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Measuring Bipartite Quantum Correlations of an Unknown State

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We report the experimental measurement of bipartite quantum correlations of an unknown two-qubit state. Using a liquid state Nuclear Magnetic Resonance setup and employing geometric discord, we evaluate the quantum correlations of a state without resorting to prior knowledge of its density matrix. The method is applicable to any $2 \otimes d$ system and provides, in terms of number of measurements required, an advantage over full state tomography scaling with the dimension d of the unmeasured subsystem. The negativity of quantumness is measured as well for reference. We also observe the phenomenon of sudden transition of quantum correlations when local phase and amplitude damping channels are applied to the state.

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Introduction.—Quantum mechanics rules the physical world, but sometimes its effects can be elusive. In particular, entanglement [1], the genuinely quantum type of correlation shared by two parts of a composite system, is not directly measurable in the laboratory. Indeed, there is no self-adjoint operator quantifying the amount of entanglement of a state. Hence, an *a priori* knowledge of the density matrix appears necessary to evaluate entanglement. This is a serious drawback, since dealing with high dimensional systems makes the state reconstruction extremely demanding if not unfeasible in terms of required resources. The problem has been overcome by introducing nontrivial lower bounds to entanglement measures, expressed as nonlinear functions of the density matrix coefficients, whose values can be detected by means of a limited number of measurements [2,3].

However, it has been acknowledged that even separable (unentangled) mixed states show a distinctive nonclassical behavior, benchmarked by their *quantum discord* [4,5]. Arguably considered the most general form of quantum correlations, it quantifies the minimum induced disturbance on a state of a bipartite system when a local measurement is made on one subsystem. Currently, massive theoretical and experimental efforts are dedicated to discover the potential of such correlations for quantum information processing [6–15]. The reason is that discord has appealing properties: For pure states, it reduces to entanglement, while for mixed states, even unentangled states (apart from a subset of null measure) have nonvanishing discord [16]. A number of phenomenological investigations have proven discord to be easier to create and far more robust than entanglement under decoherent dynamics [17]. In spite of that, even if at the theoretical level a plethora of discordlike measures have been

introduced [6,18], and some discord witnesses have been implemented [19–21], the situation is similar to entanglement: There is not an observable quantity grasping the amount of such general quantum correlations in a state. One could try to recast a measure as a function of density matrix elements and therefore of observable quantities, but most known quantifiers are entropic and, thus, cannot be associated with observables. Taking into account distance-based measures offers a solution to such a conundrum.

In this Letter, following the theoretical proposal of Ref. [22], we report the experimental measurement of quantum correlations of unknown two-qubit states in a room-temperature NMR system [23–26]. In this setting, the information is stored in the nuclear spins, while transformations and state preparation are implemented by applying highly controllable radio frequency (rf) pulses, magnetic field gradients, and evolutions under spin interactions [27]. On the other hand, the environment affects the spin system by inducing relaxation that drives the system back to the thermal equilibrium distribution according to two independent characteristic times T_1, T_2 [25].

We pick primarily the geometric discord D_G as the quantifier of bipartite quantum correlations [28]. Its peculiarity is that it can be expressed, for arbitrary states of $2 \otimes d$ systems, as a state-independent function of the density matrix elements, and consequently in terms of observables [22,29]. In fact, there is no need to have full information on the state in order to measure geometric discord. We experimentally verify the theoretical results by preparing an unknown two-qubit Bell diagonal state (the choice of the state is due to experimental convenience exclusively) and retrieving the value of geometric discord by means of local measurements over one of the subsystems. Then, we investigate the robustness of quantum

correlations under phase damping and amplitude damping channels acting separately on each qubit. It is predicted that, by appropriately engineering the initial state, measures of discord should undergo a *sudden transition* in their dynamical evolution [30,31], exhibiting different regimes of resilience to decoherence under noisy conditions. We carry out a comprehensive analysis of general quantum correlations. We monitor in fact the evolution of geometric discord [28], of its lower bound defined in Ref. [22], as well as of the so-called negativity of quantumness [32] for the produced states (the latter measure, here investigated for the first time in open systems), linking the singularity in their expression with the discontinuity in the dynamics.

