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A Cellular Potts Model of single cell migration in presence of durotaxis / Rachele, Allena; Scianna, Marco; Preziosi, Luigi. - In: MATHEMATICAL BIOSCIENCES. - ISSN 0025-5564. - 275:(2016), pp. 57-70. [10.1016/j.mbs.2016.02.011]

Availability: This version is available at: 11583/2649594 since: 2020-02-18T22:19:47Z

Publisher: Elsevier Inc.

Published DOI:10.1016/j.mbs.2016.02.011

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1	A Cellular Potts Model of single cell migration in
2	presence of durotaxis
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9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	Abstract_ Cell migration is a fundamental biological phenomenon during which cells sense their surroundings and respond to different types of signals. In presence of durotaxis, cells preferentially crawl from soft to stiff substrates by reorganizing their cytoskeleton from an isotropic to an anisotropic distribution of actin filaments. In the present paper, we propose a Cellular Potts Model to simulate single cell migration over flat substrates with variable stiffness. We have tested five configurations: i) a substrate including a soft and a stiff region, ii) a soft substrate including two parallel stiff stripes, iii) a substrate made of successive stripes with increasing stiffness to create a gradient and iv) a stiff substrate with four embedded soft squares. For each simulation, we have evaluated the morphology of the cell, the distance covered, the spreading area and the migration speed. We have then compared the numerical results to specific experimental observations showing a consistent agreement. Keywords_ Cell migration, Durotaxis, Cell polarity, Anisotropy, CPM Corresponding Author_ Rachele Allena e-mail: rachele.allena@ensam.eu Telephone: +33 (0)1 44 24 61 18 Fax : +33 (0)1 44 24 63 66
31	1. Introduction
32	Cell migration is a critical phenomenon occurring in several biological
33	processes, such as morphogenesis [1], wound healing [2] and tumorogenesis [3].
34	It takes place in successive and cyclic steps [4] and it is triggered by specific
35	interactions with the ExtraCellular Matrix (ECM). Actually, cell migration may
36	occur in the absence of external signals thereby typically resulting in a random

walk. However, in most situations, cells are able to sense their surrounding 37 38 environment and to respond for instance to chemical (i.e., chemotaxis) [5], 39 electrical (i.e., electrotaxis) [6] or mechanical (i.e., mechanotaxis) [7] fields or yet 40 to stiffness gradients (i.e., durotaxis) [8,9]. The latter mechanism consists of the cell preferential crawling from soft matrix substrates to stiffer ones, even in the 41 42 absence of any additional directional cues [10,11]. By forming local protrusions 43 (i.e., pseudopodia), the cells are in fact able to probe the mechanical properties of 44 the surrounding environment and to more strongly adhere over stiff regions. Additionally, such behaviour results in a substantial reorganisation of the 45 46 intracellular cytoskeleton. In fact, over soft substrates cells typically show an 47 unstable and isotropic distribution of actin filaments, which are poorly extended 48 and radially oriented, whereas over stiff substrates cell morphology is more stable 49 and exhibits significant spreading and often anisotropic arrangements of actin 50 filaments in the direction of migration (i.e., polarization) [12–16].

51 Although several computational models have been proposed in literature to 52 investigate single cell migration, only few of them deal with durotaxis. Among 53 others, it is worth to cite the work by Moreo et al. [17] who proposed a continuum approach based on an extension of the Hill's model for skeletal muscle behaviour 54 55 to investigate cell response on two-dimensional (2D) substrates. They showed, in agreement with experimental observations, that cells seem to have the same 56 57 behaviour when crawling on stiffer substrate and on pre-strained substrates. 58 Harland et al. [18] instead represented a cell as a collection of stress fibres 59 undergoing contraction and birth/death processes and showed that on stiff 60 substrates cells exhibit durotaxis and stress fibres significantly elongate. Dokukina and Gracheva [19] developed a 2D discrete model of a viscoelastic 61

