

Kinetic Study Based on the Carbide Mechanism of a Co-Pt/-Al<sub>2</sub>O<sub>3</sub> Fischer–Tropsch Catalyst Tested in a Laboratory-Scale Tubular Reactor

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Article

# Kinetic Study Based on the Carbide Mechanism of a Co-Pt/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> Fischer–Tropsch Catalyst Tested in a Laboratory-Scale Tubular Reactor

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**Abstract:** A Co-Pt/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> catalyst was manufactured and tested for Fischer–Tropsch applications. Catalyst kinetic experiments were performed using a tubular fixed-bed reactor system. The operative conditions were varied between 478 and 503 K, 15 and 30 bar, H<sub>2</sub>/CO molar ratio 1.06 and 2.11 at a carbon monoxide conversion level of about 10%. Several kinetic models were derived, and a carbide mechanism model was chosen, taking into account an increasing value of termination energy for  $\alpha$ -olefins with increasing carbon numbers. In order to assess catalyst suitability for the determination of reaction kinetics and comparability to similar Fischer–Tropsch Synthesis (FTS) applications, the catalyst was characterized with gas sorption analysis, temperature-programmed reduction (TPR), and X-ray diffraction (XRD) techniques. The kinetic model developed is capable of describing the intrinsic behavior of the catalyst correctly. It accounts for the main deviations from the typical Anderson-Schulz-Flory distribution for Fischer–Tropsch products, with calculated activation energies and adsorption enthalpies in line with values available from the literature. The model suitably predicts the formation rates of methane and ethylene, as well as of the other  $\alpha$ -olefins. Furthermore, it properly estimates high molecular weight n-paraffin formation up to carbon number C<sub>80</sub>.

**Keywords:** Fischer–Tropsch synthesis; Co-Pt/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>; kinetic model; carbide mechanism; cobalt; platinum

## 1. Introduction

The need for reducing the impact of industrial activities on the environment has led to the deployment of several technologies capable of favoring a fast transition towards a circular and fossil-free economy [1]. Among them, the Fischer–Tropsch Synthesis (FTS) can contribute to the transition away from fossil resources. The FTS is an exothermal reaction that converts CO and H<sub>2</sub> into intermediates suitable for synthetic fuels and chemicals by means of a solid catalyst. The reaction yields a wide range of hydrocarbons of carbon number C<sub>1</sub>–C<sub>100</sub> (i.e., paraffins, olefins, alcohols, and isomer compounds) [2,3]. These hydrocarbons can be further refined to transportation fuels such as gasoline, diesel, and jet fuels, or to more valuable chemicals, e.g., raw materials for additives used in paints, coatings, or sealants [4,5]. Regardless of the final application, it is beneficial to maximize heavy hydrocarbon production, as heavy hydrocarbons could be used as such or hydrocracked into specific lighter fractions. Moreover, the FTS can be part of Power-to-Liquid or Biomass-to-Liquid pathways. Conventional fossil-based syngas sources, such as natural gas or coal, are substituted with hydrogen produced with renewable electricity by water electrolysis, while the carbon source originates from biomass, CO<sub>2</sub> air capture, or, more likely, industrial flue gases [6–8]. Hence, captured carbon

dioxide is reduced to CO and fed to the FTS unit contributing to the mitigation of greenhouse gas emissions [9,10].

There is a dependency between product distribution and the selected catalyst. Several metals are active in FT reaction, such as nickel (Ni), ruthenium (Ru), cobalt (Co), and iron (Fe). Shafer et al. [11] recently tested different types of catalysts in a continuously stirred tank reactor, showing how each metal-based catalyst results in dissimilar product selectivity. They found out that Co and Ru catalysts were more selective towards n-paraffins and  $\alpha$ -olefins, while the Fe catalyst would be responsible for the synthesis of a higher amount of branched isomers. Similar to cobalt, Ru tends to have high activity under FTS conditions and good selectivity towards high molecular weight waxes. Disadvantages are the high price and scarcity which make Ru unfavourable for industrial applications. Nickel is an inexpensive catalyst compared to Co and Ru. However, it has the tendency to promote undesired methanation easily [12]. Fe-based catalysts are employed for the synthesis of lighter FTS products [3], while Co-based catalysts have proven to be the most effective in promoting longer chain hydrocarbons [13]. Furthermore, Co exhibits lower activity towards the water-gas-shift reaction compared to Fe catalysts. Such a reaction counteracts the benefits of the FTS in terms of CO conversion to useful products [14,15].

Activity tests and kinetic modeling can provide useful information about catalyst performance in terms of activation energies and product selectivity [16,17]. Different methodologies have been applied to perform kinetic studies on FTS and are described in the open literature. Power law expressions are widely used to describe the consumption of the syngas reactants [18–20]. Two recent studies by Moazami et al. [21] and Ostadi et al. [22] provide a summary of this typology of rate equations. Selectivity models can instead provide a higher amount of information. Specifically, they focus on the description of the FTS reactant consumption and cluster the products into two to five groups of carbon numbers [22]. For instance, Moazami et al. [23] derived a selectivity model for a Co/SiO<sub>2</sub> catalyst, studied in terms of CO conversion and selectivity towards carbon dioxide, methane, C<sub>2</sub>, C<sub>3</sub>, C<sub>4</sub>, and C<sub>5+</sub>. Finally, mechanistic models can provide a thoughtful set of information about the catalyst, ranging from reactants consumption rates to product selectivity, and can unveil evidence about the prevailing reaction mechanism evolving over the catalytic surface. Thus, numerous mechanistic models have been proposed to describe the FTS product formation [17,21,24–28]. Such kinetic models differ from each other depending on the chain initiation, the termination steps, and the hydrocarbon building units (i.e., CO insertion [17], carbide [27], enolic [29], and alkenyl [30] mechanisms). The carbide mechanism, also known as the CH<sub>2</sub> insertion mechanism, is one of the most widely used formulations. This mechanism was first proposed by Fischer and Tropsch [31], and it postulates the dissociation of CO and H<sub>2</sub> onto the catalyst surface, and later, the hydrogenation to the group CH<sub>x</sub>, the building block responsible for the chain growth [25].

Alongside the studies on reaction mechanisms, much research effort has also been spent on finding an effective description of the deviations from the Anderson-Schulz-Flory (ASF) distribution (i.e., higher methane selectivity than expected, lower ethylene selectivity, increasing chain growth probability, and decreasing olefin-to-paraffin ratio with increasing carbon number). The most commonly accepted explanations are the different activation energies for CH<sub>4</sub> and C<sub>2</sub>H<sub>4</sub> from the other paraffins and olefins [32], the accumulation of heavy compounds in the reactor system [33], and the presence of secondary reactions after termination steps [34]. This last group typically involves olefinic compounds, and the suggested mechanisms comprise of either  $\alpha$ -olefin re-adsorption and their latter hydrogenation, or chain-length dependent  $\alpha$ -olefins desorption [35–37]. In a recent kinetic study, Sonal et al. [38] investigated the performance of a bimetallic Fe-Co catalyst tested in a continuous fixed bed reactor. The authors derived alkyl and alkenyl mechanistic models up to carbon number C<sub>20</sub> based on both of the two major  $\alpha$ -olefins secondary reactions. They concluded that the chain-length dependent  $\alpha$ -olefin desorption theory proposed by Botes et al. [36] proved to be the most reliable approach in describing the non-ASF FTS behavior, being able to correctly predict the exponential dependency of olefins formation at increasing carbon numbers. Todic et al. proficiently applied the same methodology in describing a Co-Re/Al<sub>2</sub>O<sub>3</sub> catalyst tested in a stirred tank slurry reactor in the presence of a CO-insertion model [17]

and a carbide mechanistic model [39], up to compounds of carbon number  $C_{15}$ . Finally, to the best of our knowledge, only a few authors described the outcomes of their kinetic models at high carbon number values, among which Visconti et al. [16,40], who provided a mechanistic kinetic model up to carbon number  $C_{49}$ , and Kwack et al. [41] up to carbon number  $C_{40}$ .

