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# Design, Verification, Test and In-Field Implications of Approximate Computing Systems

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Abstract—Today, the concept of approximation in computing is becoming more and more a "hot topic" to investigate how computing systems can be more energy efficient, faster, and less complex. Intuitively, instead of performing exact computations and, consequently, requiring a high amount of resources, Approximate Computing aims at selectively relaxing the specifications, trading accuracy off for efficiency. While Approximate Computing gives several promises when looking at systems' performance, energy efficiency and complexity, it poses significant challenges regarding the design, the verification, the test and the in-field reliability of Approximate Computing systems. This tutorial paper covers these aspects leveraging the experience of the authors in the field to present state-of-the-art solutions to apply during the different development phases of an Approximate Computing system.

Index Terms-approximate computing, circuit, design, test.

#### I. Introduction

"The reliance of the society on the use of information and communications technology (ICT) devices and systems is ever increasing. From the proliferation of e-mail and electronic document exchange, social media and apps to the ready use of mobile devices (already in their fourth generation), data analytic, and advanced computing to solve big challenges, ICT is having a disruptive impact on our society" [1]. However, the ICT energy consumption is unsustainable and it will heavily impact on the future climate change.

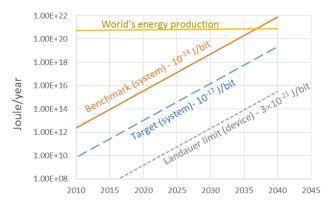


Fig. 1: Energy consumption trend in computing vs. the world energy production. Source: SIA/SRC [2]

Following the current trend, by 2040 computers will need more electricity than the world energy resources can generate, as illustrated in Figure 1. Already by 2025, data centers alone will consume 20% of all available electricity [3]. A similar trend exists on the communications side where, for example, energy consumption in mobile broadband networks and mobile terminals is comparable to data centers. In addition to the traditional personal communications, the Internet-of-Things (IoT) will soon connect up to 50 billion devices through wireless networks to the cloud, which will accelerate these trends [4].

Approximate and transprecision (i.e., adaptive precision) computing combined with application-specific processing structures are emerging computing paradigms able to support achieving the required energy efficiency improvements.

Since energy consumption (computing or communication) is the product of time and average power consumption of the device while carrying out an operation, these two factors, time and power, must be optimized for achieving energy savings. Approximate computing foresees to achieve this goal by considering a precious third design dimension, i.e., accuracy. The rationale at the base of this computing paradigm is that, in several parts of the global data acquisition, transfer, computation, and storage systems, it is possible to trade-off accuracy to either less power or less time consumed - or both.

As examples, numerous sensors are measuring noisy or inexact inputs; the algorithms processing the acquired signals can be stochastic; the applications using the data may be satisfied with an "acceptable" accuracy instead of exact and absolutely correct results; the system may be resilient against occasional errors; and a coarse classification or finding the most probable matches may be enough for a data mining system [5]–[7]. By introducing a new dimension – accuracy – to the design optimization, the energy efficiency can even be improved by a factor of 10x-50x.

While Approximate Computing gives several promises when looking at systems' performance, energy efficiency and complexity, it poses significant challenges regarding the design, verification, test and the in-field reliability of the approximated systems:

• Design: while several papers propose different approx-

imation techniques at hardware and software level, the decision of "what" to approximate and "how" to approximate given a target precision is still a challenging design space exploration problem that must be supported by dedicated design solutions and tools;

- Verification and Testing: verifying an approximated system and testing it at the end of production is a complex task. Traditional techniques for verification and testing start from the assumption that a system behaves in a deterministic way and any deviation from the planned behavior represents a hazard that must be addressed. This constraint is relaxed when Approximate Computing is applied, thus opening the path to different verification and testing techniques;
- In-field: once deployed in-field, approximated systems are still exposed to sources of errors (e.g., soft errors) like traditional precise systems. However, approximated systems have an intrinsic degree of error resilience, thus exposing inherent fault tolerance properties that can be exploited to reduce the reliability tax. This must be carefully budgeted when considering the reliability of the final system.

This paper overviews the above mentioned implications by presenting main challenges and state-of-art solutions derived from the application of Approximate Computing techniques in complex computing systems. The paper is structured following the main phases of the development cycle and use of a system: Section II considers the design phase, Section III the verification phase, Section IV the testing phase and Section V the implication of Approximate Computing on in-field operation. Finally, Section VI summarizes the main contributions of the paper.

