

Impaired coronary blood flow at higher heart rates during atrial fibrillation: Investigation via multiscale modelling

Original

Impaired coronary blood flow at higher heart rates during atrial fibrillation: Investigation via multiscale modelling / Scarsoglio, S.; Gallo, C.; Saglietto, A.; Ridolfi, L.; Anselmino, M.. - In: COMPUTER METHODS AND PROGRAMS IN BIOMEDICINE. - ISSN 0169-2607. - ELETTRONICO. - 175:(2019), pp. 95-102. [10.1016/j.cmpb.2019.04.009]

Availability:

This version is available at: 11583/2731324 since: 2019-04-19T11:47:38Z

Publisher:

Elsevier Ireland Ltd

Published

DOI:10.1016/j.cmpb.2019.04.009

Terms of use:

This article is made available under terms and conditions as specified in the corresponding bibliographic description in the repository

Publisher copyright

Elsevier postprint/Author's Accepted Manuscript

© 2019. This manuscript version is made available under the CC-BY-NC-ND 4.0 license
<http://creativecommons.org/licenses/by-nc-nd/4.0/>. The final authenticated version is available online at:
<http://dx.doi.org/10.1016/j.cmpb.2019.04.009>

(Article begins on next page)

Impaired coronary blood flow at higher heart rates during atrial fibrillation: investigation via multiscale modelling

S. Scarsoglio^{‡*}, C. Gallo[‡], A. Saglietto[‡], L. Ridolfi[‡], and M. Anselmino[‡]

[‡] *Department of Mechanical and Aerospace Engineering
Politecnico di Torino, Torino, Italy*

[‡] *Division of Cardiology, "Città della Salute e della Scienza di Torino" Hospital
Department of Medical Sciences, University of Turin, Italy*

[‡] *Department of Environment, Land and Infrastructure Engineering
Politecnico di Torino, Torino, Italy*

* *Corresponding author: stefania.scarsoglio@polito.it*

*Department of Mechanical and Aerospace Engineering, Politecnico di Torino
Corso Duca degli Abruzzi 24, 10129, Torino, Italy. Phone: +39-0110906821.*

Abstract

Background. Different mechanisms have been proposed to relate atrial fibrillation (AF) and coronary flow impairment, even in absence of relevant coronary artery disease (CAD). However, the underlying hemodynamics remains unclear. Aim of the present work is to computationally explore whether and to what extent ventricular rate during AF affects the coronary perfusion.

Methods. AF is simulated at different ventricular rates (50, 70, 90, 110, 130 bpm) through a 0D-1D multiscale validated model, which combines the left heart-arterial tree together with the coronary circulation. Artificially-built RR stochastic extraction mimics the *in vivo* beating features. All the hemodynamic parameters computed are based on the left anterior descending (LAD) artery and account for the waveform, amplitude and perfusion of the coronary blood flow.

Results. Alterations of the coronary hemodynamics are found to be associated either to the heart rate increase, which strongly modifies waveform and amplitude of the LAD flow rate, and to the beat-to-beat variability. The latter is overall amplified in the coronary circulation as HR grows, even though the input RR variability is kept constant at all HRs.

Conclusions. Higher ventricular rate during AF exerts an overall coronary blood flow impairment and imbalance of the myocardial oxygen supply-demand ratio. The combined increase of heart rate and higher AF-induced hemodynamic variability lead to a coronary perfusion impairment exceeding 90-110 bpm in AF. Moreover, it is found that coronary perfusion pressure (CPP) is no longer a good measure of the myocardial perfusion for HR higher than 90 bpm.

Keywords: atrial fibrillation, coronary blood flow, cardiovascular multiscale modelling, heart rate, computational hemodynamics

1. Introduction

Atrial fibrillation (AF) is the most common self-sustained arrhythmia, leading to faster and irregular beating [1]. It is associated with increased morbidity and mortality [2] and is becoming a major public health burden in developed and developing countries [3]. AF induces several disabling symptoms such as palpitations, fall in blood pressure, decreased exercise tolerance, pulmonary congestion [4]. Beside these, AF patients may sometimes experience angina-like chest pain and symptoms attributable to alterations of the myocardial perfusion and transient myocardial ischemia, even in the absence of significant coronary artery disease (CAD) [5, 6]. The impact of the beat-to-beat AF variability on the vascular structure has been recently investigated, with both clinical and computational approaches [7, 8]. However, many hemodynamic questions still have to be disentangled. For example, regarding the coronary circulation - which is ruled by the diastolic phase - it is so far unknown which of the myocardial layers is mainly and first affected by AF rhythm. Moreover, it is important to understand whether repeated and continuous exposure to AF irregular beating can damage in the long-term the proper coronary functioning [5].

The reciprocal implications between AF and coronary perfusion impairment have long been discussed [6]. Although clear causal relations are still lacking, recent clinical studies suggest that AF promotes an impairment of the coronary flow [9] and a mismatch of coronary blood flow and myocardial metabolic demand [5]. Even in absence of significant CAD, AF can exacerbate the subendocardium perfusion during diastole. Several mechanisms - such as reduced aortic pressure related to short RR intervals, coronary vasoconstriction, and reduced coronary blood flow - have been proposed to explain how irregular ventricular rhythm can exert negative effects on the coronary hemodynamics. However, the precise mechanisms through which AF impacts the coronary circulation still remain to be explored [10].

Since CAD and AF frequently coexist and share several risk factors, clinical literature mostly considers the concomitant presence of both pathologies, e.g. [11, 12, 13]. On one hand, this helps in shedding light on their interaction but, on the other hand, does not help in capturing the net impact of AF on coronary hemodynamics. If the role of irregular ventricular rhythm in AF is still unexplored to date, another open question is related to the impact of ventricular rate on the coronary perfusion. Even though lenient (resting HR <110 bpm) and strict (resting HR <80 bpm) rate control strategies were found not to differ in terms of mid-term cardiovascular outcomes [14], definitive evidence is still missing [15] and specific data referred to coronary flow impairment are overall scarce.

We therefore propose a computational approach, based on a validated multiscale model, to investigate to what extent coronary perfusion is impaired in AF and how this relates to the ventricular rate. Modeling aspects of the 0D-1D multiscale approach are recalled in Section 2, together with the stochastic RR beating extraction and the definition of the hemodynamic parameters. Results are presented and discussed in Sections 3 and 4, focusing on waveform and amplitude variations of left anterior descending (LAD) artery, as well as on coronary blood flow perfusion. Limiting aspects are reported in Section 5, which precedes the Conclusions (Section 6).

2. Methods

The proposed computational approach can be sketched as a three-steps algorithm: (a) RR beating extraction, (b) 0D-1D cardiovascular modelling resolution, (c) coronary perfusion evaluation. The three phases are described in the following subsections and schematically represented as overall flow chart of the stochastic modelling approach in Fig. 1.

