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New Measurement Method in Drug Sensing by Direct Total-Charge Detection in Voltammetry

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Abstract—Electrochemical biosensors are promoting point-of-care and wearable instrumentation due to their high versatility in measuring human metabolites. There is a considerable number of biological compounds that can be detected and measured through voltammetry based techniques. Voltammetry some times requires peak identification and quantification that are non-trivial to be efficiently implemented by automatic instrumentation. To overcome the complexity of automatic peak estimation, we propose here an instrumentation circuit for edge-computing in pharmacology relying on an entirely novel measurement method via Total-Charge Detection in Cyclic voltammetry (TCDC). Namely, our TCDC method innovatively applies the coulometry measurement to the well-established voltammetry procedure. The proposed instrumentation accumulates the total charge exchanged in the faradaic process, exploiting a Nagaraj integrator as charge suppressor to fit the application-specific constraints. The work shows accurate simulations of the TCDC circuit on a set of experimental measures, acquired on paracetamol as benchmark drug. The proposed measurement technique and the developed circuit are compared to the peak detection method usually adopted in literature. The results demonstrate that the proposed system is a perfect trade-off between the doubled limit-of-detection and a tenfold reduction in measurement errors. At the same time, we eliminate any need for data oversampling and processing, promoting the TCDC as an efficient new measurement method for point-of-care and wearable monitoring of biological compounds.

Index Terms—Biosensor, Measurement Method, Point-of-Care, TCDC, Voltammetry Based Sensing

I. INTRODUCTION

Patient’s real-time monitoring of drug response could improve the effectiveness of medical treatments, helping to avoid over or under dosage during therapy [1]. Several methods have been proposed for detecting biological compounds in human tissue. In the pharmaceutical analysis, electrochemical techniques are widely adopted, being precise, low cost, and suitable to selectively identify a large number of compounds [2]. In particular, Voltammetry Based Sensing (VBS) techniques, like Cyclic Voltammetry (CV) and Differential Pulse Voltammetry (DPV), are amperometric sensing methods widely adopted to determine the concentration of several drugs [2], [3]. CV and DPV are required to compensate for poor stability and high variability over time of reference electrodes and reference potentials. While VBS methods exploit on-line monitoring of patients [4], [5], most of the point-of-care or wearable platforms present in literature usually calculate the drug concentration offline, instead of leveraging

on VBS techniques for direct determination of concentration. Indeed, in point-of-care and wearable system, the difficulty of automatically retrieve the final information directly by the electronics limits the application of VBS.

Typically, the VBS system consists of a sensor to measure the biological compound and an electronic unit (potentiostat) to drive and read the sensor. The sensor is typically a three electrodes electrochemical cell, composed by a Reference Electrode (RE), a Counter Electrode (CE) and a Working Electrode (WE) [6]. In order to perform a CV, the potentiostat drives a voltage ramp within a specific window depending on the target biological compound and then the potentiostat samples the current produced by the electrochemical reaction induced in the cell. Based on the shape of the so-called voltammogram (current upon the voltage), it is possible to extract information, e.g. the concentration of the drug present in the sample. One of the best features which help for the discrimination of drugs is the Redox/Oxidation current peak produced by the faradaic process [7]. To reliably detect those peaks and correctly quantify the related drugs is usually required to implement a custom digital architecture [8], adopt an operating system based processor [9], or process the information offline [10]. Unfortunately, all of those techniques require power and area demanding electronic architectures, with suitable sampling rate [11]. Those factors conflict with the edge-computing paradigm [12] needed for the connected point-of-care or wearable monitoring.