In order to create a model for FT synthesis, which could be used to optimize catalyst behavior and select optimal process conditions, this work presents a study of an in-house fabricated cobalt-based catalyst. We derived an effective carbide mechanism kinetic model capable of describing the intrinsic behavior of the catalyst based on the chain-length  $\alpha$ -olefin desorption theory. We tested different operating FT conditions and included high molecular weight waxes in our model, with a description of the hydrocarbons formation rates up to carbon number  $C_{80}$ .

## 2. Results

### 2.1. Catalyst Characterization

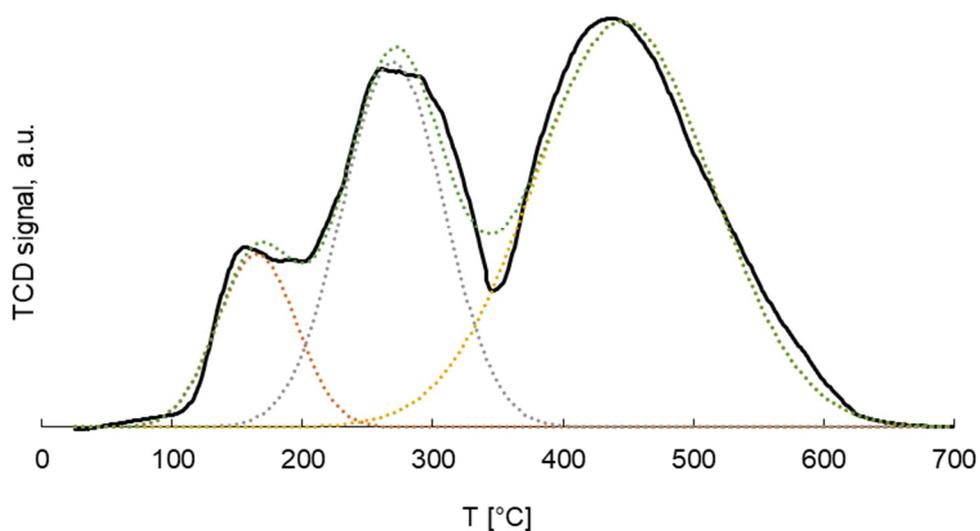
Different catalyst characterization methods were used to verify manufactured catalyst suitability for kinetic model experiments. The characterization results are summarized in Table 1 for physisorption, chemisorption, and X-ray diffraction (XRD) methods. From the prepared Co-Pt catalyst, the characterization results presented in Table 1 correspond to ones found from the literature [42–45]. These values are in the same range of the results provided by Karaca et al. [43], and Nabaho et al. [44] for similar platinum promoted cobalt catalysts. Moreover, several studies describe the effect of cobalt particle size on catalyst activity and selectivity for  $C_{5+}$  and  $CH_4$ , where a 10–50 nm particle size was found to be optimal for low  $CH_4$  formation and increased  $C_{5+}$  selectivity [42,45–47]. The performed  $H_2$ -chemisorption technique confirmed cobalt metallic dimensions ( $d_{Co^0}$ ) for the tested catalyst to be within the range of relevant literature.

**Table 1.** Catalyst characterization summary results.

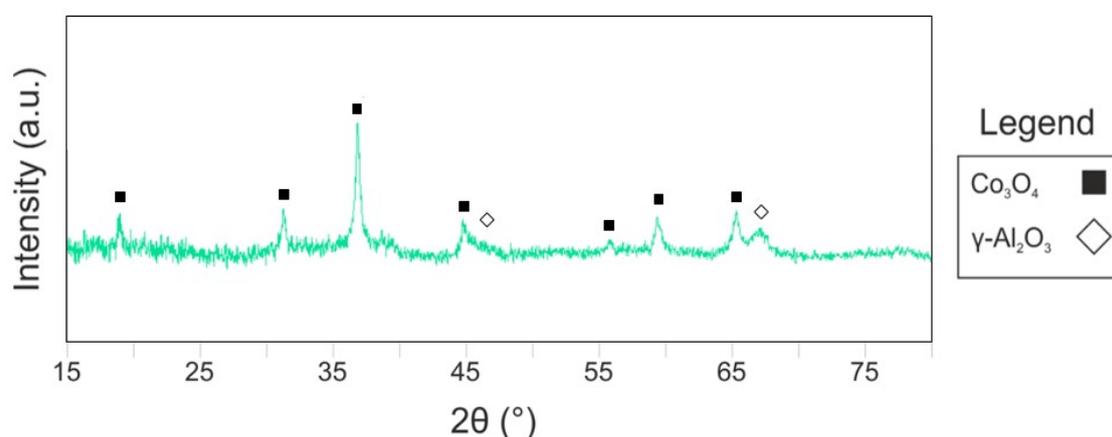
Catalyst	21%Co 0.2%Pt/ $\gamma$ - $Al_2O_3$
Dispersion (%) <sup>a</sup>	8.2
BET surface area ( $m^2/g$ ) <sup>b</sup>	53.5
Average pore diameter (nm)	11.7
Pore volume ( $cm^3/g$ )	0.15
$d(Co^0)$ <sup>c</sup> (nm)	16.6
$d(Co_3O_4)$ <sup>d</sup> (nm)	17.5

<sup>a</sup> reduced catalyst; <sup>b</sup> non-reduced catalyst; <sup>c</sup>  $H_2$ -chemisorption result; <sup>d</sup> X-ray diffraction (XRD) result.

Figure 1 presents the Temperature-programmed reduction (TPR) result profile, while Figure 2 shows the XRD pattern for the selected catalyst. From the TPR, it is possible to recognize the typical Co catalyst reduction profile, with its main peaks at around 290°C and 440°C. According to Rønning et al. [47], the first peak relates to  $Co_3O_4$  to CoO transition, and the second peak corresponds to CoO to Co metallic transition.  $H_2$ -chemisorption and XRD measurements revealed  $Co^0$  (16.6 nm) and  $Co_3O_4$  (17.5 nm) particle size correspondence to values found from the literature [42,47,48]. The  $H_2$ -chemisorption was performed on the reduced catalyst and XRD on the non-reduced catalyst. Catalyst characterization results show that the in-house fabricated catalyst is comparable to similar FTS applications and is suitable for kinetic model reaction experiments.

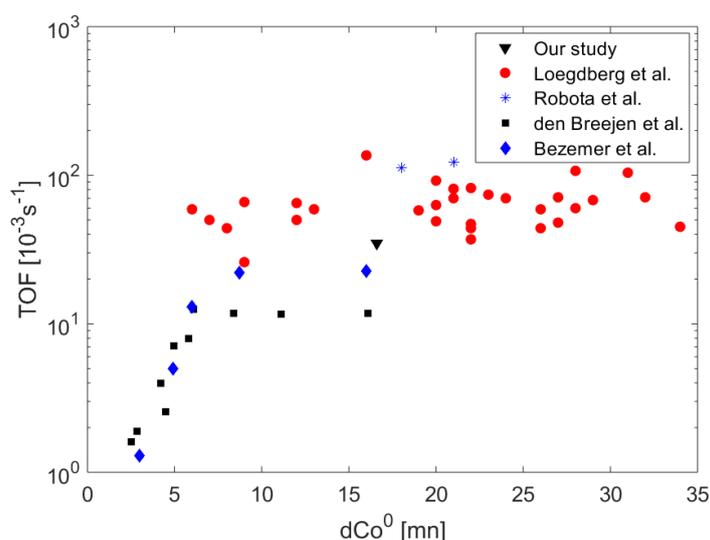


**Figure 1.** Temperature-programmed reduction (TPR) results for the studied Co-Pt/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> catalyst.



**Figure 2.** XRD diffractogram for Co-Pt/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> non-reduced catalyst.

Moreover, the intrinsic catalytic activity—based on dispersion H<sub>2</sub> chemisorption, i.e., the turnover frequency (TOF)—has been calculated and confronted with data reported in other open literature studies. At test conditions of 483 K, 30 bar, and an H<sub>2</sub>/CO molar ratio of 2.04 at the inlet of the reactor, the turnover frequency (TOF) results in  $33.6 \cdot 10^{-3} \cdot \text{s}^{-1}$ . This value is in line with literature findings and lays in the plateau of reported results for Co-catalyst. As reported, the TOF of Co-based catalysts can be found approximately constant for a  $d_{\text{Co}^0}$  above 6–10 nm at typically employed FTS conditions (Figure 3) [49,50]. This provides one other element of encouraging suitability for the catalyst employed in our study.



