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DYNAMIC MODEL OF A GROOVED THRUST BEARING: NUMERICAL MODEL AND EXPERIMENTAL VALIDATION

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Abstract. *Aerostatic thrust bearings are widely used in applications where high accuracy is requested, e.g., machine tools, measuring instruments, precise positioning systems, manufacturing and medical equipment. Conventional procedures to select or design aerostatic thrust bearings are commonly based on their static characteristics. The prediction of their dynamic behaviour is essential since the dynamic loads affecting this kind of bearings may significantly compromise their performance. This paper presents a dynamic model of a grooved rectangular aerostatic thrust bearing whose results have been experimentally validated on a frequency range from 0 up to 200 Hz, employing a sweep identification test.*

b	Bearing dimension along the x-axis
b_G	Groove length along the x-axis
c	Bearing damping
c_d	Discharge coefficient of supply holes
d_s	Diameter of the bearing supply holes
F	Bearing load capacity
F_a	Amplitude of force oscillations
F_s	Static force
f	Frequency
f_s	Sampling frequency
G	Bearing air consumption
G_{in}	Flow rate provided by the ATB supply holes (Experimental)
G_{th}	Flow rate provided by the ATB supply holes (Theoretical)
h	Bearing air gap height
h_a	Amplitude of air gap height oscillations
h_s	Static air gap height
$H(\Omega)$	Bearing transfer function
K	Static stiffness
k	Dynamic stiffness
L	Bearing dimension along the y-axis
L_G	Groove length along the y-axis
p	Air gap pressure
p_a	Ambient pressure
p_c	Downstream pressure at the ATB holes
p_s	Upstream pressure at the ATB holes
R	
T	Air gap temperature
t	Time
w_h	Flow rate per unit area related to ATB supply holes
X	x-axis of the Cartesian reference frame
Y	y-axis of the Cartesian reference frame
Δx	Length of model elements along the x-direction
Δy	Length of model elements along the y-direction
ΔA	Area of model elements
Ω	Excitation frequency
μ	Air gap viscosity
ρ	Air gap density
φ	Bearing phase lag

Table 1: List of Symbols

<i>ATB</i>	Aerostatic Thrust Bearing
<i>FRF</i>	Frequency Response Function
<i>FT</i>	Fourier Transform

Table 2: List of Acronyms

1 INTRODUCTION

Due to their distinctive features, Aerostatic Thrust Bearings (ATBs) are widely employed in applications where high accuracy is requested, e.g., high speed spindles [1, 2], machine tools [3, 4], measuring instruments [5], precise positioning systems [6, 7], manufacturing and medical equipment [8]. Thanks to their low friction, wear and losses, they make it possible to achieve very smooth and accurate positioning . The performance of conventional ATBs mainly depends on their:

- supply pressure;
- active surface geometry (e.g, conicity, roughness) and
- feeding system (e.g., compound, pocketed or unpocketed restrictors);

Supply pressures typically vary from 4 to 6 absolute bar, but occasionally, pressurised air can be supplied up to 10 absolute bar or higher by using dedicated compressors and bottled gas respectively [9, 10].

The geometrical features of ATB surfaces are an essential element, since it was found that both recess shapes and roughnesses can considerably influence their performance and stability. Plessers and Snoyes [11] discovered the higher static and dynamic performance of gas bearings with a convergent shape gap. Chen and He [12] provided a valuable analysis on the performance of ATB with different recess shapes (rectangular, spherical and non recessed).

Regarding bearing design, selecting the type, geometry, number and shape of restrictors represents a key aspect. Indeed, restrictors, through their inherent pneumatic resistance, make it possible to restore equilibrium conditions after occurrences of load variations (*inherent or passive compensation* [13, 14]). Belforte et. al [15, 16] developed a valuable experimental study providing empirical formulas for assessing the discharge coefficients of different types of pneumatic supply restrictors. Using compound restrictors represents a very widespread technical solution aimed at enhancing ATB performance without using active components, such as integrated valves [17], piezo actuators [18, 14] or other active devices [19]. They consist in simple restrictors surrounded by grooves which can have various geometries. Introducing grooves provides higher and more regular pressure distributions, therefore enhancing ATB static performance, i.e, bearing stiffness and carrying capacity. Literature presents both numerical and experimental studies confirming this higher static performance compared to conventional restrictors, especially for low supply pressures [20, 21, 22, 23].