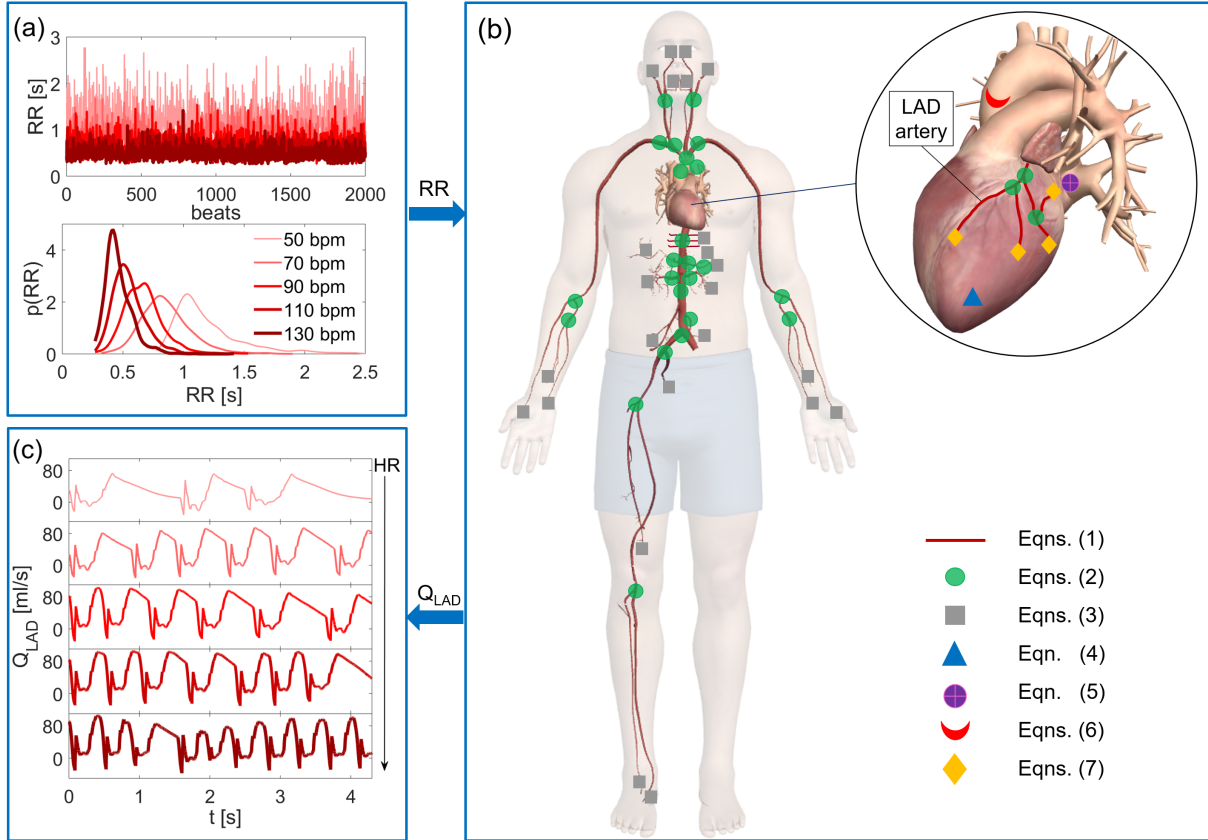


Figure 1: Flow chart of the computational algorithm. (a) RR beating. 2000 RR beats extracted in AF at the selected HR (50, 70, 90, 110, 130 bpm) and the corresponding probability distribution functions. (b) Schematic representation of the 0D-1D cardiovascular model, together with the corresponding governing equations of each district. (c) Examples of the resulting Q_{LAD} time-series at different HRs.

2.1. RR beating features

RR [s] is defined as the cardiac beating period, with the heart rate, $HR=60/RR$, expressed in [bpm]. We use artificially built RR intervals to avoid the patient-specific details (e.g., sex, age, weight, and cardiovascular diseases) inherited by real RR beating. RR intervals during AF are described by the superposition of two independent times, $RR = \varphi + \eta$. φ is taken from a Gaussian distribution and the extraction relies on the correlated pink noise. η is taken from an Exponential distribution (with rate parameter γ) and the extraction is based on the uncorrelated white noise. The resulting RR is thus represented by an exponentially modified Gaussian distribution, which

	50 bpm	70 bpm	90 bpm	110 bpm	130 bpm
μ [s]	1.20	0.86	0.67	0.55	0.46
σ [s]	0.29	0.21	0.16	0.13	0.11
γ [Hz]	3.56	6.71	8.47	9.58	10.35

Table 1: Mean (μ), standard deviation (σ), and rate parameter (γ) values of the RR distributions at the different HRs considered (the resulting cv values are constant and equal to 0.24).

is the most common distribution during AF [16, 17, 18]. By varying the HR from 50 to 130, each distribution is built keeping the coefficient of variation, $cv = \sigma/\mu$ (σ is the standard deviation, μ is the mean value of the RR distribution), constant and equal to 0.24, which is typically observed during AF [19]. The rate parameter, γ , is approximated as a linear function of the mean RR ($\gamma = -9.2RR + 14.6$), as estimated from 84 long-term ECG recordings of paroxysmal AF [20]. The in-silico RR intervals have been tested and validated over clinically measured data [16, 17, 21, 22], thus we adopt them as the most suitable and reliable RR time-series to mimic AF conditions. Mean, standard deviation and rate parameter values of all configurations here considered (from 50 to 130 bpm) are reported in Table 1, while probability distributions and time-series of the extracted RR are shown in Fig. 1a.

For each HR simulation, the multiscale modelling is integrated in time until the main statistics (mean and standard deviation) of the hemodynamic variables are insensitive to further temporal extension; 2000 cardiac periods guarantee the statistical reliability of the results to be reached. Thus, all the hemodynamic variables presented in the Results, as well as the reference heart rate of each configuration (50, 70, 90, 110, 130 bpm), are intended as mean values averaged over 2000 cycles.

2.2. Mathematical modelling

The present study relies on the multiscale model proposed by Guala et al. [23], which combines the 0D-1D modelling of the left heart and arterial tree [24, 25, 8] together with the coronary circulation model as introduced by Mynard et al. [26, 27]. The geometrical domain includes the arterial tree, the left heart, with mitral and aortic valves, and the left coronary circulation. Figure 1b shows a schematic representation of the cardiovascular model, together with the corresponding governing equations of each district. A brief description of the heart-arterial-coronary modelling is recalled hereunder, while more details are offered elsewhere [24, 23, 26, 27].

Arterial tree

The systemic arterial circulation consists of 48 large-medium arteries and 24 distal groups. Both left and right arm vessels are taken into account because of their asymmetric geometry, while only the right leg is introduced exploiting the symmetry in leg arteries. The large-medium arteries are described through the 1D form of the mass and momentum equations, in terms of pressure, section area, and flow rate. For each 1D artery, a constitutive equation relating pressure and area completes the differential system

$$\begin{cases} \frac{\partial A}{\partial t} + \frac{\partial Q}{\partial x} = 0, \\ \frac{\partial Q}{\partial t} + \frac{\partial}{\partial x} \left(\beta \frac{Q^2}{A} \right) = -\frac{A}{\rho} \frac{\partial P}{\partial x} + N_4, \\ P = B_1 + B_2 A + B_3 A^2 + B_4 A^3 - B_5 \frac{1}{\sqrt{A}} \frac{\partial Q}{\partial x}, \end{cases} \quad (1)$$

where x is the spatial coordinate along the vessel axis, t is time, A is the vascular section, Q is the flow rate, P is the radially-constant pressure, ρ is the blood density, β is the Coriolis coefficient, N_4 is the viscous term, and coefficients B_i ($i = 1, \dots, 5$) contain the information about the local viscoelastic mechanical properties.

Conservation of mass and total pressure is set at each arterial junction (the subscript 0 refers to the parent artery, while the subscripts 1 and 2 are associated to the daughter vessels)

$$\begin{cases} Q_0 = Q_1 + Q_2, \\ P_0 + \frac{1}{2} \rho \bar{u}_0^2 = P_1 + \frac{1}{2} \rho \bar{u}_1^2, \\ P_0 + \frac{1}{2} \rho \bar{u}_0^2 = P_2 + \frac{1}{2} \rho \bar{u}_2^2, \end{cases} \quad (2)$$

where \bar{u} is the mean blood velocity.