#### II. DESIGN PHASE

Several publications have contributed to the definition of different approximation techniques applicable at different design abstraction levels (e.g., gate level or architectural level) and different levels of the system stack (e.g., hardware level or software level). Every technique is in general characterized at the application level to understand the provided accuracy/implementation costs trade-offs. In general, the proposed approximation techniques can be grouped in three main categories [8]:

- Software approximations: approximate the software could correspond to functional approximations, such as a reduction in the number of iterations in an iterative-improvement algorithm [9], timing relaxation, and domain specific approximations. This approach has also proved to be resilient to fault, if needed [10].
- Data approximations: approximate data could be used to reduce the storage for data-intensive applications or for data resilient applications, such as neural networks and classifiers, to leverage the inherit error resiliency of the architecture [11], [12].
- *Hardware approximation*: approximate the hardware could replace or enhance the hardware layer with specific

approximate components, such as adders and multipliers, to introduce intentional errors without modifying the algorithm [13].

When looking at evaluating a design, a primary concern is the fact that quality metrics may differ. Despite metrics such as delay/throughput, area, and power dissipation can be quantified at different levels of the design, and can still be comparable, the accuracy metric may be measured differently at various stages of design (refer to Figure 2). In fact, if for a multimedia application the Peak Signal-to-Noise Ratio (PSNR) or the Structural Similarity Index Metric (SSIM) can be a way to report the error, on other classification applications it can be the percentage of true positives [14]. If we move down in the system layers, at hardware level, the error metric can be evaluated as bit error rate (BER), or a probability distribution of error.

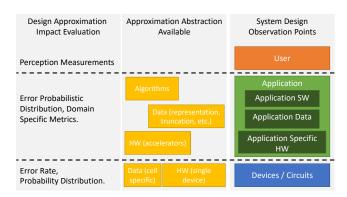


Fig. 2: Design approximation impact evaluation vs the levels of abstraction

It is clear that for the approximate computing to be effectively exploited within a design flow, it is essential to build quantitative approaches to model errors at each level of abstraction and to translate them to errors at other levels, in order to exploit the usage of the approximation at different levels of abstraction.

Another major concern for the approximate design regards the size of the design space to be explored. In fact, most of the research works already published address this problem by profiling the execution of the application several times, each time with a different version generated by combining one or more approximate operators together. The different design options are then compared with a golden approximate-free implementation [15]–[18]. This analysis can also be used to perform multi-objective optimization as proposed in [19] where authors exploit genetic programming for an automated functional approximation of combinational circuits at the gate and register-transfer levels.

In terms of multi-objective approaches, an interesting contribution is proposed in [20]. Authors report a survey of approximation techniques with some relation with the energy efficiency of the computation, in a cross-layer fashion. Despite this work only addresses hardware components (adders and multipliers), it introduces the idea that the design should be

able to consider different points of intervention within the full stack of the system and also includes an experimental setup that addresses verification exploiting several versions.

A tool called IDEA, proposed in [21], moves the design to a higher level of abstraction by supporting a design space exploration based on the annotation of relaxing points into an application. Those relaxing points express the accuracy reduction constraints that are exploited by the tool to generate variants of a C/C++ application including different approximation techniques. Those variants are analyzed using a branch and bound technique. While this approach proposes a solution to the problem of automating the application of different approximate computing techniques to a program, it still resorts to the creation of variants and their execution to evaluate the impact of each approximation on the results based on benchmark specific metrics.

To cope with the timing required by the exploration of a huge design space, in [22] the authors propose a methodology for searching, selecting and combining the most suitable approximate circuits, from a set of available libraries, in order to generate an approximate accelerator. The methodology exploits machine learning techniques to generate several computational models of the accelerator. Each model is designed to ease the evaluation of the quality of the processing and the energy efficiency by means of a Pareto Frontier evaluated for each model. The whole approach is bounded to a given application but the machine learning approach reduces the time-consuming exploration.

A broaden approach is described in [23], where the optimization starts from a RTL or HDL description of the hardware to optimize, thus still application-dependent, and its achieved by generating approximate high-level variants, through three steps: (i) transform the description into an Abstract Syntax Tree (AST) structure; (ii) create variants through transformations to the AST; and (iii) write the modified AST back into readable a RTL or HDL description. The interesting aspect of the approach is that the operators that can be targeted include data type simplifications, arithmetic operation approximations, arithmetic expressions transformations, variable-to-constant substitutions, and loop transformations. The final evaluation resorting to a multi-objective strategy inherited from NSGA-II [24].

Looking at all those contributions, the design phase seems to be burden more by an excess of alternatives to build and test than by the issue of properly evaluating them. For this reason, more sophisticated approaches, based on the stochastic properties of the approximation error have been proposed.

In [25], readers can find a first attempt to model the approximation resorting to statistic. The goal is to reduce the impact of the analysis by exploiting a circuit level model that makes feasible to characterize different approximate circuits. To effectively model the approximation in each circuit, the paper introduces the concept of *error profile*. The error profile resembles how, given the data distribution, the approximation error is introduced on the output of the approximate circuit.

