Sensorless Control of Matrix Converter-Fed Synchronous Reluctance Motors Based on Direct Flux Vector Control Method

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Abstract: A Sensorless control technique based on direct flux vector control scheme is proposed for matrix converter-fed synchronous reluctance motor drives. The amplitude of stator flux and current component quadrature to stator flux are closed loop controlled in constant switching frequency. A hybrid current-voltage model based flux observer is used so that at low speeds stator flux is estimated through current-to-flux maps and at high speeds, flux estimation is based on back-electromotive force integration. Moreover, a hybrid position and speed observer is proposed in order to estimate rotor position in a wide speed range. At low speeds and also in standstill, rotor position is retrieved based on high-frequency signal injection while at high speeds, back-EMF based model is used to estimate the rotor position. Also, matrix converter is modulated based on indirect space vector modulation. Simulation results for a 2.2 kW synchronous reluctance motor are presented to show the effectiveness of proposed sensorless drive.

Key words: Direct flux vector control; High frequency injection; Matrix Converter; Sensorless; Synchronous reluctance motor.

1. Introduction

Matrix converters as ac-to-ac converters have emerged to become an alternative to conventional converters. These converters show attractive advantages such as high quality power output waveforms, bidirectional power flow, and lack of bulky capacitors [1-4].

Synchronous reluctance motors (SyRMs) have been widely adopted in recent years due to their advantages such as low manufacturing cost and simple structures [5-8]. Moreover, due to high saliency features of these machines, SyRMs can be readily adopted to sensorless control methods.

Conventionally, sensorless control methods are categorized into two main control techniques including back-electro motive forced (EMF) based methods and the ones based on high-frequency injection signals. At medium and high speeds, rotor position is estimated based on back-EMF techniques. However, at low speeds and standstill where back-EMF signal is poor, rotor position estimation is inaccurate and impossible at standstill. Therefore, a high-frequency signal, usually voltage, is injected to the motor and high-frequency component of corresponding current is demodulated and then rotor position is retrieved through a tracking loop.

Direct torque control (DTC) method poses different advantages compared to vector control methods such as fast dynamic and robust implementation. However, variable switching frequency and high torque ripple are the two most drawbacks of this control method [11-12]. Direct flux vector control (DFVC) method which was presented in [13], maintains the main features of DTC and vector control methods such as fixed switching frequency and straightforward limitation of current amplitude. This control operates in stator coordinates $(d_s, q_s)$ where the amplitude of stator flux and current quadrature to stator flux are the two controlled variables. The amplitude of stator flux is regulated using voltage component on $d_s$-axis, while the torque producing current is controlled by means of $q_s$ voltage channel.

Despite the aforementioned advantages of matrix converters and SyR motors, there are a few literature for control of matrix converter-fed synchronous reluctance motor drives [14-15]. Therefore, this paper proposes a sensorless control technique for matrix converter-fed synchronous reluctance motor drives based on direct flux vector control method. To do so, a combined voltage-current model flux observer is adopted. At low speeds, flux observation is based on current model coming from a 2-D current-to-flux tables. While at high speed, flux observation is based on back-EMF integration. In order to cover a wide speed range control, a hybrid speed and position observer is proposed where at low speeds and standstill, high frequency voltage is injected into estimated rotor $\hat{d}$-axis and high frequency component of flux response is demodulated. Provided that in this method high frequency component of flux response is demodulated in place of high frequency component of current response, the cross-saturation effect which may cause to position estimation error is inherently overcome [16]. Above 50 [rpm], high frequency injection starts to be decreased and above 100 [rpm] is completely dropped out and position estimation will be purely base on back-EMF technique.

In the following sections, indirect space vector modulation (ISVM) of matrix converters and its nonlinear errors are briefly investigated and then proposed sensorless technique is studied in details. Eventually, simulation results are presented to
validate the proposed method.

2. Matrix converter modulation and nonlinear errors

A. Indirect space vector modulation [17]

The power circuit topology of a three-phase to three-phase matrix converter is shown in Fig.1. Indirect space vector modulation is used to synthesize the output voltage vectors to the input current vectors. The basic idea of this modulation is to separate the matrix converter into a fictitious voltage source rectifier (VSI) and a fictitious voltage source inverter (VSI). Modulation of output voltage vector \( (V_A^*, V_B^*) \) is done based on VSI while VSR is responsible for control of input phase current \((\theta_{in}^*)\). The phase angles of output voltage and input current vectors are used to determine the output and input sectors, respectively. Fig.2 shows the two adjacent active vector and one zero vector used to synthesize the output and input reference vectors. The duty cycles of four active vectors and one zero vector are expressed as (1) to (5).

