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Analysis and Experiment of Equilateral Triangular Uniaxial-Anisotropic Dielectric Resonator Antennas

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ABSTRACT The design procedure of a uniaxial anisotropic equilateral triangular dielectric resonator antenna (ETDRA) is presented for the first time. The uniaxial material is realized by a periodic stack of sheets of two dissimilar materials with different dielectric constants. It is proven that the increase of the boresight gain and impedance bandwidth of the ETDRA is possible by using the uniaxial material for the antenna prism. The gain improvement is due to the increase in the sidewall radiations and the bandwidth enhancement is owing to the lowering of the effective permittivity of the structure. The fabricated anisotropic ETDRA offers an impedance bandwidth of 27.7% between 3.025 and 4 GHz with a measured gain above 8 dB. The simulation results agree well with the experimental ones.

INDEX TERMS Gain, fundamental mode, impedance bandwidth, equilateral triangular dielectric resonator antenna (ETDRA).

I. INTRODUCTION

Over the last few decades, the dielectric resonator antenna (DRA) has been drawing enormous attention to prompt significant progress in microwave and millimeter wave antenna technologies. The dielectric resonator antennas have offered several advantages such as high efficiency, light weight, compact size, low cost and shape versatility [1]–[3]. These days, DRAs become a feasible alternative to conventional low-gain elements such as microstrip patches, dipoles and monopoles [4]. Triangular DRA has the advantage over the rectangular and circular ones of having smallest size when the DRAs have the same dielectric constant, height and operating frequency [5]–[8].

Modern communications set the bandwidth requirement high and the DRA technology, even if of wideband by nature, needs to keep up with it. Some efforts have been devoted to developing wideband triangular DRAs [9], [10]. In [9], two different modes of the ETDRA have been combined to give a wideband design. In [10], a new feeding mechanism based on a conducting conformal strip has been adopted to fulfill the requested impedance match bandwidth.

DRAs operating in their lowest order modes all radiate like short magnetic or electric dipoles. Mounting them on a moderate to large ground plane results in the generation of the radiation patterns with the maximum directivity of about 5dB [2]. There are some published works on the triangular dielectric resonator antennas (TDRAs) with enhanced gain [9], [11]. In [9], by exciting the higher order mode of the TDRA, a gain increase of up to 7.5 dB has been achieved. Also, in [11], the increased gain has been obtained by arraying the TDRAs.

However, a limited number of papers on wideband and enhanced gain ETDRAs has been reported so far. Therefore, there is still much room for development in this field.

Theoretical and experimental investigations have been reported on rectangular [12]–[14], and cylindrical [15] shaped anisotropic DRAs; however, at the best of the authors' knowledge, the anisotropic triangular DRA has not yet been explored. It has been reported that, by using the uniaxial anisotropic material, with the tensor ratio of $\varepsilon_z/\varepsilon_x$ smaller than one, inside the rectangular DRA [13] and cylindrical DRA [15], the intensity of the radiated fields from their sidewalls compared to those of their top wall will be augmented which in turn enhances their boresight gain. The aforementioned uniaxial anisotropic material is realized by a periodic stack of multiple layers of two dissimilar dielectric

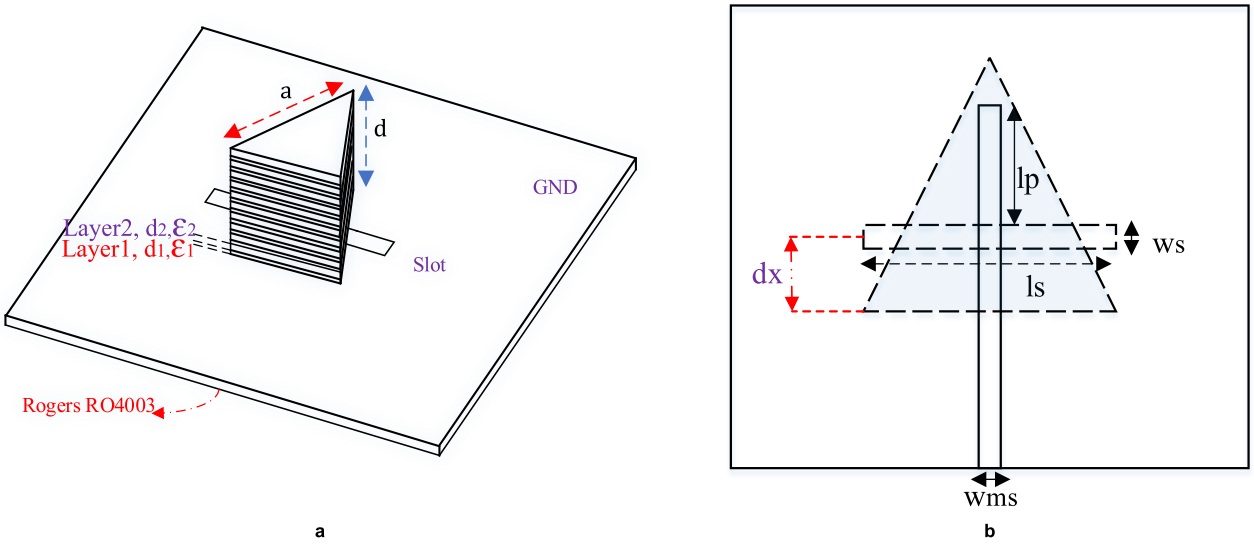


FIGURE 1. The configuration of the proposed equilateral triangular uniaxial-anisotropic DRA, (a) 3D view, (b) Bottom view.

sheets with different dielectric constants [16], [17]. Note that, to achieve the low tensor ratio of $\varepsilon_z/\varepsilon_x$, the low permittivity layers should be sandwiched between the high permittivity ones, which lowers the effective permittivity of the antenna (built with the only high permittivity material) and enhances its impedance bandwidth.

