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Filter Transients onboard DC Rolling Stock and Exploitation for the Estimate of the Line Impedance

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Abstract—Power supply transients in dc railways related to filter charging may trigger network and filter oscillatory responses, as well as cause very fast voltage spikes. These phenomena are relevant not only for Power Quality and EMC, but also for their impact on the measured pantograph quantities e.g. for power and energy consumption estimate. The broadband excitation of the system gives the possibility of attempting the identification of the network impedance. The experimental results are discussed and compared to the output of a circuit and a distributed parameter simulator. Matching between simulated and experimental data is very good.

Keywords—Harmonics, Power Quality, Power supply transient, Railways, Rolling stock

I. INTRODUCTION

Power Quality (PQ) in railways has been investigated from different standpoints: line voltage distortion coupled to other trains connected to the same line section or reflected back on the utility side [1]-[3]; current harmonics interfering with signaling and telecommunications [4]-[6]. Considering rolling stock and in a normative perspective, harmonics and distortion may affect the line voltage [7] or have impact also on the power and energy consumption assessment, both as an external unwanted interference [8] or as a contributing factor [9]. For DC vehicles harmonic active power was found to be negligible [9], although transients may disturb and alter the measured pantograph electrical quantities.

This work has as first objective the electrical characterization of the transients caused by the charging of the on-board filter of a dc locomotive. Transients for a dc vehicle originate at the sliding contact mechanism by electric arcs [12]-[14] or may be caused by the switching of onboard loads, including the case of a nearby train. Any electric transient with a broad frequency spectrum can excite the resonance modes of the system, thus triggering oscillations at a lower frequency, that can couple onto the measuring systems. Such oscillations and transients further worsen the stationarity of the signals associated to the line electrical quantities and weaken the conditions for the applicability of standardized Fourier-based processing methods [15].

The second objective is the investigation of the possibility

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of exploiting such transients as probing signals for a passive identification of the network impedance (i.e. the traction line impedance). The knowledge of the network impedance is beneficial for a more accurate estimate of harmonic distortion and the identification of disturbing loads, but also for network stability, harmonic resonance and prevention of oscillations [16][17].

The problem has already been considered for smart grids [18]-[21], using both active and passive methods: active methods inject a specific pilot signal to probe actively the network impedance; passive methods exploit existing measured quantities, passively listening to the network. A well-promising approach for passive methods is the use of advanced techniques for model identification (Least Mean Squares, recursive minimization, Kalman filter, etc.), but so far the adopted models are of the R-L type and neglect the effect of stray capacitance, with justifications that cannot be applied to railways and rapid transit systems.

The work is structured as follows: Section II contains an introduction to the problem of network modeling and network impedance identification, considering the approaches used in smart grids and distribution networks, and then focusing on railway networks and the interaction between the network and the locomotive; the results shown in Section III consist of the explanation of the observed electrical phenomena and interactions, and a preliminary estimate of the traction line impedance.

II. NETWORK MODEL AND NETWORK IMPEDANCE ESTIMATE

A. General method

The general method is based on the estimate of the load and/or network impedance exploiting two (or more) measurements of voltage and current at the pantograph (indicated with V_p and I_p) carried out under different supply conditions. In other words the flowing current I_p is measured after an ideally instantaneous change of the supply voltage. This method has been extensively applied to smart grids [18]-[22], with the following basic equations that assume a reference state and a perturbed state, e.g. by means of the inclusion/exclusion of a series-connected lumped element or ideally varying the network voltage supply.

The reference circuit is shown in Fig. 1, where the load (the train) is considered with its Norton equivalent circuit. The dashed resistance R_a represents the switched lumped component suggested for application in distribution networks and smart grids, as well as the electric arc resistance, where electric arcs might be exploited as a driving event in a future development.

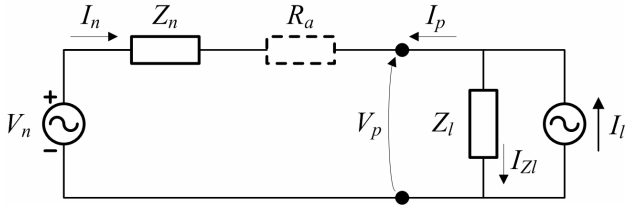


Fig. 1. Equivalent circuit for the supply network and rolling stock with electric arc occurring at the sliding contact (the resistance $R_a=0$ when the electric contact is perfect and no detachment occurs).

