \frac{V_{D D}}{n k T / q}\left(1+4 \pi \frac{f_{S}}{f_{G B W}} \frac{C_{M U L}}{C_{i n t}} \frac{I_{O N}}{I_{C M}} \frac{V_{O U T}^{2}}{V_{D D}^{2}}\right) \\
& \quad \approx \frac{P_{\text {gates }}}{P_{C S}}=\frac{1}{4 \pi g_{m} r_{o}} \frac{C_{i n t}}{C_{M U L}} \frac{I_{C M}}{I_{O N}} \frac{V_{D D}}{n k T / q} \tag{20}
\end{align*}
$$

where the $P_{\text {DIGOTA }}$ is approximately equal to (17). Simulations
in 180 nm CMOS at $V_{D D}=0.3 \mathrm{~V}$ for $f_{S}=2 \mathrm{~Hz}$ lead to the parameter values in Table I, from which the ratio in (20) makes the DIGOTA power 23X lower than the conventional CS stage. This improvement is achieved thanks to the suppression of the constant power required by a bias current, in view of the digital nature of DIGOTA.

When the DIGOTA power is dominated by the $P_{\text {out }}$ in (18) (e.g., large $C_{L}$, signal amplitude $\Delta V_{\text {OUT }}$, and frequency $f_{S} \simeq$ $f_{G B W}$ ), the expression of the power ratio in (20) becomes

$$
\begin{equation*}
\frac{P_{D I G O T A}}{P_{C S}} \approx \frac{1}{g_{m} r_{0}} \cdot \frac{1}{n k T / q} \frac{V_{O U T}^{2}}{V_{D D}} \tag{21}
\end{equation*}
$$

which corresponds to a 16X power saving under full-swing output $V_{\text {OUT }}=V_{D D} / 2$. From (20)-(21), DIGOTA has an intrinsic advantage in power efficiency regardless of the specific load and input signal. This explains the competitive power efficiency measured in Section VIII. When compared to inverter-based OTAs [7], this power advantage is halved with respect to the CS stage, and hence results to $8 \mathrm{X}(11.5 \mathrm{X})$ when the power is (is not) dominated by the output stage. This is because the transconductance in an inverter gate is doubled compared to the CS stage [7].

The above advantage is proportional to $1 / T$ and becomes more pronounced at higher temperatures from (20)-(21), at which the sub-threshold current and hence the power consumption is inherently higher $\left(4.6 \% /{ }^{\circ} \mathrm{C}\right.$ from simulations). Such temperature dependence is mostly due to the subthreshold current dependence on the temperature (this technology has the same leakage sensitivity to temperature of $4.6 \% /{ }^{\circ} \mathrm{C}$ ). The latter is ascribed to the adopted technology rather than the specific circuit techniques, and is not inherently mitigated by the DIGOTA architecture. Hence, such temperature dependence can be mitigated by resorting to the several existing temperature compensation techniques for the sub-threshold current, as previously demonstrated in digital circuits down to $175-\mathrm{mV}$ supply (see, e.g., [29], [30]).

## VII. Circuit Design Considerations and Testchip

The DIGOTA architecture in Fig. 2a is fully digital and can hence be designed with digital standard cells and no passives, drastically reducing the design and the system integration effort. Compared to conventional analog design, DIGOTA enables digital-like area scaling across technology generations, and design and technology portability. As main limitation, the adoption of standard cells restricts the choice of transistor sizes to the discrete set of strengths available in the adopted library. Also, Muller-C cells might not be directly available in the library, although they can be easily implemented by merging an open-drain NAND and NOR gate, as shown in Fig. 2a.

In the $180-\mathrm{nm}$ testchip designed to experimentally validate the DIGOTA models, cells were sized to pursue high power efficiency, as quantified by the well-known small-signal and the large-signal figures of merit in (22a-b) [23]:

$$
\begin{align*}
& F O M_{S}=\frac{f_{G B W} \cdot C_{L}}{\text { power }}  \tag{22a}\\
& F O M_{L}=\frac{S R \cdot C_{L}}{\text { power }} \tag{22b}
\end{align*}
$$