Similar approaches have been proposed in [26]–[28], where

specific implementations of hardware components, such as adders and multipliers are addressed. The basic idea is taking into account the different probability distributions of the input bits and evaluate the error distribution on the outcomes. All contributions point out that evaluating the error is faster than running several versions of approximation with data patterns to evaluate the accuracy. Nevertheless, since all papers do not consider scenarios in which sequences of heterogeneous approximate operations are performed, a full exploitation of the stochastic approach is still not possible.

The propagation of the error is modeled in the approach described in [29], [30]. In the paper, authors report a formalization of the error introduced by different implementations of approximate operators and try to model its propagation within the application. The clear advantage is that the approach does not require several executions of the applications because the outcome reports the error distribution, with the only limitation of having the formalization application dependent.

In a more recent paper, [31], authors propose an error statistics evaluation for block-based approximate adders. The contribution is interesting because of the good characterization methodology for a single component that relies on a complete enumeration of all possible output deviations and the evaluation of their occurrences. Along with the limited types of approximate components addressed, the methodology does not consider the cumulative effects of the error propagation.

All previous probabilistic approaches are limited by the assumption regarding the data distribution of the inputs of the application. For more insight regarding what happens when the data distribution differs from the expected one, the reader can refer to [32]. Authors propose a study of the stability of the approximate circuits when the circuit targets a particular data distribution but the final workload differs from it.

This limitation, together with the proof that a probabilistic approach can simplify the evaluation of the accuracy of approximate designs, is what makes a stochastic approach able to support the design of approximate systems, allowing the assessment of the overall application error in a faster and reliable way. The idea is eventually addressed by few papers in the recent years [33], [34].

In order to model the effect of an approximate operation on the application result, these papers propose a stochastic approach based on a Bayesian Network (BN) model. The BN mimic the application with nodes representing data and operators, and arcs following the data-flow. The network makes it possible to model the error propagation along the data-flow of the application by populating the node with a set of probabilities of reporting the error distribution out of single approximate components. Accuracy assessment can be eventually done by estimating the error distribution of the application exploiting the Bayesian inference theory. Results are reported for several applications in which the approximation is obtained by scaling the precision of hardware operations and data registers. The main advantages of a fully stochastic methodologies are the need of profiling the application only once to construct the model, as well as, characterizing the operators only once and to be able to easily change the input data distribution. Moreover, the methodology can effectively support the design exploration by giving an easy model to properly select the components of the application that might be worth approximate.

Finally, the design exploration can also take advantage of new metrics and strategies to select the components to be addressed by the approximation. Some very early and new research are exactly going in that direction [35]. The main idea is to anticipate the effect of the approximation by analyzing the data flow from the usage perspective, in order to further reduce the amount of different alternatives to be evaluated.

#### III. VERIFICATION PHASE

Determining the error of an approximate circuit or deciding whether an approximate circuit satisfies a given error constraint represent not only fundamental theoretical problems, but also highly practically relevant problems that must be routinely solved during the design of approximate circuits. While, at design time this task can be performed in an approximate way to support quick design space exploration, a precise analysis is required to verify that the final requirements of the system are met. A straightforward method to solve these problems is to use circuit simulation and estimate the error. If the exact error has to be determined then the circuit simulation has to be performed for all possible input vectors; however, this is applicable for small problem instances only. Hence, this section is focused on exact error analysis of approximate circuits by means of formal methods which are more scalable than circuit simulation in many cases. As arithmetic circuits frequently appear in the most popular error resilient applications (such deep learning and video processing), we focus on efficient exact error analysis of adders and multipliers. But the formal methods can be applied to effectively analyze errors of other combinational circuits (e.g., complex median networks [36]) as well as sequential systems [37].

Approximate implementations are usually created by (i) 'manual' modifications of exact circuits (see a detailed overview in [38]), (ii) developing new application-specific approximation schemes (see, e.g., new approximation techniques for FP multipliers [39]) or (iii) automated design space exploration algorithms [15], [19]. Fast and accurate error analysis is especially important in the case (iii) because the design space exploration methods sometime need to generate and evaluate millions of candidate design points.

#### A. Relaxed Equivalence Checking

Formal verification techniques that are widely adopted in the conventional circuit design flow are often based on *equivalence checking*, i.e., checking whether a mathematical model of a circuit under design meets a given specification. Two main approaches have been developed in this direction — techniques based on Reduced Ordered Binary Decision Diagrams (ROBDD) and satisfiability (SAT) solvers [40]. In both cases, an auxiliary circuit, the so-called *miter*, is constructed and then analyzed. Fig. 3(a) shows that the miter

instantiates both the candidate circuit F (to be checked) and the golden circuit  $\hat{F}$ , and compares their corresponding outputs to detect a difference in their behavior. In the context of approximate computing, we need to extend this concept to relaxed equivalence checking, by stressing the fact that the considered circuits will be checked to be equal up to some bound w.r.t. a suitably chosen distance (error) metric such as the worst case error and the average error. The (approximation) miter always contains an additional component enabling us to determine the error, see Fig. 3(b).