\[
d_{\mu \nu} = d_{\mu} \cdot d_{\nu} = \frac{2}{3} \frac{|V_0^*|}{|V_{in}|} \sin \left( \frac{\pi}{3} - \theta_{in}^* \right) \sin \left( \frac{\pi}{3} - \theta_{0}^* \right)
\]

\[
d_{\mu \delta} = d_{\mu} \cdot d_{\delta} = \frac{2}{3} \frac{|V_0^*|}{|V_{in}|} \sin \left( \theta_{in}^* \right) \sin \left( \frac{\pi}{3} - \theta_{0}^* \right)
\]

\[
d_{\nu \delta} = d_{\nu} \cdot d_{\delta} = \frac{2}{3} \frac{|V_0^*|}{|V_{in}|} \sin \left( \theta_{in}^* \right) \sin \left( \theta_{0}^* \right)
\]

\[
d_{\nu \gamma} = d_{\nu} \cdot d_{\gamma} = \frac{2}{3} \frac{|V_0^*|}{|V_{in}|} \sin \left( \frac{\pi}{3} - \theta_{in}^* \right) \sin \left( \theta_{0}^* \right)
\]

\[
d_0 = 1 - (d_{\mu \nu} + d_{\mu \delta} + d_{\nu \delta} + d_{\nu \gamma})
\]

Fig. 1. Schematic diagram of a three-phase matrix converter.

![Schematic diagram of a three-phase matrix converter.](image)

Fig. 2. Indirect space vector modulation: (a) rectification space vector modulation, (b) inversion space vector modulation.

B. Matrix converter nonlinear errors [18]

Similar to conventional converters, matrix converter nonlinear errors come from voltage drop of semiconductors and commutation resulted errors called edge uncertainty effects.

In MCs, two devices are always conducting. The forward voltage of a power device can be approximated by a fixed threshold value \((V_{th})\) which is the average effect of one diode and one IGBT. Thus, the VD is modeled as (6) where \(R_d\) accounts for resistance of two devices in series.

\[
V_{di} = 2V_{th} \text{sign}(i) + R_d i, \quad i = \{a, b, c\}
\]

When the output voltage is changed from one input phase to the other phase, a voltage is introduced which is dependent to commutation sequence, and commutation pattern. In this paper, a four-step current based commutation is adopted while commutation pattern is double-sided. As an example, it is assumed that the output phase voltage \(V_A\) changes from input phase A to input phase B. Fig.3 illustrates the commutation sequence when output phase current \(i_a\) is positive and input phase voltage \(V_A\) is more positive than \(V_B\) where, \(t_c\) is commutation time, \(t_f\) is IGBT falling time, and \(t_{d1}\) and \(t_{d2}\) stand for commutation delay. As can be seen, there is a voltage error between ideal voltage \(V_A^*\) and the real one that can be expressed as (7). If Fig.3 is extended to a double-sided switching pattern for one switching period \(T_{PWM}\), the ideal and real output phase voltage \(V_A\) are as (8) and (9), respectively (for details see [18]), where \(T_0\) is the timing of actuating zero vectors and \(t_p\) is IGBT rising time. Comparing (8) with (9), it seen that a voltage error is added to the ideal voltage due to the commutation. Generally, the edge uncertainty effect in matrix converters for different input and output sectors is shown as (10) where \(j\) denotes for input phases and \(i\) stands for output phases.

![Diagram illustrating the commutation sequence.](image)

Fig. 3. Four-step current based commutation when output current is positive and input phase voltage \(V_A\) is more positive than \(V_B\): commutation is from input phase A to input phase B.
3. Direct flux vector control method

In this section DFVC method is investigated briefly. First, SyR motor model in rotor dq frame is analyzed and then model is transferred to stator reference frame $d_s q_s$ since DFVC method operates in stator coordinates. Fig.4 shows the different reference frames adopted in this paper.

A. Motor model in rotor frame

The voltage and torque equations of a SyR motor in rotor frame can be expressed as (11)-(13), where $R_s$ is stator resistance, $p$ is pole pairs numbers, $\lambda_{dq}$ is stator flux linkage vector, and $L_d$ and $L_q$ are inductances in $d$- and $q$-axis. Equation (13) is implemented in the form of 2-D look up table to include the saturation and cross-saturation effects. Fig.5 illustrates the flux linkage maps for the SyR motor under test, evaluated experimentally.

