Wireless Sensor Networks and TSCH: A Compromise Between Reliability, Power Consumption, and Latency

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ABSTRACT

Reliability, power consumption, and latency are the three main performance indicators of wireless sensor networks. Time slotted channel hopping (TSCH) is a promising technique introduced in the IEEE 802.15.4 standard that performs some steps ahead in the direction of the final dream to meet all the previous requirements at the same time. In this article, a simple and effective mathematical model is presented for TSCH that, starting from measurements performed on a real testbed, permits to characterize both the network and the surrounding environment. To better characterize power consumption, an experimental measurement campaign was purposely performed on OpenMote B devices. The model, which was checked against a real 6TiSCH implementation, can be employed to predict network behaviour when configuration parameters are varied, in such a way to satisfy different application contexts. Results show that, when one of the three above indices is privileged, unavoidably there is a worsening of the others.

INDEX TERMS

Energy consumption, Internet of Things, low latency, power consumption, reliability, wireless sensor networks, time slotted channel hopping (TSCH).

I. INTRODUCTION

Wireless sensor networks (WSN) \cite{1} are becoming more and more one of the core enabling technologies for the Internet of Things (IoT). They permit simple devices, often powered on batteries and typically equipped with sensors (and, sometimes, actuators), to be easily interconnected and integrated in a monitoring/control system. When actuation is possible, they are typically referred to as wireless sensor and actuator networks (WSAN).

WSNs, and in general WSANs, are gaining ground in many application contexts characterized by very different and often conflicting requirements. Notable examples are environmental monitoring \cite{2}, smart and precision agriculture \cite{3}, greenhouse automation \cite{4}, heating, ventilation, and air conditioning (HVAC) systems \cite{5}, natural disaster management \cite{6}, wireless body area networks (WBAN) for healthcare \cite{7}, military applications \cite{8}, unmanned surveillance \cite{9}, and retrofitting of large industrial plants for monitoring and diagnostics \cite{10}.

Depending on the specific field of application, a number of requirements are demanded to the WSN. In most cases, reduced power consumption is the primary goal \cite{11}–\cite{15}. Typically, WSN nodes (also referred to as motes) are battery-powered, and in some cases they are deployed in harsh areas or in places that are difficult to reach (e.g., when used for environmental monitoring and natural disaster management), making battery replacement a cumbersome task.

As a matter of fact, WSNs cannot be used for time-critical applications requiring extremely low latencies and jitters (in the order of a few milliseconds), such as cable replacement \cite{16}, \cite{17}. In these cases, specific high-performance wireless solutions have been recently defined, often identified with the term ultra-reliable and low-latency communications.
(URLLC) [18]. Nevertheless, many contexts in the real world may benefit from (and sometimes demand for) the ability of the underlying network to ensure relatively short (seconds) and bounded latency on packet delivery. This is the case, e.g., of industrial monitoring and surveillance applications.

Similarly to power consumption and transmission latency, also the required degree of reliability the network must ensure depends on the specific application. In theory, this goal can be easily achieved by means of Automatic Repeat reQuest (ARQ) techniques [19], which rely on confirmed message exchanges and operate by retransmitting those frames for which no corresponding acknowledgement (ACK) was received. In practice, retransmission increases both power consumption and latency.

Taking all above requirements into account at the same time is typically a complex task to deal with. To this aim, a popular solution is time slotted channel hopping (TSCH) [20]. TSCH was first proposed as an enhancement of IEEE 802.15.4 (known as 802.15.4e) and then included into the most recent version of the related standard specification [21].

Currently, many standards for wireless networks exist [22] that can be profitably adopted in practical implementations of the Internet of Things (IoT) paradigm, and often several heterogeneous communication technologies coexist within the same system, which are transparently exploited by applications [23]. Popular IoT solutions that rely on IEEE 802.15.4 for frame exchanges include, e.g., ZigBee and WIA-PA. Concerning IEEE 802.15.4e, two operating modes are defined, i.e., the deterministic and synchronous multi-channel extension (DSME) and TSCH (used by WirelessHART, ISA 100.11a, and 6TiSCH). Other technologies commonly adopted in IoT are IEEE 802.11 (Wi-Fi), 4G/5G, LoRa, and Bluetooth Low Energy (BLE).

The analysis presented in this article specifically refers to TSCH, and experimental results were obtained on motes complying to the IPv6 over the TSCH mode of IEEE 802.15.4e (6TiSCH) protocol [24]–[26]. We opted for TSCH because it shows a deterministic behavior [27] for what concerns the metrics for IoT systems we took into account, namely reliability, power consumption, and latency. Protocol behavior can be finely tuned by means of a number of parameters, most of which can be easily configured by the user. However, since the above metrics are deeply intertwined, it is generally impossible to optimize one without worsening the others. Therefore, proper network configuration to meet the application requirements must necessarily rely on holistic approaches.

The main contribution of this article is a simple and effective mathematical formulation that describes the behavior of a TSCH network, with the ultimate goal to ease tuning procedures. The model depends on both protocol configuration parameters and estimated quantities aimed at characterizing the network and the surrounding environment, obtained from experimental measurements performed on a real setup. Logged data were also used for validating the model.

The second relevant contribution of the paper is the experimental characterization of the power consumption of OpenMote B devices. Although these motes are quite widespread, as they are currently employed for developing and testing any newly added feature or improvement of both 6TiSCH and the OpenWSN operating system, to the best of our knowledge such a kind of analysis is not available in the literature yet. From our point of view, this characterization is required to enable an adequate and truthful estimation of the power consumption in the network model.

In the following, Section II describes the main aspects of TSCH. The network and power consumption models are presented in Section III and Section IV, respectively. Details about the experimental analysis are provided in Section V, while considerations on some relevant, practical application contexts with respect to performance indicators are reported in Section VI. Finally, some concluding remarks are given in Section VII.

II. TSCH

The TSCH mode of the IEEE 802.15.4-2015 [21] standard was first defined in 2012, and was initially included in the IEEE 802.15.4e amendment [28]. On the one hand, TSCH is an effective way to counteract disturbance caused by either electromagnetic noise or transmissions on the wireless medium performed by other communication technologies that operate in the same (or on an overlapping) frequency range. On the other hand, it increases communication predictability and reduces power consumption.

More in detail, time in a TSCH network is divided into slots of fixed duration, organized in slotframes made up of a defined number $N_{\text{slot}}$ of slots. Slotframes repeat in time and are exploited by a time slotted mechanism for controlling wireless medium access. This requires all motes to be time-synchronized [29], [30]. In commonly available implementations, the duration $T_{\text{slot}}$ of a slot ranges from 10 ms to 20 ms.

A second mechanism is additionally defined, known as channel hopping, aimed at changing the transmission channel according to a known pattern. In our implementation, the 16 channels defined by IEEE 802.15.4 in the 2.4 GHz ISM band are exploited, each of which has a width of 5 MHz, lying in the range between 2.405 GHz (channel 11) and 2.480 GHz (channel 26).

From the motes’ point of view, the wireless spectrum is conceptually partitioned in frequency and time through one (or more) matrices, where the rows of the matrix represent the 16 channels while each column represents a specific slot in the slotframe [31]. An example of this matrix is shown in Fig. 1. According to the TSCH terminology, rows identify channel offsets, columns refer to slot offsets, and the matrix defines the slotframe usage. In particular, a cell located at the intersection between a specific row and a specific column of the matrix (i.e., channel and slot offsets) describes a link between neighbor nodes at the data-link layer.
Each slot in a TSCH network is uniquely identified by the absolute slot number (ASN), which is a counter initialized to 0 at the beginning of the network formation and incremented by one on every slot. A mechanism is defined that enables all nodes to know, at any time, the global value of ASN for the network they belong to. This permits each node to determine the offset of the current slot in the slotframe by simply computing ASN mod $N_{\text{slot}}$. The physical channel used for transmission in any given cell is selected according to a pseudo-random function that is known by all the nodes of the network and depends on both the ASN value and the related channel offset. Typically, the transmission channel changes in each repetition of the slotframe.

On the one side, cells within the matrix can be configured to obtain the desired schedule [32], [33], which, thanks to the time-slotted mechanism, increases network determinism by preventing intra-network collisions. For instance, a sequence of cells that defines a multi-hop path between motes $M_1$ and $M_3$ is shown in Fig. 1. On the other side, the channel hopping mechanism is effective to counteract narrowband disturbance and external interference that may affect communication. In particular, every time the transmission in a cell is corrupted, the physical channels used for retries in the following slotframes will be very likely different.