The basic equations are:

$$I_p = I_l - I_{Zl} \quad I_{Zl} = \frac{V_p}{Z_l} \quad (1)$$

The two equations must be written for each of the two states of the network, that is before and after the voltage change, with the quantities that vary identified with a prime and a double prime. Then replacing I_{Zl} and solving for Z_l , and then focusing on I_p , it is possible to achieve two explicit expressions in terms of measured pantograph quantities only:

$$Z_l = \frac{V_p' - V_p''}{I_p' - I_p''} \quad I_l = I_p' + \frac{V_p'}{Z_l} \quad (2)$$

No similar closed-form expressions are available for the network impedance estimation, although in cases where the Norton impedance Z_l is much larger than the network impedance Z_n , then Z_n is readily given by V_p/I_p for those frequencies at which the network generation V_n may be passivated. The condition for passivation of the generator is that the network is not a source of significant voltage at a given frequency (e.g. choosing components different from the characteristic harmonics of the substation). Also in case of a moderately large Z_l , then the Z_n can be calculated back from the electrical parallel of the two with an acceptable error. Considering $v_p(t)$ and $i_p(t)$, and the cross-spectrum $G_{vi}(f)$ and auto-spectrum $G_{ii}(f)$, a convenient way to express Z_n is as the ratio of the two (holding the conditions on Z_l).

The Welch method is used for the calculation of the auto-spectrum and cross-spectrum.

B. Other models

As anticipated in the introduction, parametric methods make use of a reference model on which an optimization or identification algorithm is run. In [20] the Kalman filter is a well founded approach, but the model is simplistic from two standpoints: the network is only resistive-inductive (RL series connection) and the selected state variables track only the fundamental and two harmonics (whereas we know that dc and ac railway systems feature complex spectra for the electrical quantities at the pantograph [23][24]).

The approach used in [19] makes direct use of the network model as in Fig. 1, relying on a redundant (overdetermined) set of equations (1 to n) to solve using an iterative technique. However, the main assumption is that the network is stationary, i.e. the configuration and generation do not change during the measurement.

Apparently a solution to the specific problem has been proposed very recently [25]. However, the focus is on an ac railway using an active probing method, i.e. injecting test signals by suitably driving the on-board four-quadrant converter as large-power waveform generator. This solution was already adopted for tests carried out with FLIRT trains with the permit of the operator and by modifying the

software of the on-board converter (so, not an easy task), as documented in [26].

C. Application to DC railways

As a preliminary work on this topic, the approach is phenomenological, focusing on the electric behavior of the subsystems, the quality of the signals, and plausibility of the results. To this aim the signals are mostly studied in the time domain using a reference simulation model for confirmation. The measuring setup was preliminarily described in [27][28]: although the uncertainty assessment has not been completed yet, the used instrumentation and the care in grounding, shielding and EMC in general during the installation indicate that the uncertainty will be dominated by the voltage and current probes.

The simulation model must be fed with accurate estimates of the parameters to represent the real behavior of the line:

- it is known that using a few lumped parameters cells to model a distributed parameter system has a fitness error that increases with frequency and is particularly large at resonances and anti-resonances; stopping the reasoning to the first line resonance for a preliminary assessment allows the satisfactory use of a model with only two pi cells [5];
- lumped loads represented by the other trains in the same supply section or in the adjacent sections can modify the line response, especially introducing additional damping at line resonances and in general slightly shifting line resonances due to the reactive elements onboard.

In the high-voltage input stage of the E464 locomotive shown in Fig. 2 the following elements can be recognized: the main circuit breaker (of the HSCB type, High-Speed Circuit Breaker, for dc applications), the second-order LC resonant filter (with the capacitance contributed mainly by the traction converters, but also at a lesser extent by the connected auxiliaries) and the charging system. The switch-gear section is composed of the main circuit breaker and of an additional parallel-connected branch, with a contactor and the charging resistor R_{ch} with a nominal value of 52 Ω .