We present here a novel measurement method based on Total-Charge Detection in Cyclic-voltammetry (TCDC) instead of the full-voltammogram analysis. This approach scales down significantly the complexity at the edge-computing in drugs detection systems. The TCDC originally applies a charge measurement on the top of a standard voltammetry-based procedure to detect, through coulometry, the concentration of the target biological compound. The paper also shows a complete circuit implementation of our TCDC method to prove that it is feasible to implement it in consequent medical instrumentations. The proposed instrumentation and the new TCDC method are both validated using real data. Acquisitions with electrochemical sensors on paracetamol (N-acetyl-para-aminofenolo) are here considered as the benchmark of electrochemical determination of pharmacological drugs [13].

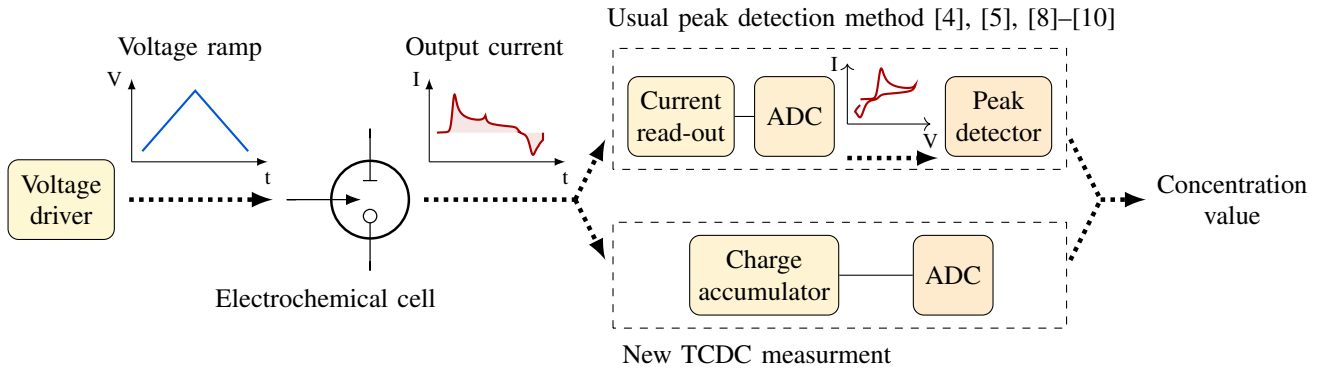


Fig. 1: In the TCDC measurement method, the total charge is acquired to determine the drug concentration, avoiding computation and oversampling typically needed by the usual peak detection method .

II. TCDC MEASUREMENT METHOD

Amperometric electrochemical detection methods usually rely on the determination of compounds by measuring the faradaic current. Differently, the TCDC measurement method presented here focuses on the total-charge exchanged in the electrochemical cell due to the faradic process. The coulometry method (the measurement of the charge) has already been applied for the determination of biological compounds [14]. However, to the best of our knowledge, the measurement of charge has never been applied in VBS method for continuous drug monitoring, since standard current sampling in CV is usually exploited [15]. Several electro-active therapeutic drugs can be involved in an electrochemical reaction [2], in which the total net charge exchanged Q_{tot} is defined as the sum of the faradaic process Q_F and the non-faradaic one Q_{NF} , as described in (1).

$$Q_{tot} = Q_F + Q_{NF} \quad (1)$$

If we approximate faradaic charge with the Faraday's laws of electrolysis and the non-faradaic charge to the double-layer capacitance effect on the interface [6], then the total charge at the electrochemical interface is:

$$Q_{tot} = nFN + C_dV \quad (2)$$

Where n is the number of electrons transferred in the reaction, F the Faraday constant, N the number of moles involved in the reaction, C_d the equivalent capacitance of the double layer, and V the potential applied at the interface. From (2) it is possible to derive the calibration equation:

$$Q_{tot} = Q_0 + S \cdot C \quad (3)$$

which relates Q_{tot} and the concentration of target analyte C . S is the Sensitivity defined as Coulomb per Molar (C/M) and Q_0 is the total non-faradaic exchanged charge. To a first approximation, Q_0 does not depend on the analyte concentration, and it can be extracted as a calibration constant.