Concerning a single mote, generally speaking a scheduled cell in the matrix can be configured for either transmission (TX) or reception (RX). When no cell is scheduled for the current time slot, the mote can switch off its radio module (transceiver), consequently saving energy. If the width of the matrix (i.e., $N_{\text{slot}}$) is large and the number of RX cells is small, the mote is enabled to spend most of the time in a deep-sleep state. This means reduced duty cycles and permits noticeable energy saving. Regarding TX cells, in optimized implementations motes wake up only if packets ready to be sent are pending in transmission buffers, whose destination address matches the link described by the current cell.

A cell is defined as shared in the case more than one mote is enabled to transmit in it. The resulting behaviour resembles slotted-Aloha, and a mechanism based on random backoff is foreseen to deal with possible collisions. Typically, shared cells are used for frames devoted to network management, while for application data exchanges (which is what we want to model in this article) dedicated (non-shared) cells are more appropriate (and typically exploited).

It is worth remarking that TSCH is part of the medium access control (MAC), and it manages only the communication schedule between neighbour nodes at the data-link layer. Matrices that define slotframe and spectrum usage are configured by means of other protocols operating at higher levels of the protocol stack.

Many papers in the scientific literature focus on techniques for configuring the TSCH matrix [32], [34]–[37], but only a few propose mathematical models to describe performance in the presence of transmission errors. In particular, some theoretical analyses about how a Wi-Fi interfering traffic may affect legacy IEEE 802.15.4 networks (i.e., not based on TSCH or DSME) were reported in [38], [39]. Instead, a model based on Markov chains that describes the traffic on shared cells was proposed in [20], [40]. Finally, some preliminary models describing communication over dedicated cells in TSCH were sketched in [19] and then refined in [41], but without taking into account energy consumption and multi-hop networks.

As said before, experimental evaluation in this article was performed on devices complying to the 6TiSCH protocol. This is for two main reasons. Firstly, 6TiSCH is the most recent among the solutions based on TSCH for which devices are available off-the-shelf (even though their firmware has still to be finalized). A second point in favour of 6TiSCH is that it adopts IPv6 at the network layer (according to the outcomes of the 6LoWPAN project), which fully adheres to the IoT paradigm by permitting each mote to be assigned a unique address within the whole Internet scope. Concerning higher-layer protocols in the 6TiSCH suite, the most relevant ones are the 6TiSCH Operation Sub-layer Protocol (6P) [42] to configure TSCH matrices and the Routing Protocol for Low-Power and Lossy Networks (RPL) [43] to manage multi-hop communication between pairs of nodes by creating and maintaining a tree network topology.
A taxonomy of the scientific works about WSN/WSAN referred to in this article, categorized according to the specific aspects they investigate, is reported in Table 1.

**Table 1. Taxonomy of the scientific works cited in the paper.**

<table>
<thead>
<tr>
<th>Topic</th>
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<tbody>
<tr>
<td>WSN/WSAN applications</td>
<td>[2]–[10]</td>
</tr>
<tr>
<td>TSCH/6TiSCH</td>
<td>[20], [24]–[27], [31]</td>
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<tr>
<td>IEEE 802.15.4 specifications</td>
<td>[21], [28]</td>
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<td>Scheduling and TSCH configuration</td>
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<td>Mathematical models</td>
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<tr>
<td>WSN/WSAN high-level protocols</td>
<td>[42] (6P), [43] (RPL), [46] (CoAP)</td>
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<tr>
<td>Power consumption</td>
<td>[11]–[15], [48], [53]</td>
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### III. MATHEMATICAL MODEL

Star topologies, in which every node is one hop away from the root, are typically found in many wireless networks conceived for industrial systems (see, e.g., [44]). An example of this kind of architectures can be found in robotized production cells, where sensors fastened to moving (or mobile) parts of the equipment have to be wirelessly connected to a centralized control unit. In this case, all nodes but the root are leaves and conceptually lie at the same network level.

In the case not all nodes of the network are in line of sight, a proper routing mechanism is required for communication, which relies on packet relays performed by intermediate nodes according to a multi-hop transmission technique. A tangible advantage of these solutions is the ability to cover larger areas, at the price of an increased communication latency. Multi-hop WSNs often rely on a multi-level tree topology that stems from a root node [45]. As a matter of fact, mesh topologies also exist where routes between nodes are (somehow) arbitrary, but they are less common in practice and will not be analyzed in this work. Many WSN protocol stacks, like 6TiSCH, rely on RPL to obtain a tree logical topology out of a mesh physical topology.

The mathematical model proposed in this section describes the most general case of a multi-level tree topology, but it can be easily adapted to single-level star topologies. $N_{level}$ is the distance (in terms of levels) between the farthest leaf node and the coordinator of the WSN (i.e., the root of the tree). Clearly, in the single-level case, $N_{level} = 1$. In this analysis, our attention is focused on the request/response paradigm, which is employed, e.g., by the Constrained Application Protocol (CoAP) [46], a quite relevant solution in modern WSNs. Hence, every interaction between two motes consists in a request packet that traverses the path in the forward direction, immediately followed by a response packet in the reverse direction. In the following, with a slight abuse of notation, and in order to simplify equations, we will use the term “packet $i$” to refer to both the request packet and the related response packet. This means that two-way packet exchanges in star topologies can be described by setting $N_{hop} = 2$ (one hop from the root to the target mote and another from that mote back to the root). Likewise, the number of hops needed to query a node at level $l$ is $N_{hop} = 2 \cdot l$. When a leaf node is queried in a balanced tree, $N_{hop} = 2 \cdot N_{level}$.

The following analysis has been split in two main phases. In the first phase, reported in Sections III-A, III-B, and III-C, we describe the network model and how it can be fit to a real setup. In particular, we show that estimates of the performance indicators we are interested in (reliability, power consumption, and latency) can be evaluated from the model, and that many parameters of the model can be derived directly from a set of measurements performed on a simple experimental setup. In the second phase, described in Section III-D, the model parameters derived directly from the setup are used to indirectly obtain additional derived quantities, which in turn permit to model to a complete extent the expected behavior of a TSCH network when its protocol parameters are varied. The proposed methodology permits to relate model/protocol parameters and performance indicators, and enables a swift network configuration starting from the requirements of applications.

When model parameters are estimated in the first phase, queuing insides nodes is not considered. In other words we assumed that, for any given mote, only one packet with the same destination for the next hop can be found in the queue at any given time. From our viewpoint, this condition is not very restrictive. In fact, it can be easily met if the packet rate with which measurements are performed is much below the available capacity of the path [47]. It is worth pointing out that, in most real application scenarios, the period of data transmissions on a WSN is quite long, which means that queuing phenomena are typically negligible. In the following analysis, we considered paths with a single dedicated cell for each hop, i.e., the matrix of each mote does not contain more than one cell targeted to the same destination. Again, this can be considered a typical configuration for such matrix.

The main quantities used in the model, including protocol parameters and performance indicators, are summarized in Table 2.

### A. RELIABILITY

For applications demanding high reliability, it is of utmost importance that all transmitted packets (or, at least, the vast majority of them) are correctly delivered to destination. ARQ schemes, like the one exploited in TSCH, permit the transmission of every packet to be reiterated (upon failures) on each traversed link up to the retry limit. The likelihood for any packet to eventually reach the target node is related to the frame error probability $\epsilon$ (i.e., the probability for a single attempt in the frame transmission process between neighbor nodes to fail), the maximum number $N_{tries}$ of allowed tries per frame at the MAC layer (retry limit plus one), and the number $N_{hop}$ of hops performed at the routing layer (we considered both directions). As a consequence, the packet delivery probability on the whole (two-way) path between
requester and responder, also termed reliability, equals one minus the packet loss probability \( \epsilon_{\text{pkt}} \) and can be obtained as

\[
1 - \epsilon_{\text{pkt}} = \left( 1 - \epsilon_{\text{N tries}} \right)^{N_{\text{hop}}}. \tag{1}
\]

Above equation holds if the three following assumptions are verified. First, the value of \( \epsilon \) for the transmission between any two given motes must be the same irrespective of the direction (upward or downward). This reasonably holds, provided that the radio modules of motes are similar. Second, the value of \( \epsilon \) must not vary over time. While this is generally untrue, experiments performed on a 6TiSCH network deployed in a real environment and subject to non-negligible interference caused by several nearby Wi-Fi networks [41] showed that this approximation is often acceptable. Third and last, the value of \( \epsilon \) has to be the same for all the links of the path. This is mostly true for small networks based on a star topology but, when \( N_{\text{level}} \geq 2 \), it may not be verified in some circumstances, because the amount of disturbance and interference could differ sensibly over the coverage area of the WSN (which for multi-hop configurations can be quite large).