Before closing the main HSCB supplying the locomotive, the input stage is configured to perform a pre-charge of the filter capacitors C_{filt_m} (the capacitors inside the traction converters) and C_{filt_a} (the capacitors inside the auxiliary converters) through the resistor R_{ch} . During the pre-charge the line current is absorbed from the catenary and delivered to the capacitors through the resistor R_{ch} and the filter inductor L_{filt} of 8.5 mH. After 0.8 s, the voltage across the capacitor bank (made of the parallel-connected capacitors) reaches a given percentage of the line voltage, sufficient to conclude the charging operation more quickly through the main HSCB, closing it to by-pass the charging resistor. A smaller current impulse is then absorbed by the capacitor bank, where the limiting elements are the filter inductor L_{filt} and the line impedance Z_p . The equivalent RLC series circuit that during pre-charge was over-damped thanks to the R_{ch} resistor becomes under-damped after the closing of the main HSCB, giving rise to visible oscillations (the only relevant resistive element contributing to damping being the supply line resistance).

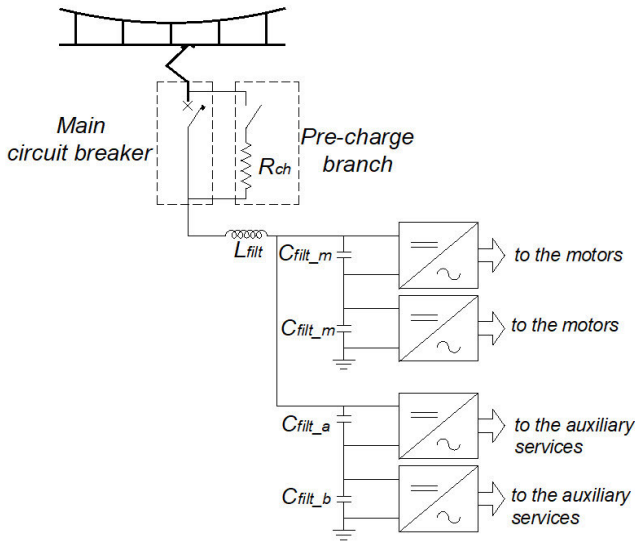


Fig. 2. Electrical scheme of the E464 locomotive, showing the onboard LC filter, the main circuit breaker and the pre-charging circuit with the limiting resistor R_{ch} .

III. RESULTS

This section shows first the behavior of the filter charging transient associated to the circuit and procedure described in sec. II.C above (see Fig. 3). The observed electrical phenomena are explained, using the information of the supply and traction line models. The spectrum characteristics, the time duration, etc. are considered for their impact on Power Quality and on the connected measuring systems.

In the second part, then, portions of the measured waveforms are used to estimate the network impedance, verifying the quality of the so obtained estimate in terms of density of points on the frequency axis, noise and noise suppression capability, etc.

A. Phenomenological analysis

The two transients following the two switching events shown in Fig. 3 may be explained with a little insight into the behavior of the circuit. To start the charging of the filter capacitor, the pantograph is raised against the catenary using a series resistor R_{ch} for protection purposes, limiting the inrush current into the capacitor bank through the filter inductor. The rate of rise of the current through the inductor is quite large anyway and excites the line resonance.

The steep edge of the current I_p is visible in Fig. 3(b) lasting for about $80 \mu\text{s}$ and reaching a value of 32.6 A . This corresponds to a 3800 V line voltage that charges an inductor of 8.5 mH , resulting in a rate of rise of 447 kA/s , that after the said $80 \mu\text{s}$ gives 36 A . This first part of the rising exponential is able to excite the line resonance, resulting in a quick reduction of the pantograph voltage (the negative voltage spike); more accurately the tip of the spike occurs after $20 \mu\text{s}$, when the current is less than 10 A . It is briefly observed that a higher sampling rate is needed to better follow the evolution of the signal, when higher-order modes are excited: some recordings at a 5 or 10 times higher sampling rate are scheduled for the next test campaign.

The slower transient occurring when the charging resistor is bypassed at 2.34 s in Fig. 3(c) shows the damped oscillation of the onboard filter.