Fig. 1 schematically explains the proposed TCDC measurement in comparison to the usual peak detection method presented in literature [4], [5], [8]–[10]. Both in the standard

CV procedure and TCDC, a voltage ramp is applied to the electrochemical cell. In CV, the system samples the output current, although, in TCDC, the instrumentation accumulates the charge to measure the total net charge exchanged during the whole electrochemical process. Therefore, the TCDC does not require any more oversampling of the current to extract a feature from its shape. The here proposed measurement system gives the concentration value directly in the form of a voltage linearly proportional to the target drug concentration. In terms of instrumentation, TCDC presents a drastic reduction in complexity, eliminating both processing and oversampling required in CV techniques, paving the road for several applications where standard microcontroller-based systems are not suitable.

III. IMPLEMENTATION

To implement the TCDC method, a charge to voltage converter is designed to accumulate the total charge produced in the electrochemical process. The output of the converter is implemented to input an ADC to get a digital value linearly proportional to the input concentration. The design of the circuit is constraint by the time involving the electrochemical reaction. For example, the time required to perform a CV-detection on paracetamol is around 10s at a Scan Rate (SR) of 0.2 V/s [4], [5], [11]. Even though a simple integrator can perform the charge-to-voltage conversion, a standard inverting integrator is not suitable for the TCDC since the long-time constant will requires area-demanding component, usually avoided in any conventional CMOS implementation. In order to reduce the capacitor sizes, attenuation techniques are applied, helping to eliminate part of the input charge [16]. In particular, the parasitic-insensitive Nagaraj integrator [17] exploits the attenuation.

A. Circuit Implementation

In order to demonstrate the principle of the TCDC method, the here proposed instrumentation is fully-based on Switch Capacitors (SC), without resistance components, planning a future CMOS implementation. Fig 2 shows the implemented TCDC instrumentation: in the first stage, A_1 operates as Nagaraj charge-attenuator, while in the second stage, A_2 operates

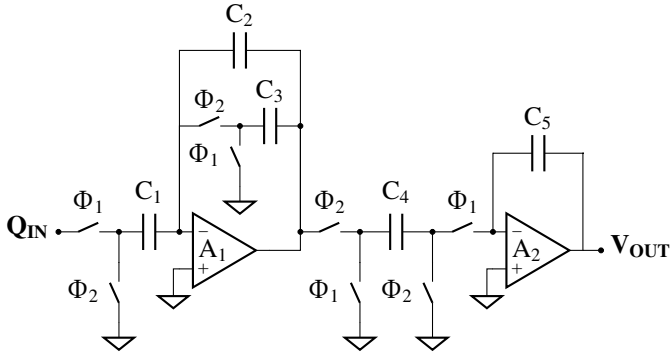


Fig. 2: TCDC instrumentation. The Nagaraj integrator (A_1) and the SC integrator (A_2) accumulate and convert the total input charge into the output voltage, during the two non-overlapped clock phase (Φ_1 , Φ_2)

as standard SC integrator. Due to the long time period of charge accumulation required by the electrochemical drug detection, the Nagaraj topology does not operate as an ideal integrator, since the long time constant suppresses its normal operating behaviour. Therefore, the proposed instrumentation relies on a two-stage circuit with the novelty of taking advantages by [17] to attenuate the input charge, and to achieve the specific purpose goal. The SCs are controlled by a two not-overlapped phase of the same clock (Φ_1 and Φ_2). During Φ_1 , the charge is transferred from C_1 to C_2 , and sampled by C_3 . In Φ_2 , C_1 withdraws the charge stored in C_2 , while C_1 redistributes its charge with C_2 .