Not unreasonably, we can assume that the spatial distribution of interfering Wi-Fi devices (and, in general, of equipment exploiting wireless communication technologies) is more or less homogeneous, and the same holds for the traffic they generate. In fact, placement of access points is often planned by IT managers with this goal in mind.

The frame error probability \( \epsilon \) can be estimated starting from a set of measurements concerning round trip times. Let \( d_{i} \) be the network latency, as seen by the originator, between the transmission time of the packet conveying the \( i \)-th request and the reception time of the packet that bears the related response (coming from the target mote). The quantity \( d_{i} \) is defined only for successful transactions, where both the request and the response packets are correctly delivered.

The overall number \( n_{\text{tra}, i} \) of transmission attempts actually performed on air for the packets involved in any given request/response iteration \( i \), all hops considered (in both directions), can be inferred from the duration \( d_{i} \) using the following equation

\[
n_{\text{tra}, i} = \left\lfloor \frac{d_{i} - d_{\text{min}}}{T_{\text{frame}}} \right\rfloor + N_{\text{hop}}, \tag{2}
\]

where \( d_{\text{min}} \) is the minimum communication latency, evaluated over all the experiments (that depends on the configuration of the cells in the TSCH matrix), and \( T_{\text{frame}} = N_{\text{slot}} \cdot T_{\text{slot}} \) represents the duration of the TSCH slotframe.
To ease understanding of (2), an example is shown in Fig. 2 about a possible configuration of the TSCH matrix for a network including 3 motes. Mote $M_1$ is the root, $M_2$ its child, and $M_3$ (not in line of sight with $M_1$) the child of $M_2$. The notation $x \rightarrow y$ in a cell of the TSCH matrix denotes a cell reserved for transmission from $M_x$ to $M_y$. For instance, $1 \rightarrow 2$ specifies that the cell is reserved for transmission from $M_1$ to $M_2$, while $2 \rightarrow 1$ means it is reserved for transmission in the opposite direction, i.e., from $M_2$ to $M_1$.

In the case of a request/response iteration between the root $M_1$ and the leaf mote $M_3$ performed without transmission errors (i.e., when no retransmissions take place), $n_{tra,i} = 4$ and latency is in the range $d_{min} \leq d_i < d_{min} + T_{sframe}$. In particular, when $d_i$ equals (or is slightly above) $d_{min}$ (Fig. 2.a), this means that the packet to be sent was queued on $M_1$ just before cell $1 \rightarrow 2$. Since packet generation by applications is not synchronous with the TSCH matrix, the time when the transmission request is issued relative to the slotframe boundaries can be modeled as a random variable uniformly distributed between 0 and $T_{sframe}$. The maximum delay in the case of no retransmissions is bounded by $d_{min} + T_{sframe}$, and is experienced when the packet was queued immediately after the beginning of the $1 \rightarrow 2$ cell, which means that it is sent in the next $1 \rightarrow 2$ cell (Fig. 2.b).

Finally, when transmission errors are experienced, the latency $d_i$ is increased by the duration of one slotframe ($T_{sframe}$) per every frame retransmission. For instance, in the case a single retransmission is performed (Fig. 2.c), on any link, bounds $d_{min} + T_{sframe} \leq d_i < d_{min} + 2 \cdot T_{sframe}$ can be defined on latency. Equation (2), which permits to calculate the actual number of transmission attempts on air, is derived directly from these bounds on latency.

The probability $p_{tra}$ that a packet is correctly exchanged with the minimum number of transmission attempts (i.e., the probability that no retransmissions are performed for it) can be estimated from experiments as

$$p_{tra} = (1 - e)^{N_{hop}} = \frac{[i \mid n_{tra,i} = N_{hop}]}{N_{sam}},$$
(3)

where $[i \mid n_{tra,i} = N_{hop}]$ is the number of packets that reached the destination after exactly $N_{hop}$ transmission attempts (on the whole path), while $N_{sam}$ is the number of samples collected in the experiment, i.e., the number of request/response iterations executed by the application.

From (3), the frame error probability can be easily obtained as

$$\epsilon = 1 - \left(\frac{[i \mid n_{tra,i} = N_{hop}]}{N_{sam}}\right)^{N_{hop}}.$$  

(4)

Actually, this estimated value for $\epsilon$ takes into account the error rates on each one of the 16 different channels used for transmission by TSCH. In the case of a multi-level network, it also "aggregates" the failure probabilities on all the links that make up the path between the source and the destination of the request/response exchange, and provides a simple yet effective model of the overall behaviour of the wireless spectrum in the place where the WSN is deployed. As said before, this approximation is only acceptable if the error rates on the links composing the path do not differ significantly.

### B. POWER CONSUMPTION

Analysis of power consumption is rather important in WSNs, since motes cannot usually count on a stable external power source but must rely on batteries and/or energy harvesting. A simple but quite effective power consumption model [48] subdivides the total energy consumption into separate contributions

$$E = E_{tx} + E_{rx} + E_{listen} + E_{cpu} + E_{sleep},$$

(5)

where $E_{tx}$ is the overall energy required for transmission (that includes transmission of data frames and reception of the related ACK frames), $E_{rx}$ is the overall energy required for frame reception (that includes reception of data frames and transmission of the related ACK frames), and $E_{listen}$ is the energy consumed to listen to the channel when waiting for the reception of frames and the related slots remain idle (idle listening).

In this work, the two contributions $E_{cpu}$ and $E_{sleep}$ have been embedded in the same quantity $E_{comp} = E_{cpu} + E_{sleep}$, which represents the energy consumed by the mote when no specific application runs on it that uses the network. In the following, we concentrate only on the energy consumed for communication. However, the measured value of $E_{comp}$ for the motes we used in the experimental campaign is provided in Section IV.

The energy consumption $E_{net}$ of the network component over a given time interval can be directly derived from the number $n_{listen}$ of cells reserved for transmission (as per the TSCH matrix) that remain unused, in which receiving nodes uselessly sense the channel, and the number $n_{tra}$ of cells in which transmission is actually performed

$$E_{net} = E_{tx} + E_{rx} + E_{listen}$$
$$= n_{tra} \cdot E_{rx}^f + E_{rx}^f + n_{listen} \cdot E_{listen}^f,$$

(6)

where $E_{tx}^f$ and $E_{rx}^f$ correspond to the energy consumed to send and receive a single frame (data plus the related ACK), respectively, while $E_{listen}^f$ is the energy consumed to listen to the channel when a reserved cell is not used.

Equation (6) can be rewritten in terms of the power $P$ as

$$P = f_{tra} \cdot (E_{rx}^f + E_{rx}^f) + f_{listen} \cdot E_{listen}^f,$$

(7)

where $f_{tra}$ is the mean number of confirmed frame transmission attempts per second actually performed on air by all motes (i.e., the mean overall frame transmission rate), while $f_{listen}$ represents the mean number of cells allocated for reception over a time span of one second in which idle listening occurred.

The rate $f_{tra}$ can be obtained dividing the total number $N_{tra}$ of frames transmitted on air in the experiment by the overall duration of the experiment itself

$$f_{tra} = \frac{N_{tra}}{T_{app} \cdot N_{sam}}.$$

(8)
where $T_{app}$ is the period with which requests are repeatedly issued by the originating mote.