**Figure 3.** TOF measure (black triangle) comparison against literature reported data: red dots from Loegdber et al. [51], blue stars from Robota et al. [52], black squares from den Breejen et al. [50], blue diamonds from Bezemer et al. [45].

## 2.2. FT Mechanism

The selected kinetic model corresponds to the mechanistic model number FT-02 (Supporting material section A. The reaction path of this specific model is provided in Table 2. This model assumes dissociative hydrogen chemisorption onto the catalyst surface, followed by a slow CO adsorption on an  $H^*$  catalyst active site to  $H^*CO$ . The latter intermediate species is then subjected to a series of subsequent hydrogenation steps needed to generate  $C_nH_{2n-1}^*$  and the chain growth precursor  $C_nH_{2n}^*$ , and to release water. Afterward, the chain growth monomer interacts with adsorbed hydrogen in the form of  $H^*$ , producing a lengthening of the hydrocarbon chain. Lastly, the intermediate  $C_nH_{2n+1}$  undergoes a hydrogenation step to paraffins,  $C_nH_{2n+2}$ , or a desorption step to olefins,  $C_nH_{2n}$ .

**Table 2.** Mechanistic kinetic steps.

Reaction	Reaction Step	Constant Parameter
0	$H_2 + 2^* \leftrightarrow 2H^*$	$K_H$
1 rds	$CO + H^* \leftrightarrow H^*CO$	$k_{CO}$
	$CO + C_nH_{2n+1}^* \leftrightarrow C_{n+1}OH_{2n+1}^*$	
2	$H^*CO + H^* \leftrightarrow CH^* + OH^*$	$K_1$
	$C_{n+1}OH_{2n+1}^* + H^* \leftrightarrow C_nH_{2n-1}^* + OH^*$	
3	$C_nH_{2n-1}^* + H^* \leftrightarrow C_nH_{2n}^* + ^*$	$K_2$
4	$C_nH_{2n}^* + H^* \leftrightarrow C_nH_{2n+1}^* + ^*$	$K_3$
5	$OH^* + H^* \leftrightarrow H_2O + 2^*$	$K_4$
6 rds	$CH_3^* + H_2 \rightarrow CH_4 + H^*$	$k_{Meth}$ $k_{Par}$
	$C_nH_{2n+1}^* + H_2 \rightarrow C_nH_{2n+2} + H^*$	
7 rds	$C_2H_5^* \rightarrow C_2H_4 + H^*$	$k_{Eth}$ $k_{OI}$
	$C_nH_{2n+1}^* \rightarrow C_nH_{2n} + H^*$	

\*: catalyst surface species/vacancy.

The outcomes of a non-linear regression on the experimental data are listed in Table 3. The model provides both activation energies,  $E_i$ , and adsorption enthalpies,  $-\Delta H_{a,i}$ , higher than zero. Details about the results and model selection are provided in Discussion Section 3.1.

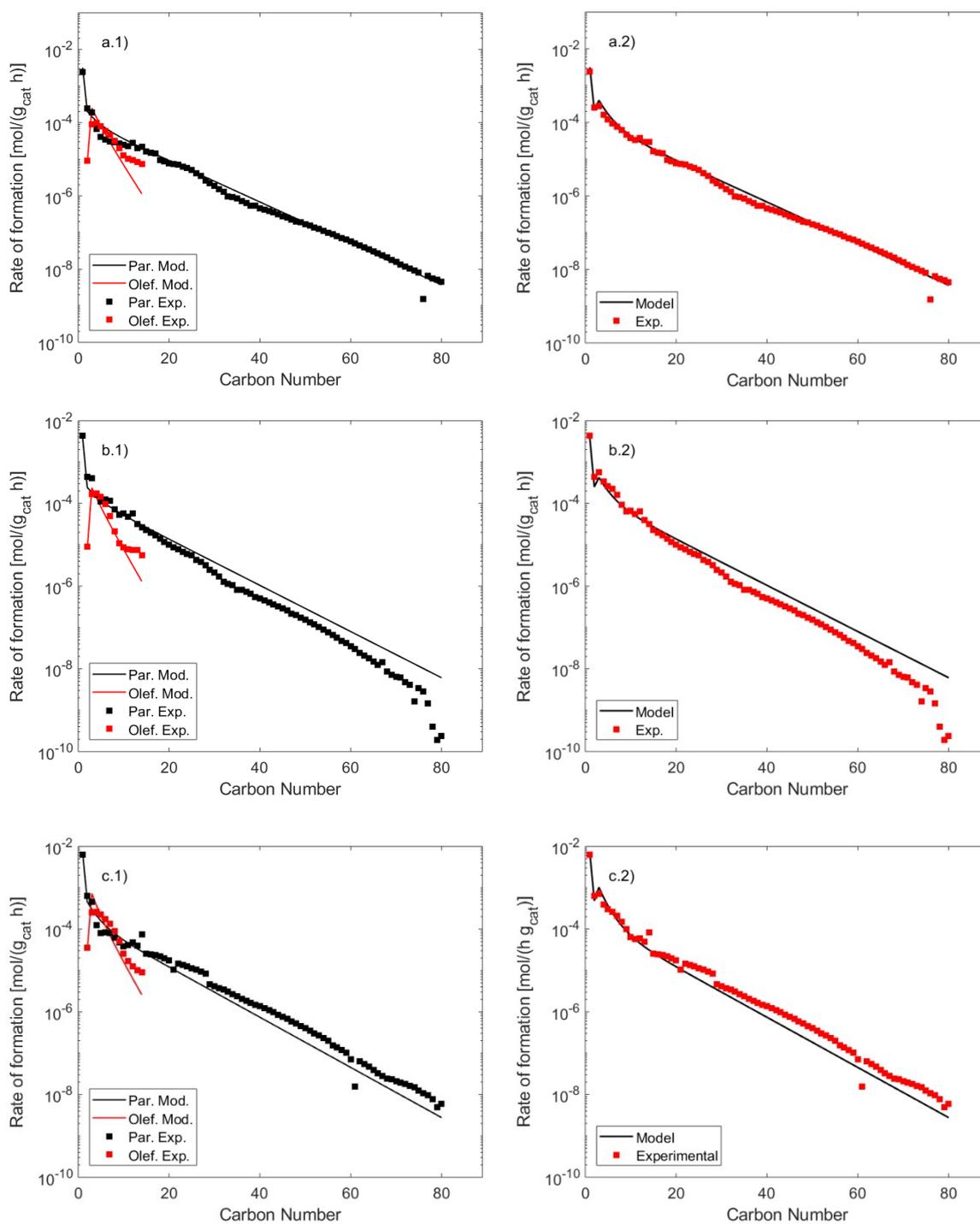
**Table 3.** Kinetic parameters obtained from the non-linear regression routine by application of the genetic algorithm for global optimum search and Levenberg–Marquardt algorithm for local optimum search.  $F_{\text{value}}(20,909,0.05) = 133.7 > F_{\text{cr.}} = 1.86$ ;  $t_{\text{cr.}}(0.05,21) = 1.64$ .