The distal groups consist of three-element Windkessel submodels

$$\frac{\partial Q_b}{\partial t} - \frac{1}{R_1} \frac{\partial P_b}{\partial t} = \frac{P_b - P_{ven}}{R_1 R_2 C} - \left(1 + \frac{R_1}{R_2} \right) \frac{Q_b}{R_1 C}, \quad (3)$$

where Q_b and P_b are the flow rate and pressure at the outlet of the generic terminal artery, R_1 equals the characteristic impedance of the artery, R_2 and C represent the viscous and elastic features of the distal area, respectively. These groups form the outlet boundary conditions, accounting for the missing cerebral circulation at the terminal carotid and vertebral arteries, the peripheral micro-circulation, the venous return and the right heart.

Left heart

Left ventricle is described through a time-varying elastance model,

$$E_{LV} = \frac{P_{LV}}{V_{LV} - V_0}, \quad (4)$$

which relates left ventricular pressure, P_{LV} , and volume, V_{LV} (V_0 is the unstressed left ventricular volume). Mitral valve is simulated as an ideal diode with resistance R_{MI} , and the mitral flow, Q_{MI} , is ruled by the pressure gradient across the valve (P_{LA} is the left atrial pressure):

$$\begin{cases} Q_{MI} = \frac{P_{LA} - P_{LV}}{R_{MI}}, & \text{if } P_{LA} > P_{LV}, \\ Q_{MI} = 0, & \text{if } P_{LA} \leq P_{LV}. \end{cases} \quad (5)$$

The aortic valve is instead modeled by means of a pressure-flow rate relation which, through the valve opening angle $\theta(t)$, accurately accounts for blood flow effects such as forces due to the pressure difference across the valve (F_{pr}), frictional effects from neighboring tissue resistance (F_{fr}), the dynamic effect of the blood acting on the valve leaflet (F_{bm}), and the action of the vortex downstream of the valve (F_{vo}) [28]:

$$\begin{cases} L \frac{dQ_{AA}}{dt} + RQ_{AA} + B|Q_{AA}|Q_{AA} = \Theta (P_{LV} - P_{AA}), \\ \Theta = \frac{(1 - \cos(\theta))^4}{(1 - \cos(\theta_{max}))^4}, \\ I_{ao} \frac{d^2\theta}{dt^2} = F_{pr} - F_{fr} + F_{bm} - F_{vo}, \end{cases} \quad (6)$$

where Q_{AA} and P_{AA} are the flow rate and pressure at the entrance to the aorta, L , R and B stand for the inertance, viscous and turbulent flow separation effects, respectively. The function Θ simulates the nonideal behaviour of the valve orifice, while θ_{max} is the maximum aortic valve opening angle (here, $\theta_{max}=75^\circ$), and I_{ao} is the rotational inertia of the aortic leaflets.

The adoption of the pressure-flow rate relation (6) instead of an aortic diode model allows us to include important arterial flow features, such as the physiologic back flow in the aortic valve following its closure and the occurrence of the dicrotic notch, which would not be captured by the simplified model. In fact, this latter, by only considering unidimensional flow, is not able to reproduce the complexity of the valvular flow, such as the presence of stenotic or regurgitant flow, and sinus vortices downstream of the valve [28, 29]. Moreover, the diode model does not account for geometry variations [29], as well as accurate pressure effects with respect to the current state (or position) of the valve [28, 30].

Equations (4), (5), and (6) represent the complete set of inlet boundary conditions of the arterial tree.

Left coronary circulation

The left coronary circulation originates from the aortic root and includes 7 large-medium arteries, which are modelled as the systemic arterial tree (Eqns 1). Each artery ends up with a microvascular distal district, identified at the entrance by a characteristic impedance, Z_{pa} , pressure, P_a , and compliance, C_{pa} , of the corresponding 1D coronary artery, and composed by three transmural layers: the subepicardium ($j=1$), the midwall ($j=2$), and the subendocardium ($j=3$). Each layer is forced by an intramyocardial pressure, P_j^{im} , and is divided into two compartments, the arterial one and the venous one. Each compartment is described by a resistance and a compliance, R_{1j} and C_{1j} are the arterial resistances and compliances, while R_{3j} and C_{2j} are the venous resistance and compliances. An intermediate resistance, R_{2j} , matches the arterial and venous compartments, with $P_{1j} - P_{2j}$ being the pressure difference through it. Compliances are constant in time, while all resistances vary in time, based on instantaneous volume filling of each sublayer. The time-varying resistance mimics the autoregulation capability to supply the appropriate blood flow level to the heart in physiological conditions. The venous compartments of the microvascular model converge into a venula, which is characterized - as the entrance

- by a specific impedance, Z_{pv} , pressure, P_v , and compliance, C_{pv} . Pressure at the outlet of the coronary microcirculation model, P_{out} , is taken constant and equal to 5 mmHg. Combining constitutive and conservation equations, each coronary distal group is ruled by the following system

$$\begin{cases} C_{1j} \frac{dP_{1j}}{dt} = C_{1j} \frac{dP_j^{im}}{dt} + \frac{P_a - P_{1j}}{R_{1j}} - \frac{P_{1j} - P_{2j}}{R_{2j}}, & j = 1, \dots, 3, \\ C_{2j} \frac{dP_{2j}}{dt} = C_{2j} \frac{dP_j^{im}}{dt} + \frac{P_{1j} - P_{2j}}{R_{2j}} - \frac{P_{2j} - P_v}{R_{3j}}, & j = 1, \dots, 3, \\ C_{pa} \frac{dP_a}{dt} = \frac{P_{in} - P_a}{Z_{pa}} - \sum_{j=1}^3 \frac{P_a - P_{1j}}{R_{1j}}, \\ C_{pv} \frac{dP_v}{dt} = \sum_{j=1}^3 \frac{P_{2j} - P_v}{R_{3j}} - \frac{P_v - P_{out}}{Z_{pv}}, \end{cases} \quad (7)$$

where all parameters are set as in [26, 27].

The complete heart-arterial-coronary modelling results in a system of hyperbolic partial differential equations, which is numerically solved through a Discontinuous-Galerkin Runge-Kutta scheme. Parameter setting relative to the coupling of different models relies to a great extent on what proposed by [23]. Further tuning of the geometrical and mechanical parameters was guided by achieving reliable coronary flow rate signals in normal sinus rhythm, as obtained by [26, 27].

2.3. Definition of hemodynamic parameters for coronary perfusion

We here introduce the hemodynamic parameters used to quantify coronary blood flow variations at different HRs during AF. In particular, all parameters are computed based on the left anterior descending (LAD) artery, which is the most important vessel in terms of myocardial blood supply (see Fig. 1c). By dividing the RR interval into systolic, RR_{sys} , and diastolic, RR_{dia} , periods, we can define V_{sys} [ml/beat] as the volume of blood flowing through the LAD artery during the systole (see Fig. 2)

$$V_{sys} = \int_{RR_{sys}} Q_{LAD}(t) dt, \quad (8)$$

where Q_{LAD} is the flow rate signal in the LAD artery. Similarly, V_{dia} [ml/beat] is introduced as the volume of blood flow through the LAD artery during the diastole (see Fig. 2)

$$V_{dia} = \int_{RR_{dia}} Q_{LAD}(t) dt. \quad (9)$$

The combination of V_{sys} and V_{dia} gives the net flow through the LAD artery, defined as LAD stroke volume, $SV = V_{sys} + V_{dia}$ [ml/beat]. By means of SV, the coronary blood flow per beat through the LAD artery is expressed as $CBF = SV \times HR$ [ml/min], giving a measure of myocardial perfusion and oxygen supply. Other quantities related to the LAD flow rate are $Q_{max,sys}$, defined as the maximum flow rate during RR_{syst} , and

$Q_{max,dia}$, which is the maximum flow rate in the RR_{dia} interval. Q_{min} is instead defined as the absolute minimum flow rate value reached during RR . The hemodynamic parameters introduced so far are all beat-to-beat measures, that is for each RR beat a value is obtained. In the end, a 2000 data distribution is available for each parameter at a fixed HR configuration. A typical LAD flow rate signal, Q_{LAD} , is reported for a single AF beat (0.87 [s]) in Fig. 2, together with indication of V_{sys} , V_{dia} , $Q_{max,dia}$, $Q_{max,sys}$, and Q_{min} .