Fig. 8. a) Test bench, micrograph of the DIGOTA 180-nm testchip and layout, b) sine/square wave response when directly powered by a $1-\mathrm{mm}^{2}$ solar cell at $<100$ lux (dark overcast day) ( $2.5-\mathrm{Hz}$ frequency, $75-\mathrm{mV}$ amplitude).
where $S R=I_{O N} / C_{L}$ is the slew rate averaged between the rising and falling transitions. By substituting (13) and (16)-(18) in (22a-b), the figures of merit can be simplified as

$$
\begin{align*}
F O M_{S} & =\left(\frac{g_{m} r_{o}}{2 \pi c_{i n t} V_{D D}^{2}} \frac{c_{M U L}}{I_{C M}}\right) \cdot I_{O N}  \tag{23a}\\
F O M_{L} & =\left(\frac{1}{c_{\text {int }} V_{D D}} \frac{c_{M U L}}{I_{C M}}\right) \cdot I_{O N} \tag{23b}
\end{align*}
$$

In (23a-b), both FOMs are inversely proportional to $C_{i n t}$ and the slope $I_{C M} / C_{M U L}$ of the Muller-C element output voltage.
Hence, the FOMs expectedly benefit from the adoption of minimum-sized logic gates and the reduction in the selfoscillation frequency in (5a), as they both reduce the consumption associated with the logic gates in the selfoscillating loop. Regarding the output stage, higher strength and $I_{O N}$ in the output stage directly improve both figures of merit.

The cell strengths within the self-oscillating loop were chosen as a tradeoff between the offset voltage in (14), the bandwidth (i.e., $f_{G B W}$ in (13)), and the input-referred noise power $\bar{v}_{n}^{2}$ in (15). In particular, reducing $V_{\mathrm{OS}}$ requires transistor up-sizing in the first stage, whereas improving $f_{G B W}$ requires transistor up-sizing in the output stage so that a higher $I_{O N}$ is delivered. The strength of the output stage cell was set to drive a load capacitance of $C_{L}=150 \mathrm{pF}$ at $f_{G B W}=800 \mathrm{~Hz}$, to demonstrate the power efficiency of DIGOTA even under heavy capacitive loads. The DIGOTA transistor sizes in the testchip are summarized in Table I.

The DIGOTA core occupies an area of $982 \mu \mathrm{~m}^{2}$, as shown in Fig. 8a. The DIGOTA testchip was characterized in the voltage follower configuration at $0.25-0.5 \mathrm{~V}$ supply voltage range via


Fig. 9. Open-loop frequency response at $V_{D D}=0.3 \mathrm{~V}, C_{L}=150 \mathrm{pF}$ : a) magnitude and b) phase from testchip measurements and model in (11)-(13).
conventional OTA testing in static and dynamic conditions. The measurement results across dice are discussed in Section VIII.

## VIII. Measurement Results and Model Validation

The measured response of the DIGOTA circuit in the voltage follower configuration to sine and square wave inputs is shown in Fig. 8 b under a $0.3-\mathrm{V}$ supply generated directly by a mmscale solar cell. The measurements in the following were carried out by setting the supply voltage with a sourcemeter, to assure repeatable and well-defined testing conditions.

The DIGOTA open-loop frequency response is plotted in Fig. 9, as evaluated from testchip characterization and the model in (10)-(13). At the low voltage of 0.3 V and a heavy capacitive load of 150 pF , this figure shows a $30-\mathrm{dB} \mathrm{DC}$ gain, a $250-\mathrm{Hz}$ gain-bandwidth product, and a $\sim 90^{\circ}$ phase margin. Fig. 9 shows good agreement between the model and the measurements, with an average (maximum) error of 1.13 dB $(3.4 \mathrm{~dB})$ for the magnitude, and $4.6^{\circ}\left(11^{\circ}\right)$ degrees for the phase. For DC inputs, the measured CMRR is 41 dB , whereas the measured PSRR is 30 dB at the same $0.3-\mathrm{V}$ supply. The openloop output resistance $r_{\text {OUT }}$ is $21 \mathrm{M} \Omega$.

The measured spectrum of the response to a $2.5-\mathrm{Hz}$ sine wave with $75-\mathrm{mV}$ amplitude is reported in Fig. 10a, which shows the harmonics due to distortion and the out-of-band self-oscillation frequency tone at $\sim 8 \mathrm{kHz}$. The resulting total harmonic distortion THD in Fig. 10b is less than 2\% for input amplitudes exceeding $90 \%$ of the rail-to-rail swing, corresponding to 7 -bit linearity. The THD was found to slightly increase by $\sim 0.1 \%$ at higher frequencies.