It is important to discuss the consistency of geometric discord D_G as a reliable estimator of quantum correlations. Recent works have shown that measures built on the Hilbert-Schmidt norm, as geometric discord is, can increase under local reversible operations on the unmeasured subsystem, being biased by the purity of the global state [33,34]. In spite of that, geometric discord is still a useful signature of quantum correlations in a number of relevant cases. For example, it can be legitimately used to investigate correlations between a system and environment in open quantum evolutions [35], which are globally unitary, thus leaving the purity unchanged. Even for a bipartite state under local decoherent evolutions, as studied in this Letter, the geometric discord reliably identifies the sudden transition point in the dynamics as well as other full-fledged measures of discord [4,30,31]. Specifically, for a system of two qubits (keeping the dimension fixed), as in our case, the problem highlighted in Ref. [33] cannot occur, and D_G admits moreover an operational interpretation in terms of fidelity of remote state preparation [11], while also bounding from above [36] the entanglement quantified by the negativity [37]. In general, D_G is a valid lower bound to measures of quantum correlations based on relative entropy [6].

As anticipated, we also investigate experimentally two other discordlike quantities. First, we take into account a nontrivial experimentally friendly lower bound Q to geometric discord [22]: such a quantity is less accurate and does not reveal any of the mentioned dynamical phenomena, as its expression is continuous [38]. Then, we consider as a reference a fully *bona fide* measure of discord, the negativity of quantumness Q_N^A introduced in Ref. [10] and discussed in detail in Ref. [32]. Such a measure quantifies the minimum negativity [37] created with an apparatus during a local measurement over one subsystem of a bipartite system. It can be alternatively interpreted (when the measured subsystem is a qubit) in terms of the minimum trace distance from the set of zero-discord states. The Q_N^A is unfortunately harder to compute and less accessible experimentally; to measure it from direct data, without tomography, we need a partial knowledge of the form of the state, specifically the fact that it is a

Bell diagonal state. Such a measure is found to detect the same dynamical features as geometric and entropic discord (see also Ref. [39]).

Theoretical predictions.—In the following, we consider a bipartite state of a $2 \otimes d$ system, described by a density matrix written in the Bloch representation [40]:

$$\begin{aligned} \rho &= \frac{1}{4} \sum_{\nu, \lambda=0}^{3, d^2-1} R_{\nu\lambda} \sigma_\nu \otimes \tau_\lambda \\ &= \frac{1}{4} \left(\mathbb{1}_{2d} + \sum_{\nu=1}^3 x_\nu \sigma_\nu \otimes \mathbb{1}_d + \sum_{\lambda=1}^{d^2-1} y_\lambda \mathbb{1}_2 \otimes \tau_\lambda + \sum_{\nu, \lambda=1}^{3, d^2-1} c_{\nu\lambda} \sigma_\nu \otimes \tau_\lambda \right), \end{aligned} \quad (1)$$

where $R_{\nu\lambda} = \text{Tr}[\rho(\sigma_\nu \otimes \sigma_\lambda)]$, $\sigma_0 = \mathbb{1}_2$, σ_ν ($\nu = 1, 2, 3$) are the Pauli matrices and $\{\tau_\lambda\}$ their d -dimensional generalizations, while $\vec{x} = \{x_\nu\}$, $\vec{y} = \{y_\lambda\}$ are the column vectors associated to each subsystem, and $C = (c_{\nu\lambda})$ is the correlation matrix. Quantum discord evaluates the minimum induced disturbance on the state by a measurement over one subsystem, say A . One can adopt a geometric point of view and quantify quantum correlations as the minimum distance of the state to the set of classical-quantum states, i.e., the zero-discord states, which take the form $\chi = \sum_i p_i |i\rangle\langle i|_A \otimes \rho_{Bi}$, where $\sum_i p_i = 1$ and $\{|i\rangle\}$ is an orthonormal vector set [6]. In this context, the geometric discord introduced in Ref. [28] is defined as $D_G(\rho) = 2 \min_\chi \|\rho - \chi\|_2^2$, where the squared Hilbert-Schmidt norm $\|M\|_2^2 = \text{Tr}[M^\dagger M]$ is picked as metric. An explicit formula of geometric discord for $2 \otimes d$ states is $D_G(\rho) = \frac{1}{2} (\|\vec{x}\|^2 + \|C\|_2^2 - 4k_{\max}) = 2(\text{Tr}[S] - k_{\max})$, where k_{\max} is the largest eigenvalue of the matrix $S = \frac{1}{2d} (\vec{x}\vec{x}^\top + CC^\top)$. Expressing k_{\max} explicitly, the geometric discord can be recast as a state-independent function of the density matrix elements [22]:

$$D_G = \frac{4}{3} \text{Tr}[S] - \frac{2}{3} \sqrt{6\text{Tr}[S^2] - 2\text{Tr}[S]^2} \cos\left(\frac{\theta}{3}\right), \quad (2)$$

where $\theta = \arccos\{\sqrt{2}(2\text{Tr}[S]^3 - 9\text{Tr}[S]\text{Tr}[S^2] + 9\text{Tr}[S^3]) \times (3\text{Tr}[S^2] - \text{Tr}[S]^2)^{-3/2}\}$. Fixing $\theta = 0$, one obtains a tight lower bound Q to the geometric discord, which is itself a faithful estimator of quantum correlations [22]. The result allows us to recast D_G and Q as functions of the expectation values of a set of observables $\{\mathcal{O}_i\}$: $D_G = f_{D_G}[\langle \mathcal{O}_i \rangle]$, $Q = f_Q[\langle \mathcal{O}_i \rangle]$ [38]. The choice of the specific operators depends on the experimental setting. A proposal for an all-optical setup has been advanced in Refs. [22,29]. In the present Letter, an NMR system is used. In this context, the column vectors \vec{x} and \vec{y} are proportional to the magnetization of each nuclear spin, $\vec{x} = 2\langle \vec{I} \otimes \mathbb{1}_2 \rangle$ and $\vec{y} = 2\langle \mathbb{1}_2 \otimes \vec{I} \rangle$, where $\vec{I} = \{I_x, I_y, I_z\}$ is the nuclear spin operator, which for spins-1/2 is $\vec{I} = \vec{\sigma}/2$. The elements of the correlation matrix $c_{\nu\lambda} = \langle \sigma_\nu \otimes \sigma_\lambda \rangle = 4\langle I_\nu \otimes I_\lambda \rangle$

and $\vec{x} = 2\langle \vec{I} \otimes \mathbb{1}_2 \rangle$ are proportional to a combination of multi quantum coherences [24,25].

A full state reconstruction demands $4d^2-1$ spin measurements. However, to compute D_G and Q one can get rid of d^2-1 local measurements on one the subsystems, as the Bloch vector \vec{y} does not account for the S matrix. Indeed, quantum correlations are evaluated from observables of the type $\langle \mathcal{O}_{\nu\lambda} \rangle = \text{Tr}[\sigma_\nu \otimes \tau_\lambda \rho]$, $\nu = 1, \dots, 3$; $\lambda = 0, \dots, d^2 - 1$, but global measurements can be replaced by local ones [26]:

$$\begin{aligned} \text{Tr}[(\sigma_\nu \otimes \sigma_\lambda)\rho] &= \text{Tr}[(\sigma_1 \otimes \mathbb{1}_d)\xi_{\nu\lambda}], \\ \xi_{\nu\lambda} &= U_{\nu\lambda}\rho U_{\nu\lambda}^\dagger, \end{aligned} \quad (3)$$

where $U_{\nu\lambda} = K_{A \rightarrow B} R_{\phi_\nu, \phi_\lambda}(\theta_{\nu\lambda})$, for $R_{\phi_\nu, \phi_\lambda}(\theta_{\nu\lambda}) = R_{\phi_\nu}^A(\theta_{\nu\lambda}) \otimes R_{\phi_\lambda}^B(\theta_{\nu\lambda})$, being $R_{\phi_{\nu(\lambda)}}^{A(B)}$ a rotation by an angle $\theta_{\nu\lambda}$ over the direction $\phi_{\nu(\lambda)}$, the indexes $\nu, \lambda = 1, 2, 3$ refer to the rotations for measuring the C matrix elements and $K_{A \rightarrow B}$ represents the CNOT gate with A being the control qubit (see the Supplemental Material [41] for details).