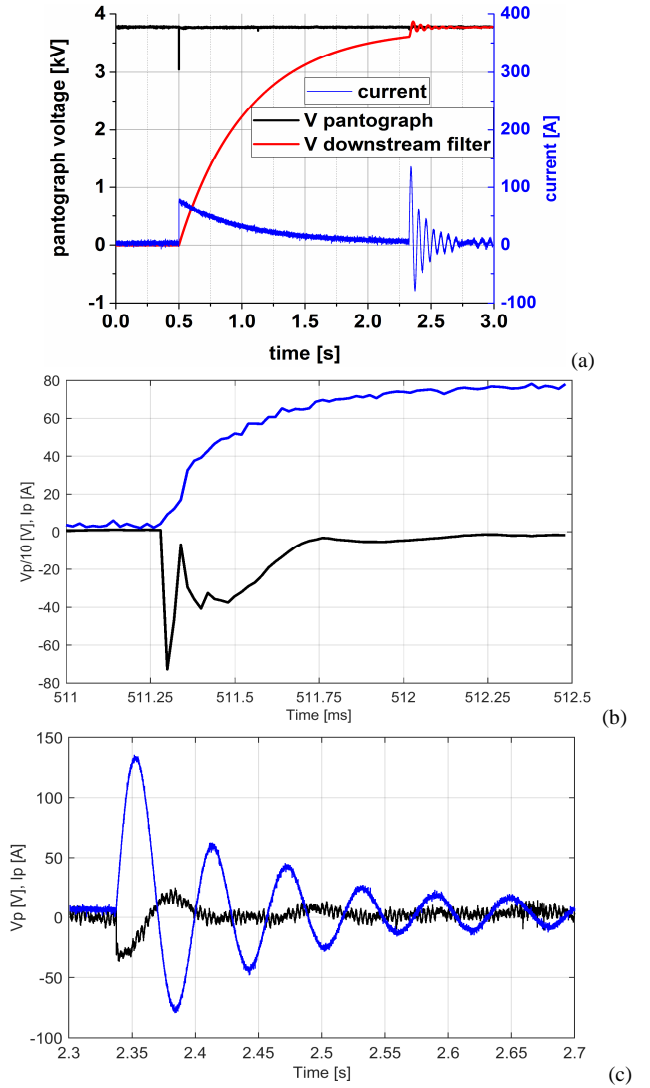


Fig. 3. Measured waveforms of pantograph voltage V_p , pantograph current I_p and capacitor voltage downstream of filter V_f : (a) overall screenshot of the relevant time interval, (b) zoom of the first insertion with resistor R_{ch} , (c) zoom of the residual oscillation when the resistor R_{ch} is bypassed.

Two points should be observed:

- the current I_p flowing in the filter is oscillating around zero; the negative portions of the current cannot in principle be absorbed back by the substation that consist of rectifier groups with all the diodes showing their cathodes facing the catenary; in reality, with a bias current flowing to supply other trains along the line, the diodes simply will see their current modulated by the oscillating charging current, with a dynamic resistance that is approximately constant if the charging current intensity is small compared to the current feeding the other trains (some other experimental results confirm that this situation may degenerate in low-traffic situations, when the supply section is not or lightly loaded);
- the oscillation has not a constant frequency: a closer look shows that the positive half-periods are slight but consistently longer than the negative ones (the measured intervals are 29.6 , 32.9 and 32.1 ms for the positive half-periods, and 28.8 , 27.4 and 27.2 ms for the negative ones); this is a symptom of a non-linear characteristic that might be explained with the behavior of the substation diodes when the sourced current is very low. Variability was analyzed by parametric simulation, changing the load current biasing the substation diodes.

The experimental curves of Fig. 3 allow also a preliminary evaluation of the impact caused by the transients triggered by the charging operation: the duration of the oscillation is in the order of 0.5 s, its frequency is the resonant frequency of the onboard filter, usually between 15 and 22 Hz for the known implementations. The same phenomenon occurs whenever the traction demand is discontinued, e.g releasing the throttle during an intense acceleration, and it is a known problem for many out of scale readings of connected instruments.