Parameter	Unit	$t_{\text{value}}$	Parameter	Unit	$t_{\text{value}}$	Lit. Range		
$A_{\text{H}}$	$1.83 \times 10^{-2}$	$\text{MPa}^{-1}$	88.8	$\Delta H_{\text{H}}$	-5.97	kJ/mol	133.8	-2.1/-25 [24,39,53]
$A_{\text{CO}}$	$9.11 \times 10^7$	$\text{mol} \cdot (\text{h g}_{\text{cat}} \text{MPa})^{-1}$	139.3	$E_{\text{CO}}$	82.39	kJ/mol	756.4	80/120 [17,24,54]
$A_{\text{Par}}$	$1.02 \times 10^8$	$\text{mol} \cdot (\text{h g}_{\text{cat}} \text{MPa})^{-1}$	58.7	$E_{\text{Par}}$	93.65	kJ/mol	767.9	60/100 [24,39]
$A_{\text{Meth}}$	$5.57 \times 10^8$	$\text{mol} \cdot (\text{h g}_{\text{cat}} \text{MPa})^{-1}$	94.1	$E_{\text{Meth}}$	89.97	kJ/mol	138.9	60/100 [24,39]
$A_{\text{Ol}}$	$6.27 \times 10^8$	$\text{mol} \cdot (\text{h g}_{\text{cat}})^{-1}$	739.6	$E_{\text{Ol}}$	95.24	kJ/mol	565.4	90/130 [24,32]
$A_{\text{Eth}}$	$8.63 \times 10^8$	$\text{mol} \cdot (\text{h g}_{\text{cat}})^{-1}$	3.2	$E_{\text{Eth}}$	112.82	kJ/mol	112.7	90/130 [24,32]
				$\Delta E$	1.249	kJ/mol(CH <sub>x</sub> )	32.7	1.1/2.15 [17,38]
$A_1$	$1.84 \times 10^2$	-	36.1	$\Delta H_1$	27.98	kJ/mol	249.3	-
$A_2$	$7.77 \times 10^2$	-	71.9	$\Delta H_2$	37.00	kJ/mol	323.1	-
$A_3$	$9.02 \times 10^3$	-	35.3	$\Delta H_3$	9.60	kJ/mol	82.5	-
$A_4$	14.3	MPa	105.7	$\Delta H_4$	13.39	kJ/mol	194.3	-

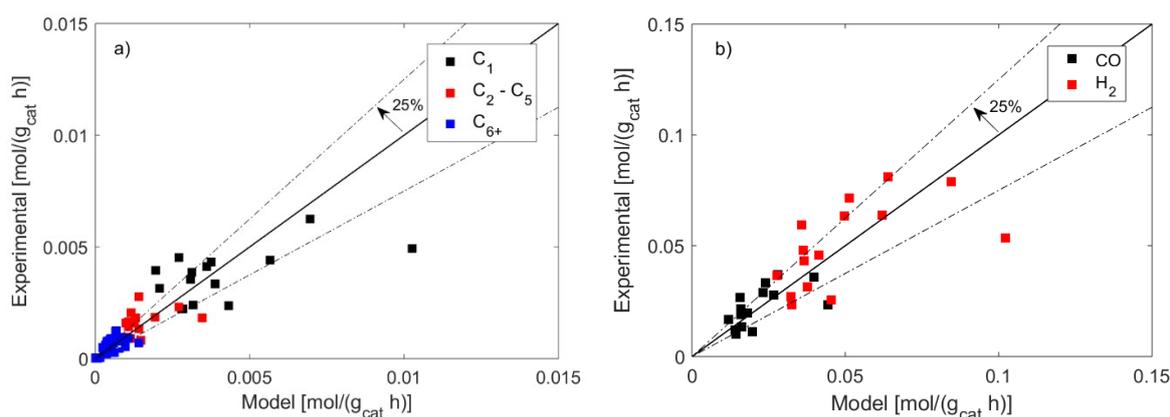
### 2.3. FT Products Distributions

The results of the hydrocarbon distribution and reactant consumption rates are presented in Figures 4 and 5, with a direct comparison of the experimental and kinetic model outcomes. Figure 4 displays the FTS distributions at different operating conditions, for both n-paraffins and  $\alpha$ -olefins. It is possible to note that the model can deliver reasonably good fits with the variation of the most influencing operative parameters. It can estimate the formation of most of the two major FTS products accounted. Moreover, it can also predict the formation rates of n-paraffins at considerably high carbon numbers (up to C<sub>80</sub>). Finally, the model properly accounts for major deviations from the ASF distribution. This corresponds to a higher methane selectivity and a lower ethylene selectivity than expected and a decreasing olefin-to-paraffin ratio with increasing carbon number, resulting in a bend of the distribution of the products at carbon numbers C<sub>15–20</sub>.

Figure 5 shows the parity plots of the model against the experimental results on both reactants consumption and product generation. The dispersed deviation lies in a range of error around  $\pm 25\%$  in the case of H<sub>2</sub> and CO reactants consumption, and between  $\pm 25\%$  and  $\pm 30\%$  for the formation rates of paraffins and olefins. These percentages of error could be associated to the constraint made on the analysed carbon species, as suggested also by both Sonal et al. [38] and Todici et al. [39] (i.e., only n-paraffins and  $\alpha$ -olefins have been considered in the data regression routine, while other minor compounds have been left out due to the small concentration found in the outlet flow). Nevertheless, the error range evaluated in this work is suitably acceptable and comes to an agreement with many mechanistic kinetic studies with error bands oscillating from  $\pm 15\%$  to  $\pm 30\%$  [21,24,38,39,55]. Finally, the rates of consumption of syngas (namely, carbon monoxide, and hydrogen) can be evaluated from the stoichiometry of the reaction, i.e., the sum of calculated rates of formation of each of the selected hydrocarbons [17,39]. This determines a 0th order dependency over the partial pressure of CO and a positive dependency around the unity with respect to H<sub>2</sub>. Such results are consistent with literature findings, where reported values of reaction orders with respect to CO and H<sub>2</sub> under FTS conditions are in the range of around (-1) to (+0.65) and (0.5) to (2) [53,56].



**Figure 4.** Experimental and calculated FTS distribution comparison for paraffins and olefins (left column) and total distribution (right column): (a)  $T = 482$  K,  $p = 20$  bar,  $H_2/CO = 2.08$ ; (b)  $T = 488$  K,  $p = 30$  bar,  $H_2/CO = 2.04$ ; (c)  $T = 503$  K,  $p = 15$  bar,  $H_2/CO = 2$ .



**Figure 5.** Experimental and calculated rates comparison: (a) products formation rates; (b) CO and H<sub>2</sub> consumption rates.

### 3. Discussion

#### 3.1. FT Kinetic Model

An activation energy  $E_{CO}$  of 82.4 kJ/mol was obtained for the initial step of CO dissociation (activation energy of the FTS process) in the kinetic parameter estimation. This results in the range of 80 to 120 kJ/mol reported by many kinetic and SSITKA studies (Steady State Isotopic Transient Kinetic Analysis) on cobalt-based catalysts for FTS reaction [24,54,57–59]. Keyser et al. found a similar value of 79.9 kJ/mol [59], Nikparsaa et al. estimated an activation energy of 88.4 kJ/mol [60], Todic et al. of 100.4 kJ/mol [39]. The adsorption heat of hydrogen of  $-5.97$  kJ/mol was found to be in the lower range of literature findings [24,53], being close to the value reported by Bhatelia et al. of  $-2.14$  kJ/mol for their cobalt catalyst [24]. Energy termination barriers of *n*-paraffins and  $\alpha$ -olefins (93.7 kJ/mol and 95.2 kJ/mol, respectively) are in good agreement with the kinetic results reported by other authors [17,21]. In addition, methane and ethylene activation energies differ from the other paraffins and olefins, as assumed in the kinetic model formulation.  $E_{Meth}$  is lower than  $E_{Par}$  as well as  $E_{Eth}$  is higher than other olefins. This outcome describes the FT distribution, which is depicted in Figure 4 and mentioned earlier. Methane activation energy,  $E_{Meth}$ , is of 89.9 kJ/mol—very close to outcomes obtained by Bhatelia et al. [24] 82.4 kJ/mol, Todic et al. [39] 63.0 kJ/mol, and Ghouri et al. [61] 83.6. The activation energy for ethylene,  $E_{Eth}$ , corresponds to 112.8 kJ/mol, in the middle of the reported value of 125.3 of Moazami et al. [21] and 103.2 of Todic et al. [17]. The energy barrier for the step of olefin desorption ( $\Delta E$ ) is 1.25 kJ/mol, in accordance with analogous studies applying the chain-length dependent  $\alpha$ -olefin desorption theory [17,38,39]. By application of Equation (1), this outcome determines a rise in the  $\alpha$ -olefin termination step barrier from 95.3 kJ/mol at carbon number C<sub>2</sub> to 113.9 kJ/mol at carbon number C<sub>15</sub>. This behavior confirms the description of Cheng et al. [62] that attributes a higher activation energy value for  $\alpha$ -olefins desorption at increasing carbon numbers. This is most likely due to a higher value of Van der Waal's attractive forces of  $\alpha$ -olefins on the catalyst surface at high carbon numbers [63]. Additionally, at a 95% confidence level, the  $F_{test}$  has a value of 133.6, higher than its critical value of 1.86. Similarly, the lowest absolute value obtained from the  $t_{test}$  (corresponding to 3.2) is higher than the critical value of 1.64. Both the  $F_{test}$  and the  $t_{test}$  allow the examination of the statistically meaningful fit and the statistical difference from zero of every kinetic parameter, respectively [64].