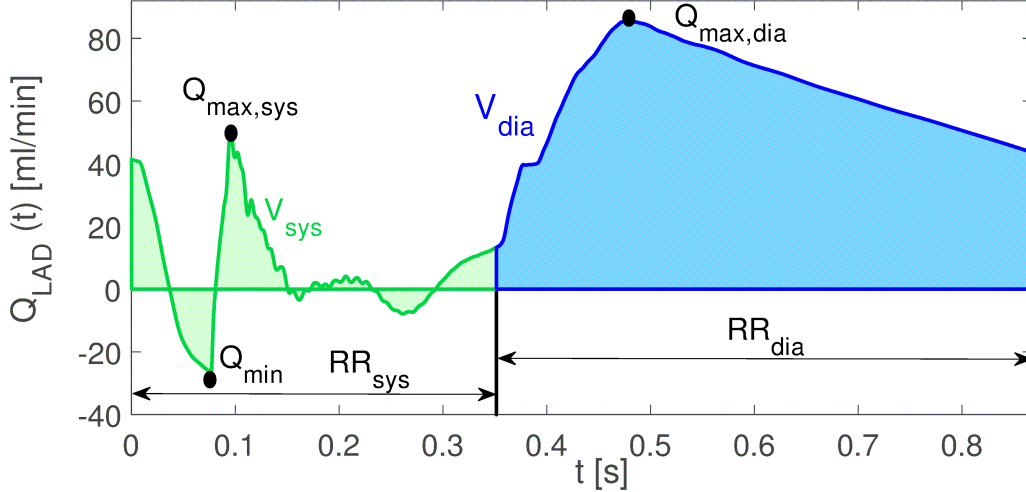


Figure 2: Example of LAD flow rate, Q_{LAD} , during AF ($RR=0.87$ [s]). Q_{min} is the minimum flow rate, $Q_{max,sys}$ and $Q_{max,dia}$ are the maximum flow rates during the systolic RR_{sys} and diastolic RR_{dia} periods, respectively. V_{sys} (green) and V_{dia} (blue) are the blood volumes per beat during RR_{sys} and RR_{dia} , respectively.

To better compare the different HRs, we also define the average behaviour of the LAD flow rate per beat over N cardiac periods

$$\langle Q_{LAD} \rangle = \frac{1}{N} \sum_{i=1}^N Q_{LAD_i}(\tau), \quad (10)$$

where here $N = 2000$, Q_{LAD_i} is the Q_{LAD} of the i -th heartbeat ($i = 1, \dots, N$), while $\tau = t/RR_i$ is the non-dimensional temporal coordinate ($\tau \in [0, 1]$). For each HR configuration, $\langle Q_{LAD} \rangle$ is introduced to highlight the average LAD flow rate waveform over 2000 cardiac cycles and expressed in terms of the non-dimensional beating period, τ . Beside $\langle Q_{LAD} \rangle$, we can also evaluate the standard deviation of the Q_{LAD_i} signals, namely $\sigma_{Q_{LAD}}$. Through the adimensional time τ , both $\langle Q_{LAD} \rangle$ and $\sigma_{Q_{LAD}}$ vary in the temporal interval $[0, 1]$ for all the HRs, and are therefore fully comparable.

We also introduce the coronary perfusion pressure, $CPP = P_{dia} - P_{lved}$, where P_{dia} is the diastolic aortic pressure, while P_{lved} is the end-diastolic left-ventricular pressure. CPP is usually referred to as a surrogate measure for myocardial perfusion [31]. In the end, to evaluate the myocardial oxygen supply-demand ratio, we compute

the rate pressure product, $RPP = P_{sys} \times HR$ [mmHg/min] (where P_{sys} is the systolic arterial pressure), which is an estimate of the oxygen consumption [32].

3. Results

3.1. Waveform and amplitude of the coronary blood flow rate

We first focus on how waveform and amplitude of the coronary blood flow rate change with HR during AF. Fig. 3 shows the different $\langle Q_{LAD} \rangle$ flow rates, together with the corresponding $\sigma_{Q_{LAD}}$, while Table 2 reports $Q_{max,dia}$, $Q_{max,sys}$, and Q_{min} at different HRs. It should be recalled that Fig. 3 and Table 2 highlight different aspects of the signal shape: the average LAD flow rate represents the characteristic mean waveform per beat as averaged over 2000 beats, while Table 2 reports the basic statistics of minima and maxima distribution, as measured over 2000 beats. For this reason, the average LAD flow rate definition is mainly exploited to compare waveform variations at different HRs, while minima and maxima of the flow rate signal are monitored to quantify amplitude variations.

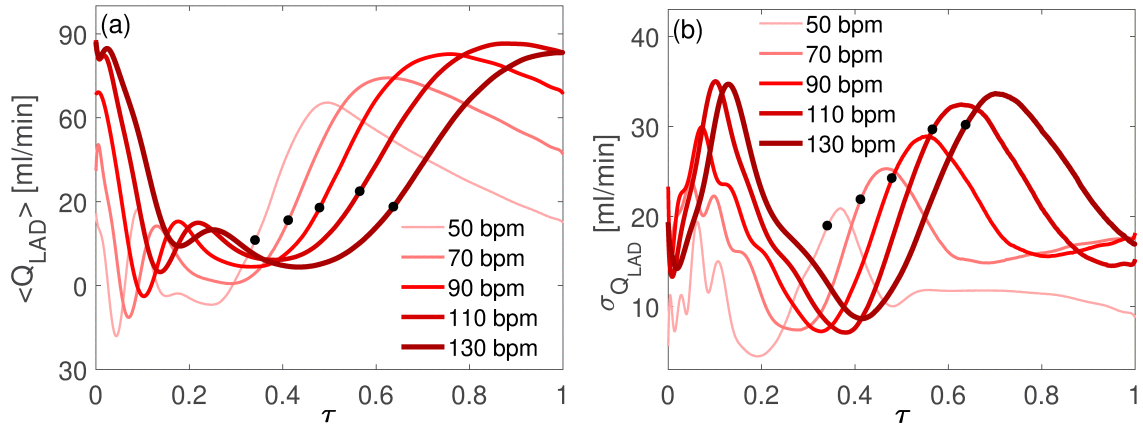


Figure 3: (a) Average ($\langle Q_{LAD} \rangle$) and (b) standard deviation ($\sigma_{Q_{LAD}}$) LAD flow rate signals at different HRs (50, 70, 90, 110, 130 bpm) as function of the non-dimensional time, τ . Black dots indicate the beginning of the diastole.