Additionally, it was demonstrated that employing compound restrictors may significantly compromise ATB dynamic performance by increasing the likelihood of instability. For this reason, accurate dynamic characterisations are essential especially for bearings presenting compound restrictors. The main goal of this kind of procedure is the identification of the (dynamic) stiffness and damping capabilities of ATBs. Generally speaking, dynamic characterisations consist

in exciting the investigated bearing and assessing its dynamic features by analysing its response. Excitation to bearings can be provided in many different ways and they can be categorised into two main types, based on their power spectral density (PSD) distributions. There are broadband and narrowband frequency excitations. Broadband excitations are provided by applying impulsive or step force excitations as input to ATBs. Broadband excitations exhibit a near constant and well distributed energy content over a large frequency band. Conversely, narrowband excitations are commonly obtained with the aid of modal exciters (shakers) which make it possible to focus the energy content of the utilised forcing function in a narrow and well defined frequency range. Bearing responses to this excitation are considered in terms of air gap variations. Bearing dynamic characterisations are usually studied through the analysis of their Frequency Response Functions (FRFs) which is the ratio between the output and the input signal related to the investigated system considered in the frequency domain. This paper presents both a numerical and an experimental investigation regarding the static and dynamic performance of an ATB with grooves and compound restrictors. A numerical distributed model is employed for simulating and predicting both static and dynamic performance of this bearing. Static features are assessed through load, stiffness and air consumption curves of the bearing, whereas the dynamic ones are evaluated by employing a sweep identification test over a frequency band ranging from 0 to 200 Hz.

2 THE AEROSTATIC THRUST BEARING MODEL

A distributed parameter model was used to simulate the ATB both in static and dynamic conditions. The model computes the pressure distribution under the ATB by solving the Reynolds' equation for compressible fluids:

$$\frac{\partial}{\partial x} \left(\frac{\rho h^3}{12\mu} \frac{\partial p}{\partial x} \right) + \frac{\partial}{\partial y} \left(\frac{\rho h^3}{12\mu} \frac{\partial p}{\partial y} \right) + w_h = \frac{\partial(\rho h)}{\partial t} \quad (1)$$

where h is the air gap height, whereas p , μ and ρ are the air pressure, density and viscosity respectively. w_h is the input flow rate (G_{in}) per unit area provided by the supply holes of the bearing.

$$w_h = \frac{G_{in}}{\Delta x \cdot \Delta y} \quad (2)$$

Based on the following assumptions:

- the fluid is under isothermal conditions
- the supply holes according to ISO 6538 [24]

The theoretical flow rate G_{th} through a hole is computed as:

$$G_{th} = \frac{\pi d_s^2}{4} \frac{0.6855}{\sqrt{RT}} p_s \sqrt{1 - \Phi^2} \quad (3)$$

where d_s and p_s are the diameter and the upstream pressure of the supply holes respectively. The term Φ expresses the pressure drop between the upstream (P_s) and downstream (P_c) pressures relating nozzles.

$$\Phi = \frac{\frac{P_c}{P_s} - 0.528}{1 - 0.528} \quad (4)$$

In the presence of sonic flows through holes, Φ is equal to zero and the theoretical flow rate is computed as [25]:

$$G_{th} = \frac{\pi d_s^2}{4} \frac{0.6855}{\sqrt{RT}} p_s \quad (5)$$

Theoretical and experimental flow rates are related through the discharge coefficient c_d proposed by Belforte et al. [16].