The line resonance peak location and height depends on many factors, beside the geometrical and per-unit-length electrical parameters of the line: first of all the length of the line between the two adjacent substations and the presence of other trains in the same section, loading the line and reducing the factor of merit of the resonance. The curves of Fig. 4 show the variability of the network impedance at the pantograph Z_p for a train moving along the line of 25 km length between two substations. The first and second resonances are located at 5.8 kHz and 11.7 kHz with a peak height between 400 and 4000 Ω for the first and between 800 and 2000 Ω for the second resonance. The height of the successive peaks is further reduced since the damping is quite large. The line voltage is quickly excited by the high-order resonances at the limit of the sampling time and beneath it (50 kHz), then the profile in Fig. 3(b) around 511.5 ms shows a damped oscillation at a lower frequency, compatible with the first resonance. The negative spike reaches -750 V and it is thus not dangerous in terms of overvoltage, but it is the byproduct of the broadband excitation of line resonances.

Observing the results in Fig. 5 the simulated current profile is quite well matched with the experimental one. However, the simulation model makes some approximations regarding the equivalent circuit for the substation rectifier and does not include a complete model for nearby trains, replaced by an equivalent loading resistor. The voltage profile is well matched for the initial high-frequency part, but the subsequent low-frequency damped oscillation needs some additional work.

B. Identification of the network impedance

The transient signals at the beginning of the charging operation (time 0.5 s in Fig. 3(b)) have been extracted for the calculation of the auto- and cross-spectrum. The procedure is complicated because of the limited number of samples (47) and the large amount of noise. The frequency resolution has been improved using interpolation; the noise is reduced by the averaging implicit in the Welch method.

The Welch method has unavoidably a lower frequency resolution than DFT, although the latter is a bad choice due to excessive spectral leakage, when processing signals with an underlying exponential damping component. In addition, spectrum estimation algorithms have in general better incoherent noise suppression than DFT.

The curve shown in Fig. 6 is affected by a large uncertainty due to the small number of original points, the averaging for the auto- and cross-spectrum estimates and the successive interpolation. However, it is very close to the one simulated in Fig. 4 for a line of $L=25$ km and train positioned at $x=0.1L$ (2.5 km) from the substation (confirmed by the annotations during the tests).

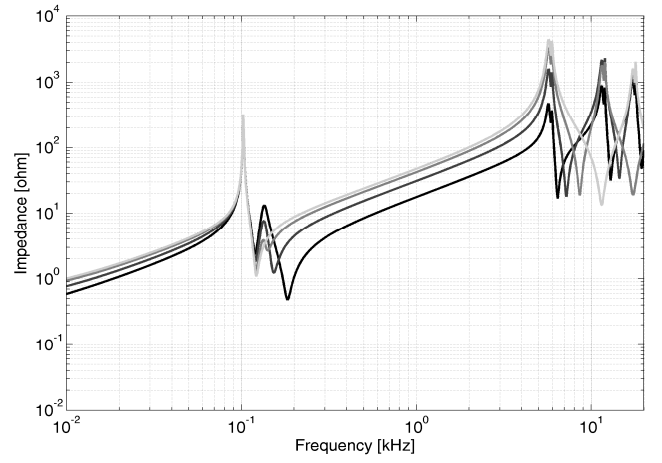


Fig. 4. Network impedance at the pantograph (Z_p) for $L = 30$ km of separation between ESSs and four train positions (from black to light grey) $x=0.1, 0.2, 0.33, 0.5 L$ [10].