Instead, the rate $f_{listen}$ was obtained by subtracting $N_{tra}$ (i.e., the number of cells that were actually used in the whole experiment) from the total number of cells reserved for transmission in the same interval, and then dividing by the duration of the experiment

$$f_{listen} = \frac{1}{T_{app}} \cdot \frac{N_{hop} \cdot T_{app} \cdot N_{sam}}{T_{frame}} - N_{tra},$$  

(9)

which can be rewritten as the slot repetition frequency $1/T_{slot}$ multiplied by the fraction of slots in the slotframe reserved for the transmission of the considered request/response packets, minus the mean overall frame transmission rate $f_{tra}$

$$f_{listen} = \frac{N_{hop}}{T_{frame}} - f_{tra} = \frac{N_{hop}}{T_{slot} \cdot N_{slot}} - f_{tra}.$$  

(10)

Quantity $N_{tra}$ is composed of two contributions: the number $N_{deliv}$ of transmitted frames associated to packets correctly delivered to destination and the number $N_{tra, lost}$ of transmitted frames associated to packets that went lost

$$N_{tra} = N_{deliv} + N_{tra, lost}.$$  

(11)

$N_{tra, lost}$ can be computed directly from the $n_{tra,i}$ values inferred by applying (2) to experimental samples

$$N_{tra, lost} = \sum_{i=1}^{N_{sam}} n_{tra,i}.$$  

(12)

Instead, the value of $N_{tra, lost}$ cannot be evaluated directly in our experimental setup. In fact, latency is not defined for lost packets, which implies that (2) cannot be applied. An estimate of it, we denoted $N_{tra, lost}$, can be derived from the value of $\epsilon$ provided by (4) by means of (13), as shown at the bottom of the page, which will be introduced and explained in Section III-D. As a consequence, in the following analysis, in the place of $N_{tra}$ we will actually use its estimate $\hat{N}_{tra}$, obtained by substituting $N_{tra, lost}$ in (11). It is worth remarking that, in the case no packets are lost in the experiment (i.e., when $N_{tra, lost} = 0$), the quantity $N_{tra}$ can be derived directly from experimental data, and the same holds for $f_{tra}$ and $f_{listen}$.

Equations (8) and (10) hold only when the generated traffic does not exceed the allocated network capacity, that is, if $f_{tra} \leq N_{hop}/T_{frame}$. Otherwise, network behavior is unstable and the number of packets queuing in the motes’ transmission buffers would grow indefinitely. Instead, equation (2), which uses the round-trip time $d_i$ measured on the given path to compute the number $n_{tra, i}$ of transmission attempts performed for the $i$-th request, holds only if packets never experience queuing delays due to previously buffered packets that use the same outgoing cell. Clearly, the same limitation also affects all the formulas that depend on (2). However, as highlighted in Section III-D, the approximation above is acceptable provided that the traffic injected in the network is low. Since disturbance and interference on air do not depend in any way on queuing, $\epsilon$ can be reliably estimated by setting $T_{app}$ for measurements long enough, so as to prevent buffer overrun conditions.

### C. LATENCY

In hard and soft/firm real-time systems, latency is of primary importance, and it is required to strictly obey application-dependent deadlines. For this kind of systems, delays due to communication over a digital network must be bounded, and specific real-time industrial protocols and implementations are typically employed that offer some guarantees (under a statistical basis, for soft/firm real-time systems) for the worst-case transmission times [49, 50]. In TSCH, this can be achieved by exploiting deterministic channel access (i.e., time slotting) coupled with a proper scheduling of exchanges (matrix configuration). The theoretical worst-case latency ($\text{Max}_d$), assuming that the only source of delays are retransmissions, can be computed analytically as

$$\text{Max}_d = N_{hop} \cdot N_{tries} \cdot T_{frame}.$$  

(14)

Equation (14) only holds if, for every link in the path, no queuing of packets occurs inside any motes. A sufficient condition for this to happen, in the case all the cells reserved for the request/response exchange are not used by other traffic, is that $T_{app} \geq \text{Max}_d/N_{hop} = N_{tries} \cdot T_{frame}$.

Conversely, when queuing phenomena take place, $\text{Max}_d$ can be obtained by multiplying the value in (14) by the maximum size of the local queues (including the packet under transmission). From (14), it is clear that the worst-case latency can be reduced by lowering $N_{slot}$ (which increases power consumption) or by lowering $N_{tries}$ (which decreases power consumption but worsens reliability).

### D. DERIVED QUANTITIES

We now change perspective by laying the ground for a comprehensive analysis of TSCH-based WSNs: starting from experimental results (packet losses and measured transmission latencies) we will show that a complete characterization of the network performance can be obtained in terms of reliability, power consumption, and latency. The basic idea is to firstly estimate $\epsilon$ from a set of experimental data by means of (4). Then, a number of intermediate quantities are derived, which permit the expected network behavior to be modelled and evaluated analytically.

$$\hat{N}_{tra, lost} = \hat{N}_{tra} \cdot \sum_{h=0}^{N_{hop}-1} \left[ \frac{(1 - \epsilon^{N_{tries}})^h}{1 - (1 - \epsilon^{N_{tries}})^h} \right] \cdot \left( \frac{1}{1 - \epsilon} - \frac{N_{tries} \cdot \epsilon^{N_{tries}}}{1 - \epsilon^{N_{tries}}} \right) + N_{tries}.$$  

(13)
Besides $\varepsilon$, which describes to what extent disturbance and interference impact on communication, the quantities that affect TSCH operation depend on:

- the characteristics of the protocol decided in the network design/configuration phase ($N_{\text{slot}}$, $T_{\text{slot}}$, and $N_{\text{tries}}$);
- the characteristics of the path, which mainly depend on the physical placement of nodes and obstacles ($N_{\text{hop}}$);
- the characteristics of the hardware of motes in terms of power consumption ($E_{\text{tx}}^f$, $E_{\text{rx}}^f$, and $E_{\text{listen}}^f$);
- the characteristics of the software application that communicates over the network ($T_{\text{app}}$ and $N_{\text{sam}}$).

One of the problems with the formerly presented analysis is that the measured number $N_{\text{lost}}$ of failed requests in typical operating conditions may not describe disturbance and interference reliably. In fact, unless experiments are protracted for very long times (months), no packets are usually lost with the default retry limit. A more reliable estimate of the number of failed requests (for which no response is obtained) can be derived from (1) and corresponds to

$$\hat{N}_{\text{lost}} = N_{\text{sam}} \cdot \varepsilon \cdot \left(1 - (1 - \varepsilon^{N_{\text{tries}}})^{N_{\text{hop}}}ight).$$  \hspace{1cm} (15)

The expected number of transmission attempts performed for a packet correctly delivered on a single hop is described by a truncated geometric series

$$\frac{1}{1 - \varepsilon^{N_{\text{tries}}}} \sum_{k=1}^{N_{\text{tries}}} k(1 - \varepsilon)e^{k-1}.$$  

Concerning the whole path, it can be easily demonstrated that an estimate $\hat{n}_{\text{tra}}$ of the average number of frames transmitted on air for a successful request/response exchange can be computed as

$$\hat{n}_{\text{tra}} = N_{\text{hop}} \cdot \left(1 - \varepsilon^{N_{\text{tries}} \cdot \varepsilon^{N_{\text{loss}}}} \right).$$  \hspace{1cm} (16)

An estimate $\hat{N}_{\text{tra}}$ of the overall number of frame transmission attempts associated to failed requests can be obtained from (13), where the factor in square brackets represents the fraction of packets that are lost in hop $h + 1$ (that is, for which the preceding $h$ hops were successful), while the factor in round brackets represents the average number of transmitted frames for each one of these packets (the first term resembles (16), while for the latter it should be remembered that, when a packet is lost because its transmission failed on a certain link, the number of attempts on that link equals $N_{\text{tries}}$).

An estimate of the rate $f_{\text{tra}}$, as defined by (8), can be obtained from the derived quantities $\hat{N}_{\text{lost}}$, $\hat{n}_{\text{tra}}$, and $\hat{N}_{\text{tra}}$, and corresponds to

$$f_{\text{tra}} = \frac{\hat{n}_{\text{tra}} \cdot (N_{\text{sam}} - \hat{N}_{\text{lost}}) + \hat{N}_{\text{tra}}}{T_{\text{app}} \cdot N_{\text{sam}}}.$$  \hspace{1cm} (17)

By substituting $f_{\text{tra}}$ in (10), the estimate $\hat{f}_{\text{listen}}$ can be easily computed. In turn, the power consumption $P$ is obtained from $\hat{f}_{\text{tra}}$ and $\hat{f}_{\text{listen}}$ by means of (7). The quantities $E_{\text{tx}}^f$, $E_{\text{rx}}^f$, and $E_{\text{listen}}^f$ for the commercial motes we used in our setup were evaluated experimentally, as described in the following section.

Finally, since the overall number of frames transmitted on air for a single end-to-end packet exchange equals $N_{\text{hop}}$ when no errors occur, and every retry takes an additional slotframe, an estimate of the average transmission latency (that for request-response pairs coincides with the round-trip time) can be obtained from $\hat{n}_{\text{tra}}$ and $d_{\text{min}}$ as

$$\hat{\mu}_d = d_{\text{min}} + \left(1 + \hat{n}_{\text{tra}} - N_{\text{hop}}\right) \cdot T_{\text{frame}}.$$  \hspace{1cm} (18)

From a practical point of view, equations (15)–(17) are valid also in the presence of queuing phenomena. The only limitation is that they do not consider those packets that went lost due to the fact that the queue in the receiver (either an intermediate node or one of the end-points) was completely full at the time of arrival. This situation takes place seldom in real cases, and its occurrence is an indirect evidence that the network was not sized correctly. On the contrary, neglecting queuing delays as done in (18) constitutes an acceptable approximation only when (most of the times) packets manage to be forwarded at the earliest opportunity (i.e., in next suitable link). However, if the average delay experienced by packets in the queues of the traversed motes along the path can be estimated in some way, equation (18) can be updated to take into account this latency contribution as well.