As mentioned, the selected kinetic model assumes hydrogenation of CO and latter CH<sub>x</sub> formation, the predominant monomer responsible for the build-up of hydrocarbons. This finds agreement with literature studies provided by Ojeda et al. [57], and more recently by Chen et al. [65], where they experimentally demonstrated the role of H-assisted routes to obtain CO dissociation for latter chain-growth. Also, Rytter et al. [66] suggested that a pool of CH<sub>x</sub> is responsible for the generation of

the FT hydrocarbons. Furthermore, our kinetic model results in the dissociation of HCOH to CH<sub>x</sub> and OH, an FTS reaction step that can also be found in the work of Visconti et al. [16]. As a matter of fact, this is one of the main potential reaction pathways to generate CH<sub>x</sub>, and SSITKA studies show that other probable reaction chains can occur over the catalyst surface [65,67].

The final selected model shows the lowest value for the MARR (Mean Absolute Relative Residual) among the competing mechanisms, with a percentage of 41.2%, just slightly higher than most reported values (in the range 20–30%). The other models did not provide satisfactory experimental data fit. The reason for this higher MARR value could be linked to the experimental data scattering found in the FTS distributions. In a recent study on a Co/Al<sub>2</sub>O<sub>3</sub> catalyst, Ghouri et al. [61] estimated a MARR value of 48.4%. They attributed this behavior to their small amount of experimental observations. Kruit et al. [68] suggested that distribution deviations could be potentially related to slight temperature gradients at the catalyst bed or particle levels. Yang et al. [69] postulated that the process of separation and condensation of heavy hydrocarbons could enwrap water in the wax matrix, determining a small overestimation of this fraction. In addition to these observations, especially with heavy FT product analysis (C<sub>80+</sub>), sample preparation methods, and analysis equipment could provide misleading interpretations and affect the MARR final value. When the experimental data were found to be highly scattered, data points had been excluded from the proposed data fitting routine (e.g., Figure 2b at carbon number range C<sub>73</sub>–C<sub>80</sub>, Figure 2a at carbon number C<sub>76</sub>, or Figure 3c at carbon number C<sub>60</sub>). Sample solvent could also have an effect on high molecular weight wax analysis. When FT products are dissolved into a solvent, light hydrocarbon constituents have a tendency to dissolve faster and thus saturate solvent prior to heavy component dissolution. It is logical to assume that these matters are likely to be interconnected to the complex nature of the FTS reaction, and further investigations beyond the scope of this study are suggested.

The kinetic model is also capable of providing information about the growth probability values of the FTS products and surface coverage values. Depending on the reaction conditions, the calculated surface coverage of hydrogen ranged between 3% and 10%, while one of all the species containing CO varies between 15% and 55%. These results are supported by literature findings, for which hydrogen and carbon monoxide surface coverage estimates are reported lower than 5–10% and between 20% and 65%, respectively [24,65]. Moreover, the model evaluates growth probability values between 0.8 and 0.93, depending on process conditions. Specifically, the growth probability of the hydrocarbons gradually increases up to an asymptotic condition that is reached in the neighborhood of the carbon number C<sub>20–25</sub>, after which the probability growth remains constant. This behavior, which is in accordance with Todić et al. [17] assessments, can be related to the decreasing influence of the  $\alpha$ -olefins term in the expression of the growth probability for high molecular weight hydrocarbons (Equation (10)) due to a higher interaction with the catalyst surface. Finally, the evolution of the growth probability explains the change in the positive bend of the FTS distribution.

## 4. Materials and Methods

### 4.1. Catalyst Preparation and Characterization

The catalyst was prepared on  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> support (Puralox SCCa 5/150) with 21.4 % wt cobalt and 0.2 % wt Pt loading. The preparation method consisted of one-step incipient wetness impregnation of an aqueous solution of cobalt nitrate (Co(NO<sub>3</sub>)<sub>2</sub> · 6H<sub>2</sub>O) and platinum nitrate (Pt(NO<sub>3</sub>)<sub>2</sub>). The prepared catalyst was dried (353 K) and calcined in a rotavapor with a flow of air at 523 K (ramp 2 K/min, GHSV 1000 ml/g<sub>cat</sub>/h). In order to remove particle sizes below 50  $\mu$ m, the catalyst batch was sieved after calcination. The particle size used in the experiments was 50–150  $\mu$ m.

After preparation, the catalyst was characterized by H<sub>2</sub>-chemisorption, TPR, XRD, and physisorption methods. A Micromeritics 3Flex 3500 was used for H<sub>2</sub>-chemisorption, TPR, and physisorption measurements. Physisorption used Brunauer-Emmet-Teller (BET) isotherm to determine surface area, and Barret-Joyner-Halenda (BJH) isotherm for pore volume and average pore diameter.

A catalyst sample (~100 mg) was outgassed before physisorption analysis at 473 K for 12 h. With H<sub>2</sub>-chemisorption, a catalyst sample (~100 mg) was reduced under hydrogen flow (1 bar, 50 ml/min) at 623 K for 16 h (ramp 2 K/min). After reduction, the catalyst bed was evacuated (0.01 bar H<sub>2</sub> pressure), the temperature decreased to 303 K, and adsorption measurements started to obtain isotherm data between 0.001 and 0.03 bar. In TPR measurements, a catalyst sample (~100 mg) was cleaned under He flow at 473 K for 2 h. The catalyst bed temperature was decreased to 303 K, and reduction was started with ramp rate 10 K/min to 1223 K in a constant flow of 10% H<sub>2</sub>/Ar (50 ml/min). An XRD diffractometer PANalytical X'Pert PRO MPD Alfa-1 instrument with CuK $\alpha$ 1 radiation was used to examine a range of 2 $\theta$  for a catalyst sample from 15° to 80° with step size 0.026° (collection time 1.25 sec). Analysis run time was 60 min and X-ray source operating at 40kV/40mA. Support characterization before catalyst preparation indicated values for the surface area (140 m<sup>2</sup> g<sup>-1</sup>), the pore volume (0.46 cm<sup>3</sup> g<sup>-1</sup>), and the pore diameter (13.2 nm). Scherrer's equation [70] was used to determine the average Co<sub>3</sub>O<sub>4</sub> crystallite thickness with cobalt oxide peak (311) at 2 $\theta$  = 36.9°.

#### 4.2. Catalyst Testing

The experiments were conducted in a tubular fixed-bed micro-reactor (PID-Micromeritics Microactivity Effi).

Figure 6 presents a scheme of the reactor system. The equipment consisted of a reactor tube and an electrically heated furnace, a wax trap (hot trap) and a liquid-liquid-gas separation unit (cold trap). The reactor tube was of the type Hastelloy C (9.1 mm i.d., and a total length of 304.8 mm), with a K-type thermoelement inserted into the catalyst bed, and a porous plate where the catalyst was deposited (pore size 20  $\mu$ m). The reactor and the wax trap were located in a temperature-controlled hotbox. The hotbox ensured isothermal conditions (373 K) for both the reactor and the wax trap. The wax trap was connected to the reactor outlet, and it was covered by an aluminum housing. The aluminum housing contained both a compressed air inlet tube and a K-type thermocouple for the trap temperature control. The wax trap temperature was set to 363 K to ensure product collection and to avoid any undesired wax fraction run away from the trap through the downstream line. After the collection of high molecular weight waxes into the wax trap, the remaining products continued to a liquid-liquid-gas separator (LLGS). The LLGS was cooled down to a temperature of 280 K by a Peltier element. At this temperature and reaction pressure applied in the separator (10 to 30 bar), both water and oil products were condensed and separated from each other inside the LLGS. The water was collected in a tank, and the oil products were sent to a sampling line for further analysis. The remaining gas fraction composed of light hydrocarbon continued from the LLGS to a gas chromatograph for on-line gas analysis. Calibrated mass flow controllers (Bronkhorst Ltd, El-flow Select F-211CV) adjusted the gas feed to the reactor. The feeding line was equipped with a check valve was to prevent backflow.