From Fig. 10a, the input-referred RMS noise model in (15) of $18.16 \mu \mathrm{~V}_{\text {RMs }}$ agrees well with the measured value of 21

(b)

Fig. 10. a) Output spectrum under sine wave input ( $2.5 \mathrm{~Hz}, 75-\mathrm{mV}$ ), b) THD vs amplitude under sine wave input ( 2.5 Hz ), at $V_{D D}=0.3 \mathrm{~V}, C_{L}=150 \mathrm{pF}$.
$\mu \mathrm{V}_{\mathrm{RMS}}$. Hence, linearity sets the ultimate limit to the resolution of sensor interfaces based on DIGOTA, rather than noise.

The power consumption at $0.25-0.5 \mathrm{~V}$ supply and $150-\mathrm{pF}$ capacitive load range from 850 pW to 107 nW , as plotted in Fig. 11a. The power model in (16)-(18) agrees with measurements with an average error of $9 \%$. From the same figure, the gainbandwidth product ranges from 40 Hz to 57.5 kHz , which is modeled by (13) with an average error of $15 \%$. The exponential increase of power and $f_{G B W}$ with $V_{D D}$ in Fig. 11a is due to the exponential increase in the transistor sub-threshold current $I_{O N}$ in (13), and consequently in the frequency $1 / T_{0}$ in (17). Also, Fig. 11b shows the nearly-linear dependence of the power consumption on the input frequency $f_{S}$, as expected from the power contribution of the output stage in (18).
The resulting figures of merit $F O M_{S}$ in (22a) $\left(F O M_{L}\right.$ in (22b)) are in the $7.1-80.2 \mathrm{MHz} \cdot \mathrm{pF} / \mu \mathrm{W}$ range (4.2-26.5 (V/ $\mu \mathrm{s}) \cdot \mathrm{pF} / \mu \mathrm{W}$ range). The average error of the model in (23a) and (23b) with respect to the measurements is respectively $25 \%$ and $12 \%$.

Regarding the voltage dependence, Fig. 11c confirms that $F O M_{S}$ is proportional to $\mathrm{e}^{2 V_{D D} /(n k T / q)} / V_{D D}^{2}$ as in (23a), and $F O M_{L}$ is proportional to $\mathrm{e}^{2 V_{D D} /(n k T / q)} / V_{D D}$ as in (23b), at low voltages that keep transistors in the sub-threshold region.
The consistency of the above results under process variations was validated through the characterization of twelve DIGOTA die samples, as plotted in Fig. 12 for the closed-loop frequency response in the voltage buffer configuration. At the voltage of 0.3 V and without the support of any bias circuitry, the mean value and standard deviation of the DC gain are respectively -0.33 and 0.23 dB . The mean value and the standard deviation for the -3 dB cutoff frequency are respectively 265 Hz and 99 Hz , leading to variability of $37 \%$. This confirms reasonable


Fig. 11. a) Power and gain-bandwidth product vs $V_{D D}$, b) power vs input frequency ( $50-\mathrm{mV}$ amplitude, $V_{D D}=0.3 \mathrm{~V}$ ), c) figures of merit $\mathrm{FOM}_{\mathrm{S}}$ ( y -axis on the left) and $\mathrm{FOM}_{\mathrm{L}}$ (y-axis on the right) vs $V_{D D}$.
consistency without the need for calibration, unlike previously proposed digital OTAs [31]. The same conclusions hold under temperature variations, with a maximum DC gain change of 5 dB in the entire $-20-80^{\circ} \mathrm{C}$ range from simulations.

The gain-bandwidth product, the slew rate, and the power consumption for the measured die samples are reported in Fig. 13. This figure confirms fairly consistent performance across dice, despite operation at very low voltage and the absence of a bias current reference. From Fig. 13, the variability of $f_{G B W}$, $S R$, and power is respectively $37.7 \%, 15.7 \%$, and $34 \%$. As a reference, the variability of the technology is quantified by the $51 \%$ variability of the $F O 4$ delay at $V_{D D}=0.3 \mathrm{~V}$. Accordingly, the variability of $f_{G B W}, S R$, and power is lower than the $F O 4$ variability, confirming the resilience of the DIGOTA architecture against process variations. At 0.5 V , the variability of $f_{G B W}, S R$, and power become $15 \%, 64 \%$, and $30 \%$, respectively.