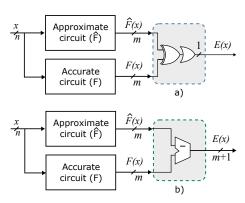


Fig. 3: Miter for equivalence checking (a) and arithmetic error analysis (b).

If the error analysis is performed using ROBDDs, a new ROBDD representing the miter is constructed by a procedure which reads the miter 'gate by gate' and adds appropriate nodes to ROBDD. ROBDDs can be directly used for the worst-case as well as the average-case analysis because every library for ROBDD manipulation is equipped with operations enabling us to address questions related to the satisfiability of the miter, namely finding one satisfying assignment and counting the number of satisfying assignments. The first operation provides a single input assignment x from the ONset of a Boolean function. The second operation computes the size of the ON-set. As ROBDDs are inefficient in representing classes of circuits for which the number of nodes in BDD is growing exponentially with the number of input variables (e.g., multipliers and dividers), their use in relaxed equivalence checking is typically possible for adders and other less structurally complex functions. Anyway, for example, 128 bit adders can be quickly analyzed in terms of all relevant error metrics [40].

If the error analysis is based on SAT solving, the miter is represented as a logic formula in Conjunctive Normal Form (CNF) for which SAT solver decides whether is satisfiable or unsatisfiable. The interpretation of this outcome depends on construction of the miter, see Section III-B. Common SAT solvers are, in principle, applicable to the worst-case analysis only. However, this approach is more scalable than ROBDDs for the error analysis of multipliers [19]. Specialized SAT solvers (#SAT) are capable of counting the number of satisfiable assignments, but their scalability is very limited and thus they are currently less practical for the exact error

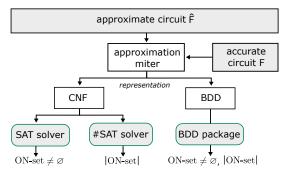


Fig. 4: Overview of formal error analysis approaches

analysis [40].

#### B. Worst Case Error Analysis

The worst-case error analysis is typically based on an iterative approach in which a variant of binary search is applied.

# Algorithm 1: Worst-case absolute error computation

Input: n-input approximation miter with m-bit signed output E in the two's complement Output: maximum absolute arithmetic error  $(e_{wce})$   $l \leftarrow 0; r \leftarrow 2^m - 1$  while  $l \leq r$  do  $t \leftarrow \lceil (l+r)/2 \rceil$  if WCEGT(E,t) then  $l \leftarrow t+1$  else

For computing the worst-case arithmetic error, for example, the miter given in Fig. 3(b) is used. Algorithm 1 illustrates the principle of determining the worst case arithmetic error, i.e. calculating the error magnitude at the m-bit output of the miter denoted as E. The principle of this procedure is to iteratively check whether the error is greater than a given threshold (denoted as t in the algorithm). The search procedure gradually narrows down the interval where the exact error value lies. After a finite number of steps, a single value is determined. As the binary search runs in logarithmic time with respect to the range, at most m comparisons are required. The checking can be ensured by means of the magnitude comparator which is used to form a Boolean function whose output is equal to 1 if and only if a given worst-case error  $\mathcal T$  is violated by the circuit under analysis.

WCEGT
$$(E, \mathcal{T}) = \exists_{x \in \mathbb{B}^n} |E(x)| > \mathcal{T}$$
  
= ON-set $\left( [\overline{e_m} \wedge (E > \mathcal{T})] \vee [e_m \wedge (\overline{E} > (\mathcal{T} - 1))] \right) \neq \emptyset$ .

Then, the satisfiability of this function can be investigated. An incremental SAT solver should be employed to mitigate a potential overhead caused by the necessity of constructing a different comparator in each iteration [40].

#### C. Average-case error analysis

Determining the average-case error represents a substantially harder problem because it requires the counting of the number of satisfiable assignments. For computing the average-case arithmetic error, for example, the same miter as in the previous case is used. The mean absolute error can be obtained by determining the error probability per each output bit. The obtained counts are then weighted according to the significance of the output bits and summed up. This is illustrated in Algorithm 2.