After computing the value of $\varepsilon$ by means of (4), all the performance indicators we are interested in for describing a WSN based on TSCH from the point of view of applications, namely reliability $(1 - \varepsilon_{\text{pkt}})$, power consumption $(P)$, theoretical worst-case latency $(\max_\varepsilon)$, and average latency $(\mu_d)$, can be obtained analytically using equations (1), (7), (14), and (18), respectively.

IV. POWER CONSUMPTION MODEL

In this section, the power consumption for the specific motes we used in our experimental campaign was measured experimentally. Two main goals were reached: firstly, the real power consumption of OpenMote B devices was assessed; secondly, the actual values of $E_{\text{tx}}^f$, $E_{\text{rx}}^f$ and $E_{\text{listen}}^f$ were obtained. By substituting them in (7), an estimate of the actual power consumption for this kind of motes can be obtained, given the network traffic and TSCH configuration parameters.

A. OpenMote B DEVICES AND EXPERIMENTAL SETUP

All experiments were performed on OpenMote B devices [51]. These motes are equipped with a TI CC2538 System-On-Chip microcontroller, which integrates an ARM® Cortex™ M3 CPU with 32 KB of dynamic RAM memory and 512 KB of flash memory, and a radio transceiver compliant to IEEE 802.15.4 for transmission in the 2.4 GHz band. A second radio chip (Atmel AT86RF215), not used in our experiments, is also included on the electronic board of the motes, which

\footnote{The actual value of $d_{\text{min}}$ can be also derived from the configuration of the TSCH matrix—see the example of Fig. 2.}
manages sub-GHz transmissions (868/915 MHz). In addition, these motes are equipped with temperature and relative humidity sensors, and four indicator LEDs. Typically, such a kind of devices are operated on batteries, but they can also be powered by means of a conventional USB cable. From a software point of view, the OpenWSN [52] and the Contiki operating systems are supported. Both of them are available as open source, and so their code can be easily inspected and modified, if needed.

All the experimental campaigns we describe in this article are based on OpenWSN (version REL-1.24.0), as it includes the most recent version of the 6TiSCH protocol stack. In particular, measurements for both power consumption and latency (this latter reported in Section V) were carried out using a simple network setup, made up of two OpenMote B devices (the root plus a leaf mote acting as a responder) located about 2 m apart. The root mote was connected to a PC running the Linux operating system, on which OpenVi-sualizer (the network management software distributed along with OpenWSN) was executed. This tool was used to select the root mote, as well as to control and monitor the state of the WSN. Samples about round-trip times and packet losses were collected on the PC by periodically invoking the ping command to query the leaf mote.

### B. CHARACTERIZATION OF POWER CONSUMPTION

The power consumption of OpenMote B motes was estimated by means of a Tektronix MDO3024 oscilloscope equipped with two TPP0250 probes. The probes were connected to two specific pins of the printed circuit board of the mote that are devoted to measuring the total current flow it absorbs. Current absorption was measured only on the leaf mote, which is the one that, in real applications, is powered on batteries. The OpenWSN code was modified to disable the onboard LEDs (very power-hungry), so that all the experimental results were obtained with such indicators switched off. This led to a reduction of the absorbed current equal, on average, to about 6 mA, corresponding to about 360 µJ saved for every slot.

The experimental measures of the current drained by the leaf mote over one slotframe are reported in Fig. 3.a, where the x-axis represents the offset (in milliseconds) from the beginning of the slotframe. The many regularly-spaced short peaks are related to activities performed by the protocol stack at the beginning of every slot. Consequently, their number is equal to \(N_{\text{slot}} = 101\). Fig. 3.b zooms out part of the diagram in Fig. 3.a, and includes seven peaks, which clearly appear to occur every \(T_{\text{slot}} = 20\) µs. The two current consumption patterns labeled RX DATA and TX ACK, which rise above the previous peaks, refer to a confirmed transmission (associated to a ping request/response exchange) as seen by the point of view of the leaf mote that manages the RX cell.

For all the experiments described in this section, the cells in the TSCH matrix are configured as follows:

- **Slot 0** (time offset 0 ms) is a shared TXRX cell, which is typically associated with channel offset 0. It is used to send frames related to network formation and maintenance (e.g., enhanced beacons).
- **Slot 16** (time offset 320 ms) is configured in the root as a shared TXRX cell, while from the point of view of the responder it behaves as a dedicated RX cell. After the initial network configuration phase, it is typically used by the root only to send confirmed packets to its children in the downward direction, hence collisions may not happen. In the context of this article, this cell is used for transferring ping request packets. An example that shows what happens to current absorption in the responder during the reception of a frame bearing the ping request and the transmission of the related ACK frame can be found in Fig. 4.b. When no frame is transferred and the cell remains unused, the responder still spends a considerable amount of energy to listen to the channel (idle listening), as shown in Fig. 4.c.
- **Slot 98** (time offset 1960 ms) is configured in the responder as a non-shared TX cell, reserved for transmitting packets to its parent (the root) in the upward direction. In the experiments, this cell is used for transferring packets.
FIGURE 4. Power consumption for the different types of cells: slot including a confirmed frame transmission (a), slot including confirmed frame reception (b), slot in which idle listening occurs (c), and dissection of a confirmed frame reception into separate contributions (d).

TABLE 3. Energy consumption for different types of actions within a slotframe matrix with OpenMote B motes. In bold quantities used in Eq. (7).

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Action(s)</th>
<th>Slot offset</th>
<th>Energy [µJ]</th>
<th>Size [bytes]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_{rx-data}^f$</td>
<td>RX DATA frame</td>
<td>16</td>
<td>178</td>
<td>87</td>
</tr>
<tr>
<td>$E_{tx-ack}^f$</td>
<td>TX ACK frame</td>
<td>16</td>
<td>106</td>
<td>33</td>
</tr>
<tr>
<td>$E_{rx-data}^f$</td>
<td>RX DATA frame</td>
<td>98</td>
<td>187</td>
<td>90</td>
</tr>
<tr>
<td>$E_{tx-ack}^f$</td>
<td>TX ACK frame</td>
<td>98</td>
<td>79</td>
<td>33</td>
</tr>
<tr>
<td>$E_{listen}^f$</td>
<td>Idle listening</td>
<td>16</td>
<td>138</td>
<td>-</td>
</tr>
<tr>
<td>$E_{comp}^f$</td>
<td>Computation</td>
<td>-</td>
<td>628</td>
<td>-</td>
</tr>
<tr>
<td>$E_{tx}^f$</td>
<td>RX DATA + TX ACK</td>
<td>16</td>
<td>284</td>
<td>120</td>
</tr>
<tr>
<td>$E_{rx}^f$</td>
<td>TX DATA + RX ACK</td>
<td>98</td>
<td>266</td>
<td>123</td>
</tr>
</tbody>
</table>

bearing the ping response, an example of which is shown in Fig. 4.a.

- Slot 52 (time offset 1040 ms) is configured in the responder as a shared TXRX cell, and is devoted to communication with its children. However, as this mote in our setup is a leaf (i.e., it has no children) the cell remained unused in the experiment.

Experimental results related to power consumption are reported in Table 3. They were obtained by performing a numerical integration on the experimental samples included in the above plots (plus other samples not reported for space reasons), and by multiplying the resulting area, which refers to an overall electric charge in microcoulombs (µC), by the supply voltage of the mote (3 V), in order to obtain the power consumption in microjoule (µJ).

In particular, the quantity $E_{comp}^f$ refers to the power consumption when no transmission or reception are performed within the slot, i.e., the global consumption of the mote excluding operations of the network component. Such a quantity corresponds to the rectangular area at the bottom of Fig. 4.d filled with a continuous-green-lines pattern and, for a time slot lasting 20 ms, it is about 628 µJ. This value is noticeably higher than for other kinds of motes. For instance, in [53] a similar analysis was performed for motes based on the STM32F103RB 32-bit microcontroller and the Atmel AT86RF231 radio chip. In that case, the power consumption (obtained by multiplying the charge in microcoulomb reported in the paper by 3 V) was about 113.4 µJ. The abnormally high power consumption we obtained in our setup depends essentially on the fact that OpenMote B devices, under several respects, are still prototypes, and the software they run (OpenWSN) is not optimized for energy saving yet (e.g., by switching the CPU to deeper sleep states when no operations are needed).
TABLE 4. Experimental results about the influence of \(N_{\text{slot}}\) on latency, reliability, and power consumption (measures on real devices).