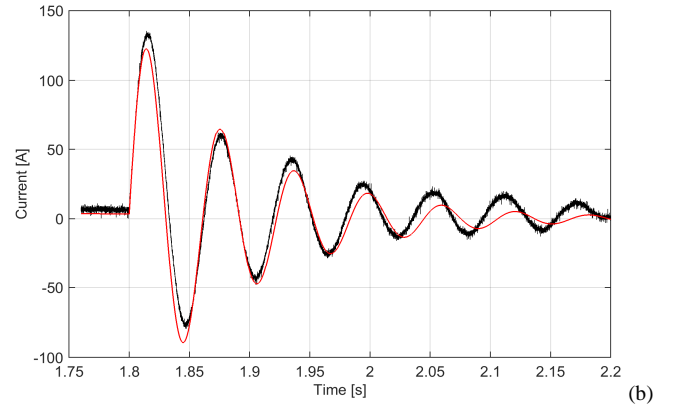
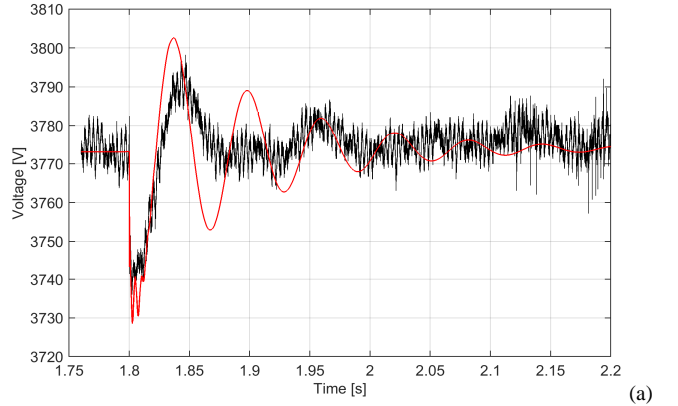


Fig. 5. Comparison of simulated (red) and measured (black) waveforms for (a) pantograph voltage V_p and (b) pantograph current I_p with fictitious line loading of 380 A.

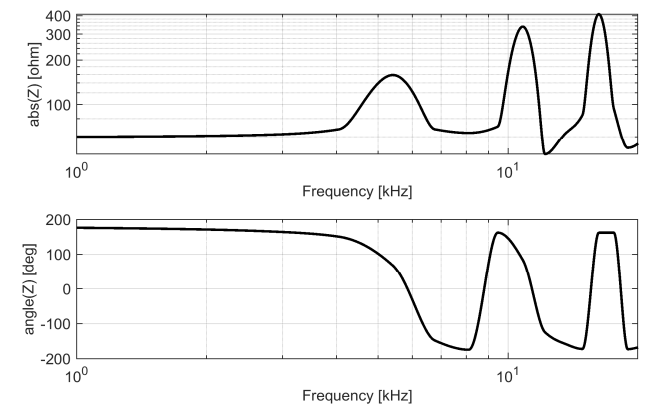


Fig. 6. Identified network impedance Z_n after calculation of cross- and auto-spectrum, ratio, compensation of the electric parallel with the onboard filter, and interpolation to visually improve frequency resolution.

IV. CONCLUSION

This work has considered the problem of the identification of the network impedance for electrified railways, making a comparison to existing techniques for smart grids. It turns out that several methods have been implemented using simplified models of the network or simplifying assumptions, which hardly hold for railways and rapid transit systems: the pantograph impedance varies with the train movement and also with the relative position of the other trains. The problem is also complicated by the large amount of noise that characterizes the measured pantograph quantities.

For these reasons a parametric method should be considered, using a reference model and feeding data extracted from the measurements. Presently, although preliminarily considered, no numeric technique or automatic identification algorithm is used: data and results have been analyzed using a phenomenological approach, to understand what are the exploitable characteristics of the signals, the typical transient responses and the limitations of the adopted approach.

Network impedance estimation for railways (including dc and ac systems), besides the many challenges, may benefit from the abundance of electric transients caused by filter charging, transformer inrush, onboard auxiliaries' commutation, electric arcs. This work has focused on the onboard filter inrush for a dc locomotive.

The simulation results match well the experimental data, for what regards the filter oscillatory current, whereas there is some discrepancy in the calculated line voltage, possibly due to the non-linearity of the substation. The non-linearity of the system has been demonstrated by observing the asymmetry of the measured sinusoidal oscillation of the filter current.

The observations on the first transient when the pantograph is raised and the filter is supplied through the charging resistor are in agreement with the expected system response and the estimate of the spike in the line voltage quite accurately correspond to the measured values.

Last, the estimated network impedance match well the simulated curve obtained by the distributed parameter simulator, although the procedure and the uncertainty related to the many non idealities must be confirmed: the number of sampled data during the transient is too low and the Welch algorithm is thus operating in non-ideal conditions. To this aim the necessity of a higher sampling rate for the next test campaign has already been discussed.

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