The system is designed to fit a clock frequency of 32.768 kHz, the most widely adopted resonator in low-cost systems [18] and the supply voltage is set to 1.8 V matching the CMOS 180 nm technology for future developments. Considering the first stage, C_2 is equal to 20 fF, while C_1 and C_3 are 70 aF, value slightly above the current size limit of CMOS 180 nm technology [19], minimizing therefore the size of the circuit until the technological limit. In the second stage, C_4 is 3 fF and C_5 is 40 pF to have an equivalent resistance of 10 G Ω to separate the two stages and avoid leakages. Folded-cascode Operational Transconductance Amplifiers (OTA) implement both operational amplifiers in the design. All the values mentioned above are selected by a process variation analysis. During the simulation, tolerance values obtained by literature [19] are considered to cover extreme cases and to guarantee the compensation of process variation by clock frequency tuning. Particularly, this analysis is performed on the value of C_1 and C_3 due to their small value. Supposing a typical process variation of 50%, both capacitor values are tested in the range 70 ± 30 aF.

B. Circuit Behaviour

Fig. 3 presents the behaviour of the proposed TCDC instrumentation. For the sake of simplicity, the current produced by the sensor (top left) represents the input charge. The Nagaraj integrator suppresses partially the input charge producing an

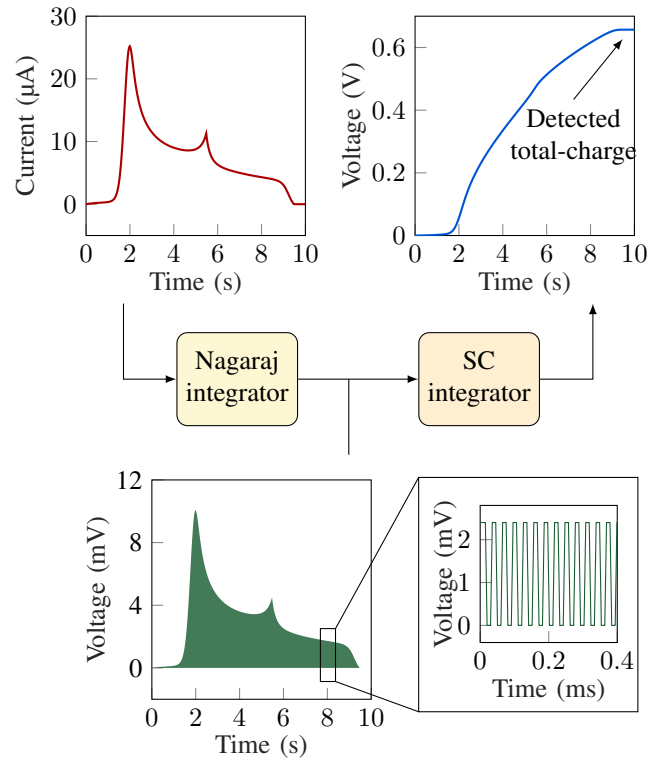


Fig. 3: TCDC circuit behaviour. The Nagaraj integrator suppresses partially the input charge while the SC integrator output-voltage is proportional to the total charge.

attenuated switching voltage signal (bottom). The SC integrator accumulates the charge from the begin of the CV procedure until its end. The maximum voltage reached by the output can be held, sampled, and fed to an ADC as the final detected value of the total charge. The voltage fits the conversion range of the ADC avoiding saturation and can be adapted to a wide range of measure tuning either statically by the component size or dynamically by the clock frequency.

IV. VALIDATION

Real data sets are collected experimentally in a lab environment to validate the TCDC method and its related instrumentation. The data are used for both analytical comparisons as well as input for simulating the implemented measurement circuit.