# Algorithm 2: Mean absolute error computation

```
Input: n-input approximation miter with m-bit signed output e in the two's complement, i.e. E = 2^m e_m - \sum_{i=0}^{m-1} 2^i e_i Output: mean absolute arithmetic error (e_{mae}) \varepsilon, c \leftarrow |\operatorname{ON-set}(e_m)| for i \in \{0, 1, \dots, m-1\} do if c > 0 then \varepsilon \leftarrow \varepsilon + 2^i |\operatorname{ON-set}(e_i \oplus e_m)| else \varepsilon \leftarrow \varepsilon + 2^i |\operatorname{ON-set}(e_i)| return 2^{-n}\varepsilon;
```

#### D. Comparison

Detailed analysis of relaxed equivalence checking algorithms has recently been performed in [40]. The analysis revealed that the computational complexity of the SAT-based methods heavily depends on the actual worst-case error. The computational time increases with a decreasing error, which is noticeable especially on multipliers. For example, tens of milliseconds are needed to analyze the 12-bit multipliers having the error higher than 2.7%. On the other hand, higher tens of seconds are needed for instances having the error in the range (0.37%, 2.71%] and no result was obtained for multipliers having the worst-case error below 0.05%.

Figure 5 shows the computational requirements of the WCEGT procedure (i.e. worst-case error checking) for five different thresholds applied to 8-bit multipliers. The worstcase error checking is extremely fast (few milliseconds are required) but only if the actual WCE is higher than a given threshold  $\mathcal{T}$ . If this condition is violated, the CPU time may increase by several orders of magnitude. Surprisingly, the difference between the worst case and the best case CPU time increases with decreasing the threshold  $\mathcal{T}$ . Performing WCEGT for thresholds below 1.5\% represents the most difficult case. Up to 100 seconds are required to analyze the circuit instances whose WCE is lower than the chosen threshold. Considering this fact, the design of multiplier-based approximate circuits with low error will be a challenging task because the checking will represent the bottleneck of the whole design process.

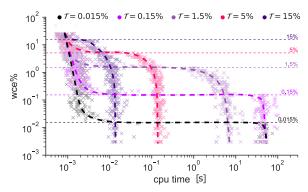


Fig. 5: The computational requirements of the WCEGT procedure proving that  $e_{wce} > \mathcal{T}$  of 8-bit approximate multipliers taken from EvoApprox library.

#### IV. TESTING PHASE

The application of approximate computing at hardware level results in systems widely referred to as Approximate Integrated Circuits (AxICs). An extensively used method to design those circuits is functional approximation of conventional integrated circuits [41]. This section focuses specifically on the testing aspects of functionally approximate circuits. Indeed, since approximation changes the functional behavior of circuits, techniques to test them must be revisited. As a matter of fact, extending the basic testing concepts to AxICs is not straightforward. In particular, during the test of a conventional circuit, any change in its functional output signals with respect to the expected values leads to labeling the circuit as faulty, and discarding it. When moving to AxICs, the presence of a fault may lead the circuit to behave differently than expected, yet still in an acceptable manner. In this case the circuit should not be discarded. Mastering these mechanisms may lead to increase the production process yield.

This section presents a whole new test flow - called Approximation-Aware (AxA) test flow – to deal with such aspects. It is the result of several contributions in the last years [42]–[51]. The flow is composed of three main steps: (i) AxA fault classification, (ii) AxA test pattern generation and (iii) AxA test set application. Briefly, the fault classification divides faults producing catastrophic effects on the circuit behavior from those producing acceptable effects. The test pattern generation produces test stimuli able to cover all the catastrophic faults and, at the same time, to leave acceptable faults undetected, as much as possible. Finally, the test set application labels AxICs under test as catastrophically faulty, acceptably faulty, or fault-free. Only AxICs falling into the first group will be discarded, thus minimizing overtesting (i.e., minimizing AxICs discarded due to acceptable faults). Next subsections describe each AxA test step.

## A. AxA fault classification

The first step of the AxA testing is the *fault classification*. It aims at separating acceptable faults from catastrophic ones. Moreover, fault classification establishes the *expected yield* 

increase of the AxA testing w.r.t. conventional test. Measuring the output deviations of AxICs is a crucial task for a successful classification. Different error metrics have been proposed in the literature to measure AxIC output deviations [52]. In [49], we showed that the classification task complexity drastically changes depending on the considered error metric. We showed that some metrics – referred to as *Single Condition Test (SCT) metrics* – entail a smaller effort for the fault classification compared to metrics based on the calculation of a mean – referred to as *Mean Error (ME) metrics*.