In this paper, for the first time, a uniaxial anisotropic equilateral triangular DRA is investigated both theoretically and experimentally. Using the theoretical model described in [8] for the isotropic ETDRA, the electric and magnetic fields inside the anisotropic ETDRA are derived. Then, the design formula of the TM^z_{101} mode of the uniaxial anisotropic ETDRA is obtained by using perfect magnetic wall assumption. It is concluded that, by decreasing the ratio of $\varepsilon_z/\varepsilon_x$, one can increase the boresight gain of the antenna. Also, it results in a noticeable enhancement in the impedance bandwidth results. To explain the reason behind the high gain nature of the anisotropic ETDRA, the far-field electric component of the radiation patterns of the different walls of the anisotropic ETDRA are analytically calculated. The proposed antenna is fabricated and measured. The measured and simulated results show an increase in the boresight gain and impedance bandwidth of the antenna. The simulations agree well with the measurements.

Note that, the smaller size of the anisotropic ETDRA compared to the rectangular [13] and cylindrical [15] anisotropic DRA is an advantage for the anisotropic ETDRA, as it was already mentioned for the isotropic ones [5]–[8].

This paper is organized as follows: in Section II the antenna configuration is described and the method for realizing the anisotropic ETDRA is explained in more detail. Also, the mechanism of gain improvement of the anisotropic ETDRA is discussed. In Section III, the measured results of the fabricated prototype are discussed. Finally, Section IV is devoted to the conclusion of this work.

II. ANTENNA CONFIGURATION

Figure 1 shows the proposed DRA configuration, where a multilayer ETDRA resides on a 90mm $\times$ 90 mm ground plane on a RO4003 substrate of thickness 0.508 mm and permittivity 3.38 and excited by a slot aperture of length l_s and width w_s. A 50 Ω microstrip line ($w_{ms} = 1.15$ mm) is used to feed the DRA through the aperture. The microstrip line is extended over the aperture by a length l_p. The antenna is a periodic stack of ten layers of Rogers RT5870 ($\varepsilon_{r1} = 2.33, \tan\delta_1 = 0.0012, d_1 = 0.787$ mm) and ten layers of Rogers RT6010($\varepsilon_{r2} = 10.2, \tan\delta_2 = 0.0023, d_2 = 1.27$ mm). With reference to Fig. 1, the layers are parallel to to the XY plane, and periodic along the z axis. When the thickness of the layers is small compared to the wavelength, the stacked structure behaves as a homogeneous anisotropic material with the following equivalent diagonal permittivity tensor [16]–[17].

$$\varepsilon_x = \varepsilon_y = \frac{\varepsilon_1\varepsilon_2(d_1+d_2)}{\varepsilon_1 d_1 + \varepsilon_2 d_2} \quad \varepsilon_z = \frac{\varepsilon_1 d_2 + \varepsilon_2 d_1}{d_1 + d_2}$$
$$\varepsilon_r = \begin{pmatrix} 7.19 & 0 & 0 \\ 0 & 7.19 & 0 \\ 0 & 0 & 4.45 \end{pmatrix} \tag{1}$$

Using the method reported in [8], the electric and magnetic field components of the TM^z_{101} mode inside the anisotropic ETDRA are obtained as follows

$$E_x = E_{z0}\frac{\varepsilon_z}{\varepsilon_x}\frac{2Ak_z}{\chi^2}\sin(A(x+R))\cos(By)\cos(k_z(d-z)) \tag{2}$$

$$E_y = E_{z0}\frac{\varepsilon_z}{\varepsilon_x}\frac{2Bk_z}{\chi^2}[\cos(A(x+R))\sin(By) + \sin(2By)]\cos(k_z(d-z)) \tag{3}$$

$$E_z = E_{z0}[2\cos(A(x+R))\cos(By) + \cos(2By)]\sin(k_z(d-z)) \tag{4}$$

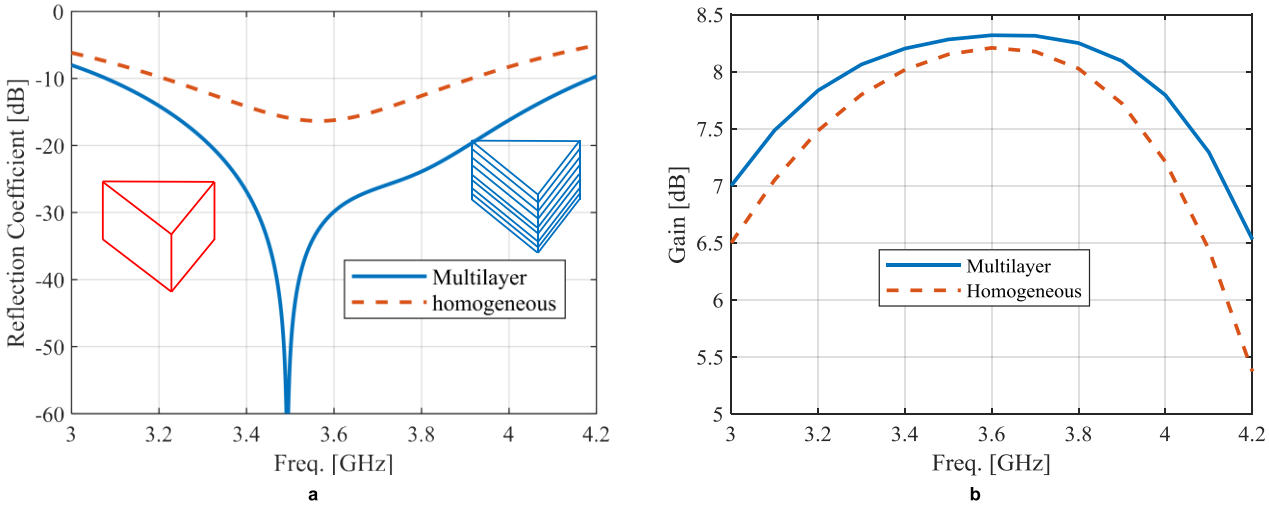


FIGURE 2. Comparison between the simulated results of the multilayer ETDRA and its homogeneous anisotropic counterpart, (a) reflection coefficient, (b) gain.