$$c_d = \frac{G_{in}}{G_{th}} = 0.85 \left(1 - e^{-8.2 \frac{h}{d_s}} \right) \left(1 - 0.3e^{-0.001Re} \right) \quad (6)$$

where, Re is the Reynolds' number corresponding to the cross section of the supply hole.

$$Re = \frac{4G}{\pi \mu d_s} \quad (7)$$

The load capacity of the pad is obtained by integrating the gauge pressure distribution on the bearing surface:

$$F = \int_A (p - p_a) dA \quad (8)$$

The dynamic stiffness k and damping c of the ATB are computed by imposing periodic air gap variations at different (static) air gap height values h_s

$$h(t) = h_s + h_a \cos(\Omega t) \quad (9)$$

where, Ω is the excitation frequency. The related bearing force is finally computed as the sum of a static (F_s) and dynamic (F_a) contributions

$$F(t) = F_s + F_a \cos(\Omega t + \varphi) \quad (10)$$

where φ is the phase lag between $F(t)$ and $h(t)$. Hence, dynamic stiffness and damping are computed by Equations 11 and 12.

$$k = \frac{F_a \cos(\varphi)}{h_a} \quad (11)$$

$$c = \frac{F_a \sin(\varphi)}{h_a} \quad (12)$$

60 3 EXPERIMENTAL SET-UP

3.1 The Aerostatic Thrust Bearing (ATB)

Figure 1 sketches the geometry of the investigated ATB. It has a rectangular base with $b=75$ mm and $L= 50$ mm. This bearing presents four compound restrictors with a diameter $d_s=0.155$ mm and a rectangular shape groove ($b_G= 55$ mm and $L_G = 30$ mm). These restrictors are located
65 in the middle of each side of the rectangular groove.

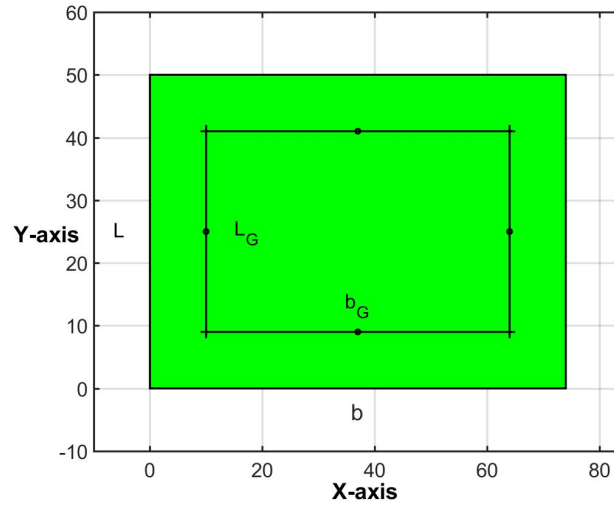


Figure 1: The ATB geometry.