<table>
<thead>
<tr>
<th>(N_{\text{slot}})</th>
<th>(d_{\text{min}})</th>
<th>(d_{\text{avg}})</th>
<th>(d_{\text{max}})</th>
<th>(n_{\text{tra}})</th>
<th>(\mu_d)</th>
<th>Max(\epsilon)</th>
<th>(P_{\text{lost}})</th>
<th>(1 - \epsilon_{\text{pkt}})</th>
<th>(f_{\text{tra}})</th>
<th>(f_{\text{listen}})</th>
<th>(P)</th>
<th>(f_{\text{tra}})</th>
<th>(f_{\text{listen}})</th>
</tr>
</thead>
<tbody>
<tr>
<td>11</td>
<td>0.212</td>
<td>0.409</td>
<td>0.194</td>
<td>1.231</td>
<td>1.438</td>
<td>2.34</td>
<td>0.399</td>
<td>7.040</td>
<td>0.0</td>
<td>0.148</td>
<td>12-nines</td>
<td>2.00</td>
<td>0.907</td>
</tr>
<tr>
<td>31</td>
<td>0.491</td>
<td>0.982</td>
<td>0.431</td>
<td>2.301</td>
<td>3.419</td>
<td>2.27</td>
<td>0.969</td>
<td>19.840</td>
<td>0.0</td>
<td>0.119</td>
<td>14-nines</td>
<td>1.91</td>
<td>32.06</td>
</tr>
<tr>
<td>51</td>
<td>0.258</td>
<td>1.024</td>
<td>0.649</td>
<td>3.007</td>
<td>3.054</td>
<td>2.25</td>
<td>1.021</td>
<td>32.640</td>
<td>0.0</td>
<td>0.110</td>
<td>15-nines</td>
<td>1.88</td>
<td>19.41</td>
</tr>
<tr>
<td>91</td>
<td>0.497</td>
<td>1.741</td>
<td>1.046</td>
<td>4.861</td>
<td>5.397</td>
<td>2.25</td>
<td>1.858</td>
<td>58.240</td>
<td>0.0</td>
<td>0.110</td>
<td>15-nines</td>
<td>1.87</td>
<td>10.80</td>
</tr>
<tr>
<td>101</td>
<td>0.352</td>
<td>2.046</td>
<td>1.588</td>
<td>8.764</td>
<td>10.457</td>
<td>2.28</td>
<td>1.936</td>
<td>64.640</td>
<td>0.0</td>
<td>0.124</td>
<td>14-nines</td>
<td>1.95</td>
<td>9.70</td>
</tr>
<tr>
<td>151</td>
<td>2.877</td>
<td>5.036</td>
<td>1.755</td>
<td>8.846</td>
<td>14.557</td>
<td>2.25</td>
<td>5.135</td>
<td>96.640</td>
<td>0.0</td>
<td>0.110</td>
<td>15-nines</td>
<td>1.85</td>
<td>6.44</td>
</tr>
<tr>
<td>201</td>
<td>0.726</td>
<td>4.216</td>
<td>2.880</td>
<td>12.131</td>
<td>14.050</td>
<td>2.36</td>
<td>4.193</td>
<td>128.640</td>
<td>0.0</td>
<td>0.153</td>
<td>12-nines</td>
<td>1.97</td>
<td>4.78</td>
</tr>
</tbody>
</table>

The other quantities reported in the table refer to the network component only. For instance, the values of \(E_{\text{rx, data}}\) and \(E_{\text{tx, ack}}\) were obtained through numerical integration of the areas filled with red-dashed-lines and blue-horizontal-dashed-lines patterns in Fig. 4. d. respectively. Starting from the consumption related to DATA and ACK frames, the quantities \(E_{\text{rx}} = E_{\text{rx, data}} + E_{\text{rx, ack}}\) and \(E_{\text{tx}} = E_{\text{tx, data}} + E_{\text{tx, ack}}\) can be obtained, which, for a confirmed frame exchange, correspond to the consumption on the receiver side (RX DATA + TX ACK) and on the transmitter side (TX DATA + RX ACK), respectively.

To emulate application-level request/response exchanges (as those performed by CoAP), we used the ping utility. In all the experiments, the size of the payload included in ping packets was set to 30 bytes. These packets are encoded using the rules of the IEEE 802.15.4 standard, which leads to the frame sizes reported in Table 3 (that also include the physical preamble). Since in our setup we considered the responder (leaf node), \(E_{\text{rx}}\) is associated to an ICMP echo request packet while \(E_{\text{tx}}\) is associated to an ICMP echo reply packet.

V. EXPERIMENTAL RESULTS

Two sets of experiments were performed to analyze the effects of the most relevant protocol parameters on reliability, power consumption, and latency. In particular, we evaluated what happens when either the length of the slotframe or the maximum number of allowed tries are varied.

The WSN under test is composed of two nodes (OpenMote B devices), and is exactly the same as the setup used for evaluating power consumption in Section IV-A. This overly simplified configuration does not limit validity of results. In fact, concerning data exchanges, the TSCH matrix permits to partition the whole traffic into independently managed cells according to a known and configurable schedule. The only additional complexity when dealing with multi-level networks is that, due to the wider coverage of the network, the frame error probability \(\epsilon\) on distinct links may differ, and (4) only provides an aggregated value for it. The ping generation period (that corresponds to \(T_{\text{app}}\)) was set to 120 s, and every experiment lasted 4 hours. Therefore, the number of samples collected in each experiment is \(N_{\text{sam}} = 120\).

To emulate a harsh environment, four interfering IEEE 802.11 stations were placed near the two OpenMote B devices to inject a configurable amount of traffic on air, which adds to the background traffic generated by Wi-Fi networks deployed in nearby offices and labs. So that the injected traffic can affect all the 16 channels defined by IEEE 802.15.4 in the ISM band (from 2.405 to 2.480 GHz), remembering that the width of an OFDM channel in IEEE 802.11 is 20 MHz, we configured four access points (AP) to operate on channels 1 (2.412 GHz), 5 (2.432 GHz), 9 (2.452 GHz) and 13 (2.472 GHz), respectively, and associated each interfering station to a different AP. Details about inner operation of interferers can be found in [17]. Basically, every interfering station executes a finite state machine with two states, inactive and active. In the active state a burst of packets is generated. The number of packets within the burst is selected randomly according to a truncated exponential distribution: on average, 100 packets (but no more than 500) are sent. Packets within the burst are generated periodically with period 400 \(\mu\)s, and their size is 1500 B. After the burst the interfering station enters the inactive state, where it stops transmitting for a random time (gap) whose duration follows a truncated exponential distribution with mean 560 ms. The maximum duration of the inactive state is limited to 20 s.

A. PERFORMANCE VS. SLOTFRAME LENGTH

In the first set of experiments we analyzed the impact of the number \(N_{\text{slot}}\) of slots in a slotframe on the performance indicators analyzed in Section III. In particular, this parameter was varied between 11 and 201 (the default value in OpenWSN is \(N_{\text{slot}} = 101\)). Motes were restarted at the beginning of every experiment. This is unavoidable, because modifying \(N_{\text{slot}}\) requires the operating system to be recompiled and reloaded on every mote, which implies a new network formation and hence a new TSCH matrix. For this reason, each experiment is characterized by a different value of \(d_{\text{min}}\). The other parameters of the network were kept at their default value, and in particular \(N_{\text{tries}} = 16\).

Results of the experimental campaign are reported in Table 4. As expected, smaller values of \(N_{\text{slot}}\) improve network responsiveness: if \(N_{\text{slot}} = 11\) the measured maximum latency is 1.438 s, whereas for \(N_{\text{slot}} = 201\) it grows up...
TABLE 5. Experimental results about the influence of $N_{\text{tries}}$ on latency, reliability, and power consumption (measures on real devices).