(b)

Fig. 12. a) Magnitude and b) phase-frequency response of the closed-loop transfer function of twelve DIGOTA dice in the voltage follower configuration
As for other non-idealities, the offset voltage standard deviation across the twelve dice is 4.7 mV , from the available samples in Fig. 11. The total harmonic distortion in Fig. 16 has a variability of $23.1-25.5 \%$, across the range of moderate to large amplitudes, above 50 mV and up to 125 mV . The variability increases by 1.1-1.8X at extreme input amplitudes, due to the intrinsic transistor non-linearity on the higher end, and the non-linearity source in footnote 1 on the lower end.


Fig. 13. Measurement results across twelve dice and effect of process variations on gain-bandwidth product, slew rate and power consumption ( $V_{D D}=0.3 \mathrm{~V}$ ).


Fig. 14. Measured input offset voltage of twelve DIGOTA dice and resulting mean value and standard deviation.

From Fig. 17, the large-signal (small-signal) power efficiency figure of merit has a $23.3 \%$ (29.6\%) variability, indicating that nearly power efficiency is fairly consistent across process variations. Regarding the impact of temperature, from Fig. 15a the DC gain $A_{V 0}$ is relatively independent of the temperature with a maximum fluctuation of 5 dB over the highest value of 34.3 dB . From the same figure, $f_{G B W}$ increases exponentially at a rate $\alpha$ of $2.8 \% /{ }^{\circ} \mathrm{C}$, where the exponential growth rate $\alpha$ is defined as:

$$
\begin{equation*}
\alpha=\left(\frac{f_{G B W} \mid T_{1}}{\left.f_{G B W}\right|_{T_{0}}}\right)^{\frac{1^{\circ} \mathrm{C}}{T_{1}-T_{0}}}-1 \tag{24}
\end{equation*}
$$

in which $\left.f_{G B W}\right|_{T_{1}},\left.f_{G B W}\right|_{T_{0}}$ are the $f_{G B W}$ values at $T_{0}=-20^{\circ} \mathrm{C}$ and $T_{1}=80^{\circ} \mathrm{C}$, respectively.
From Fig. 15b, the total harmonic distortion (THD) is nearly independent of the temperature, due to the minor temperature effect on the static characteristics of CMOS logic gates [2]. The power expectedly increases exponentially with the temperature at a rate of $4.6 \% /{ }^{\circ} \mathrm{C}$ defined as in (24) (see Section VI.B), as determined by the adopted technology since leakage increases by the very same rate. Again, such temperature dependence can be mitigated through existing temperature compensation techniques in sub-threshold [29], [30]. Nevertheless, from Table II the DIGOTA power is at least an order of magnitude lower than prior art even without such compensation.
The DIGOTA performance is compared with state-of-the-art ultra-low-voltage and ultra-low power OTAs in Table II. At the supply voltage of 0.3 V , DIGOTA operates at the nW - range power, which is at least an order of magnitude lower than

(b)

Fig. 15. Temperature dependence of a) DC voltage gain and gain-bandwidth product vs. temperature, b ) total harmonic distortion and power (simulations).


Fig. 16. Measured total harmonic distortion (THD) of twelve DIGOTA dice, their mean value, and standard deviation vs input sinewave amplitude ( 2.5 Hz input, $\left.V_{D D}=0.3 \mathrm{~V}, C_{L}=150 \mathrm{pF}\right)$.


Fig. 17. Measured figures of merit $F O M_{S}$ and $F O M_{L}$ across DIGOTA dice. Power has been measured for sine wave ( 2.5 Hz input, $V_{D D}=0.3 \mathrm{~V}, C_{L}=150 \mathrm{pF}$ ).
prior art. Such power is also efficiently used when driving heavy capacitive loads, as indicated by the smallsignal $\mathrm{FOM}_{S}=15.6 \mathrm{MHz} \cdot \mathrm{pF} / \mu \mathrm{W}$, which is $1.5-34 \mathrm{X}$ better than prior OTAs operating in the same supply voltage range [6]-[8], [32]. As intrinsic limitations of DIGOTA, the DC gain is 19.830 dB lower than prior art and the CMRR is accordingly lower by $21.5-37 \mathrm{~dB}$, the PSRR is $8-46 \mathrm{~dB}$ lower, and the THD is $1 \%$ higher.