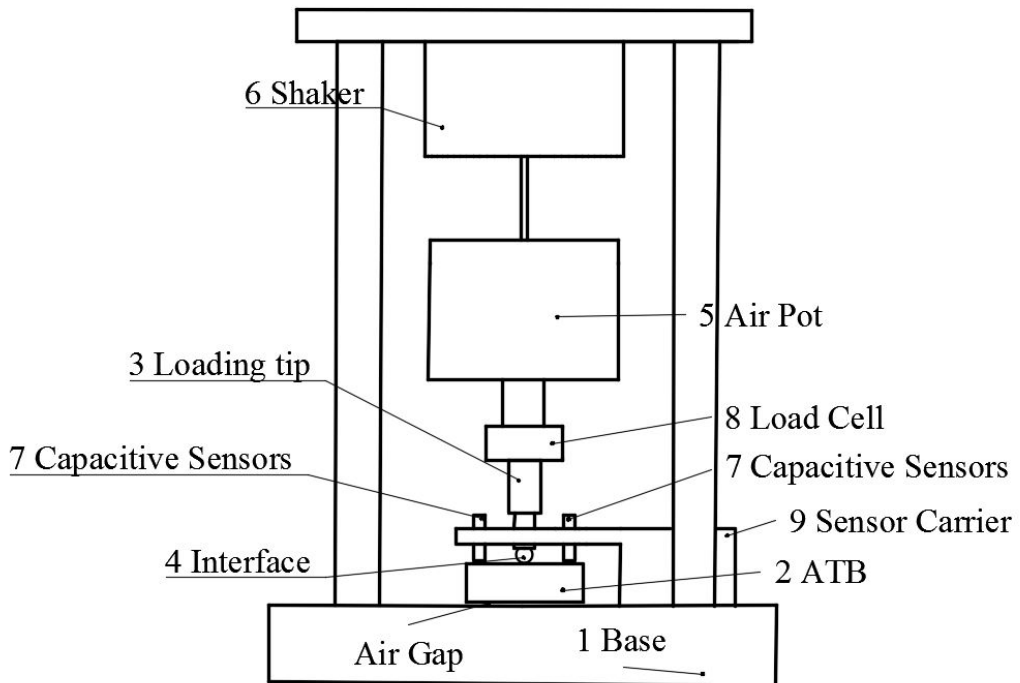


Figure 2: Test rig scheme.

3.2 Test Rig

Figure 2 shows the mechanical structure of the test rig adopted for static and dynamic characterisations of the investigated ATB. The test rig consists of base 1 which supports the investigated ATB 2, which is loaded through small tip 3 and interface 4. Static loads (or pre-loads) are applied on the bearing through air pot 5, whereas dynamic excitations are superimposed to static ones utilising shaker 6. Air gap variations and forces are measured by four capacitive sensors 7 and piezoelectric load cell 8 respectively. Capacitive sensors are placed above the upper surface of the ATB through sensor carrier 9.

4 EXPERIMENTAL PROCEDURES

This section describes the experimental procedures which were adopted to statically and dynamically characterise the investigated ATB. As discussed before, these features depend on the bearing supply pressure and the topology of its bearing surface, i.e, number, dimension and type of the adopted restrictors. Static and dynamic characterisation was performed by employing the test rig described in Section 3.2 where an air pot and a modal exciter respectively provide the static and dynamic loads acting upon the bearing.

4.1 Static

Static characterisations consist in achieving the load, air consumption and stiffness curves of the investigated bearing. These curves respectively plot the load carrying capacity, the air consumption and the stiffness of the bearing as functions of its air gap height, in the presence of a constant supply pressure ($P_s = 0.425$ MPa). Load and consumption curves were achieved by gradually varying the load applied on the bearing and measuring the correspondent air gap height and air consumption. The stiffness curve was then obtained by the differentiation of the load curve based on the following definition:

$$K = -\frac{dF}{dh} \quad (13)$$

where k is the bearing stiffness, whereas dF and dh are the infinitesimal variation of the external load and the related air gap height variation respectively.

4.2 Dynamic procedure

Assessing the dynamic stiffness and damping capabilities of ATBs is the main goal of dynamic characterisations. Literature describes many different dynamic characterisation procedures which mainly consist in exciting the bearing under test through forcing functions and assessing the dynamic performance by the analysis of its response. Step [18], impulsive [26, 27], sinusoidal [28] and sweep are the most used types of forcing functions. It is worth outlining that this choice is strictly related with the dimension of the investigated frequency range and the signal-to-noise ratio characterising the acquired signals. Bearing response can be analysed using time or frequency domain identification methods [28]. In this study, the dynamic excitations provided were superimposed to static preloads by using a modal exciter. The selected forcing function was a linear sweep with a duration of 80 s, exciting a frequency range from 0 up to 200 Hz. The dynamic features of the bearing was investigated in the presence of a constant supply pressure P_s of 0.425 MPa and at different air gap height h . Figure 3 shows an example of the applied forcing function and the related bearing response expressed in term of air gap height