$$H_x = -jE_{z0}\frac{2B\omega\varepsilon_0\varepsilon_z}{\chi^2}\left[\cos\left(A\left(x+R\right)\right)\sin\left(By\right) + \sin(2By)\right]\sin(k_z(d-z)) \tag{5}$$

$$H_y = jE_{z0}\frac{2A\omega\varepsilon_0\varepsilon_z}{\chi^2}\sin(A(x+R))\cos(By)\sin(k_z(d-z)) \tag{6}$$

$$H_z = 0 \tag{7}$$

Where $A = \frac{2\pi}{\sqrt{3}\,a}$, $B = \frac{2\pi}{3a}$, $\chi = \frac{4\pi}{3a}$, $k_z = \frac{\pi}{2d}$, $R = \frac{a}{\sqrt{3}}$, and $\omega = 2\pi f_r$. Other parameters are as shown in Fig. 1. Note that all the walls of the ETDRA are assumed to be perfect magnetic conductors (PMCs).

The following approximate design formula is used to obtain the primary design parameters, which are subsequently optimized using the simulation results,

$$f_r = \frac{c}{2\pi\sqrt{\varepsilon_z}}\sqrt{\chi^2 + \frac{\varepsilon_z}{\varepsilon_x}k_z^2} \tag{8}$$

where c is the speed of light and the other parameters are defined above. Note that, since the permittivity tensor elements along the X and Y directions are equal, the resonant frequency depends only on ε_z and ε_x. This formula is derived from the dispersion equation, which is calculated by substituting Eqs. (2-7) into Maxwell equations. The accuracy of this formula can be further increased by using the effective dimensions of the ETDRA operating at TM^z_{101} mode as reported in [8, eq. (23–24)], Note that, in these equations, ε_r is replaced by $\varepsilon_r = (\varepsilon_x + \varepsilon_z)/2$.).

The optimized dimensions of the proposed antenna in terms of the optimum gain and impedance bandwidth are as follows: $a = 38.4$, mm, $d = 20.57$, mm, $l_s = 42.1$ mm, $l_p = 16.4$, mm, $w_s = 1.6$ mm. By substituting the value of these parameters in (8) the predicted resonant frequency for the TM^z_{101} mode is 3.7 GHz.

To confirm that the uniaxial anisotropic ETDRA can be realized by the dielectric stacking method, the simulation results of the multilayer ETDRA and that of a homogeneous anisotropic ETDRA with the dielectric constant tensor of (1) and the same dimensions as those of the multilayer one are compared. From simulations, it is apparent that the TM^z_{101} mode resonant frequency of the multilayer and homogeneous anisotropic ETDRAs are 3.5 GHz and 3.55 GHz, respectively, which are very close to each other. Note that, in multilayer ETDRA, the slot aperture is in contact with the first layer which is the dielectric layer with low permittivity (Rogers 5870, $\varepsilon_{r1} = 2.33$, $d_1 = 0.787$ mm), unlike the homogeneous structure, in which the slot aperture is directly in contact with the anisotropic medium. So, one can expect that, even though both the homogeneous and multilayer anisotropic ETDRAs should resonate at nearly the same frequency, their impedance matching level may be different, as shown in Fig. 2(a). Also, the inconsistency between the simulated gains of the multilayer and homogeneous structures can be ascribed to the first layer effect (Fig. 2(b)). So, to prove that the first layer is responsible for the aforementioned inconsistencies between the simulated results, the multilayer structure is modeled as the homogeneous anisotropic ETDRA placed on the layer1, as depicted in the inset of Fig. 3(a). Observe in Figs. 3(a) and (b) that, now the simulated reflection coefficients and gains of the multilayer ETDRA and its modified homogeneous anisotropic counterpart are very close to each other.

Note that, it appears in Fig. 3 that the antenna has 8.3 dB peak gain, which is relatively high for a dielectric resonator antenna operating at its fundamental radiating mode [2]. Thus, to explore the reason behind the high gain nature of this antenna, a theoretical study of the far-field radiation patterns is carried out. But before proceeding, for a fair comparison, an isotropic ETDRA with the same aspect ratio as that of the anisotropic ETDRA ($\frac{d}{a} = 0.536$) and filled with the isotropic material (Rogers RT6010, $\varepsilon_{r2} = 10.2$, $\tan\delta = 0.0023$) is designed. With reference to Fig. 1, the optimized dimen-