A. Materials and Method

Paracetamol is the drug selected as benchmark, and its powder is dissolved in Phosphate Buffer Saline (PBS) solution at pH 7.4, which acts as background electrolyte. All the chemicals are from Sigma Aldrich[®]. A Screen-Printed Electrode (SPE), namely DropSens DRP-110 composed of a carbon-based WE (4 mm of diameter), a carbon CE, and a silver RE, is immersed in the solution to detect the drug via the electrochemical reaction. The sensor is connected to the Metrohm Autolab PGSTAT 302N, driven by the software Nova 1.11, which is a lab measurement instrumentation designed

to perform high-quality and high-resolution CV procedures. Subsequent concentration steps of $50\ \mu\text{M}$ of paracetamol in the pharmacological therapeutic range of the target drug ($50:300\ \mu\text{M}$) are added to the buffer solution. The instrumentation performs each time a full CV voltammogram at a Scan Rate (SR) of $0.2\ \text{V/s}$ in the voltage range between $-0.1\ \text{V}$ and $1.1\ \text{V}$. In order to consider the experimental variability, each measure is repeated three times with a new electrode. The lab instrument samples the current produced by the sensor at a rate of around $33.3\ \text{sample/s}$ ($400\ \text{samples per CV}$) and stored.

B. Simulation and Data Analysis

In the simulation of the implemented circuit, the waveforms obtained by the lab measure are applied as input vectors. The same waveforms are also analytically processed to have a fair comparison with the usual offline methods of peak estimation. The analytical processing of the data is performed in Matlab[®], the built-in function *findpeaks* returns the height of the oxidation peak shown by the voltammogram. Meanwhile, the built-in function *trapz* mathematically estimates the total-charge considering the trapezoidal numerical integration. The electrical simulations are performed with OrCAD[®] PSpice[®], and the output voltage is sampled after $12\ \text{s}$, namely, at the end of the CV excitation.

V. RESULTS

The data collected through the experiment are here analysed to define better the capability and limitation of the proposed TCDC method. The analysis also helps to understand the performance related to different possible range of charge accumulation in the CV. After the simulation, the detecting performances of the proposed measurement circuit are compared with the analytical results obtained with the conventional peak detection method.

A. Measurement Results

Fig. 4 presents the voltammogram curves acquired by the lab instrument and the SPE electrode on the prepared paracetamol samples. The increasing of paracetamol concentration reflects on a linear increase of both oxidation and reduction peaks.

According to the definition of TCDC provided in Section II, the total charge exchanged in the faradaic process expresses the concentration of the analyte. Fig. 5 presents the current versus time acquired during the lab test at a concentration of $300\ \mu\text{M}$. Considering a standard CV is possible to define different intervals of integration in time, which are related to different ranges of charge accumulation. The range A is related to the first part of the voltammogram, where the positive-increasing voltage drives the electrochemical cell. The range A+B consider the total positive-only charge in all the voltammogram. Finally, the negative charges highlighted in C can be both considered as discharge, obtaining the total natural charge in CV (range A+B-C) or, adding a rectifier, as another additive charge, obtaining the cumulative total charge (interval

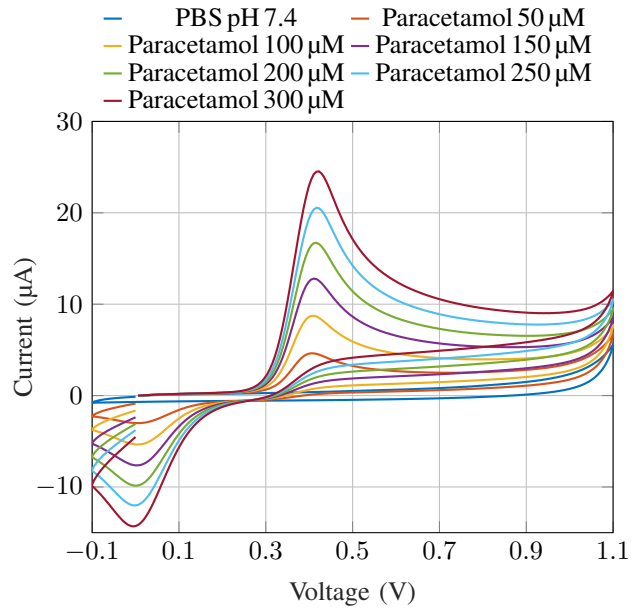


Fig. 4: Collected CV waveform during lab experiment, considering different concentration of paracetamol in the therapeutic range.