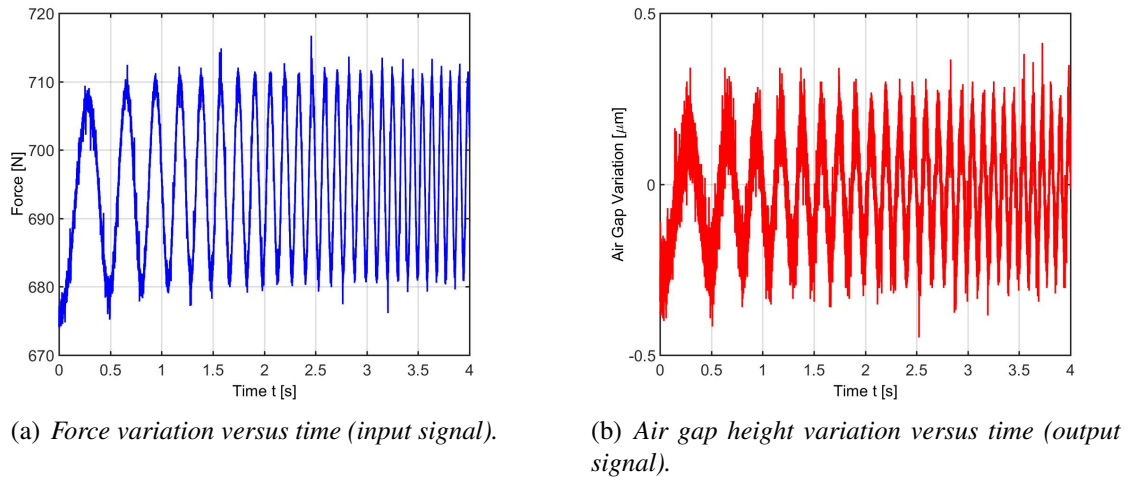


Figure 3: Sweep excitation and bearing response.

variations.

Stiffness and damping coefficients were achieved with the aid of the MATLAB[®] function *tfestimate* [29]. Given the input and output signals related to the analysed bearing, this function makes it possible to compute the following transfer function $H(\Omega)$

$$H(\Omega) = \frac{F(\Omega)}{h(\Omega)} \quad (14)$$

where, $F(\Omega)$ and $h(\Omega)$ are the transfer functions of the input force and the related air gap variation.

5 RESULTS AND DISCUSSIONS

This section presents experimental results from the static and dynamic bearing characterisation.

5.1 Static

As discussed before, the static performance of the bearing was assessed, in the presence of a constant supply pressure $P_s = 0.425$ MPa, through a conventional procedure that varied the applied load and simultaneously recorded the air gap height and air consumption (see Section 4.1). Figure 5 compares the experimental and numerical static curves of the bearing. Figures 4(a), 4(b) and 4(c) show respectively the load capacity, the static stiffness and the air consumption of the bearing. Figures 4(a) and 4(b) illustrate the experimental tests on five pads with the same geometry. The experimental results shows some dispersion, due to the tolerance when making the supply holes and the active surfaces of the bearings. Figure 4(b) shows numerical and experimental curves related to the static stiffness of the bearing. Static stiffness curves were achieved by integrating load curves. In this instance, for the sake of clarity, numerical and experimental results are compared by considering only one experimental curve.

5.2 Dynamic

The dynamic characterisation of the bearing was achieved, in the presence of a constant supply pressure $P_s = 0.425$ MPa, using a numerical model and carrying out experimental tests. Section 2 presents the main equations and assumptions adopted for building the numerical model,