The negativity of quantumness Q_N^A is defined for $2 \otimes d$ systems as the minimum trace distance from the set of classical-quantum states (see Ref. [32] for other definitions and interpretations), $Q_N^A(\rho) = \frac{1}{2} \min_\chi \|\rho - \chi\|_1$, where $\|M\|_1 = \text{Tr}[\sqrt{M^\dagger M}]$ is the trace norm. For the particular case of Bell diagonal two-qubit states, Q_N^A is analytically computable [32,42]. Denoting the ordered singular values of the Bloch correlation matrix C as $|c_i| \geq |c_j| \geq |c_k|$, where i, j, k are permutations of 1, 2, 3, then the negativity of quantumness is given by half the intermediate one, $Q_N^A = |c_j|/2$. Therefore, the negativity of quantumness can be also experimentally determined as described above.

Experimental results.—In our implementation we set $d = 2$. The state of a NMR two-qubit system in the high temperature approximation is given by $\rho = \frac{1}{4}\mathbb{1}_4 + \varepsilon\Delta\rho$, where $\varepsilon = \hbar\omega_L/4k_B T \sim 10^{-5}$ is the ratio between the magnetic and thermal energies, ω_L is the Larmor frequency, k_B is the Boltzmann constant, and T the room temperature [23]. All measurements and transformations affect only the deviation matrix $\Delta\rho$, which in fact contains the information about the system state. The unitary operations over $\Delta\rho$ are implemented by radiofrequency pulses and evolutions under spin interactions with an excellent control of the rotation angle and direction. NMR probes the transverse magnetization, which is proportional to the average values of the $\langle I_x \rangle$ or $\langle I_y \rangle$ operators, so only a few elements (single quantum coherences) are directly accessible. In this direction, to obtain a full characterization of $\Delta\rho$ it is necessary to execute a set of independent measurements after applying specific rotations to the system, which characterize NMR quantum state tomography [25]. It is worth remarking that, since in NMR experiments only the deviation matrix is detected, the calculations of

the \vec{x} vector and of the correlation matrix C are done in units of ε .

The experiments were performed on a liquid state carbon-13 enriched chloroform sample (CHCl_3) at room temperature, with the two qubits being encoded in the ^1H and ^{13}C spin- $\frac{1}{2}$ nuclei [41]. Two initial Bell diagonal states $\rho_{1,2} = \frac{1}{4}(\mathbb{1}_4 + \sum_i c_i^{(1),(2)} \sigma_i \otimes \sigma_i)$ were prepared by mapping the correlation matrix into the deviation matrix, as described in Refs. [31,41]. Note that the methodology here employed is not restricted to this class of states, but extends to arbitrary states of $2 \otimes d$ systems. To verify the correct preparation of the states, the pulse sequences proposed in Refs. [20,31] were applied followed by a quantum state tomography procedure [43]. The resulting deviation matrices are shown as block diagrams in Fig. 1. We remark that tomography is performed just to test the quality of the state preparation procedure, and the acquired information is not used for the direct estimation of quantum correlations. The interaction with the environment in a NMR system is described by phase and amplitude damping channels [44]. As can be seen in Refs. [20,31], the correlations presented in the initial state of Fig. 1(a) should decay monotonically in time, while the state of Fig. 1(b) is expected to exhibit a nontrivial behavior of quantum correlations during the evolution.

According to Eq. (1) and the accompanying discussion, quantum correlations in a two-qubit system are obtained from the expectation values of the correlation matrix elements $c_{\nu\lambda} = \langle \sigma_\nu \otimes \sigma_\lambda \rangle = \text{Tr}[(\sigma_\nu \otimes \sigma_\lambda)\rho]$ and $\vec{x} = \langle \vec{\sigma} \otimes \mathbb{1}_2 \rangle$. These can be calculated for instance from the experimentally tomographed deviation matrix. However, using the rotations described by Eq. (2) with a proper set of angles, the evaluation of D_G and Q is reduced to a set of