<table>
<thead>
<tr>
<th>$N_{\text{tries}}$</th>
<th>$d_{\text{min}}$</th>
<th>$\mu_d$</th>
<th>$\sigma_d$</th>
<th>$d_{\text{99}}$</th>
<th>$d_{\max}$</th>
<th>$n_{\text{tra}}$</th>
<th>$\mu_d$</th>
<th>$\text{Max}_d$</th>
<th>$P_{\text{lost}}$</th>
<th>$\epsilon$</th>
<th>$1 - e^{\epsilon \text{pkt}}$</th>
<th>$P_{\text{tra}}$</th>
<th>$f_{\text{tra}}$</th>
<th>$f_{\text{listen}}$</th>
<th>$P$</th>
<th>$f_{\text{tra}}$</th>
<th>$f_{\text{listen}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>0.496</td>
<td>1.851</td>
<td>1.015</td>
<td>4.441</td>
<td>5.377</td>
<td>2.17</td>
<td>1.861</td>
<td>8.080</td>
<td>0.017</td>
<td>0.9693</td>
<td>0.98154</td>
<td>1.82</td>
<td>9.71</td>
<td>144.1</td>
<td>1.82</td>
<td>9.71</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>0.342</td>
<td>1.853</td>
<td>1.272</td>
<td>6.066</td>
<td>6.090</td>
<td>2.24</td>
<td>1.850</td>
<td>16.160</td>
<td>0.00</td>
<td>0.1102</td>
<td>0.99971</td>
<td>1.88</td>
<td>9.71</td>
<td>144.3</td>
<td>1.87</td>
<td>9.71</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>0.387</td>
<td>2.031</td>
<td>1.323</td>
<td>6.906</td>
<td>7.447</td>
<td>2.32</td>
<td>2.048</td>
<td>24.240</td>
<td>0.00</td>
<td>0.1388</td>
<td>0.99999</td>
<td>1.93</td>
<td>9.70</td>
<td>144.5</td>
<td>1.93</td>
<td>9.70</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>0.726</td>
<td>2.320</td>
<td>1.558</td>
<td>8.255</td>
<td>9.890</td>
<td>2.27</td>
<td>2.285</td>
<td>32.320</td>
<td>0.00</td>
<td>0.1197</td>
<td>7-nines</td>
<td>1.92</td>
<td>9.70</td>
<td>144.5</td>
<td>1.89</td>
<td>9.71</td>
<td></td>
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<tr>
<td>16</td>
<td>0.352</td>
<td>2.046</td>
<td>1.588</td>
<td>8.764</td>
<td>10.457</td>
<td>2.28</td>
<td>1.936</td>
<td>64.640</td>
<td>0.00</td>
<td>0.1244</td>
<td>14-nines</td>
<td>1.95</td>
<td>9.70</td>
<td>144.6</td>
<td>1.90</td>
<td>9.71</td>
<td></td>
</tr>
</tbody>
</table>

Increasing the retry limit had limited effects on latency and power consumption, because the frame error probability $\epsilon$ in our setup was not particularly high (about 10 – 15%). This implies that the probability to perform many repetitions in a row is small, as demonstrated by the fact that $1 - e^{\epsilon \text{pkt}}$ quickly converges to 1. As can be seen from the table, all statistics that refer to the latency (including $\mu_d$, $\sigma_d$ and $d_{\text{99}}$) are negatively affected by an increase of the retry limit. It can be observed the good match between the mean value $\mu_d$ of the measured latency and its expected value $\mu_d$. Also the measured maximum latency $d_{\max}$ increased from 5.377 s to 10.457 s. However, it is worth noting that this quantity is not statistically reliable because of the limited number of samples. In fact, the worst-case latency Max$_d$ ranges in theory from 8.080 s when $N_{\text{tries}} = 2$ to 64.640 s when $N_{\text{tries}} = 16$.

The effects of $N_{\text{tries}}$ on power consumption are mostly negligible. In particular, $P$ lay in the range between 144.1 $\mu$W and 144.6 $\mu$W. This is due to two reasons: first, with the parameters we selected for the network and the application, consumption mainly depends on idle listening; second, multiple retries are only performed when frame transmission repeatedly fails, which is an unlikely event in our setup.

VI. PRACTICAL APPLICATION CONTEXTS

The results provided by the network model were found to be comparable with measurements obtained from real devices. Hence, the model can be profitably used alone (i.e., without a real setup) to better investigate the effect of parameters $N_{\text{slot}}$ and $N_{\text{tries}}$ on performance indicators in specific operating conditions. As the final part of this article, four experiments were carried out to assess the performance of a real setup in specific application contexts that demand high reliability, low latency, and low power consumption, respectively.

A. LEVERAGING THE MATHEMATICAL MODEL

The model was used to analyze the behavior of TSCH in the case the frame error probability $\epsilon$ is increased up to 0.4, this denoting a quite hostile environment. The value of $d_{\text{min}}$ depends on the configuration of the TSCH matrix, but for our analysis it is not so relevant, because it only causes a shift on the time-axis (latency offset). For this reason, we set $d_{\text{min}} = 500$ ms for all the plots shown in the figure.

Initially, the number of slots in a slotframe was varied between 11 and 201. Results are reported in Plot 1 of...
Fig. 5. For calculating $P$ we used (7), where the value $\hat{P}$ is obtained from (17). As expected, the average latency, obtained from (18), increases linearly with $N_{\text{slot}}$, while power consumption decreases according to an inverse proportionality law. When $N_{\text{slot}}$ is greater than $\sim 58$, power consumption falls below $250 \, \mu W$. At the same time, the average latency exceeds $2.6 \, s$. Decreasing $N_{\text{slot}}$ well below such threshold allows a consistent reduction of latency but, due to the increase in power consumption, motes should be probably connected to an external power supply.

Plots 2 and 3 of Fig. 5 are obtained by varying $N_{\text{tries}}$ from 1 to 16 for Plot 1, $N_{\text{slot}} = 101$ for Plot 2 and Plot 3. In both cases the shape of the plot is seemingly the same but, in terms of the magnitude of the increase, the ranges in which values vary are noticeably different. The average latency $\mu_d$ in Plot 2 and the power consumption $P$ in Plot 3. In both cases the shape of the plot is seemingly the same but, in terms of the magnitude of the increase, the ranges in which values vary are noticeably different. The average latency is influenced more, and increases from 1.5 s when $N_{\text{tries}} = 2$ to values slightly above 4 s when $N_{\text{tries}} \geq 5$. Instead, in the very same conditions, power consumption grows from 142 mW to 148 mW, which is indeed a modest increase. This is due to the fact that, in the considered operating conditions, the most part of energy is spent for idle listening and initial transmission attempts (including the very first retries possibly performed for each frame). On the contrary, only a limited contribution is related to the additional retransmissions made available by increasing the retry limit, since a small fraction of frames experience many repeated failures.

Summing up, increasing $N_{\text{slot}}$ has a positive effect on power consumption, a negative effect on latency, and no effects on reliability. Instead, increasing $N_{\text{tries}}$ has a positive effect on reliability, a negative effect on latency, and a slight negative effect on power consumption (practically negligible for the typical values of the frame error probability). In the following, some working points of interest were identified from the previous plots and analyzed by means of an extensive experimental campaign on real hardware.

**B. EVALUATION OF RELEVANT CONFIGURATIONS**

As stated in the introduction, WSNs are exploited in a plurality of application contexts with very different (and often conflicting) requirements. We identified four sample configurations for a TSCH network, each of which suits the needs of some specific context. They are denoted *default*, high reliability, low latency, and low power consumption, and are characterized by specific values for $N_{\text{slot}}$ and $N_{\text{tries}}$.

The *default* configuration refers to out-of-the-box Open-WSN devices. To find suitable values for the network parameters of the other configurations, we started from the plots in Fig. 5, re-evaluated for $\epsilon = 0.13$, which more closely resembles the frame error probability typically observed in our experimental environment. Results are reported in Fig. 6. Then, three reasonable working points were sought on the plots, aimed to optimize every one of the performance indicators (reliability, latency, or power consumption) without penalizing excessively the others.

The effect of separately increasing/decreasing each parameter (either $N_{\text{slot}}$ or $N_{\text{tries}}$ is varied in every plot) is shown using underlined labels. It is worth remarking that working points in the figure and configurations are not the same. For example, the working point in Plot 4 labeled “lower latency”, obtained by reducing $N_{\text{slot}}$ from 101 to 11, does not correspond to the low latency configuration. In fact, in the latter case the value of $N_{\text{tries}}$ was additionally decreased from 16 to 3, to lower the maximum latency further—see equation (14). As will be shown, there is not an optimal setting for $N_{\text{slot}}$ and $N_{\text{tries}}$ that suits all application contexts, because improving a performance indicator unavoidably worsens at least one of the others.