Starting with the waveform, Fig. 3a shows that by increasing HR the average waveform is deeply modified. During both systole and diastole, at higher HRs the $\langle Q_{LAD} \rangle$ signal is remarkably stretched forward in time with respect to lower HRs. As for the diastole, the typical behaviour revealed at lower HRs (also shown in Fig. 1c and 2) with a rapid growth, a maximum peak and a slow decrease, is completely lost at higher HRs. This can be explained considering that, at higher HR, the diastole length is much more reduced with respect to systole, with the ratio RR_{dia}/RR_{sys} ranging from 1.93 at 50 bpm to 0.57 at 130 bpm. Therefore, for $HR > 90$ bpm $\langle Q_{LAD} \rangle$, which is ruled by the diastolic phase, strongly changes its typical features: the diastolic growth of $\langle Q_{LAD} \rangle$ is much slower, so that the maximum peak is reached towards the end of the beat, without even facing the decreasing phase. As a consequence, at higher HRs the next systolic phase starts with much higher $\langle Q_{LAD} \rangle$ values.

The $\sigma_{Q_{LAD}}$ curves at different HRs are also reported in Fig. 3b. $\sigma_{Q_{LAD}}$ overall grows with HR and presents a time lag for increasing HR similar to $\langle Q_{LAD} \rangle$. Moreover, there is a maximum of $\sigma_{Q_{LAD}}$ for each of the two cardiac phases: these maxima occur where significant beat-to-beat variations emerge. With reference to Q_{min} , $Q_{max,sys}$, and $Q_{max,dia}$ (as displayed in Fig. 2), the systolic maximum of $\sigma_{Q_{LAD}}$ indicates the temporal range of rapid variations between Q_{min} and $Q_{max,sys}$, while the diastolic maximum corresponds to the temporal region of rapid growth before reaching $Q_{max,dia}$.

HR [bpm]	$Q_{max,sys}$ [ml/min]	$Q_{max,dia}$ [ml/min]	Q_{min} [ml/min]
50	48.97 ± 5.36 (0.11)	73.92 ± 7.07 (0.096)	-27.65 ± 3.54 (0.13)
70	56.36 ± 10.65 (0.19)	86.75 ± 8.60 (0.099)	-28.06 ± 3.03 (0.11)
90	71.11 ± 15.07 (0.21)	94.30 ± 9.70 (0.10)	-27.85 ± 4.02 (0.14)
110	84.68 ± 15.08 (0.18)	96.61 ± 11.15 (0.12)	-27.49 ± 3.81 (0.14)
130	87.41 ± 14.85 (0.17)	89.52 ± 17.24 (0.19)	-25.91 ± 5.45 (0.21)

Table 2: Mean (μ) and standard deviation (σ) values of $Q_{max,sys}$, $Q_{max,dia}$, and Q_{min} over 2000 beats for each simulated cardiac frequency (50, 70, 90, 110, 130 bpm) in AF. Coefficients of variation ($cv = \sigma/\mu$) are indicated in brackets.

Considering the amplitude variation of the LAD flow rate signal, Q_{LAD} , Table 2 reports mean, standard deviation and coefficient of variation values for the distribution of $Q_{max,dia}$, $Q_{max,sys}$, and Q_{min} , over 2000 cardiac beats at different HRs. Mean values of the maxima ($Q_{max,sys}$ and $Q_{max,dia}$) grow with HR: the highest and monotone increase is found for $Q_{max,sys}$ (+78% from 50 to 130 bpm), while $Q_{max,dia}$ increases by 21% (from 50 to 130 bpm), presenting a maximum value around 110 bpm. The growth of Q_{min} in average is instead much less pronounced, i.e. +6% (from 50 to 130 bpm). cv values of the three parameters overall increase ranging from 50 to 130 bpm, turning out to be quite sensitive to HR variability, especially recalling that cv of the RR series is maintained constant at all HR configurations.

3.2. Coronary perfusion

The coronary perfusion is analyzed in terms of the coronary blood flow, CBF , and the hemodynamic variables related to it. In Fig. 4 mean values (μ) and standard deviation values (in terms of $\mu \pm \sigma$) for V_{sys} , V_{dia} , SV , CBF , and RPP at different HRs are reported with solid curves and shaded areas, respectively. For increasing HR , a sharp V_{dia} decrease and a slight V_{sys} increase in absolute terms occur, thus SV overall decreases with HR . However, the diastolic volume decrease does not proportionally scales with HR, but affects mostly higher HRs. This results in a non-monotonic behaviour of $CBF=SV \times HR$, which shows a maximum around 90-110

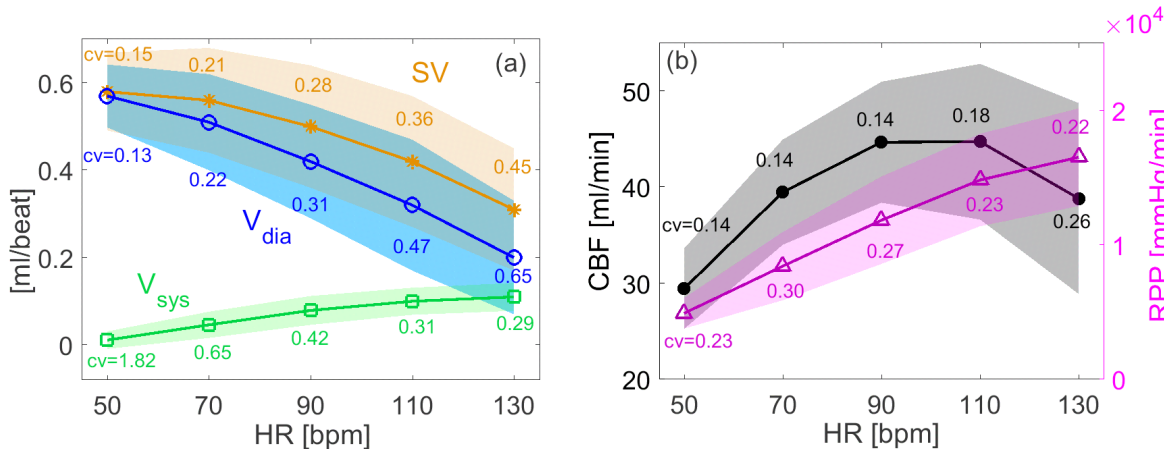


Figure 4: Mean values (μ , solid curves) and standard deviation values (in terms of $\mu \pm \sigma$, shaded areas) of hemodynamic parameters as function of HR (computed over 2000 beats): (a) V_{sys} , V_{dia} , SV ; (b) CBF (left y-axis), RPP (right y-axis). $cv = \mu/\sigma$ values are also reported for each variable and HR.

bpm and then a decrease for higher HR. The oxygen demand, expressed by RPP , monotonically grows with HR.

Fig. 4 also displays cv values which, apart from V_{sys} and RPP , all increase with HR. Beside the average trend just described for SV and CBF , it is important to remark that for these two hemodynamic parameters the AF-induced variability monotonically increases with HR, despite the input RR variability is imposed as constant for all the HRs.