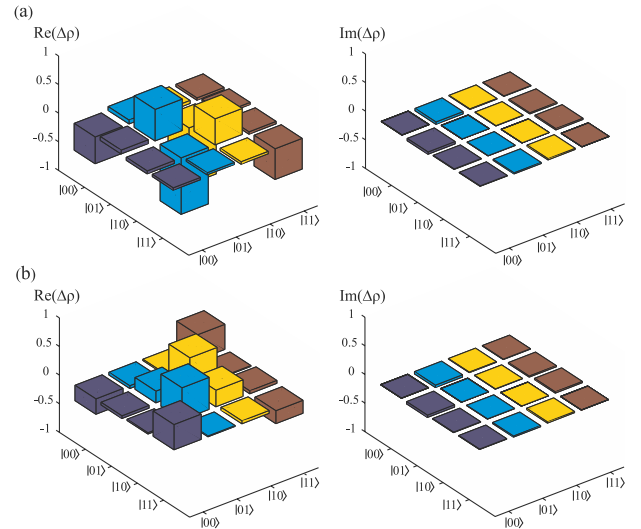


FIG. 1 (color online). Block diagrams for the deviation density matrix related to the Bell diagonal initial states. For ρ_1 in (a) we have $|c_1^{(1)}| = |c_2^{(1)}| = |c_3^{(1)}| = 0.2$, while ρ_2 in (b) reads $|c_1^{(2)}| = 0.5$, $|c_2^{(2)}| = 0.06$, and $|c_3^{(2)}| = 0.24$.

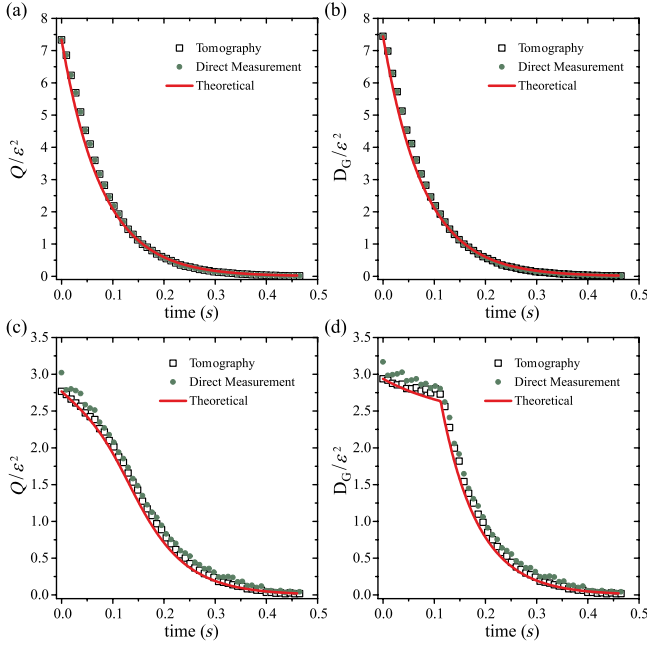


FIG. 2 (color online). Time evolution of Q and D_G for the state ρ_1 in (a) and (b), and ρ_2 in (c) and (d). The green dots represent the direct measurement and the black open squares corresponds to tomography results. The red lines depict the theoretical predictions. The relaxation times retrieved from experimental data are: $T_1 = 3.57$ s and $T_2 = 1.2$ s for the hydrogen, and $T_1 = 10$ s and $T_2 = 0.19$ s for the carbon. Quantum correlations are displayed in units of ε^2 .

spin magnetization measurements on one of the qubits. This means that, after a correct set of rotations (rf pulses) are applied to the prepared state, the geometric discord (and its lower bound) can be determined directly from the NMR signals (apart from the ε^2 factor), without having to know the state. We dub this procedure as *direct measurement*. The procedure is repeated until the thermal equilibrium state is reestablished. Concerning the negativity of quantumness [32], a partial knowledge of the state is instead required to evaluate its value. In particular, assuming (as *a posteriori* verified by tomography; see Refs. [41,45]) that the state remains in Bell diagonal form during the evolution, then the direct method still suffices to extract the correct value of Q_N^A . To benchmark the effectiveness of the direct method, overall, we compared its outcomes with the results obtained for the corresponding measures of quantum correlations by evaluating them on the state reconstructed by complete tomography as well.