$\bar{v}_{dq} = R_s \cdot i_{dq} + \frac{d \lambda_{dq}}{dt} + j \omega \cdot \lambda_{dq}$

$T = \frac{3}{2} \cdot p \cdot (\lambda_d i_q - \lambda_q i_d)$

$\begin{cases} 
\lambda_d = \lambda_d(i_d, i_q) = L_d(i_d, i_q) \cdot i_d \\
\lambda_q = \lambda_q(i_d, i_q) = L_q(i_a, i_q) \cdot i_q
\end{cases}$

B. Motor model in stator frame

If voltage and torque equations (11) and (12) are transferred to stator flux coordinates $(d_s, q_s)$, (14) and (15) are obtained where $\lambda$ is stator flux amplitude. Torque equation (15) can be written also in terms of flux amplitude and phase angle as (16) considering $\lambda_d = \lambda \cdot \cos(\delta)$ and $\lambda_q = \lambda \cdot \sin(\delta)$.

$\begin{cases} 
v_{ds} = R_s i_{ds} + \frac{d \lambda}{dt} \\
v_{qs} = R_s i_{qs} + \lambda (\alpha + \frac{d s}{dt}) \\
T = \frac{3}{2} \cdot p \cdot \lambda \cdot i_{qs}
\end{cases}$

$T = \frac{3}{2} \cdot p \cdot \frac{i_d - i_q}{2L_d L_q} \cdot \lambda^2 \cdot \sin(2\delta)$

C. Direct flux vector control

The block diagram of sensorless speed-controlled direct flux vector control is depicted in Fig.6. As said, the amplitude of stator flux and current component on $q_s$-axis are the two controlled variables. It is seen from (14) that stator flux amplitude is regulated by means of $v_{ds}$, and load angle is controlled using $v_{qs}$. From (16) it is concluded that by controlling load angle in a given flux amplitude, electromagnetic torque is regulated. However, electromagnetic torque can be controlled using (15) by regulating $i_{qs}$ which is more straightforward compared to (16) and is not dependent to motor parameters. Hence, $i_{qs}$ is closed loop controlled for the sake of torque control.

D. Stator flux observer

A combined voltage-current model stator flux observer is adopted in this paper as illustrated in Fig.7. The transfer function of flux observer is as (17) where gain $g[rad/s]$ is a cross over speed between low and high speeds. As can be seen from (17), when the speed is low, flux observation is based on current-to-flux maps and while in the opposite, when speed increases, flux observation switches to back-EMF integration. The output of the observer is flux angle $\theta_s$ and the amplitude of the flux $\lambda$. Stator flux angle is calculated as (18).

$\dot{\lambda}_{\alpha\beta} = \frac{s}{s+g}(V_{\alpha\beta} - R_{\alpha\beta}) + \frac{g}{s+g}(\dot{\lambda}_{\alpha\beta})$

$\begin{cases} 
\sin(\theta_s) = \frac{\lambda_{\theta}}{\lambda} = \frac{\lambda_{\theta}}{\sqrt{\lambda_d^2 + \lambda_q^2}} \\
\cos(\theta_s) = \frac{\lambda_{q}}{\lambda} = \frac{\lambda_q}{\sqrt{\lambda_d^2 + \lambda_q^2}}
\end{cases}$
4. Proposed sensorless control strategy

In order to cover a wide speed range control, a hybrid position observer is proposed in this paper which will be explained in details. Back-EMF based position estimation is assisted with high-frequency signal injection at low speeds, while at high speeds, high-frequency injection is dropped out and rotor position estimation is purely based on back-EMF.

A. High-frequency signal injection

In this paper a high-frequency voltage component (50 [V], 833 [Hz]) is injected to the estimated rotor d-axis as illustrated in Fig.8. Therefore, the corresponding high-frequency current component in estimated (d, q) axis are as (19) and (20). As can be seen from (19), if it is desired that rotor position is retrieved form $i_d^h$, the cross-saturation term, i.e., $L_{dq} \sin(2\Delta\theta)$ should be compensated. Otherwise, an error will be appeared in rotor position estimation. However, from (13) and using current-to-flux maps, (21) is concluded where subscript i means that high-frequency component of flux is coming from current model (flux maps). In the second term of 21, term $[1 - \cos(2\Delta\theta)]$ can be neglected if it is assumed that $\Delta\theta$ is a small angle. Therefore, (22) will be concluded.

\[
\begin{align*}
I_{dh} &= k \cdot [L_{cm} - L_{dm} \cos(2\Delta\theta) - L_{dq} \sin(2\Delta\theta)] \\
I_{qh} &= k \cdot [L_{dm} \sin(2\Delta\theta) - L_{dq} \cos(2\Delta\theta)]
\end{align*}
\] (19)

With comparing (22) with (19), it is seen that if high-frequency flux component in estimated $q$-axis is demodulated in place of current component, the cross-saturation error will be inherently overcome. If (22) is multiplied by $\sin(\omega_c t)$ and then low pass filtered (LPF), an error will be obtained (23) which will be source of a PI regulator to force it to zero. Fig.9 illustrates the tracking loop PLL used in this paper to obtain the rotor position, where $\omega_{HF}$ denotes for observed speed coming from high-frequency injection method.

\[
\begin{align*}
\epsilon &= \frac{u_c}{2\omega_c L_{dq}} \cdot [L_{qq} L_{dm} - L_{dq}^2] \sin(2\Delta\theta) \\
\Delta\theta &= \frac{1}{s} \epsilon
\end{align*}
\] (23)

Fig. 6. Sensorless DFVC of matrix converter-fed SyR motor.