The digital nature of DIGOTA reduces the area by 2-85X over prior art. Combining power and area efficiency, the areanormalized figure of merit $F O M_{S, A}$ in Table II [6]-[8], [32] is improved by $>6 \mathrm{X}$. Similarly, the area-normalized large-signal figure of merit $F O M_{L, A}$ is improved by $>9 \mathrm{X}$, compared to the prior art in the same supply voltage range.

At 0.5 V , the DIGOTA performance improves to $73-\mathrm{dB}$ DC gain, $f_{G B W}=57.5 \mathrm{kHz}$, and $19 \mathrm{~V} / \mathrm{ms}$ slew rate. The PSRR is increased to 50 dB , and becomes hence the same as [33]. Compared to OTAs with much higher supply in the $1.1-2 \mathrm{~V}$ range [3]-[8], [33], Table II shows that DIGOTA still maintains the second-best $F O M_{S}$ and $F O M_{L, A}$, and the best $F O M_{S, A}$.

## IX. CONCLUSION

In this paper, the DIGOTA architecture has been analyzed and modeled analytically to gain an insight into the dependence of its performance on process and design parameters. The

Table II. Performance Comparison with State-of-the-Art OTAs (Best Performance in Bold)

|  | $V_{D D} \leq 500 \mathrm{mV}$ |  |  |  |  | $V_{D D}>500 \mathrm{mV}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | [6] | [7] | [8] | [32] | This work | [3] | [4] | [5] | [33] | This work |
| supply voltage used for comparison (minimum voltage $V_{\min }$ ) [V] | $\begin{gathered} \hline 0.5 \\ (0.45) \\ \hline \end{gathered}$ | $\begin{gathered} 0.3 \\ (0.3) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.25 \\ (0.25) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.25 \\ (0.25) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.3 \\ (0.25) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 1.1 \\ (1.1) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 1.2 \\ (1.2) \\ \hline \end{gathered}$ | $\begin{gathered} 2 \\ (2) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.9 \\ (0.9) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.5 \\ (0.25) \\ \hline \end{gathered}$ |
| design | custom | custom | custom | custom | std cell | custom | custom | custom | custom | std cell |
| OTA architecture | bulkdriven | gatedriven | bulk- <br> driven | bulk- <br> driven | digital | PSS amplifiers | Miller | folded <br> Cascode | bulkbiased | digital |
| ext. current reference needed (Y/N) | Y | N | Y | Y | N | Y | Y | Y | Y | N |
| technology [nm] | 180 | 130 | 130 | 65 | 180 | 180 | 180 | 500 | 350 | 180 |
| area ( $\mu \mathrm{m}^{2}$ ) | 26,000 | - | 83,000 | 2,000 | 982 | 2,100 | 13,000 | 30,000 | 14,000 | 982 |
| normalized area ( $10^{3} \cdot \mathrm{~F}^{-2}$ ) | 802.47 | - | 4,911 | 473 | 30.3 | 64.81 | 401.23 | 120 | 114.28 | 30.3 |
| cap load $\mathrm{C}_{\mathrm{L}}[\mathrm{pF}]$ | 20 | 2 | 15 | 15 | 150 | 100 | 18,000 | 70 | 10 | 150 |
| power [ $\mu \mathrm{W}$ ] | $110^{\text {a }}$ | 1.8 | $0.018^{\text {a }}$ | 0.026 | $0.0024{ }^{\text {b }}$ | $7.4{ }^{\text {a }}$ | $69.6{ }^{\text {a }}$ | $100^{\text {a }}$ | 18.9 | $0.1075{ }^{\text {b }}$ |
| worst-case power across dice $(\mu \mathrm{W}$, evaluated at $\mu+3 \sigma)$ | N/A ${ }^{\text {c }}$ | $\mathrm{N} / \mathrm{A}^{\mathrm{c}}$ | $\mathrm{N} / \mathrm{A}^{\mathrm{c}}$ | $\mathrm{N} / \mathrm{A}^{\mathrm{c}}$ | $0.0048{ }^{\text {d }}$ | N/A ${ }^{\text {c }}$ | $\mathrm{N} / \mathrm{A}^{\text {c }}$ | $\mathrm{N} / \mathrm{A}^{\mathrm{c}}$ | N/A ${ }^{\text {c }}$ | $0.292{ }^{\text {d }}$ |
| DC gain [dB] | 52 | 49.8 | 60 | 70 | 30 | 100 | 100 | 76.8 | 65 | 73 |
| GBW [kHz] | 2,500 | 9,100 | 1.88 | 9.5 | 0.250 | 1,660 | 1,180 | 3,400 | 1,000 | 57.5 |