In [46], [49] we presented two fault classification techniques to address respectively SCT and ME metrics. Both techniques are based on the idea of masking acceptable fault effects by using a filter. Specifically, both the netlists of the AxIC under test and of the original precise circuit are embedded in a *classifying architecture*, along with the filter. For a given fault, the so-obtained architecture produces an anomaly only if the fault leads to catastrophic output deviations. In this way, by using conventional test approaches, it is finally possible to distinguish catastrophic faults from acceptable ones. The classifying architecture is never manufactured. It is only used in simulation to classify faults. Furthermore, the technique proposed in [46] entailed drastically reduced times compared to other state-of-the-art techniques [53], [54].

#### B. AxA test pattern generation

The second step of the AxA testing is the *test pattern generation*. In the context of AxICs, test patterns must cover all catastrophic faults and as few as possible acceptable ones. Respecting both these conditions is crucial to discard AxICs affected by catastrophic defects and, at the same time, to avoid discarding those affected by acceptable defects. Since state-of-the-art techniques [53], [54] do not focus on minimizing detected acceptable faults, in [50] we presented the first technique to suitably address the AxA test pattern generation.

This novel technique relies on a new engine capable of finding, among a set of input vectors, the smallest subset covering all the catastrophic faults and minimizing the acceptable fault coverage. Specifically, the engine generates an input vector set  $\mathcal S$  and measures its catastrophic fault coverage as well as its acceptable fault coverage. Hence, it finds within  $\mathcal S$  the optimal subset  $\mathcal V$  which attains the required goals. To accomplish this task, the engine formulates and resolves an *Integer Linear Programming (ILP)* optimization problem, whose solution is the final ax-aware test set.

Experimental outcomes achieved with the proposed technique showed an improvement spanning from 16% to 49% compared to state-of-the-art techniques. Although the achieved results are quite good, the ideal outcomes (i.e., 100% covered catastrophic faults and 0% covered acceptable faults) were still quite far from being attained. Therefore, we dedicated further efforts to effectively test AxICs, as shown in next subsection.

# C. AxA test set application

To push further the test outcomes, the third step of AxA testing, the *test pattern application*, comes into play. In this

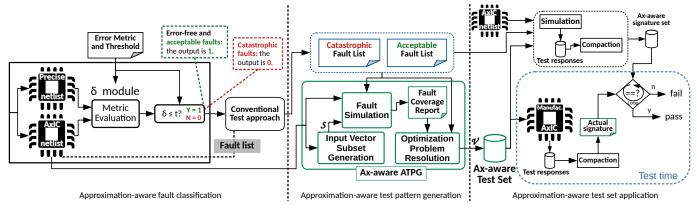


Fig. 6: Approximation-Aware (AxA) test flow

regard, in [51] we presented the AxA test set application technique. Since often it is not possible to avoid detecting acceptable faults, the basic idea is to verify, after the test application, whether the detected fault was acceptable or not.

The proposed technique is based on the well-know *signature analysis* concept, successfully applied to built-in self-test (BIST) architectures in the seventies [55] and still used in modern BIST architectures. The conventional signature analysis approach compacts test responses of a fault-free circuit into a *golden signature* (i.e., the reference behavior). In the test phase, the test responses of the circuit under test are compacted together into a signature (i.e., the actual behavior). Hence, the latter is compared with the golden one. If the two signatures are identical, the circuit under test is considered fault-free; otherwise, a malfunction is detected.

We drew inspiration from the signature analysis and proposed a technique divided into two steps:

At design time, we perform a fault simulation by using test patterns and the AxIC's faults. For each fault, we compact simulation responses into a signature. We obtain acceptable and catastrophic signatures. We remove from acceptable signatures those overlapping with catastrophic ones, thus ending up having an *ax-aware signature set*.

At test time, manufactured AxIC test responses are compacted into a signature and compared with the ones in the ax-aware signature set. If there is at least one match, then the AxIC is considered acceptable. Otherwise, the circuit is rejected.

The proposed technique is intended to be used for external test, i.e., test are applied by using an Automatic Test Equipment (ATE). Of course, it can be also adapted to a BIST context.

Results obtained with the proposed technique were excellent. Indeed, they showed yield gain results very close to the expected ones (i.e., 99.84% of the expectations, on average). In terms of covered faults, the technique delivered 100% covered catastrophic faults and 0.16% covered acceptable faults on average, that are very close to the ideal ones (i.e., 100% covered catastrophic faults and 0% covered acceptable faults).

#### V. IN-FIELD

As described before, Approximate Computing techniques have been positively introduced thanks to the intrinsic resilience of many applications [56]; as a collateral resiliency effect, it could be also stated that a resilient application is able to provide good enough outputs (i.e., acceptable) despite of the presence of hardware faults.

As initially presented in [57], here we describe how Approximate Computing can positively impact the intrinsic circuits' resilience by exploiting the fact that faulty circuits can be seen as approximate ones.