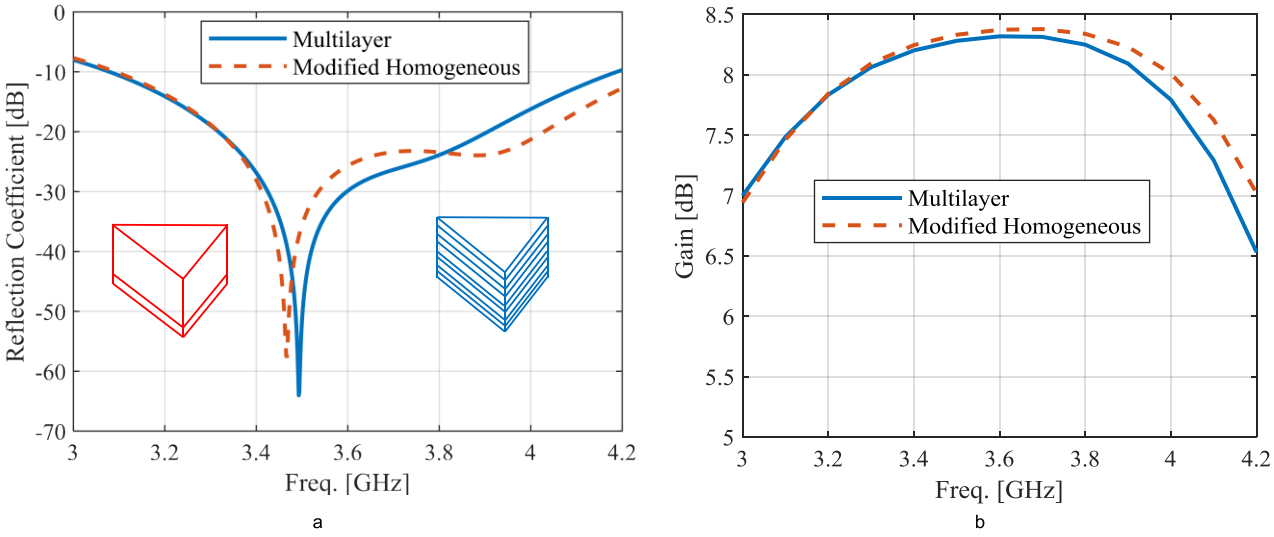


FIGURE 3. Comparison between the simulated results of the multilayer ETDRA and its modified homogeneous anisotropic counterpart, (a) reflection coefficient, (b) gain.

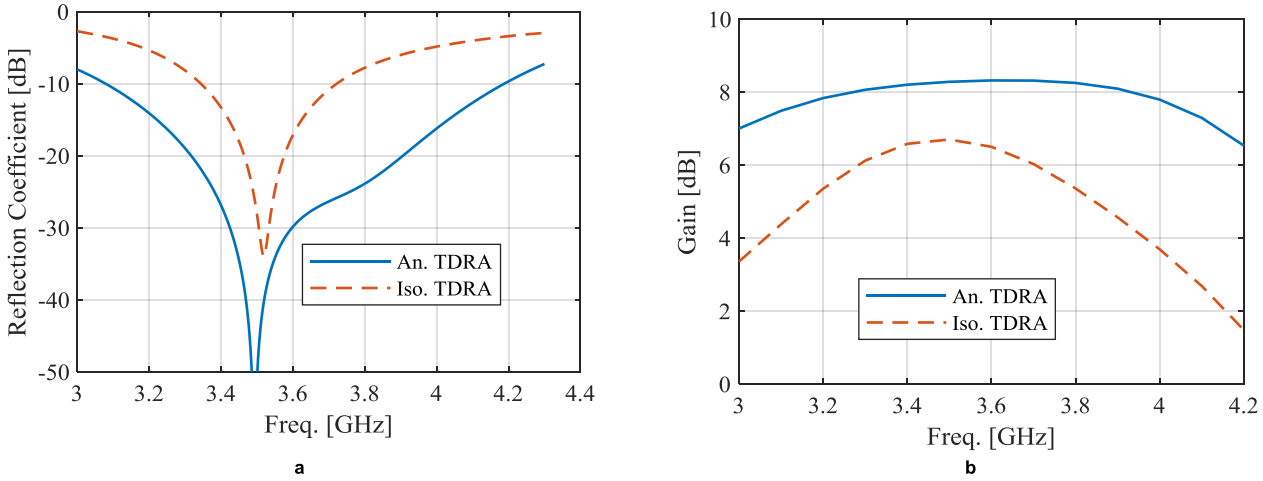


FIGURE 4. simulated results of the isotropic and anisotropic ETDRAs, (a) reflection coefficient, (b) gain.

sions of the isotropic ETDRA and its feeding network are as follows: $a = 30,\ \text{mm}, d = 16.07,\ \text{mm}, l_s = 42.1,\ \text{mm}, l_p = 11,\ \text{mm}, w_s = 1.6$ mm. Figure 4 shows the comparison between the simulated results (reflection coefficient and gain) of these two samples. As expected, the results show that the anisotropic ETDRA has a wider impedance bandwidth and higher gain compared to the isotropic one. The bandwidth enhancement of the anisotropic ETDRA is owing to the reduction in the overall permittivity of the antenna. Also, the enhanced gain of the anisotropic ETDRA is because of the increase in the sidewall-to-top wall radiation ratio of the antenna compared to the isotropic sample.

Figure 5 shows the simulated electric field distributions of the isotropic and anisotropic ETDRAs at 3.5 GHz, where both the antennas resonate. It is evident from this figure that the sidewall-to-top wall radiation of the anisotropic ETDRA is greater than that of the isotropic one. This fact can also be confirmed by comparing the E_z component in Eq. (4), to the E_x and E_y components in Eqs. (2-3). It is apparent that by employing the uniaxial material with ε_z-to- ε_x ratio smaller than one (here, $\varepsilon_z/\varepsilon_x = 0.62$) inside the ETDRA prism, the magnitude of the electric field in the z- direction is increased compared to those of the x- and y-directions. Similar to the previous works for the rectangular and cylindrical anisotropic DRAs [13], [15], it can be theoretically proved that this is the reason behind the gain improvement of the anisotropic ETDRA. The relationship between the boresight gain and the side-to-top wall radiation of the ETDRA can be obtained via the following theoretical investigation.