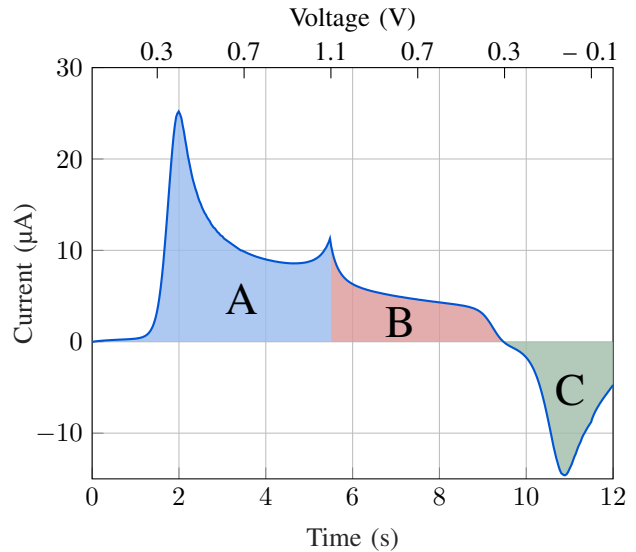


Fig. 5: Possible range of charge accumulation in applying TCDC. Positive increasing only excitation waveform (A), positive only charge (A+B), natural total charge (A+B-C), or cumulative total charge (A+B+C).

A+B+C). Quite simple instrumentations can implement all the interval.

Table I compares the possible interval of charge accumulation considering the sensitivity (as Coulomb per Molar, S , in the equation (3)), offset (Q_0 in (3)), linearity, and Limit-of-Detection (LOD). The sensitivity increases enlarging the range of integration, presenting its maximum in the interval A+B+C. The regression coefficient of the obtained calibration curve

TABLE I: Comparison between possible range of charge accumulation in TCDC measurement method.

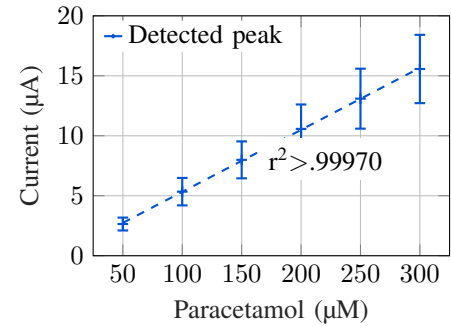
	A	A+B	A+B-C	A+B+C
Description	Increasing positive only CV	Positive-only charge	Natural total charge	Cumulative total charge
Sensitivity (nC/ μ M)	144.7 ± 1.3	207.8 ± 2.8	155.3 ± 6.5	260.7 ± 6.8
Offset (μ C)	5.27 ± 1.52	5.59 ± 2.57	3.92 ± 2.45	7.26 ± 2.70
Linearity (r^2)	.99997	.99997	.99997	.99997
LOD (μ M)	5.55 ± 0.08	5.30 ± 0.09	8.96 ± 0.38	5.34 ± 0.15

evaluates the linearity, and the increase in the accumulation time does not affect this parameter. The LOD represents the minimum concentration of drug the system can detect and, in this work, the LOD is evaluated as three times the standard deviation of the measure, divided by the sensitivity. The results demonstrate that the application of the TCDC at the interval A+B-C, which is the total charge exchanged during the CV, presents a considerable reduction of performance showing a 69% increase in the LOD. Meanwhile, the interval A+B, which is the accumulation of positive-only flowing charge, presents the best performance. For this reason, all simulations and the following considerations are then conducted considering the positive-only charge. Moreover, this choice is fully compatible with the circuit implemented and described in Section III.