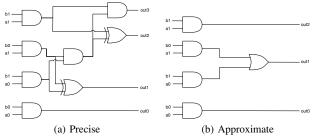


Fig. 7: Functional Approximation Example

Let us consider the accurate and approximate implementations of a 2-bit multiplier shown in Figure 7 when the given circuits are affected by a Stuck-at Fault (SaF). Due to the fault f, the 2-bit multiplier can provide wrong output values. Similarly to approximate circuits, it is possible to quantify the precision of the circuit in terms of  $WCE_f$ . The only difference, is that in our case the wrong values are not due to an approximation technique but induced by hardware fault f. If  $WCE_f \leq WCE_{tr}$  the application is still able to provide good enough results (despite the presence of f), otherwise the application results cannot be accepted due to f.

The fault universe  $F_u$  can be thus divided in two subsets:

- 1)  $F_b: \forall f_{bi} \in F_t \to WCE_{f_{bi}} \leq WCE_{tr}$
- 2)  $F_m: \forall f_{mi} \in F_c \to WCE_{f_{mi}} > WCE_{tr}$

Where  $F_b$  is the set of *Benign* Faults corresponding to faults that can be tolerated by the application,  $F_m$  is the set of *Malignant* Faults corresponding to faults that are critical because

they cannot be tolerated by the application. A methodology able to classify faults in to the two sets have been presented in [46]. Results are gathered in Table I.

TABLE I: Benign and Malignant Faults

| Circuit | $\#F_b$ | $\#F_m$ | #Tests |
|---------|---------|---------|--------|
| Precise | 25      | 23      | 4      |
| AxC     | 23      | 7       | 3      |

From the results shown in Table I, we can see that only 23 SaFs are included in the Malignant Faults set  $F_m$  in the case of precise multiplier (Fig. 7a). In other words, the circuit shown a WCE lower than  $WCE_{tr}=2$  for about half of the faults, and in the case one of these errors appear, it is possible to guarantee that the faulty circuit will work as an approximate one. Considering the approximate multiplier, it is possible to see that only 7 faults belong to the malignant fault set. On the other hand, it is important to highlight that malignant faults may impacts other metrics such as the Bit Error Rare (BER). A designer has therefore to consider more than one metrics and, most important, evaluate the benign fault impacts at application-level (see Section V-A).

Let us now follow an approach similar to [46] in order to determine whether a faulty circuit can be really used as approximate. The goal is to determine the set of benign faults when considering WCE as quality metric. In other words, we aim at investigating how many hardware faults can be tolerated by the application when a given error metric (i.e., WCE) is considered.

The whole process is composed of two steps:

- Off-line Step: it aims at identifying Malignant Faults, and Benign Faults whan a given WCE is considered as threshold. Additionally, test vectors are generated in order to test for the malignant faults only.
- On-line Step: it aims at applying the test vectors covering Malignant Faults. In the case the circuit is affected by one of these faults, it is not possible to accept the results since the WCE is higher than the permitted one. On the contrary (i.e., benign faults), the effect is close to a "graceful degradation", and the results can be simply considered as approximated.

We analyzed seven widely used 8-bit precise adders synthesized with an industrial 65nm technology library. More in detail we used the Ripple Carry (RippCarry); Carry Select (CarrySel); Higher Valency Tree Adder with HanCarlson Architecture (HVTrHCA); Higher Valency Tree Adder with Kogge-Stone Architecture (HVTrKSA); Carry Lookahead (CarryLKH); Tree Adder with Kogge-Stone Architecture (TwKSA); Tree Adder with HanCarlson Architecture (TwHCA).

Moreover, we also approximate the above adders by using the following techniques:

• **Precision Reduction**: the approximate adder is simply obtained by setting to '0' (cutting) the four LSBs of each operand. The impact of this technique to the adder quality is quantified by WCE = 15. It is important to mention that

- by using the precision reduction the circuit netlist is not modified. Therefore the number of faults does not change w.r.t. the precise adder;
- Functional Approximation: the circuit netlist is modified. For our experiments, we resort to the public available library from [58]. Among the approximate adders of that library, we selected those having the same "level of approximation" quantified by WCE = 15.

Table II summarizes the obtained results. For the case of precise adders, we reported the percentage of Malignant Faults (MF) and the related Test Vectors number (TV) accordingly to the adders version: the Precise implementation and the approximation obtained with precision reduction (4 LSB truncated (TR4)). Finally, the last 6 columns depict the results obtained when considering functional approximate adders.

From the table, it is easy to observe that the ratio of Malignant Faults is reduced when moving from the precise to the approximate circuits. Interestingly, malignant faults (and consequently the test vectors number) have drastically reduced for two approximate adders (the Add\_025 and Add\_40). This means that by carefully selecting the approximation technique is possible to achieve meaningful results in terms of malignant faults and test time reduction. Those approximate adders have been generated exploiting a genetic algorithm. We thus intend to further investigate the possibility to add the reduction of malignant faults and test vectors as objectives to be maximized during the generation. In other words the ultimate goal would be the generation of more 'resilient' approximate adders.