For the theoretical study of the anisotropic ETDRA, an infinite size perfect electric conductor is assumed as the ground plane of the antenna, and then, by using the image

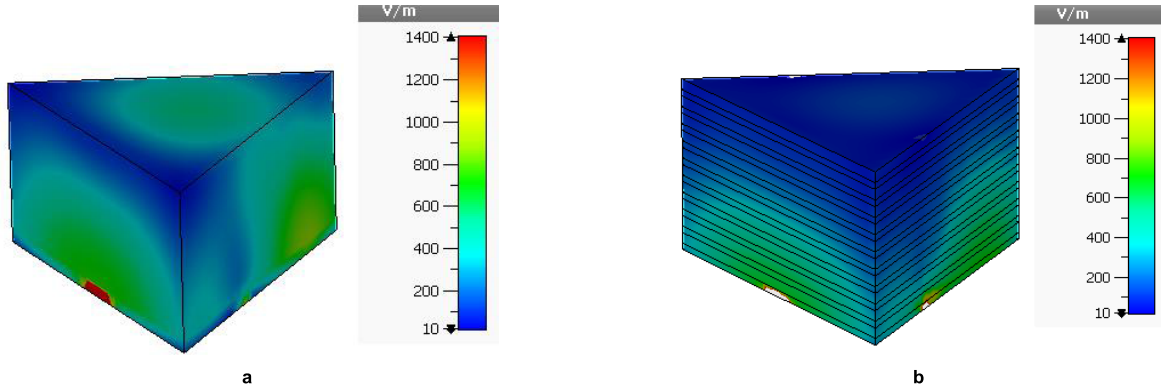


FIGURE 5. The electric field distributions at 3.5 GHz obtained by CST MW studio, (a) Isotropic ETDRA, (b) Anisotropic ETDRA.

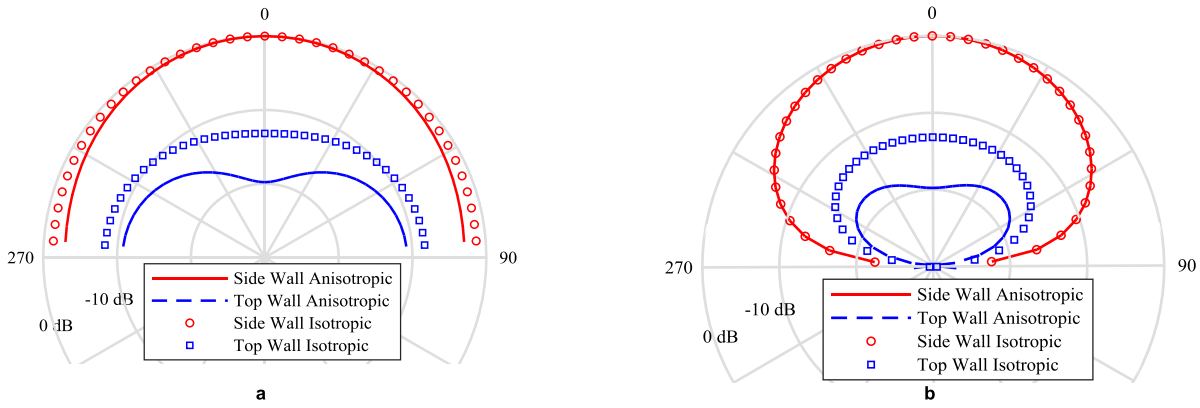


FIGURE 6. Theoretical radiation patterns originated from the walls of the iso- and anisotropic ETDRAs at 3.5 GHz, (a) XZ plane, (b) YZ plane.

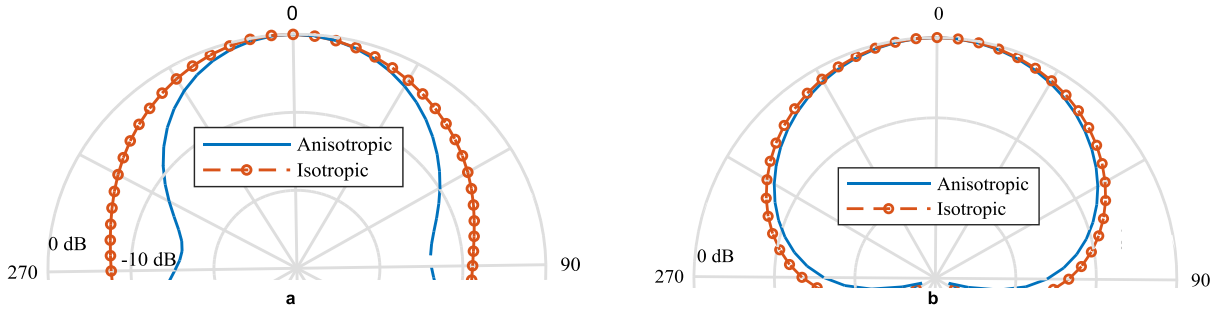


FIGURE 7. Radiation patterns of the isotropic and anisotropic ETDRAs at 3.5 GHz obtained using CST Microwave Studio, (a) XZ (E-) plane, (b) YZ (H-) plane.