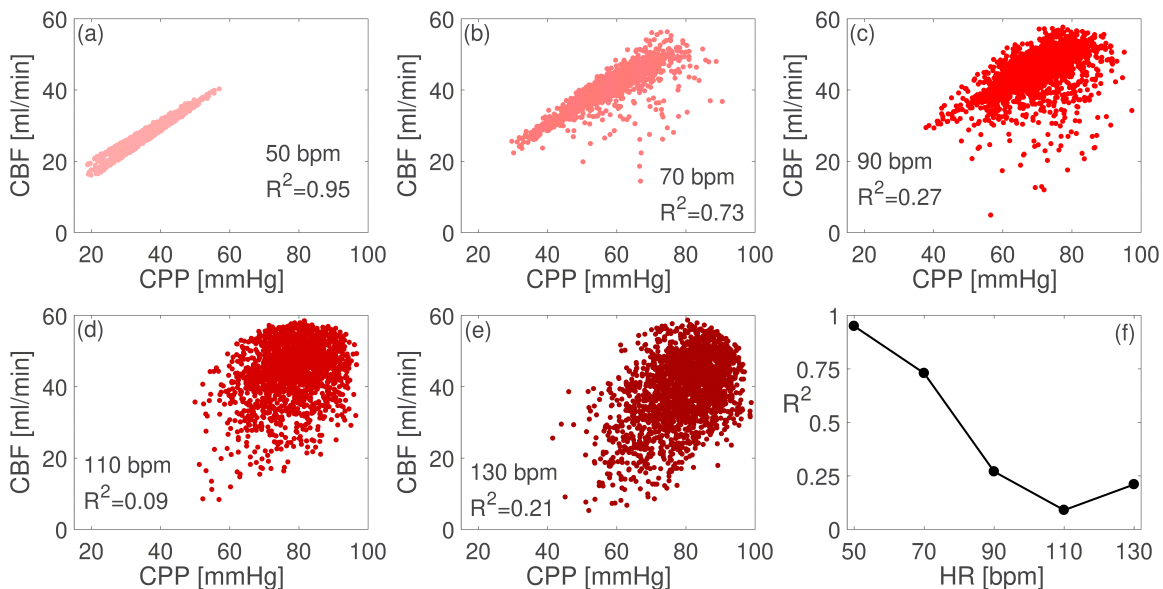


Figure 5: Coronary blood flow (CBF) as function of the coronary perfusion pressure (CPP) over 2000 cardiac cycles for HR=50, 70, 90, 110, 130 bpm (panels from a to e). Panel f shows the coefficient of determination, R^2 , for the relation $CBF(CPP)$ as function of HR.

Alongside the basic statistics of the hemodynamics parameters, to further inquire into the irregularity induced by AF, we ask whether coronary perfusion is differently affected by AF variability for increasing HR. To this end, dispersion plots of CBF as function of $CPP = P_{dia} - P_{lved}$ are proposed in Fig. 5, at different HRs (panels from a to e). In normal sinus rhythm, the relation $CBF(CPP)$ is usually exploited to estimate CBF starting from CPP, since they are positively correlated as a result of the coronary autoregulation [31]. In AF, we observe that a strong linear correlation between CBF and CPP is still present at lower HR (Fig. 5, panels a and b), while it drops at higher HR (panels c to e). It should be pointed out that, as we assume a constant left atrial pressure, fluctuations of the end-diastolic left-ventricular pressure, P_{lved} , are underestimated at any HR. Fig. 5f displays the coefficient of determination, R^2 , as function of the HR, revealing that for $HR \geq 90$ bpm CPP is no longer a good index to approximate the coronary blood flow. In this HR limit, due to the wide data dispersion, a CPP value of 70 mmHg can correspond to CPP ranging from 10 to 55 ml/s.

In the end, to quantify the beat-to-beat variability in CBF during AF, we evaluate how CBF is correlated with the current (RR), the preceding (RR_{-1}), and the pre-preceding (RR_{-2}) heart beats. Table 3 reports the Pearson correlation coefficients, r , of each relation ($CBF(RR)$, $CBF(RR_{-1})$, $CBF(RR_{-2})$), stratified over HR. For all the three relations, we move from an inverse to a direct correlation by increasing HR. Moreover, by setting $|r| > 0.3$ as significant correlation, CBF results in being mainly correlated with RR and the strength of the correlation decreases considering the preceding (RR_{-1}) and the pre-preceding (RR_{-2}) beat. In fact, $CBF(RR)$ presents significant correlation at all HRs but 90 bpm, while $CBF(RR_{-2})$ displays a significant correlation only for 70 bpm. This trend is overall in agreement with Kochiadakis et al. [5], who found significant correlation between coronary flow and current RR for all AF patients considered, while scarce and no correlation was found with RR_{-1} and RR_{-2} , respectively.

HR [bpm]	$CBF(RR)$	$CBF(RR_{-1})$	$CBF(RR_{-2})$
50	-0.70	-0.66	-0.29
70	-0.35	-0.81	-0.48
90	0.24	-0.57	-0.24
110	0.67	-0.17	0.15
130	0.73	0.05	0.28

Table 3: Pearson correlation coefficients, r , at different HRs (50, 70, 90, 100, 130 bpm) for the relations $CBF(RR)$ (II column), $CBF(RR_{-1})$ (III column), $CBF(RR_{-2})$ (IV column).

4. Discussion

The coronary impairment at higher HR during AF highlighted by the present findings has a double key to interpretation. We can roughly distinguish coronary

alterations mainly imputable to: (i) changes of the heart rate, and (ii) beat-to-beat variability. In details:

(i) we observed that average waveforms, $\langle Q_{LAD} \rangle$, are largely influenced by the HR. In particular, both diastolic and systolic waveform variations are mainly due to HR changes. In fact, as previously mentioned, if HR grows the beat length decreases, with a greater reduction in RR_{dia} than in RR_{sys} , ranging the ratio RR_{dia}/RR_{sys} from 1.93 at 50 bpm to 0.57 at 130 bpm. Therefore, at higher frequencies, the typical diastolic decay of $\langle Q_{LAD} \rangle$ observed at smaller HRs disappears, mainly because of a shorter RR_{dia} (see black dots in Fig. 3a indicating the beginning of the diastole at each HR). On the contrary, systole becomes longer than diastole for increasing HR and this results in a wider temporal range over which the high $\langle Q_{LAD} \rangle$ systolic values can be slowly damped.

Waveform variations, in turn, influence mean coronary perfusion at different HRs. In fact, the SV reduction with HR is mainly imputable to the diastole reduction as HR grows and is clearly observable from the $\langle Q_{LAD} \rangle$ waveforms of Fig. 3a: for increasing HR, $Q_{max,dia}$ is quite delayed with respect to the beginning of the diastole and this causes a consistent reduction of the diastolic flow. However, the SV reduction does not proportionally scales with HR, but is slower for lower HR and faster for higher HR. In terms of coronary blood flow ($CBF=SV \times HR$), the slow SV reduction leads to an increase of CBF up to 90-110 bpm: the slight diastole reduction does not promote consistent SV reduction, thus CBF overall grows between 50 and 90 bpm. Only beyond 90-110 bpm, the reduced diastole length makes SV, and therefore CBF, rapidly decrease, as generally expected [33]. In terms of myocardial oxygen supply and demand, both CBF and RPP increase with HR up to 90 bpm, albeit with different slopes. Once 90 bpm is exceeded, the oxygen demand still grows with HR, while CBF reaches an optimal value and then decreases. This trend implies that, up to 90 bpm, the coronary perfusion increases trying to supply the increased myocardial oxygen demand. Beyond 90-110 bpm, instead, there is a progressive coronary impairment and a consequent imbalanced oxygen supply-demand ratio.

(ii) irregularity induced by the AF-beating is not absorbed uniformly in the coronary circulation at different HRs. In general, although cv values of the RR beating are kept constant (and equal to 0.24) at all HRs, none of the hemodynamic parameters shows constant cv values as function of HR. In particular, cv values of the hemodynamic parameters exploited for the amplitude evaluation (i.e., $Q_{max,sys}$, Q_{min} , and $Q_{max,dia}$) overall increase with HR, but with different behaviours in the range [50,130] bpm: $Q_{max,sys}$ reaches a maximum cv around 90 bpm, Q_{min} has a minimum cv value for 70 bpm, while cv for $Q_{max,dia}$ increases monotonically. Maxima of the LAD flow rate ($Q_{max,sys}$ and $Q_{max,dia}$) present the highest cv increase (for both parameters, cv almost doubles from 50 to 130 bpm), and are the most prone to the AF-induced variability. Also coronary perfusion indexes, such as SV and CBF , are deeply influenced by the RR-induced irregularity, showing a monotonic growth of cv with HR.