(a) PR: SSIM = 0.904982

(b) Add23: SSIM = 0.996768

Fig. 8: Accuracy results obtained at application-level.

Obtained results are quite interesting and seem to prove the efficiency of the idea. However, to further investigate the possibility to leverage faulty circuits as approximate ones, we present a case study based on a real application.

#### A. Video Coding Application

Nova is a low-power real-time H.264 Advanced Video Coding designed for mobile devices. The Nova source code is available at [59]. In our experiment, we resort to functional approximation. We modify the Nova source code by replacing existing adders with the ones (both precise and approximate) presented in the previous section. We thus obtain several Nova implementations (each one characterized by the use of a specific adder). For each implementation, a simulation-based fault injection campaign have been performed. Injected faults are Stuck-at-Faults (SaF). For each SaF, the Nova outputs have been checked and compared to the fault free execution.

TABLE II: Malignant Fault and Test Vectors

|           | Version |    |        | Add 012 |         | Add 013 |         | Add 016 |         | Add 023 |         | Add 025 |         | Add 40 |        |    |
|-----------|---------|----|--------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--------|--------|----|
| Circuit   | Precise |    | TR4    |         | Auu_012 |         | Auu_013 |         | Auu_010 |         | Auu_023 |         | Auu_023 |        | Auu_40 |    |
|           | MF      | TV | MF     | TV      | MF      | TV      | MF      | TV      | MF      | TV      | MF      | TV      | MF      | TV     | MF     | TV |
| CarryLKH  | 82.86%  | 41 | 65.31% | 28      | 90.29%  | 18      | 50.00%  | 4       | 80.77%  | 6       | 50.00%  | 4       | 99.21%  | 13     | 45.65% | 5  |
| CarrySel  | 78.05%  | 16 | 78.05% | 15      |         |         |         |         |         |         |         |         |         |        |        |    |
| HVTrHCA   | 72.09%  | 19 | 61.24% | 14      |         |         |         |         |         |         |         |         |         |        |        |    |
| HVTrKSA   | 86.44%  | 24 | 67.51% | 19      |         |         |         |         |         |         |         |         |         |        |        |    |
| RippCarry | 53.85%  | 7  | 53.85% | 7       |         |         |         |         |         |         |         |         |         |        |        |    |
| TwHCA     | 71.74%  | 19 | 65.22% | 18      |         |         |         |         |         |         |         |         |         |        |        |    |
| TwKSA     | 85.45%  | 27 | 67.58% | 17      |         |         |         |         |         |         |         |         |         |        |        |    |



Fig. 9: Mispredicted Faults

Injected SaFs are the malignant and benign faults identified by the methodology described in the previous section. Input videos have been downloaded from [60].

In the first part of the experiments, we quantify the application-level accuracy when approximate adders are used. The application accuracy is measured by using the Structural SIMilarity (SSIM) index [61]. Please note that for the case of videos, the SSIM is determined for each frame (each image). The global SSIM is then computed as the average over the frames. Figure 8 shown an example of videos obtained when using adders approximated by the Precision Reduction (PR) technique and adders approximated by using Functional Approximation (Add23). From Fig. 8, it is clear that the worst quality is obtained when Precision Reduction is used. The SSIM is reported in the caption.

In the second part of the experiments, we perform fault injection campaign. Fig. 9 reports a video screenshot obtained when injecting a 'benign' fault in the Add23. The fault leads to obtain a SSIM of 0.95. From the picture, it is clear that the quality of the video is too much degraded despite of the fault has been classified as benign and thus the application was supposed to be able to tolerate it. This is an example of wrong classification of a fault. The reason behind faults miss-classification is related to the fact the metrics other than WCE have not been considered. In our example, the injected fault is benign w.r.t WCE because it leads to a WCE < 15. Unfortunately, the impact of the same fault to other metrics, such as bit error rate was too high. The conclusion is that the application and applied workload have to be considered during the process in order to avoid miss-predicted faults. On the other hand, the precise adders behave much better than the approximate ones, meaning that these adders can be used as an excellent approximate one when benign faults appear. This clearly demonstrates that approximation can be really used to improve the system lifetime.

#### VI. CONCLUSIONS

This tutorial paper presented an overview of different approaches to handle the design, verification, testing and infield operation of approximate computing systems. The presented solutions are not exhaustive and new publications and approaches will appear while the field becomes mature. The paper leverages on the experience of the authors to overview the major challenges that still represent a barrier to transform this interesting research field into real solutions ready to the market.

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