theorem, its far-field patterns are determined. Based on the surface equivalent theory (Huygens's Principle) [18], to calculate the far-field radiation patterns of the antenna, the ETDRA can be modeled as the equivalent magnetic surface currents, $\bar{M}_s = \bar{E} \times \hat{n}$, where $\hat{n}$ is a unit normal pointing outward from the dielectric. Then, the far-field radiated electric fields can be calculated as follows [18]:

$$E_\theta \propto (L_\varphi^s + L_\varphi^{tb}) \tag{9}$$

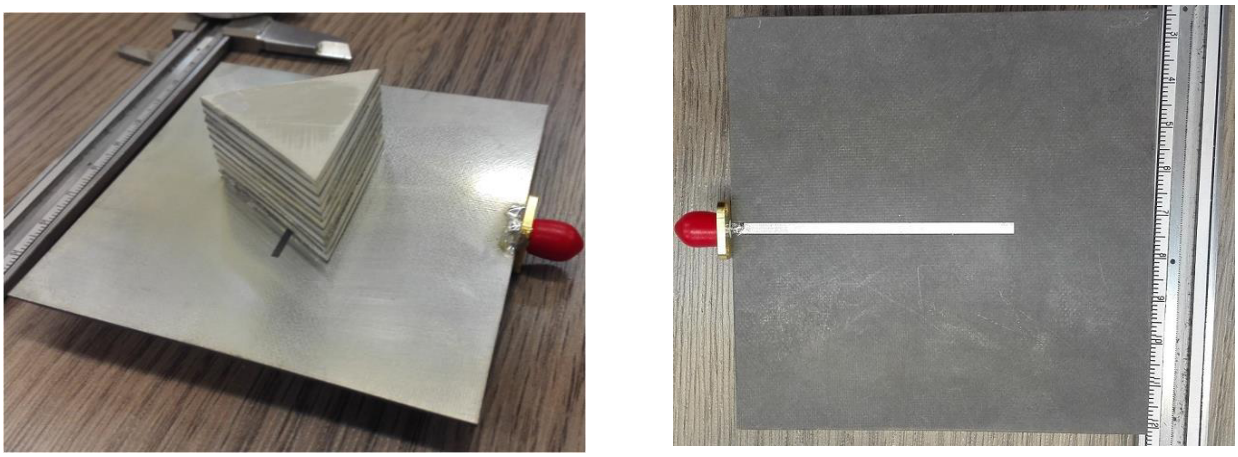
$$E_\varphi \propto (L_\theta^s + L_\theta^{tb}) \tag{10}$$

where

$$L_\varphi^{s.tb} = -F_x^{s.tb} \sin(\varphi) + F_y^{s.tb} \cos(\varphi) \tag{11}$$

$$L_\theta^{s.tb} = F_x^{s.tb} \cos(\theta) \cos(\varphi) + F_y^{s.tb} \cos(\theta) \sin(\varphi) - F_z^{s.tb} \sin(\theta) \tag{12}$$

The superscripts s and tb represent the vector potentials originated by the sidewalls and top-bottom walls of the ETDRA, respectively. The expressions of the scalar functions F above,



a b

FIGURE 8. Photograph of the fabricated prototype of the proposed antenna, (a) 3D view, (b) the bottom view.

are as follows:

$$F_x^s = 4\pi d E_{z0}\left(I_{AB}^x - I_{AC}^x\right)\frac{\cos(dk_0\cos(\theta))}{\pi^2 - 4d^2k_0^2cos^2(\theta)} \tag{13}$$

$$F_x^{tb} = -2k_z\frac{E_{z0}}{\chi^2}\frac{\varepsilon_z}{\varepsilon_x}I_{cs}\cos(dk_0\cos(\theta)) \tag{14}$$

$$F_y^s = -4\pi d E_{z0}\frac{\cos(dk_0\cos(\theta))}{\pi^2 - 4d^2k_0^2cos^2(\theta)} \times\left\{\frac{I_{AC}^x + I_{AB}^x}{\sqrt{3}} - e^{j\frac{\sqrt{3}}{2}ak_0\sin(\theta)\cos(\varphi)}I_{BC}^y\right\} \tag{15}$$

$$F_y^{tb} = 2k_z\frac{E_{z0}}{\chi^2}\frac{\varepsilon_z}{\varepsilon_x}I_{sc}\cos(dk_0\cos(\theta)) \tag{16}$$

$$F_z^s = -4\pi dj\frac{1}{\chi^2}\frac{\varepsilon_z}{\varepsilon_x}E_{z0} \times\left[\left(\frac{4}{3}\right)\left(I_{AC}^{zx} - I_{AB}^{zx}\right) - e^{j\frac{\sqrt{3}}{2}ak_0\sin(\theta)\cos(\varphi)}I_{BC}^z\right] \cdot\frac{k_0\cos(\theta)\cos(dk_0\cos(\theta))}{\pi^2 - 4d^2k_0^2cos^2(\theta)} \tag{17}$$

$$F_z^{tb} = 0 \tag{18}$$

where $I_{AB}^x, I_{AC}^x, I_{cs}, I_{sc}, I_{BC}^y$, and I_{BC}^z are defined in [8] and are omitted here for brevity.

The theoretical radiation patterns originated from the walls of the iso- and aniso-tropic ETDRAs in the XZ and YZ planes are drawn in Fig. 6. Note that, the E_θ and E_φ are the dominant components of the electric field in the XZ- and YZ- planes, respectively, which can also be deduced from Eqs. (9-17). Observe in Fig. 6(a) that the far-field E_θ patterns arising from the side walls of both the iso- and aniso-tropic ETDRAs, $E_\theta \propto L_\varphi^s$, have their maximum values in the $\theta = 0^o$ direction, but those of the top and bottom walls, $E_\theta \propto L_\varphi^{tb}$, are not directive in this direction. This behavior is due to the field distribution of the TM_{101}^z mode in the anisotropic ETDRA and is resulted from eqs. (11-17). Therefore, to achieve a highly directive radiation pattern, $E_\theta \propto (L_\varphi^s + L_\varphi^{tb})$, the radiation intensity due to the sidewalls (directive one), L_φ^s, compared to that of the top-bottom walls, L_φ^{tb}, should be increased.