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62 fibroblast cell using a Delaunay triangulation. At each node the balance of the 63 forces was determined by the contributions i) of the frictions between the cell and the substrate, ii) of a passive viscoelastic force and iii) of an intrinsic active force. 64 65 The authors then evaluated cell behaviour over a substrate with a rigidity step in good agreement with specific experimental observations. In fact, they found that 66 67 the cell preferentially moves on the stiffer substrate and turns away from the soft substrate as reported by [8]. Stefanoni et al. [20] proposed a finite element 68 69 approach able to account for the local mechanical properties of the underneath substrate and to analyze selected cell migratory determinants on two distinct 70 71 configurations: an isotropic substrate and a biphasic substrate (which consists of 72 two adjacent isotropic regions with different mechanical properties). Trichet et al. 73 [14] employed instead the active gel theory to demonstrate that cells preferentially 74 migrate over stiff substrates founding an optimal range of rigidity for a maximal 75 efficiency of cell migration. Further, in [21] a vertex-based approach (i.e., the so-76 called Subcellular Element Model, SCE) was set to represent intracellular 77 cytoskeletal elements as well as their mechanical properties. In particular, the 78 dynamics of such subcellular domains were described by Langevin equations, which account for a weak stochastic component (i.e., that mimic cytoplasmic 79 80 fluctuations) and elastic responses (i.e., modelled by generalized Morse 81 potentials) to both intracellular and intercellular biomechanical forces. The same 82 method was successfully applied in [22] for modelling substrate-driven bacteria 83 locomotion. Finally, in Allena and Aubry [23] a 2D mechanical model was proposed to simulate cell migration over an heterogeneous substrate including 84 85 slipping regions and to show that over softer regions the cell slows down and is less efficient. 86

87 In the present work, we describe a Cellular Potts Model (CPM, developed in 88 [24,25] and reviewed in [25–29]), which is a lattice-based stochastic approach employing an energy minimization philosophy, to reproduce single cell migration 89 90 over flat substrates with different rigidity. In particular, we test four configurations: i) a substrate including a soft and a stiff region, ii) a soft substrate 91 92 including two parallel stiff stripes, iii) a substrate made of successive stripes with 93 increasing stiffness to create a gradient and iv) a stiff substrate with four 94 embedded soft squares. For each scenario, we analyse cell behaviour in terms of morphology, distance covered, spreading/adhesive area and migration speed in 95 96 order to capture the essential mechanisms of durotaxis. The computational 97 outcomes are then compared with specific experimental observations taken from 98 the existing literature.

99 The rest of this paper is organized as follows. In Section 2, we clarify the 100 assumptions on which our approach is based and present the model components. 101 The simulation results are then shown in Section 3. Finally, a justification of our 102 model choices as well as a discussion on possible improvements is proposed in 103 Section 4. Additionally, the article is equipped with an Appendix that deals with 104 statistics and parameter estimates.

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2. Mathematical model

107 The cell-substrate system is represented using a CPM environment [24,25]. 108 The simulation domain is a three-dimensional (3D) regular lattice $W \in \vec{R}^2$ 109 constituted by identical closed grid sites, which are identified by their centre 110 $\mathbf{x} \in \vec{R}^2$ and labelled by an integer number $S(\mathbf{x}) \in N$ (which can be interpreted as 111 a degenerate spin) [30,31]. The boundary of a generic site \mathbf{x} , one of its neighbours and its overall neighbourhood are defined as $\P \mathbf{x}$, \mathbf{x} and $W'_{\mathbf{x}}$, respectively. Subdomains with identical label S form discrete objects S_{s} (with border $\partial \Sigma_{\sigma}$), which have an associated type $t(S_{s})$. In the case of our interest, t = M stands for the medium, t = C for the cells and $t = S_{1}$ for the i-th type of substrate. In this respect, we anticipate that each type of matrix region will differ for stiffness and therefore for adhesive affinity with moving individuals.