| average slew rate $\mathrm{SR}[\mathrm{V} / \mu \mathrm{s}$ ] | 2.89 | 3.8 | 0.0007 | 0.002 | 0.000085 | 8.67 | 0.22 | 19.25 | 0.25 | 0.019 |
| in-band input noise [ $\mu \mathrm{V}$ ] | 442.7 | 105.6 | 143 | - | 21 | - | - | 42.41 | 65 | 122 |
| CMRR [dB] | 78 | - | - | 62.5 | 41 | - | - | 112 | 45 | 65 |
| PSRR [dB] | 76 | - | - | 38 | 30 | - | - | 92 | 50 | 50 |
| THD [\%] | 1.0 | - | 1.0 | - | 2.0 | - | - | - | 0.2 | 1.0 |
| $F O M_{S}[\mathrm{MHz} \cdot \mathrm{pF} / \mu \mathrm{W}]$ | 0.45 | 10 | 1.6 | 5.48 | 15.6 | 22.4 | 305.2 | 2.4 | 0.52 | 80.2 |
| $F O M_{L}[(\mathrm{~V} / \mu \mathrm{s}) \cdot \mathrm{pF} / \mu \mathrm{W}]$ | 0.52 | 4.2 | 0.58 | 1.15 | 5.3 | 117.2 | 56.9 | 13.5 | 0.13 | 26.5 |
| area-normalized $F O M_{S, A}\left[\frac{\mathrm{MHz} \cdot \mathrm{pF}}{\mu \mathrm{W} \cdot \mathrm{mm}^{2}}\right]$ | 17.3 | - | 19 | 2,750 | 15,885 | 10,666 | 23,477 | 80 | 37.15 | 81,724 |
| area-normalized $F O M_{L, A}\left[\frac{\mathrm{~V} / \mu \mathrm{s} \cdot \mathrm{pF}}{\mu \mathrm{W} \cdot \mathrm{mm}^{2}}\right]$ | 20.2 | - | 7 | 575 | 5,397 | 55,792 | 4,377 | 450 | 9.45 | 27,000 |
| passives needed | Y | N | Y | Y | N | Y | Y | Y | Y | N |
| ${ }^{\text {a }}$ Power of current reference not accou FOM definition [1] | for [6]: FOM | Evaluat $=\frac{G B W \cdot C_{L}}{\text { power }}$ | $\begin{array}{r} 2.5-\mathrm{H} \\ \mathrm{FO} \end{array}$ | mV inp $\frac{S R \cdot C_{L}}{\text { power }}$ | $\begin{array}{r} { }^{\mathrm{c}} \mathrm{Mea}^{2} \\ F O M_{S, A} \end{array}$ | $\begin{aligned} & \text { irements on } \\ & =\frac{G B W \cdot C_{L}}{\text { power.area }} \end{aligned}$ | ne die F | $\begin{array}{r} { }_{L, A}=\frac{{ }^{\mathrm{d}} \mathrm{Me}}{\text { powe }} \end{array}$ | rements | 12 dice |

analysis expresses such dependence for the main OTA parameters, such as the DC gain, the frequency response, the gain-bandwidth product, the input-referred noise, and the input offset voltage, as well as the power consumption breakdown into its fundamental contributions. The derivations also provide a deeper understanding of the operation of the common-mode feedback loop, and the design implications of standard cell implementations. Also, it was shown that DIGOTA is essentially a self-oscillating threshold sampler, for which the self-oscillation frequency was evaluated. The power efficiency of DIGOTA was evaluated and was shown to be potentially more than an order of magnitude better than a simple commonsource stage operating in the sub-threshold region. The analytical expression of the above OTA parameters was validated through comparison with multi-die measurements, showing good agreement across two (four) orders of magnitude of power consumption (bandwidth).

At 0.3-0.5 V, the small-signal (large-signal) energy FOM improvement over prior sub-0.5 V OTAs has been shown to be at least $1.5 \mathrm{X}(1.3 \mathrm{X})$, while reducing area by $2-85 \mathrm{X}$. The DIGOTA area efficiency advantage mainly stems from its digital nature and the suppression of common-mode feedback control. This comes at the cost of reduced DC gain, PSRR and CMRR, along with higher THD and exponential variations over temperature and supply voltage, as expected from any subthreshold circuit. This makes DIGOTA suitable for medium-tolow accuracy applications, and further mitigation of the voltage and temperature effect respectively requires the adoption of voltage regulation and existing temperature compensation techniques such as in [29], [30].