The results obtained for D_G and Q using the direct measurement and tomography procedures as well as the theoretical predictions are reported in Fig. 2 for both experimentally produced states. In Fig. 3, we present the results obtained for Q_N^A by direct measurements (the ^1H nucleus was detected), tomography, and theoretical predictions for both states. We highlight a satisfactory

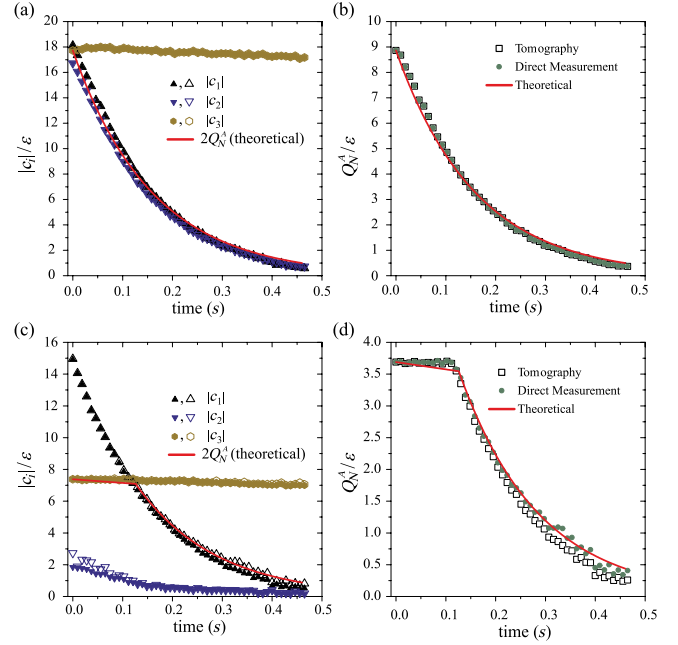


FIG. 3 (color online). Time evolution of $|c_1|$ (upward triangle), $|c_2|$ (downward triangle), and $|c_3|$ (hexagon) for state ρ_1 in (a), and ρ_2 in (c). The open symbols represent the tomography results and the filled symbols represent the direct measurement. Note that for each $|c_i|$ ($i = 1, 2, 3$) both forms of measurement are superimposed. In (b), for the initial state ρ_1 , and (d), for the initial state ρ_2 , the green dots represent the direct measurement and the black squares represent the tomography results. The red lines are the theoretical predictions for Q_N^A . Quantum correlations are displayed in units of ε .

agreement between the direct measurements, the tomographic data, and the theoretical predictions. This demonstrates that we are able to directly quantify bipartite quantum correlations in unknown (or partially known, in the case of Q_N^A) two-qubit states with our NMR setup. In particular, for the first time the negativity of quantumness is observed to undergo sudden transition in the same dynamical conditions as the geometric discord and the entropic discord [30,39]. Furthermore, directly assessing the value of D_G provides a nontomographic method to estimate *a priori* the suitability of the produced states for quantum communication via remote state preparation [11].

Conclusions.—NMR systems are a natural arena for quantum information processing with negligible entanglement and, thus, ideal testbeds for investigating dynamical properties of quantum correlations in open system dynamics. In this respect, the information stored in the density matrix of a state is often redundant to the quantification of its quantum correlations. Recent theoretical findings allow one to implement optimized protocols by reducing the number of required measurements as compared to the full state reconstruction. Here we have considered an NMR system and detected the quantum correlations of a two-qubit Bell diagonal state. Furthermore, we observed

the sudden transition of geometric discord and negativity of quantumness under phase and amplitude damping channels. The sudden transition and, in particular, the *freezing* [30], common to various measures of quantum correlations other than entanglement under particular decoherent evolutions, is certainly worthy of further theoretical and experimental investigation [46].

We finally stress that the reported experiment has to be taken as a *proof of principle*. Thanks to the explicit closed formula, without any knowledge of the initial state of a $2 \otimes d$ system, it is possible to evaluate geometric discord by $3d^2$ local spin measurements, and tune the dynamics in order to protect quantum correlations from decoherence. Also, it is remarkable that an optical setup would allow us to detect the quantumness of correlations by only seven projective measurements for any d [22], but the implementation of such quantum operations appears challenging even with state-of-the-art technology [38].

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