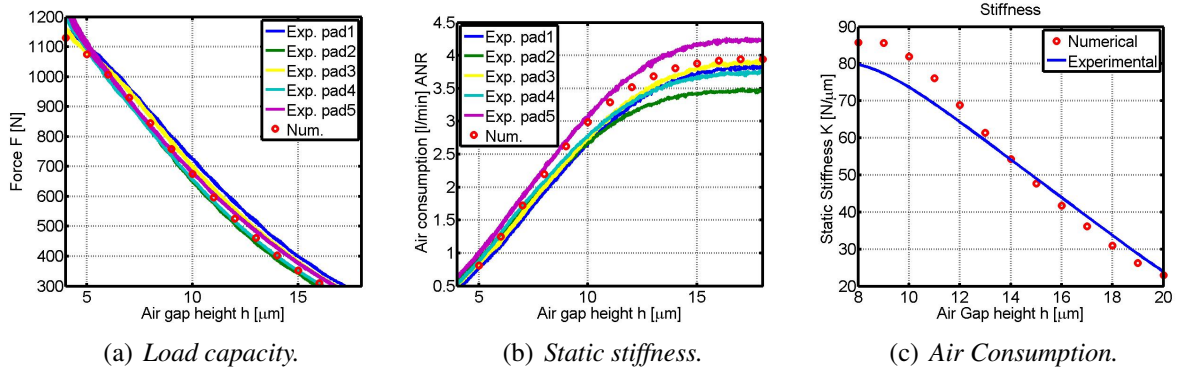


Figure 4: Static characterisation results: numerical and experimental data.

whereas Section 4 describes the procedure adopted in performing the dynamic characterisation of the bearing. Figure 5 shows the results obtained from the dynamic characterisation. Figure 5(a) illustrates the dynamic stiffness of the bearing expressed as a function of the excitation frequency f (rad/s)¹ at different air gap heights. The dynamic stiffness exhibits quite similar trends showing peaks with different amplitudes at the same excitation frequencies for all the considered air gap heights. These peaks prove that the bearing undergoes under high oscillations when subjected to forcing functions provided at 110, 165 and 205 Hz. These resonances are also evident from Figure 5(b) which shows trends of the bearing damping over the investigated frequency range. It is clear that the bearing damping drastically decays at frequencies corresponding to these peaks (110, 165 and 205 Hz). A part from this, the bearing exhibits near constant stiffness up to about 110 Hz for all the considered air gap heights. Figure 6 shows the

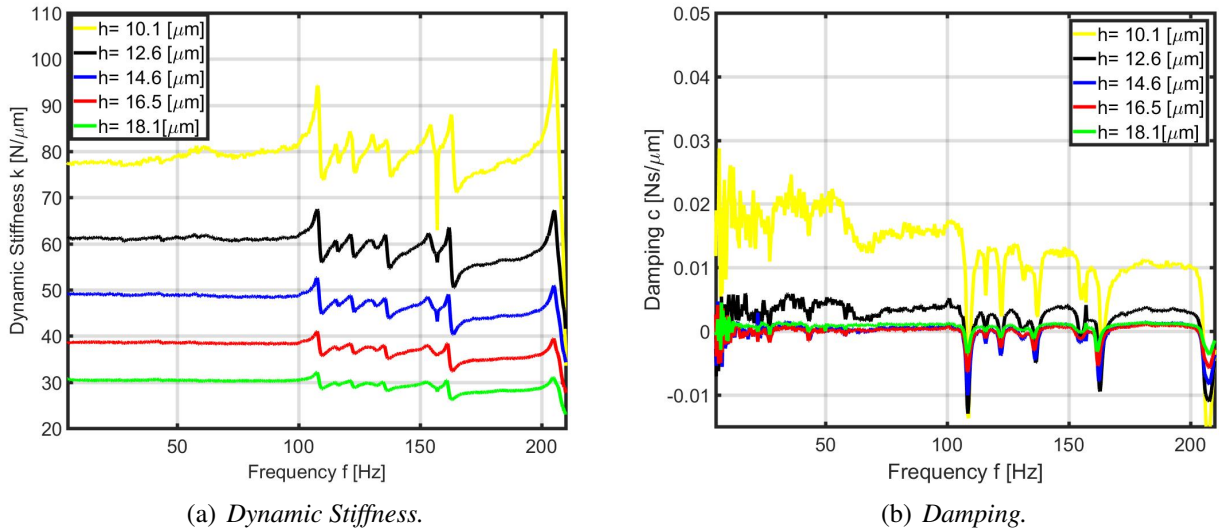


Figure 5: Dynamic characterisation results: numerical and experimental data.