The packed bed consisted of 1 g of catalyst (particle size 50–150  $\mu$ m), evenly diluted with 1 g of inert SiC (50–150  $\mu$ m). The dilution allowed reaching a homogeneous bed temperature and distributing the heat generation due to exothermal hydrogenation. A layer of quartz wool was placed above and below the catalyst, onto the porous plate.

The catalyst reduction was done with a steady flow of pure hydrogen (50 mlN/min) for 16 h, at a reactor temperature of 773 K and atmospheric pressure. The reduction temperature was reached at a stepwise rate of 1 K/min from room temperature. After reduction, nitrogen flow was started to the reactor, and the temperature was cooled down to 493 K (both nitrogen and hydrogen at 50 mlN/min). After the temperature reached 493 K, both hydrogen and nitrogen flows were set to values applied for the test runs. The reactor was set to the desired pressure and temperature. Carbon monoxide was then slowly increased to its final flow value. Operating conditions used in the kinetic tests are summarized in Table 4. With a careful carbon monoxide addition, it was possible to avoid temperature runaway, which could lead to catalyst sintering. Despite the slow reaction start-up, the catalyst usually exhibited initial activity phase. Such an initial activity decreased over time, reaching a steady-state condition. Once the activity of the catalyst was stably indicated by a steady level of CO conversion,

useful products were continuously collected for approximately 45 hours. The experimental matrix was built to ensure that the most commonly applied operating conditions at industrial levels for Co-based FT reactors were covered [71]. The temperature was kept in a range of 478–503 K, the pressure was set between 15 and 30 bar, and the H<sub>2</sub>/CO molar ratio varied from 1.06 to 2.11. The CO conversion level was kept at the low value of 10 ± 2.5%, by adjusting the weighted hourly space velocity (WHSV) in the range between 167 to 720 mlN/min/g<sub>cat</sub>. Low CO conversion allows ensuring differential conditions inside the reactor and reduces the selectivity towards methane, which is an undesired product when targeting the synthesis of long-chain hydrocarbons [14,72].

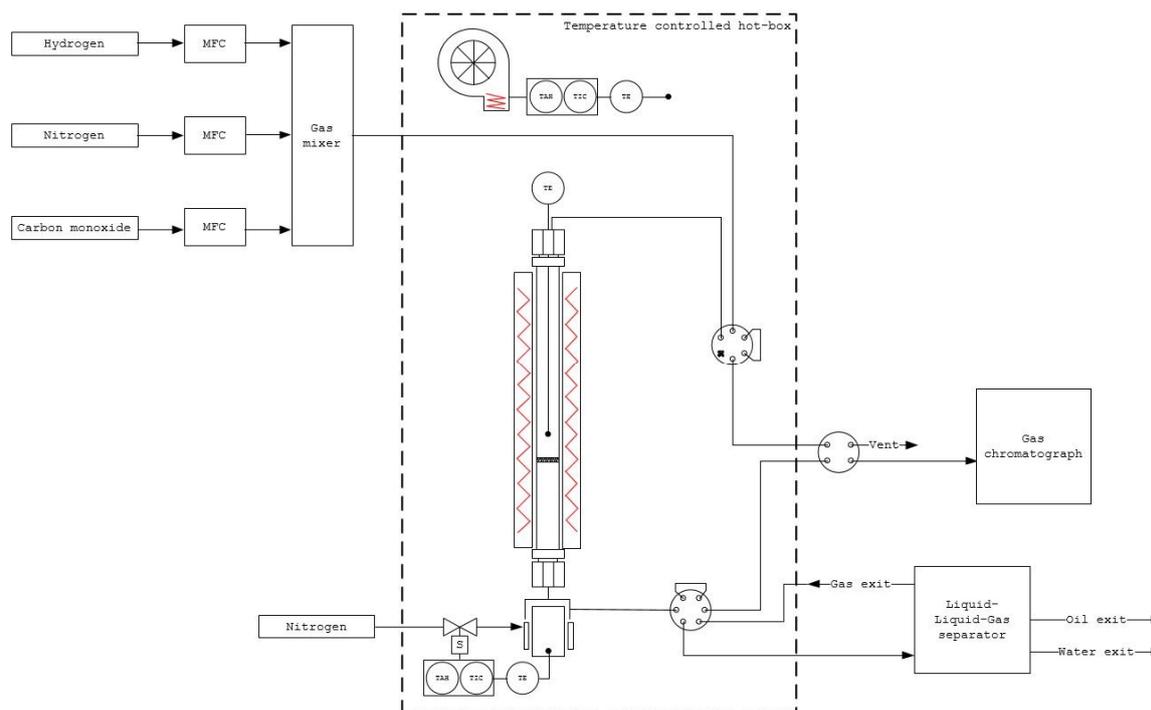


Figure 6. PID-Micromeritics tubular reactor equipment.

Table 4. Experimental conditions applied in the kinetic tests.

Temp.	Pres.	H <sub>2</sub>	CO	N <sub>2</sub>	H <sub>2</sub> /CO	X <sub>CO</sub>	WHSV
[K]	[bar,a]	[mol %]	[mol %]	[mol %]	[mol %]	[mol %]	[mlN/(min g <sub>cat</sub> )]
478	30	54%	26%	20%	2.08	6.87	188.9
488	15	63%	30%	7%	2.10	8.33	285.7
498	30	40%	36%	24%	1.11	8.50	475.0
503	15	50%	25%	25%	2.00	8.60	720.0
488	25	60%	30%	10%	2.00	8.76	400.0
488	25	45%	36%	19%	1.25	8.88	322.2
493	20	33%	31%	36%	1.06	9.53	606.1
493	25	65%	31%	4%	2.10	9.53	146.2
498	25	58%	28%	14%	2.07	10.05	682.8
482	20	50%	24%	26%	2.08	10.22	370.0
488	30	51%	25%	24%	2.04	10.67	205.8
483	25	60%	30%	10%	2.00	10.98	166.7
483	30	51%	25%	24%	2.04	11.35	196.1
483	20	46%	22%	32%	2.09	12.03	304.4
488	21	59%	28%	13%	2.11	12.42	177.9

Product analysis was carried out using a Shimadzu GC-2014 on-line gas chromatograph. The sample line was heated to 393 K to prevent condensation. CO, H<sub>2</sub>, CH<sub>4</sub>, CO<sub>2</sub>, and N<sub>2</sub> (internal standard) were analyzed with a TCD-detector and two packed columns; a Porapak-Q (1 mm i.d.,

× 1.8 m) precolumn and a Carboxen-1000 (1 mm i.d., × 2.5 m) analytical column. A 10-port valve was used to inject a sample and facilitate the backflush of heavy hydrocarbons from the precolumn. Hydrocarbons from C<sub>1</sub> to C<sub>14</sub> and C<sub>1</sub>–C<sub>9</sub> n-alcohols were analyzed using a DB-1 capillary column (i.d., 0.25 mm × 60 m × 1 μm) and an FID-detector. The analysis time was ~30 min. Response factors were determined using calibration samples. In addition to online gaseous product analysis, an offline analysis was performed for the collected oil and wax products by using a Shimadzu GC-2014 GC-system. Hydrocarbons with a carbon number from C<sub>6</sub> to C<sub>35</sub> and C<sub>1</sub>–C<sub>9</sub> n-alcohols were analyzed with an Rxi-5HT capillary column (i.d., 0.32 mm × 30 m × 0.10 μm df) and an FID-detector. High molecular weight wax analysis was performed differently as a high-temperature technique (723 K) was required. A Hewlett Packard 5890 Series II with on-column sample inlet was used for this purpose. Hydrocarbons with a carbon number ranging C<sub>10</sub> to C<sub>80</sub> were analyzed with a CP-SimDist UltiMetal capillary column (i.d., 0.53 mm × 10 m × 0.17 μm df, 1 m retention gap) and an FID-detector.