The digital nature, the ultra-low voltage operation and the nW-range power make DIGOTA very well suited for direct harvesting. The resulting suppression of intermediate DC-DC conversion enables further energy and area reductions at the system level, extending system availability under unfavorable harvesting conditions and reducing the overall system cost.

## APPENDIX A

From (3)-(4), the overall self-oscillation period $T_{0}$ can be written as the time spent in state A and C

$$
\begin{align*}
T_{0} & =T_{A}+T_{C}=\left(V_{\text {trip }}-V_{\text {min }}\right) \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, A}}+ \\
& +\left(V_{\text {max }}-V_{\text {trip }}\right) \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, C}}+2\left(\tau_{I N V}+\tau_{M C s w a p}\right) \tag{A.1}
\end{align*}
$$

$V_{t r i p}$ in (A.1) is equal to $V_{D D} / 2$ in practical cases where the standard cells INV+ and INV- are designed symmetrically, as commonplace in commercial standard cell libraries. Also, the self-oscillation period in (A.1) is upper bounded by (A.2), considering that $V_{\max }\left(V_{\min }\right)$ cannot be larger than $V_{D D}$ (lower than 0 ), being the output of a logic gate as in Fig. 4:

$$
\begin{align*}
T_{0} & \leq \frac{V_{D D}}{2} \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, A}}+\frac{V_{D D}}{2} \cdot \frac{C_{\mathrm{MUL}}}{I_{C M, C}}+2\left(\tau_{I N V}+\tau_{M C s w a p}\right)= \\
& =V_{D D} \cdot \frac{C_{\mathrm{MUL}}}{I_{C M}}+2\left(\tau_{I N V}+\tau_{M C s w a p}\right) \tag{A.2}
\end{align*}
$$

where $I_{C M}$ is defined as the average of the currents $I_{C M, A}$ and $I_{C M, C}$ (via the reciprocals)

$$
\begin{align*}
& I_{C M}=\frac{2}{\frac{1}{I_{C M, A}}+\frac{1}{I_{C M, C}}}=\frac{2}{\frac{1}{\frac{V_{D D^{-v} C_{C M}}}{\frac{n k T}{q}}}+\frac{1}{I_{0} e^{\frac{v_{C M}}{n k T}}}=}= \\
&=\frac{I_{0} e^{\frac{V_{D D / 2}}{n k T / q}}}{\cosh \left(\frac{v_{C M}-\frac{V_{D D}}{2}}{n k T / q}\right)} \tag{A.3}
\end{align*}
$$

In (A.2), PMOS and NMOS transistors in the Muller Celements were assumed to be sized to make $I_{P, 0}$ and $I_{N, 0}$ equal to the common value $I_{0}$.

The self-oscillation period reaches its upper bound in (A.2) at the extreme values of the range of $v_{C M}$ (i.e., ground and $V_{D D}$ ). Indeed, $v_{C M}=0$ makes $I_{C M, A} \gg I_{C M, C}$ and equal to the full oncurrent that the Muller C-element is capable of delivering during state A (see Fig. 4), thus making its delay comparable to the other gate delays $\tau_{I N V}$ and $\tau_{M C s w a p}$ (actually even lower than the latter, given its larger size from Section VI.A and Table I). Accordingly, from Figs. 3a and 4 the Muller C-element has more than enough time to have a full-swing transition, and hence reach $V_{\max } \approx V_{D D}$. During state $\mathrm{C}, v_{I N, C M}=0$ makes the pull-down network of the Muller C-element conduct the very minimal (leakage) current $I_{C M, C}$ above, keeping $V_{\text {min }}$ basically at $V_{D D} / 2$ during $\tau_{I N V}$ and $\tau_{M C s w a p}$. Since $I_{C M} \approx 2 I_{C M, C}$, from (A.3) the self-oscillation period $T_{0}$ in (A.1) results to (A.2), which proves the above point.