To attain this goal, the uniaxial material is used inside the ETDRA prism. Then, from Eqs. (13) and (14) one can see that decreasing the $\varepsilon_z/\varepsilon_x$ ratio leads to an increase in the magnitude of the F_x^s compared to that of the F_x^{tb} and the magnitude of the F_y^s compared to the F_y^{tb}. So, observe in Fig. 6(a) that by lowering the $\varepsilon_z/\varepsilon_x$ ratio from 1 for the isotropic ETDRA to 0.62 for the anisotropic ETDRA the radiation pattern due to the sidewalls of the antenna becomes narrower and the difference between the levels of the radiation patterns due to the side walls (directive one) and top-bottom walls is increased.

Also, the theoretical results of the YZ radiation patterns are drawn in Fig. 6(b). Note that, the radiation pattern originated from the top-bottom walls of the isotropic ETDRA is already directive and decreasing its level compared to that of the sidewalls does not change the total pattern considerably.

To further verify that the narrowing of the XZ (E-) plane radiation beam is the reason of the gain enhancement of the anisotropic antenna. The simulated XZ and YZ radiation patterns of the isotropic and anisotropic ETDRAs are plotted in Fig. 7. As discussed above in the theoretical study, one can see in Fig. 7 that by using anisotropic uniaxial material ($\varepsilon_x = 7.19$, $\varepsilon_z = 4.45$) inside the ETDRA, the beamwidth in XZ plane becomes narrower and that of the YZ plane does not change considerably. As mentioned before, this happens because of the special field distribution of the TM_{101}^z mode in the ETDRA.

III. MEASURED RESULTS

The fabricated structure for the antenna in Fig. 1 appears in Fig. 8 with the optimal design parameters. The measured and simulated reflection coefficients are drawn in Fig. 9(a). The measured result shows a wide impedance bandwidth of 27.7% (3.025-4 GHz), covering the WIMAX band(3.4-3.7 GHz). Since the existence of the air gap between

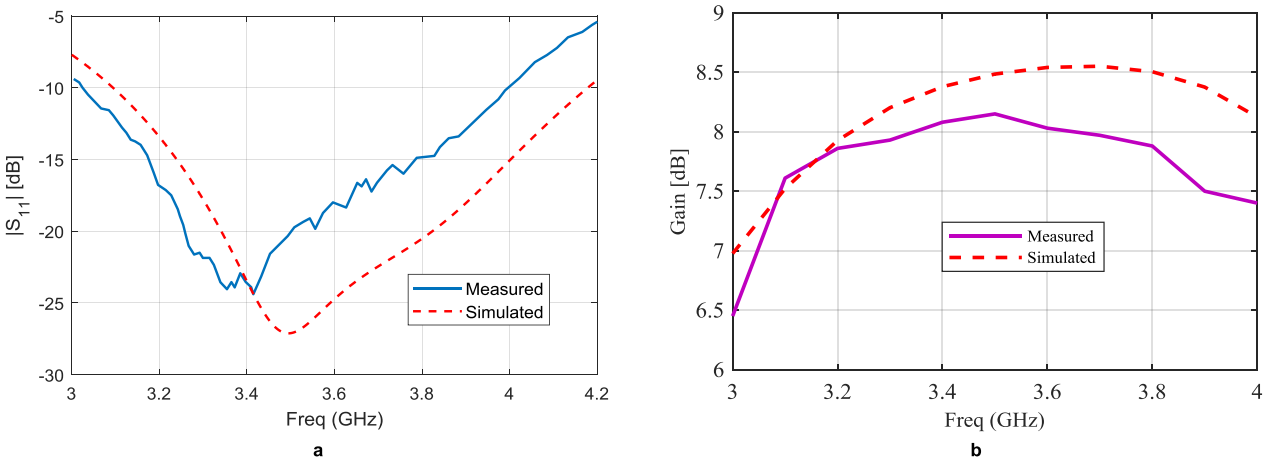


FIGURE 9. The measured and simulated results of the fabricated antenna, (a) Reflection coefficient, (b) Gain.