The increased coronary hemodynamic variability with HR is well evidenced by the CBF(CPP) scatter plots of Fig. 5, which are much sparser and less predictive for higher HR. Based on the present findings, for $HR \geq 90$ bpm CPP cannot be consid-

ered a good marker for coronary perfusion in AF. Moreover, the beat-to-beat variability, mainly related to the current RR, is an *a posteriori* proof of the uncorrelated nature of the AF beating and shows how this RR feature is assimilated by the coronary perfusion: coronary blood flow per beat is only consequence of RR and RR_{-1} , while it is substantially independent of pre-preceding beats.

The coronary hemodynamics in AF is therefore influenced by the combined effects of both heart rate variations and higher hemodynamic variability. If for the heart rate there is an optimal value (around 90 bpm) which maximizes CBF, the coronary perfusion variability increases monotonically with HR, thus being much more impacting at higher HR. Experimental data in humans demonstrated that the raise in myocardial blood flow accompanying AF may be insufficient to compensate for the increased cardiac workload due to the AF-related rise in heart rate, differently to what happens to the same hearts during atrial pacing at similar ventricular rate [10]. In addition to this reduction in coronary blood flow due to the irregularity of the RR intervals, a recent work [34] suggests that an underlying microvascular dysfunction, strictly related to left ventricular and left atrial mechanical dysfunction, may play a role in myocardial blood flow impairment in AF patients. In a similar context, the present computational framework focuses on the effects that different ventricular rates exert on the coronary circle during AF. Regardless of baseline clinical features which could act as possible confounders and potential underlying microvascular dysfunction, the present model suggests clinically relevant interpretations. In fact, also here, higher ventricular rates during AF related to worse oxygen demand-supply ratio, indicating that not only the irregularity of the rhythm, but even the ventricular response in AF, may play a significant role in impairing coronary blood flow.

5. Limitations

The present model is open-loop and only considers the left heart-arterial tree, so it neglects - similarly for all the HRs - the hemodynamic feedbacks of the systemic baroreceptor mechanisms. Second, the coronary model assumes an autoregulation mechanism related to the intramyocardial pressure and myocardial filling, but does not directly account for the metabolic regulation. Moreover, the presence of other pathologies as well as the assumption of rate control drugs is not taken into account, since the focus is on the pure hemodynamic response to rate and rhythm variations induced by AF. In the end, the 0D-1D model is not able to account for some mechanical properties of both cardiac vessels (such as viscoelasticity of extracellular matrix) and cardiac muscle (such as strain rate), which are important markers of cardiac disease [35]. Given this, however, the fundamental aim of the present work is to use a simplified but powerful computational framework to infer how coronary circle responds to an irregular heartbeat at different mean ventricular rates during AF. The use of standardized conditions, regardless of any other baseline clinical feature that could alter mechanical properties of both cardiac vessels and cardiac muscle, allows us to explore the standalone impact that the irregular AF beating exerts on the coronary circle.

6. Conclusions

The present computational study shows that higher ventricular rate during AF exerts a coronary blood flow impairment. In particular, the combined effects of both heart rate variations and higher AF-induced variability leads to the following main outcomes:

(i) waveform and amplitude of the coronary blood flow rate are deeply modified by increasing HR, with a substantial delay of the diastolic peak and a consequent flow rate reduction. The overall increase of mean systolic ($Q_{max,sys}$) and diastolic ($Q_{max,dia}$) flow rate peaks with HR is also accompanied by an increased variability, while negligible effects are encountered for Q_{min} as HR varies;

(ii) as a consequence of waveform variations, CBF presents an optimal value around 90-110 bpm. However, RPP monotonically grows with HR. Thus, exceeding 90-110 bpm in AF, coronary perfusion per beat begins to be impaired and the oxygen supply-demand ratio imbalanced;

(iii) CBF positively correlates with CPP up to 70 bpm, but for higher HR the correlation dramatically drops towards zero and data become sparse. During AF, CPP is no longer a good estimate of the myocardial perfusion for HR higher than 90 bpm.

Conflicts of interest

The authors declare that they have no conflicts of interest.

Acknowledgments

This study was performed thanks to the support of the "Compagnia di San Paolo" within the project "Progetti di Ricerca di Ateneo – 2016: Cerebral hemodynamics during atrial fibrillation (CSTO 160444)" of the University of Turin, Italy. The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

References

- [1] Kirchhof P, Benussi S, Kotecha D, Ahlsson A, Atar D, Casadei B, Castella M, Diener H-C, Heidbuchel H, Hendriks J, Hindricks G, Manolis AS, Oldgren J, Popescu BA, Schotten U, Van Putte B, Vardas P. 2016. 2016 ESC Guidelines for the management of atrial fibrillation developed in collaboration with EACTS. *European Heart Journal* 37(38): 2893—2962 DOI 10.1093/eurheartj/ehw210.
- [2] Kannel WB, Benjamin EJ. Status of the epidemiology of atrial fibrillation. 2008. *Medical Clinics of North America* (92):17—40 DOI 10.1016/j.mcna.2007.09.002.
- [3] Chugh SS, Roth GA, Gillum RF, Mensah GA. 2014. Global burden of atrial fibrillation in developed and developing nations. *Global Heart* 9(1):113–119 DOI 10.1016/j.gheart.2014.01.004.

- [4] Fuster V, Rydén LE, Cannom DS, Crijns HJ, Curtis AB, Ellenbogen KA, Halperin JL, Le Heuzey JY, Kay GN, Lowe JE, Olsson SB, Prystowsky EN, Tamargo JL, Wann S, Smith SC Jr, Jacobs AK, Adams CD, Anderson JL, Antman EM, Halperin JL, Hunt SA, Nishimura R, Ornato JP, Page RL, Riegel B, Priori SG, Blanc JJ, Budaj A, Camm AJ, Dean V, Deckers JW, Despres C, Dickstein K, Lekakis J, McGregor K, Metra M, Morais J, Osterspey A, Tamargo JL, Zamorano JL. 2006. ACC/AHA/ESC 2006 guidelines for the management of patients with atrial fibrillation. *Circulation* 114(7):700—752 DOI 10.1161/CIRCULATIONAHA.106.177031.
- [5] Kochiadakis GE, Kallergis EM. 2012. Impact of Atrial Fibrillation on Coronary Blood Flow: A Systematic Review. *Journal of Atrial Fibrillation* 5(3): 161–165 DOI 10.4022/jafb.458.
- [6] Wichter T. 2010. Impaired myocardial perfusion in atrial fibrillation cause or effect? *Europace* 12:611—613 DOI 10.1093/europace/euq084.
- [7] Olbers J, Gille A, Ljungman P, Rosenqvist M, Östergren J, Witt N. 2018. High beat-to-beat blood pressure variability in atrial fibrillation compared to sinus rhythm. *Blood Pressure* 27(5):249–255 DOI 10.1080/08037051.2018.1436400.
- [8] Scarsoglio S, Gallo C, Ridolfi L. 2018. Effects of atrial fibrillation on the arterial fluid dynamics: a modelling perspective. *Meccanica* 53(13): 3251—3267 DOI 10.1007/s11012-018-0867-6.
- [9] Luo C, Wang L, Feng C, Zhang W, Huang Z, Hao Y, Tang A, Gao X. 2014. Predictive value of coronary blood flow for future cardiovascular events in patients with atrial fibrillation. *International Journal of Cardiology* 177(2):545–7 DOI 10.1016/j.ijcard.2014.08.102.
- [10] Kochiadakis GE, Skalidis EI, Kalebubas MD, Igoumenidis NE, Chrysostomakis SI, Kanoupakis EM, Simantirakis EN, Vardas PE. 2002. Effect of acute atrial fibrillation on phasic coronary blood flow pattern and flow reserve in humans. *European Heart Journal* 23(9):734—741 DOI 10.1053/euhj.2001.2894.
- [11] Michniewicz E, Mlodawska E, Lopatowska P, Tomaszuk-Kazberuk A, Malyszko J. 2018. Patients with atrial fibrillation and coronary artery disease - Double trouble. *Advances in Medical Sciences* 63(1):30–35 DOI 10.1016/j.advms.2017.06.005.
- [12] Martin RIR, Bates MGD. 2017. Management of atrial fibrillation and concomitant coronary artery disease. *Continuing Cardiology Education* 3(2):47–55 DOI 10.1002/cce2.55.
- [13] KraleV S, Schneider K, Lang S, Süselbeck T, Borggrefe M. 2011. Incidence and Severity of Coronary Artery Disease in Patients with Atrial Fibrillation Undergoing First-Time Coronary Angiography. *PLoS ONE* 6(9):e24964 DOI 10.1371/journal.pone.0024964.