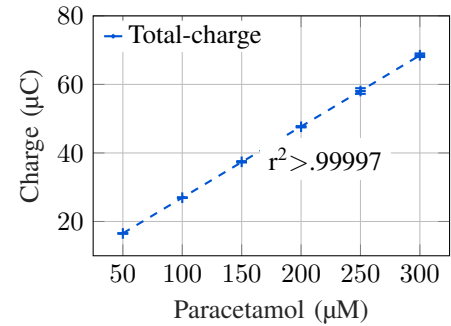
B. Simulation Results

Fig. 6 displays a comparison in the calibration curves obtained by both analytical-processing and simulation. Namely, Fig. 6a shows the resulting calibration obtained by measuring the paracetamol concentration with the extraction of the current peak. In contrast, Fig. 6b displays the analytical computation of the total-charge as integral of the current flowing in the electrochemical cell. Instead, Fig. 6c presents the calibration curve obtained by performing the TCDC circuit simulation. As visible in Fig. 6, all the method are suitable to calibrate linearly with the sensor data.

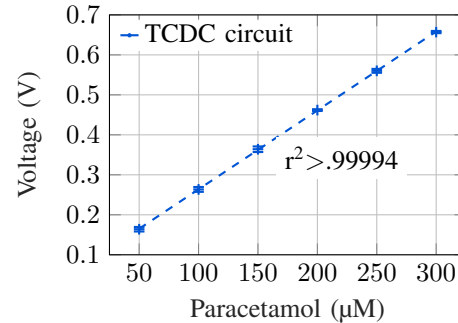
Table II compares the detection performance in term of sensitivity, offset, linearity, and LOD. The sensitivity can not be compared in absolute terms due to different outputs as obtained by the same transducer, and the same is valid for the offset. On the other hand, the linearity is the first indicator of the performance of the TCDC instrumentation since it presents an increase from 0.99970 up to 0.99994, with respect to the peak detection method. Applying the TCDC method, the LOD increases due to the trade-off between the proposed dramatic reduction in complexity and the quality of the measure. The LOD increases because TCDC collects all the charge in the CV, therefore, acquiring a higher background noise related to the not-faradaic phenomena [6]. Although, we here demonstrate that the increase of LOD can be kept under control since it is limited approximately to 2.2 times with respect to peak detection by conventional methods. The LOD always remains one order of magnitude lower than the typical minimum



(a)



(b)



(c)

Fig. 6: Calibration curves obtained by extraction of current peak (a), analytical total charge (b), and TCDC circuit simulation (c).

TABLE II: Comparison between peak detection method and TCDC, both analytical and simulation results.

	Peak detection*	Total charge*	TCDC circuit
Sensitivity	51.7 ± 9.2 nA/ μ M	207.8 ± 2.8 nC/ μ M	1.97 ± 0.03 mV/ μ M
Offset	0.15 ± 0.15 μ A	5.59 ± 2.57 μ C	66.4 ± 9.0 mV
Linearity (r^2)	0.99970	0.99997	0.99994
Limit of detection	1.93 ± 0.94 μ M	5.30 ± 0.09 μ M	6.09 ± 0.12 μ M

* Matlab[®] analytical results.

pharmacological concentration. Therefore, the quality of the measurements is not compromised. Moreover, we prove here that the proposed method significantly reduces the error on the single drug measure (defined as a statistical error, that is three times the standard deviation), clearly visible directly in Fig. 6. Namely, our approach scales the measurement error down from 17.8 % to just 1.7 % because of the higher obtained sensitivity which reflects on a higher resolution.

VI. CONCLUSION

We have introduced a novel measurement method, we called TCDC (Total Charge Detection in Cyclic Voltammetry), for drugs detection. We successfully demonstrated that the related innovative instrumentation provides better calibration (higher linearity and tenfold measurement error reduction), thanks to an edge-computing lower-complexity method which removes both processing and oversampling, trading off a slightly more than doubled LOD. Hence, the proposed method fits the requirement for point-of-care and wearable real-time monitoring. Future works will include the implementation in CMOS 180 nm technology, already considered by design, and the validation of different pharmacological compounds.

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