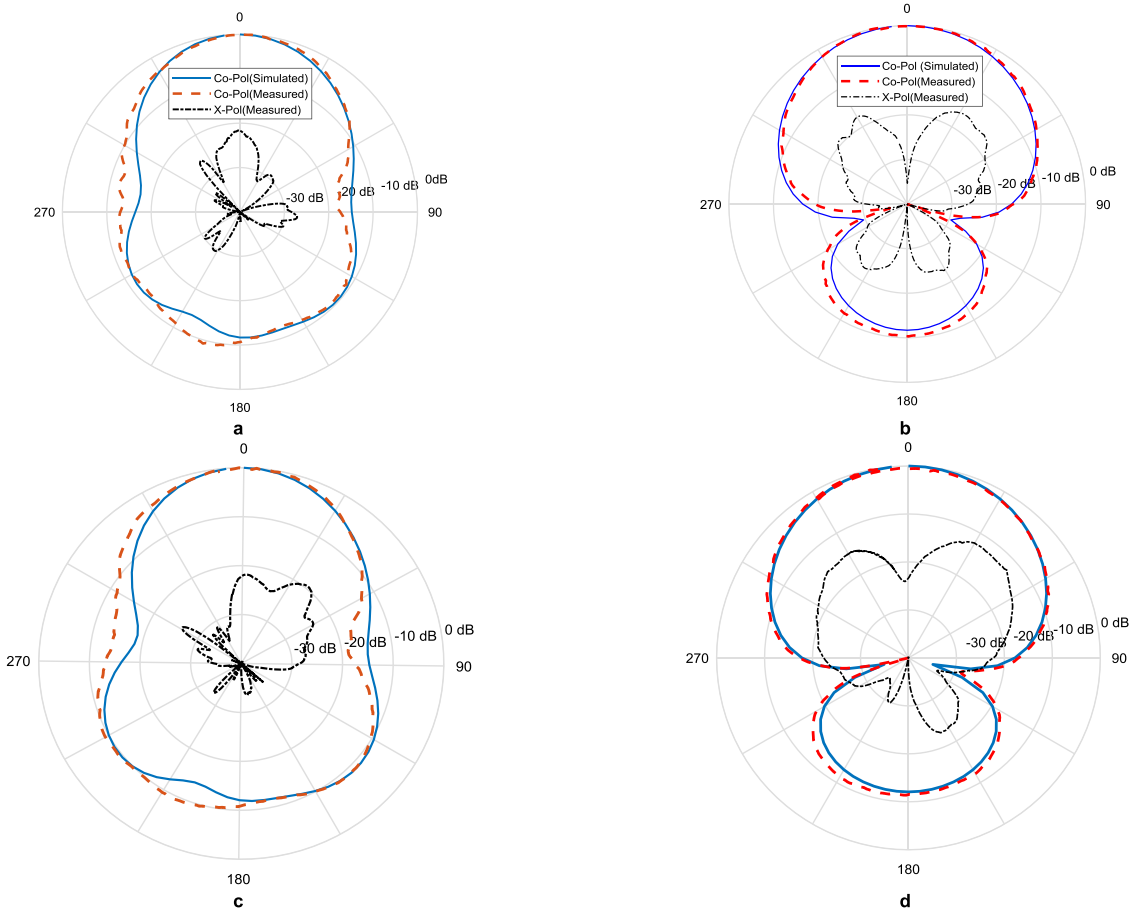


FIGURE 10. The measured and simulated radiation patterns of the proposed antenna, (a) XZ plane at 3.5 GHz, (b) YZ plane at 3.5 GH, (c) XZ plane at 3.7 GHz, (d) YZ plane at 3.7 GHz.

the layers of the antenna is unavoidable, its effect on the reflection coefficient should be studied [19]–[21]. It is found that by considering the value of 0.02 mm for the air gap thickness, the simulation results show good agreement with the measured data. The curves are not included for brevity. However, still, an inconsistency between the measured and simulation results is observed which is due to the fabrication errors. Moreover, there is another minimum in the reflection coefficient curve at 3.7 GHz. By changing the slot length, it can be verified that this is due to the slot resonance. The parametric study on the slot length is not included here for the sake of brevity.

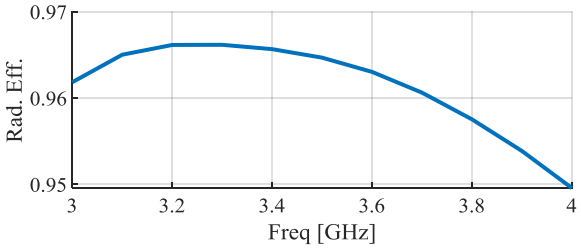


FIGURE 11. The radiation efficiency of the proposed antenna.

Also, the measured and simulated gains are plotted in Fig. 9(b). It shows that the proposed antenna has a maximum measured gain of 8.1 dB. This is about 2 dB higher than that of the isotropic ETDRA, as it can be seen in Fig. 4(b). This proves the predictions of the theory and simulation.

In [5], the maximum measured gain of the isotropic ETDRA is 5.2 dBi which is about 2.9dB lower than that of the anisotropic ETDRA presented in this work. In [9], the measured peak gain of the isotropic triangular DRA operating at its fundamental radiating mode is about 5dB. But the peak measured gain of the anisotropic triangular DRA is 8.1dB. So, a gain improvement of 3.1 dB is achieved.

The radiation patterns of the fabricated antenna are measured in an anechoic chamber. The measured and simulated radiation patterns in the XZ-plane (E-plane) and the YZ- plane (H-plane) at 3.5 and 3.7 GHz are drawn in Fig. 10. It can be noticed that the TM^z_{101} mode of the anisotropic ETDRA has a broadside radiation (Fig. 10(a) and (b)). As shown in Fig. 10(c) and (d), the radiation patterns at 3.7 GHz, where the slot resonates, are also broadside. (Observe that the maximums of the radiation patterns are in the $\theta = 0^o$ direction.) Symmetrical radiation patterns with low cross-polarization levels (lower than -20 dB in the boresight direction $\theta = 0^o$) are observed in the measurements and simulations. Finally, observe in Fig. 11 that the simulated result of the radiation efficiency is higher than 95% over the whole bandwidth.

IV. CONCLUSION

The use of the uniaxial anisotropic material with the $\varepsilon_z/\varepsilon_x$ ratio smaller than unity inside the triangular DRA prism improves the performance of the antenna. This idea is studied theoretically and verified experimentally in this work. It is shown that about 2 dB gain enhancement can be achieved using this technique. Also, a wideband antenna is obtained thanks to the reduction in the overall permittivity of the antenna. At the authors' best knowledge, this is the first anisotropic triangular DRA that has been studied until now.

ACKNOWLEDGMENT

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