Fig. 7. Stator flux observer.

Fig. 8. Actual and estimated rotor reference frame.

Fig. 9. High-frequency injection-based tracking loop.
B. Hybrid Rotor position estimation

Above a certain speed, rotor position can be obtained using back-EMF information. In this case, rotor position and speed can be obtained using (24), and (25), respectively, where $F_s$ is the sampling frequency and subscript $F$ denotes for position and speed obtained from flux observer.

\[
\begin{align*}
\sin(\theta_F) &= \frac{\lambda_d \cdot \lambda_{R1} - \lambda,q \cdot \lambda_{R1}}{|\lambda||\lambda|} \\
\cos(\theta_F) &= \frac{\lambda_d \cdot \lambda_{R1} + \lambda,q \cdot \lambda_{R1}}{|\lambda||\lambda|} \\
\end{align*}
\]

As said, rotor position estimation based on back-EMF is assisted with high-frequency injection method. Fig.10 shows the proposed position observer. As can be seen, a gain $k$ is inserted in the high-frequency injection loop. Below 50 [rpm], $k$ equals to 1 and above 100 [rpm], $k$ becomes zero which means that high-frequency injection is dropped out completely.

It should be noted that since there is no magnet in pure SyR motors, a minimum flux always is needed to ensure minimum excitation to the motor. This lower limit of flux amplitude is considered 0.7 [Vs] in this paper.

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5. Simulation results

In this section simulation results are presented to validate the proposed method. The synchronous reluctance motor and MC data is tabulated in Table 1. A simple method is adopted for MC nonlinear error compensation [19]. The results are presented in different speed and load levels.

<table>
<thead>
<tr>
<th>SyR motor</th>
<th>Rated power/Number of poles</th>
<th>2.2 kW / 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal Speed/Rated Torque</td>
<td>1500 rpm / 14 Nm</td>
<td></td>
</tr>
<tr>
<td>Phase resistance</td>
<td>3.5 $\Omega$</td>
<td></td>
</tr>
<tr>
<td>Moment of inertia ($J$)</td>
<td>0.005 kg.m$^2$</td>
<td></td>
</tr>
<tr>
<td>EUPEC FM35R12KE3ENG module</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Power devices</td>
<td>1200 V, 35 A, IGBT</td>
<td></td>
</tr>
<tr>
<td>$t_c$</td>
<td>0.3 $\mu$s</td>
<td></td>
</tr>
<tr>
<td>$t_f / t_r$</td>
<td>65-90 ns / 30-45 ns</td>
<td></td>
</tr>
</tbody>
</table>
Fig. 12 shows the performance of the proposed sensorless controller at low speeds. At \( t = 5 \) s the speed is reversed from 50 [rpm] to -50 [rpm] under full-load condition. The estimated and actual speeds, electromagnetic torque, \( i_{qs} \), stator flux amplitude, position estimation error, and three-phase currents are depicted in this figure. As it is seen, the position estimation error is very close to zero.

Also, the performance of the system at high speeds is investigated in Fig. 13. At \( t = 1 \) s, 1000 [rpm] step speed command is applied to the drive and at \( t = 4 \) s, full load torque is applied to the motor. Similar to low speed conditions, the position estimation error and dynamics of the system are acceptable.

As said, when the speed is above 50 [rpm], high-
frequency injection starts to be decreased and above 100 [rpm] is dropped out completely. This is shown in Fig. 14, where the estimated speed and voltage on \(\alpha\)-axis has been magnified. It is evident in this figure that, between 50 and 100 [rpm], high-frequency injection is decreasing and above 100 [rpm] is dropped out. Moreover, the performance of the drive is shown in this figure when the speed goes to 1500 [rpm] and again is reversed to -1500 [rpm].

6. Conclusion
A sensorless control technique for matrix converter-fed synchronous reluctance motor has been presented in this paper based on direct flux vector control method. A hybrid position observer has been presented to cover a wide speed range control. Below 50 [rpm], rotor position is estimated based on back-EMF method assisted with high-frequency signal injection methods, while above 100 [rpm], high-frequency injection is dropped out and back-EMF method remains alone. The simulation results have been presented for various speed and load levels showing good performance in transients and steady states.

References