#### 4.3. Kinetic Model Development

In the present work, 11 mechanistic models were derived from a series of carbide mechanisms available in the literature [32,39,73]. Moreover, the chain-length dependency  $\alpha$ -olefins desorption theory is applied to each of the models. This theory considers that the strength of olefin adsorption on the catalyst surface increases with increasing carbon number. Hence, by application of the Evans–Polanyi relations [74], the activation energy of olefin desorption is composed of a chain-length independent term ( $E_{\text{olef}}^0$ ) and a chain-length dependent term ( $\Delta E_{\text{olef}}$ ) to account for increasing desorption energy for every monomeric group CH<sub>2</sub>. Following the Arrhenius equation, the rate constants for olefins at every carbon number  $n$  can be obtained:

$$E_{\text{olef}}^n = E_{\text{olef}}^0 + n \Delta E \quad (1)$$

$$k_{\text{olef}}^n = A_{\text{olef}} e^{-\frac{E_{\text{olef}}^n}{RT}} = A_{\text{olef}} e^{-\frac{E_{\text{olef}}^0 + \Delta E}{RT}} = k_{\text{olef}}^0 e^{n c} \quad (2)$$

$$k_{\text{olef}}^0 = A_{\text{olef}} e^{-\frac{E_{\text{olef}}^0}{RT}} \quad (3)$$

$$c = -\frac{\Delta E}{RT} \quad (4)$$

Each model was derived considering  $n$ -paraffins,  $\alpha$ -olefins, water, and unreacted H<sub>2</sub> and CO in the products stream. Elementary steps of  $n$ -paraffins and  $\alpha$ -olefins formation are rate-determining steps (RDS), while all the other steps were assumed to be at quasi-equilibrium. Methane and ethylene were considered with different rates of generation with respect to other paraffins and olefins, to account for the non-AFS distribution of the FTS products. Lastly, only the synthesis of Fischer–Tropsch products is assumed to evolve, and no water–gas shift reaction was accounted for to take place on the Co-based catalyst surface.

Every model was developed with a Langmuir–Hinshelwood–Hougen–Watson (LHHW) type reaction rate expression, with a dependency on the reactants partial pressures. In some reaction schemes, Eley–Rideal-type steps were also included, with one of the reacting molecules adsorbed and the other one in the gas phase. Hereby, we present the theoretical reaction steps and the hydrocarbons rates formulation of the mechanism of Table 2 (i.e., the final selected mechanism providing the most satisfactory experimental data fitting). The derivation of each of the kinetic models is provided in the Supporting material section A.

The formation rates of the different FT products and probability growths depending on the surface species were expressed as follows:

$$R_{\text{CH}_4} = k_{\text{Meth}} P_{\text{H}_2} [\text{CH}_3^*] \quad (5)$$

$$R_{C_2H_4} = k_{Eth} e^{2c} [C_2H_5^*] \quad (6)$$

$$R_{C_nH_{2n+2}} = k_{Par} P_{H_2} [C_nH_{2n+1}^*] \text{ for paraffins at } n \geq 2 \quad (7)$$

$$R_{C_nH_{2n}} = k_{Ol} e^{nc} [C_nH_{2n+1}^*] \text{ for olefins at } n \geq 3 \quad (8)$$

$$\alpha_1 = \frac{k_1 P_{CO}}{k_{CO} P_{CO} + k_{Meth} P_{H_2}} = \frac{[CH_3^*]}{[H^*]} \quad (9)$$

$$\alpha_2 = \frac{k_{CO} P_{CO}}{k_{CO} P_{CO} + k_{Par} P_{H_2} + k_{Eth} e^{c^2}} = \frac{[C_2H_5^*]}{[CH_3^*]} \quad (10)$$

$$\alpha_n = \frac{k_{CO} P_{CO}}{k_{CO} P_{CO} + k_{Par} P_{H_2} + k_{Ol} e^{cn}} = \frac{[C_nH_{2n+1}^*]}{[C_{n-1}H_{2n-1}^*]} \text{ } n \geq 3 \quad (11)$$

The fraction of vacant sites  $\theta_{vac}$  was evaluated from the balance equation of the different surface coverage values depending on the reaction scheme of Table 2:

$$1 = \theta_{vac} + \theta_{H^*} + \theta_{H^*CO} + \theta_{CH_3^*} + \theta_{C_2OH_3^*} + \theta_{CH^*} + \theta_{C_2H_3^*} + \theta_{OH^*} + \theta_{C_2H_5^*} + \theta_{CH_2^*} + \theta_{C_2H_4^*} + \theta_{\sum_3^N [C_nH_{2N+1}^*]} + \theta_{\sum_3^N [C_nH_{2N-1}^*]} + \theta_{\sum_3^N [C_nH_{2N}^*]} + \theta_{\sum_3^N [C_nOH_{2N-1}^*]} \quad (12)$$

$$\theta_{vac} = 1 / \left\{ 1 + \sqrt{(K_H P_{H_2})} * \left( 1 + \alpha_1 + \alpha_1 \alpha_2 + \sum_{j=3}^{n_c} \prod_{n=3}^j \alpha_n \right) + \left( \alpha_1 + \alpha_1 \alpha_2 + \sum_{j=3}^{n_c} \prod_{n=3}^j \alpha_n \right) \left[ \frac{1}{K_3} + \frac{1}{\sqrt{(K_H P_{H_2})} K_2 K_3} + \frac{P_{H_2O}}{(K_H P_{H_2})^{1.5} K_1 K_2 K_3 K_4} \right] + \frac{1}{K_4} \frac{P_{H_2O}}{\sqrt{(K_H P_{H_2})}} \right\} \quad (13)$$

The final generation rates applied in the parameter estimation for each product were given by substituting the probability growths (9)–(11) and the sites balance expression (13) into the Equations (5)–(8):

$$R_{CH_4} = k_{Meth} \alpha_1 \sqrt{(K_H P_{H_2})} P_{H_2} \theta_{vac} \quad (14)$$

$$R_{C_2H_4} = k_{Eth} e^{2c} \alpha_1 \alpha_2 \sqrt{(K_H P_{H_2})} \theta_{vac} \quad (15)$$

$$R_{C_nH_{2n+2}} = k_{Par} \alpha_1 \alpha_2 \prod_{n=3}^n \alpha_n \sqrt{(K_H P_{H_2})} P_{H_2} \theta_{vac} \text{ for paraffins at } n \geq 2 \quad (16)$$

$$R_{C_nH_{2n}} = k_{Ol} e^{nc} \alpha_1 \alpha_2 \prod_{n=3}^n \alpha_n \sqrt{(K_H P_{H_2})} \theta_{vac} \text{ for olefins at } n \geq 3 \quad (17)$$

$\alpha_N$  is the probability growth for each carbon number  $n$ ,  $k_i$ , and  $K_i$  are the rate and equilibrium constants evaluated by the model;  $P_{H_2}$ ,  $P_{CO}$ , and  $P_{H_2O}$  are the partial pressures of hydrogen, carbon monoxide, and generated water, respectively. Rate and equilibrium constants were formulated according to Arrhenius and Van't Hoff expressions:

$$k_i = A_i e^{-\frac{E_{a,i}}{RT}} \quad (18)$$

$$K_i = A_i e^{-\frac{\Delta H_i}{RT}} \quad (19)$$

where  $E_{a,i}$  are the activation energies,  $\Delta H_i$  are the reaction and adsorption enthalpies, and  $A_i$  are the pre-exponential factors.