curves of stiffness and damping obtained both from experimental and numerical tests, considering a constant excitation frequency $f=80$ Hz. Experimental data were obtained by testing five pads with the same geometry. these results clearly show that dynamic stiffness and damping

$$^1 f = \frac{\Omega}{2\pi}$$

coefficients exhibit non-linear decreasing trends with respect to the bearing air gap height. Furthermore, these results make it possible to better validate the model results and simultaneously statistically assess errors related to the bearing manufacturing. The numerical model acceptably approximates the experimental data.

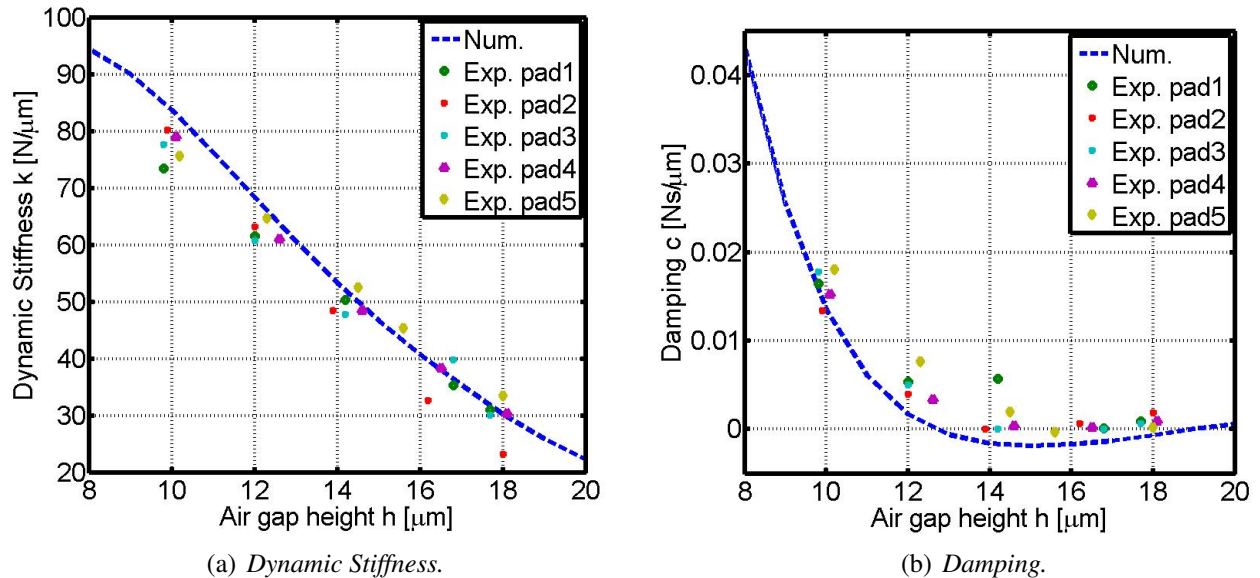


Figure 6: Dynamic characterisation results at 80 Hz: numerical and experimental data.

125 6 CONCLUSIONS

Using bearings with grooves (also called compound restrictors) represents a very widespread technical solution to achieve high performance. However, employing compound restrictors may significantly compromise the dynamic performance of the bearing by increasing the likelihood of instability. This paper presents a study of both static and dynamic performance of a grooved rectangular ATB. The bearing characterisation was obtained by using a distributed mathematical model and an experimental sweep identification procedure. The comparison between numerical and experimental results demonstrates the good accuracy of the model. The proposed experimental identification technique makes it possible to detect critical frequencies where the bearing exhibits resonances, therefore proving the value of this methodology. Moreover, the presented numerical and experimental methodology had proven to be a very useful tool for identifying bearing stiffness and damping coefficients.

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