- [14] Van Gelder IC, Groenveld HF, Crijns HJ, Tuininga YS, Tijssen JG, Alings AM, Hillege HL, Bergsma-Kadijk JA, Cornel JH, Kamp O, Tukkie R, Bosker HA, Van Veldhuisen DJ, Van den Berg MP. 2010. Lenient versus strict rate control in patients with atrial fibrillation. *The New England journal of medicine* 362(15):1363–1373 DOI 10.1056/NEJMoa1001337.
- [15] Wyse DG. 2011. Lenient versus strict rate control in atrial fibrillation some devils in the details. *Journal of the American College of Cardiology* 58(9):950–952 DOI 10.1016/j.jacc.2011.04.028.
- [16] Hennig T, Maass P, Hayano J, Heinrichs S. 2006. Exponentially distribution of long heart beat intervals during atrial fibrillation and their relevance for white noise behaviour in power spectrum. *Journal of biological physics* 32(5):383–392 DOI 10.1007/s10867-006-9022-z
- [17] Hayano J, Yamasaki F, Sakata S, Okada A, Mukai S, Fujinami T. 1997. Spectral characteristics of ventricular response to atrial fibrillation. *American Journal of Physiology - Heart and Circulatory Physiology* 273(6 Pt 2):H2811–6.
- [18] Scarsoglio S, Guala A, Camporeale C, Ridolfi L. 2014 Impact of atrial fibrillation on the cardiovascular system through a lumped parameter approach. *Medical & biological engineering & computing* 52(11):905–920.
- [19] Tateno K, Glass L. 2001. Automatic detection of atrial fibrillation using the coefficient of variation and density histograms of RR and Δ RR intervals. *Medical & biological engineering & computing*. 39(6):664–671.
- [20] Anselmino M, Scarsoglio S, Saglietto A, Gaita F, Ridolfi L. 2017. A computational study on the relation between resting heart rate and atrial fibrillation hemodynamics under exercise. *PloS ONE* 12(1):e0169967 DOI 10.1371/journal.pone.0169967.
- [21] Sosnowski M, Korzeniowska B, Macfarlane PW, Tendera M. 2011. Relationship between RR interval variation and left ventricular function in sinus rhythm and atrial fibrillation as estimated by means of heart rate variability fraction. *Cardiology journal* 18(5):538–545.
- [22] Goldberger AL, Amaral LA, Glass L, Hausdorff JM, Ivanov PC, Mark RG, Mietus JE, Moody GB, Peng C-K, Stanley HE. 2000. PhysioBank, PhysioToolkit, and PhysioNet: components of a new research resource for complex physiologic signals. *Circulation* 101(23):e215–e220.
- [23] Guala A, Scalseggi M, Ridolfi L. 2017. Coronary fluid mechanics in an ageing cardiovascular system. *Meccanica* 52(3):503–514 DOI 10.1007/s11012-015-0283-0.
- [24] Guala A, Camporeale C, Tosello F, Canuto C, Ridolfi L. 2014. Modelling and subject-specific validation of the heart-arterial tree system. *Annals of Biomedical Engineering* 43(1):222–237 DOI 10.1007/s10439-014-1163-9.

- [25] Guala A, Camporeale C, Ridolfi L. 2015. Compensatory effect between aortic stiffening and remodelling during ageing. *PLoS ONE* 10(10):e0139211 DOI 10.1371/journal.pone.0139211.
- [26] Mynard JP, Penny DJ, Smolich JJ. 2014. Scalability and in vivo validation of a multiscale numerical model of the left coronary circulation. *American Journal of Physiology - Heart and Circulatory Physiology* 306(4):H517–H528 DOI 10.1152/ajpheart.00603.2013.
- [27] Mynard JP, Smolich JJ. 2015. One-Dimensional Haemodynamic Modeling and Wave Dynamics in the Entire Adult Circulation. *Annals of Biomedical Engineering* 43(6):1443–1460 DOI 10.1007/s10439-015-1313-8.
- [28] Korakianitis T, Shi Y. 2006. Numerical simulation of cardiovascular dynamics with healthy and diseased heart valves. *Journal of Biomechanics* 39(11):1964–1982 DOI 10.1016/j.jbiomech.2005.06.016.
- [29] Aboelkassem Y, Savic D, Campbell SG. 2015. Mathematical modeling of aortic valve dynamics during systole. *Journal of Theoretical Biology* 365:280–8 DOI 10.1016/j.jtbi.2014.10.027.
- [30] Mynard JP, Davidson MR, Penny DJ, Smolich JJ. 2012. A simple, versatile valve model for use in lumped parameter and one-dimensional cardiovascular models. *International Journal for Numerical Methods in Biomedical Engineering* 28(6-7):626–41 DOI 10.1002/cnm.1466.
- [31] Koeppen B, Stanton B. 2009. *Berne & Levy Physiology* 6th Edition. Elsevier.
- [32] Westerhof N, Stergiopoulos N, Noble MIM. 2010. *Snapshots of Hemodynamics*. 2nd ed. Berlin: Springer.
- [33] Heusch G. 2008. Heart rate in the pathophysiology of coronary blood flow and myocardial ischaemia: benefit from selective bradycardic agents. *British Journal of Pharmacology* 153(8):1589–1601 DOI 10.1038/sj.bjp.0707673.
- [34] Wijesurendra RS, Liu A, Notaristefano F, Ntusi NAB, Karamitsos TD, Bashir Y, Ginks M, Rajappan K, Betts TR, Jerosch-Herold M, Ferreira VM, Neubauer S, Casadei B. 2018. Myocardial Perfusion Is Impaired and Relates to Cardiac Dysfunction in Patients With Atrial Fibrillation Both Before and After Successful Catheter Ablation. *Journal of the American Heart Association* 7(15):e009218 DOI 10.1161/JAHA.118.009218.
- [35] Huvneers S, Daemen MJ, Hordijk PL. 2015. Between $\rho(k)$ and a hard place: the relation between vessel wall stiffness, endothelial contractility, and cardiovascular disease. *Circulation Research* 116(5):895–908 DOI 10.1161/CIRCRESAHA.116.305720.