#### 4.4. Reactor Model

The reactor was modeled as a pseudo-homogeneous plug flow reactor (PFR) described by the following ordinary differential equation (ODE) combined with the proper initial condition:

$$\frac{d\dot{n}_i}{dW_{\text{cat}}} = \sum_{j=1}^{n_{\text{react}}} \alpha_{i,j} R_{i,j} \quad (i = 1, 2, 3, \dots, N_C) \quad (20)$$

$$W_{\text{cat}} = 0, \dot{n}_i = \dot{n}_{i,\text{in}} \quad W_{\text{cat}} = W_{\text{exit}} \quad \dot{n}_i = \dot{n}_{i,\text{exit}}$$

Furthermore, the partial pressure of each reactant and product considered at the outlet of the reactor and the value of CO conversion were expressed as follows:

$$P_i = \frac{n_i P_{\text{tot}}}{\sum_{i=1}^{N_C} n_i} \quad (21)$$

$$\chi_{\text{CO}} = \frac{\dot{n}_{\text{COInlet}} - \dot{n}_{\text{COOutlet}}}{\dot{n}_{\text{COInlet}}} \quad (22)$$

In Equation (20),  $\alpha_{i,j}$  and  $R_{i,j}$  are the stoichiometric coefficient and the reaction rate of formation of the  $i^{\text{th}}$  component in reaction  $j^{\text{th}}$ , respectively.  $\dot{n}_i$  is the molar flow rate of the  $i^{\text{th}}$  component,  $W_{\text{cat}}$  is the weight of the catalyst, and  $N_C$  represents the total number of components. In Equation (21),  $P_{\text{tot}}$  is the total pressure inside the reactor. The stoichiometry of the FT reactions is presented in Table 5.

**Table 5.** Stoichiometric coefficients of the involved reactions.

Reaction	Paraffins Formation ( $n \geq 1$ )	Olefin Formation ( $n \geq 2$ )
CO	-n	-n
H <sub>2</sub>	-(2n+1)	-(2n)
C <sub>n</sub> H <sub>2n+2</sub>	1	0
C <sub>n</sub> H <sub>2n</sub>	0	1
H <sub>2</sub> O	n	n

Each model was developed, accounting for n-paraffins and  $\alpha$ -olefins. Other minor FT compounds were not considered, given their lower concentration in the product stream. Heavy waxes were considered during the development of the models, to suitably describe the distribution of the products at high carbon numbers. Only hydrocarbons with carbon number higher than C<sub>48+</sub> were excluded in the modeling process due to their marginally lower peaks detected by the GC and the constant distribution trend at higher carbon values. In detail, for each of the investigated runs, 48 paraffins and 14 olefin experimental rates were used to extrapolate the kinetic information of the catalyst. The unreacted CO and H<sub>2</sub> and the produced water were also considered at the outlet stream of the reactor. Lastly, heat and mass transfer limitations have been neglected. For mass transport limitations, Thiele modulus and Mears' criterion for intraparticle and interphase diffusions have been checked [75–77], respectively. For the energy transport limitations, the Weisz-Prater's and Mears' criteria are applied for the evaluation of possible internal temperature gradients and to check the presence of any interphase heat transport limitation, respectively [78,79] (Appendix A).

#### 4.5. Data Regression

For each of the tested mechanistic models, constant kinetic parameters were estimated by application of a non-linear least-squares minimization algorithm, which seeks to minimize the following objective function (OF):

$$\text{OF} = \sum_{i=1}^{n_{\text{search}}} \sum_{j=1}^{n_e} \left( \frac{R_{i,j}^{\text{exp}} - R_{i,j}^{\text{mod}}}{R_{i,j}^{\text{exp}}} \right)^2 \quad (23)$$

$n_{\text{search}}$  is the total number of observations (n-paraffins and  $\alpha$ -olefins),  $n_{\text{exp}}$  is the total number of experimental sets, and  $R_{\text{exp}}$  and  $R_{\text{mod}}$  the rates of formation of hydrocarbons for the experimental and model outcome, respectively. Due to the non-linearity of the objective function and the possibility of having multiple local minima, the kinetic data regression is obtained via the first step of global optimization. The global optimization outcome is then used in a second step as an initial guess for local optimization. Finally, to select the most suitable kinetic expression, the competing models were screened based on the lowest value of the mean absolute relative residual (MARR).

$$\text{MARR} = \sum_{i=1}^{n_{\text{search}}} \sum_{j=1}^{n_{\text{exp}}} \frac{|R_{i,j}^{\text{exp}} - R_{i,j}^{\text{mod}}|}{R_{i,j}^{\text{exp}}} \times \frac{1}{n_{\text{search}} n_{\text{exp}}} \times 100 \% \quad (24)$$

The global optimization has been performed via the application of the genetic algorithm, which is followed by the Levenberg-Marquardt method implementation for local optimization. Both routines have been performed on the software tool MATLAB®.

## 5. Conclusions

A kinetic study for Fischer–Tropsch synthesis (FTS) over an in-house fabricated Pt-promoted cobalt catalyst was performed. Characterization techniques were used to confirm that the manufactured catalyst had targeted physical and chemical properties. The catalyst was tested under the most commonly applied FTS reaction conditions, focusing on the production of long-chain hydrocarbons.

Several mechanistic models based on a carbide mechanism coupled with a chain-length  $\alpha$ -olefins desorption approach were derived. The selection of the model was made based on model screening by computational data regression, and the model was selected by comparing the mean absolute relative residuals. The final selected kinetic model was capable of properly describing the typical non-AFS deviations, accounting for a higher methane selectivity, low ethylene selectivity, and increasing activation energy for  $\alpha$ -olefin desorption. Moreover, this kinetic model provided a satisfactory experimental data also fit for very high hydrocarbon carbon numbers ( $C_{80}$ ).

In forthcoming activities, the authors will work on developing an improved kinetic model capable of estimating the catalyst behavior under harsher conditions. Accordingly, water and  $\text{CO}_2$  will directly be fed to the catalyst in order to study its response in the presence of a more industrial-like syngas. Ultimately, the target of our research is to formulate a comprehensive model to be suitable for the scale-up and optimization for industrial application and processes aiming at targeting long-chain hydrocarbons. The present investigation represents an important first step to reach this goal.

**Supplementary Materials:** The following are available online at <http://www.mdpi.com/2073-4344/9/9/717/s1>, Section A: derivation of the kinetic model mechanistic steps. Section B: catalyst testing, Figure B1: Products distribution data reproducibility: (a) 483K, 20bar,  $\text{H}_2/\text{CO}$  2.09,  $X_{\text{CO}}$  R1: 12.31%,  $X_{\text{CO}}$  R2: 11.96%; (b) 493K, 20bar,  $\text{H}_2/\text{CO}$  1.06,  $X_{\text{CO}}$  R1: 9.34%,  $X_{\text{CO}}$  R2: 9.2%.

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**Conflicts of Interest:** The authors declare no conflict of interest.

## Appendix A

Mass and heat transport phenomena have been investigated to ensure the kinetic regime in the development of the kinetic model. All the properties of the gas mixture have been retrieved taking into account the composition of the stream at the inlet of the reactor. Our calculations show that the given criteria are satisfied for every experimental point, and no heat and mass transfer limitations have been found.

- a. Intraparticle mass transfer limitations—Thiele modulus [75,80,81]:

$$\phi = L_c \sqrt{\frac{\rho_c R_{FT}}{D_{e,CO} C_{CO}}} < 1 \quad (A1)$$

- b. Interphase mass transfer limitations—Mears' criterion [76]:

$$\frac{R_{FT} \rho_c r_c n}{k_m C_{CO}} < 0.15 \quad (A2)$$

- c. Intraparticle heat transfer limitations—Weisz-Prater criterion [78,79]:

$$\frac{E_a}{RT} \frac{(-\Delta H_{FT}^0) R_{FT} \rho_c L_c^2}{\lambda_c T} < 0.05 \quad (A3)$$

- d. Interphase heat transfer limitations—Mears' criterion [78,79]:

$$\frac{E_a}{RT} \frac{(-\Delta H_{FT}^0) R_{FT} \rho_c L_c}{h_1 T} < 0.05 \quad (A4)$$

The additional catalyst information employed in the present study are summarized in Table A1.

**Table A1.** Additional catalyst parameters used in the simulation.

Catalyst Parameter	Value
Packed bulk density [g/l]	820
Tortuosity [–]	2
Thermal conductivity [W/(m K)]	1.02
Median particle size [m]	$7.50 \times 10^{-8}$
Characteristic length [m]	$1.25 \times 10^{-8}$

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