In detail, the four configurations we considered are:

- **Default** ($N_{\text{slot}} = 101, N_{\text{tries}} = 16$): this configuration represents the default out-of-the-box setting of a WSN when motes are based on the OpenWSN operating system, and constitutes a balanced trade-off among power consumption, reliability, and latency. In the following, it will be used as the baseline.
- **High reliability** ($N_{\text{slot}} = 101, N_{\text{tries}} = 24$): this configuration is characterized by a reliability level higher than the default case. In particular, 8 additional retries were granted to every frame transmission ($N_{\text{tries}}$ is increased from 16 to 24).
Influence of $N_{\text{slot}}$ and $N_{\text{tries}}$ on reliability, power consumption, and latency, evaluated using the proposed network model ($\epsilon = 0.13$, $N_{\text{tries}} = 16$ for Plot 4, $N_{\text{slot}} = 101$ for Plot 5 and Plot 6). Effects of moving working points—marked with solid red circles (•)—away from the default configuration—marked with empty red circles (◦)—are suitably labeled.

**TABLE 6.** Latency, reliability, and power consumption, measured on real devices, related to four configurations (characterized by different values of $N_{\text{slot}}$ and $N_{\text{tries}}$) targeted to different application contexts.

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Condition</th>
<th>$N_{\text{slot}}$</th>
<th>$N_{\text{tries}}$</th>
<th>$d_{\text{min}}$</th>
<th>$\mu_d$</th>
<th>$\sigma_d$</th>
<th>$d_{\text{max}}$</th>
<th>$\text{Max}_d$</th>
<th>$P_{\text{lost}}$</th>
<th>$\epsilon$</th>
<th>$1 - e^{\text{pkt}}$</th>
<th>$f_{\text{tra}}$</th>
<th>$f_{\text{listen}}$</th>
<th>Power Consumption</th>
</tr>
</thead>
<tbody>
<tr>
<td>Default</td>
<td></td>
<td>101</td>
<td>16</td>
<td>0.528</td>
<td>2.115</td>
<td>1.310</td>
<td>6.579</td>
<td>11.049</td>
<td>64.640</td>
<td>0.0</td>
<td>0.125</td>
<td>14-nines</td>
<td></td>
<td></td>
</tr>
<tr>
<td>High Reliability</td>
<td></td>
<td>101</td>
<td>24</td>
<td>1.470</td>
<td>3.090</td>
<td>1.320</td>
<td>7.450</td>
<td>9.360</td>
<td>96.960</td>
<td>0.0</td>
<td>0.132</td>
<td>20-nines</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Low Latency</td>
<td></td>
<td>11</td>
<td>3</td>
<td>0.159</td>
<td>0.336</td>
<td>0.135</td>
<td>0.780</td>
<td>1.023</td>
<td>1.320</td>
<td>0.0042</td>
<td>0.142</td>
<td>0.9942</td>
<td>126.24</td>
<td></td>
</tr>
<tr>
<td>Low Power Cons.</td>
<td></td>
<td>201</td>
<td>16</td>
<td>2.565</td>
<td>5.535</td>
<td>2.461</td>
<td>13.637</td>
<td>22.366</td>
<td>128.640</td>
<td>0.0</td>
<td>0.112</td>
<td>14-nines</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Default (15-days)</td>
<td></td>
<td>101</td>
<td>16</td>
<td>0.522</td>
<td>2.114</td>
<td>1.289</td>
<td>6.393</td>
<td>12.382</td>
<td>64.640</td>
<td>0.0</td>
<td>0.126</td>
<td>14-nines</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- **Low latency** ($N_{\text{slot}} = 11$, $N_{\text{tries}} = 3$): this configuration is targeted to applications demanding low latency. In this case, $N_{\text{slot}}$ was reduced by one order of magnitude (from 101 to 11), which lowers all statistical indices about latency (including the average and maximum values), and $N_{\text{tries}}$ was set to 3 to provide stricter bounds on the worst-case latency.

- **Low power consumption** ($N_{\text{slot}} = 201$, $N_{\text{tries}} = 16$): this configuration is conceived for those applications where batteries on motes have to be replaced as seldom as possible. To this purpose, the value of $N_{\text{slot}}$ was doubled from 101 to 201.

An experimental campaign was carried out on real OpenMote B devices for the four above configurations, using the network setup described in Section IV-A. The duration of each experiment was set to 24 hours ($N_{\text{sam}} = 720$), and the purposely injected interfering traffic was the same as in the previous experiments. Results are reported in Table 6.

The high reliability configuration (second row in the table) is clearly characterized by an extremely low packet loss probability. Under the hypothesis that frame attempts can be modeled as Bernoulli trials, reliability $1 - e^{\text{pkt}}$ is, in theory, as high as $0.99999999999999938$, which corresponds to 20-nines. Although this parameter setting implies a tangible increase of the theoretical worst-case latency $\text{Max}_d$ with respect to the default case, both the measured latency and the power consumption were only marginally affected, as the transmission error $\epsilon$ on the channel is not excessively high.

Concerning the low latency configuration, all statistics about latency are noticeably lower than the default case. In particular, the measured maximum ($d_{\text{max}} = 1.023 \text{ s}$) is very small and quite close to the theoretical worst-case value ($\text{Max}_d = 1.320 \text{ s}$), while the average time taken to perform a request/response exchange is $\mu_d = 0.336 \text{ s}$. Unfortunately, low latency settings led to a significant increase of the measured packet losses ($P_{\text{lost}} = 0.0042 = 0.42\%$) and to a decrease of the estimated reliability ($1 - e^{\text{pkt}} = 0.9942 = 99.42\%$). As expected, power consumption is about 9 times higher than the default case, which makes this solution mostly impractical for battery-powered devices.

Finally, with the low power consumption configuration, the power consumed by motes dropped to 76.5 $\mu$W, which is about half than in the default case (144.4 $\mu$W). This is clearly due to the fact that receiving motes have to switch their radio transceivers on (to listen to the channel) less frequently. In particular, since the actual rate of packet transmissions does not vary (it only depends on the sending period $T_{\text{app}}$ of the application), $f_{\text{listen}}$ decreased from 9.71 to 4.78 occurrences of idle listening per seconds. The main disadvantage of this setting is that there is a sharp increase of the latency.

A swift characterization of the above configurations based on power consumption, reliability, and latency, is outlined in the radar charts in Fig. 7, which clearly highlight the related application contexts. Green points represent the quantity that mainly benefits from a given setting, while red points are the effects (almost always negative) that such setting implies on the other two quantities. As can be seen, optimizing all performance indicators at the same time is not possible.
To check the reliability of the statistics we obtained from experimental samples, performance evaluation for the default configuration was left running after the first 24 hours, so that the experiment lasted, on the whole, 15 days. By doing so, \( N_{\text{samples}} = 10800 \) samples were actually collected (including those used to calculate the values in the first row of Table 6). Results are reported in the last row of the table. Also in this case, no packets went lost, not even after two weeks of continuous operation, as witnessed by the fact that all ping requests succeeded. Measured latency was bounded to a maximum of 12.382 s and the 99-percentile was 6.393 s.

Results for this extended data set show a good match with those obtained over a single day, which confirms that statistics of the latter are reliable enough.

VII. CONCLUSION

In this article, a mathematical model of a TSCH-based network has been proposed, which provides three performance indicators that are relevant for WSNs: reliability, power consumption, and latency. This model relies on a few parameters that can be easily estimated from a real setup deployed in the area of interest. These parameters can then be used in a later stage to evaluate the expected network performance when some TSCH configuration parameters are varied. To provide a realistic estimation of the power consumption, we carried out a characterization of the latest version of OpenMote B motes based on measurements performed on a real setup, and the related results have been presented here.

The analysis of three relevant application contexts, characterized by specific network configuration parameters (slot-frame duration and retry limit) highlighted that reliability, power consumption, and latency are intimately connected. Therefore, it is not possible to optimize all the performance indicators at once, but their joint optimization must necessarily follow a holistic approach. TSCH proves to be a quite flexible solution, as the performance demanded by a wide range of application contexts can be easily achieved by suitably tuning these parameters. As an example we showed that, for a two-way communication where every packet performs two hops on the whole (both directions considered), in typical operating conditions it is possible to either decrease the average latency below \( \frac{1}{3} \) s, or ensure 20-nines reliability, or, finally, reduce the power consumption of the network component by half with respect to the default configuration.

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