Analogous results are achieved at the opposite end $v_{C M}=$ $V_{D D}$, and are easily extended to any $v_{C M}$, considering that the above $V_{\max }=V_{D D}$ and $V_{\min }=0$ still apply. And indeed simulations confirm that the maximum discrepancy between $V_{\max }$ and $V_{D D}\left(V_{\min }\right.$ and ground) is 23 mV at $V_{D D}=0.3 \mathrm{~V}$. Accordingly, (A.2) can be used to model $T_{0}$ across the entire common-mode range, in accordance with the observations made in Fig. 5 and Section III.

## APPENDIX B

In the small-signal circuit in Fig. 6, the overall transconductance $g_{m}$ is defined as the derivative of the current $i_{+}$with respect to the differential input voltage $v_{I N, D}$ averaged over the self-oscillation period $T_{0}$. The current $i_{+}$is provided by MP1+ (MN1+) in the sub-period $T_{A}\left(T_{C}\right)$ of the selfoscillation period when DIGOTA is in state A (C). Accordingly, $g_{m}$ can be expressed as the weighted sum of the transconductances $g_{m, A}$ and $g_{m, C}$ of the DIGOTA circuit in state A and C. The weight is given by the fraction of the period spent in each state, thus leading to

$$
\begin{align*}
g_{m} & =g_{m, A} \frac{T_{A}}{T_{0}}+g_{m, C} \frac{T_{C}}{T_{0}} \approx \\
& \approx \frac{I_{C M, A}}{n k T / q} \frac{I_{C M}}{2 I_{C M, A}}+\frac{I_{C M, B}}{n k T / q} \frac{I_{C M}}{2 I_{C M, B}}=\frac{I_{C M}}{n k T / q} \tag{B.1}
\end{align*}
$$

where, $T_{A}, T_{C}$, and $T_{0}$ were approximated by $\frac{\mathrm{V}_{\mathrm{DD}} C_{\mathrm{MUL}}}{2 I_{C M, A}}, \frac{\mathrm{~V}_{\mathrm{DD}} C_{\mathrm{MUL}}}{2 I_{C M, C}}$, and $\mathrm{V}_{\mathrm{DD}} C_{\mathrm{MUL}} / 2 I_{C M}$ from Appendix A , considering the dominance of the Muller C-element delay over $\tau_{I N V}$ and $\tau_{M C s w a p}$ in (5b) (see Section III).

The net output resistance $r_{o}$ of the PMOS transistors in the input stage is the derivative of the current $i_{+}$with respect to the source-drain voltage $v_{S D}$. This is evaluated by averaging the contributions of MP1+ (MN1+) during states A (C) in a similar fashion, leading to

$$
\begin{equation*}
r_{o}=\left(\left.\frac{\partial i_{+}}{\partial v_{S D}}\right|_{I_{C M}}\right)^{-1} \simeq \frac{n k T / q}{\lambda_{D I B L} I_{C M}} \tag{B.2}
\end{equation*}
$$

The product $g_{m} r_{o}$ is the intrinsic gain of MP1-/MP1+ (MN1$/ \mathrm{MN} 1+$ ) of the input stage in the logic state $\mathrm{A}(\mathrm{C})$.
From (B.1)-(B.2), $g_{m} r_{o}$ is approximately independent of $I_{C M}$ and the input common-mode. Furthermore, the opposite common-mode dependence of $I_{C M, A}$ and $I_{C M, C}$ makes $I_{C M}, g_{m}$ and $r_{o}$ approximately independent of the common-mode. Accordingly, the second pole of the DIGOTA circuit in (12) is also approximately common-mode independent, and the same applies to the DIGOTA frequency response in (11)-(13).

## Acknowledgement

The authors would like to thank Maksudjon Usmonov for his valuable support during the measurements. The authors acknowledge the support of the Singapore Ministry of Education (MOE2019-T2-2-189 grant).

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[^1]:    ${ }^{1}$ The output stage is activated a propagation delay $\tau_{\text {out }}$ after the circuit enters in state B or D, thus it cannot deliver the full transistor ON current if $\Delta t<\tau_{\text {out }}$, which occurs at particularly small $v_{D}$. To counteract such non-linearity, $\tau_{\text {out }}$ is

[^2]:    ${ }^{2}$ The common source is biased in weak inversion at $V_{D D}=0.3 \mathrm{~V}$, which leads to $f_{G B W}=250 \mathrm{~Hz}$ at $C_{L}=150 \mathrm{pF}$. No extra bias is taken into account.