118 Cell dynamics result from an iterative and stochastic reduction of the energy of the overall system, given by a Hamiltonian H (units: Kg·m²/s²), whose expression 119 120 will be clarified below. The employed algorithm is a modification of the 121 Metropolis method for Monte Carlo-Boltzmann dynamics [24,32], which is 122 particularly suitable to simulate the exploratory behaviour of biological 123 individuals as cells. Procedurally, at each time step t of the algorithm, called 124 Monte Carlo Step (MCS), a randomly chosen lattice site x_{source} belonging to a cell tries to allocate its spin $\sigma(\mathbf{x}_{source})$ to one of its unlike neighbours $\mathbf{x}_{target} \in W'_{x}$, 125 126 which is also randomly selected. Then, the net energy difference DH due to the 127 proposed change of system configuration is calculated as

128
$$\mathsf{D}\mathcal{H}\Big|_{\mathcal{S}(\mathbf{x}_{\text{source}})\to\mathcal{S}(\mathbf{x}_{\text{target}})} = \mathcal{H}_{(\text{after spin copy})} - \mathcal{H}_{(\text{before spin copy})}$$
(1)

129 The trial spin update is finally validated by a Boltzmann-like probability function130 defined as

131
$$P\left[S\left(\boldsymbol{x}_{source}\right) \rightarrow S\left(\boldsymbol{x}_{target}\right)\right](t) = \min\left\{1, e^{-\frac{DH}{T_{c}}}\right\} \quad (2)$$

132 where *t* is the actual MCS and $T_c \hat{\mid} R_{\uparrow}$ is a Boltzmann temperature, that has been 133 interpreted in several ways by CPM authors (see [33] for a comment on this 134 aspect). However, we here opt to give T_C the sense of a cell intrinsic motility (i.e., 135 agitation rate), following the approach in [25]. Finally, it is useful to underline 136 that the matrix substrates are considered fixed and immutable.

As seen, the simulated system evolves to iteratively and stochastically reduce its free energy, which is defined by a Hamiltonian function *H* which, for any given time step *t*, reads

$$H(t) = H_{adhesion}(t) + H_{shape}(t)$$
 (3)

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141 $H_{adhesion}(t)$ is deduced from the Steinberg's Differential Adhesion Hypothesis 142 (DAH) [24,34] and is due to the adhesion between cells and extracellular 143 components (i.e., the medium or a given type of substrate). In particular, it reads

$$\boldsymbol{H}_{adhesion}\left(t\right) = \boldsymbol{H}_{adhesion}\left(t\right) = \mathop{\text{adhesion}}_{\left(\P \times \hat{\boldsymbol{i}} \ \P S_{S}\right) \subsetneq \left(\P \times \hat{\boldsymbol{i}} \ \P S_{S^{(1)}}\right) J_{t\left(S_{S^{(1)}}\right), t\left(S_{S^{(1)}}\right)}$$
(4)

145 with \mathbf{X} and \mathbf{X}^{f} two neighbouring sites and S_s and S_{st} two neighbouring objects 146 (with borders $\P S_s$ and $\P S_{st}$, respectively). $J_{t(S_{s(\mathbf{X})}), t(S_{s(\mathbf{X})})} \hat{\mathbf{I}} R_{t}$ are constant and 147 homogeneous binding forces per unit area. They are symmetric with respect to 148 their indices and can be specified as follows:

149 - $J_{C,M}$ is the adhesive strength between the cells and the collagenous medium 150 which is constituted by a mixture of soluble adhesive ligands (i.e., carbohydrate 151 polymers and non-proteoglycan polysaccharides) and water solvent;

152 - J_{C,S_i} gives the adhesive strength between the cells and i-th type of substrate. 153 Recalling the minimization theory of the CPM, we assume that the stiffer the 154 substrate *i*, the lower the corresponding value J_{C,S_i} (i.e., the higher the adhesion 155 between the cells and the i-th type of substrate). This is a pivotal hypothesis of our 156 approach: it is consistent since it has been widely demonstrated in the

- experimental literature that cells generate higher traction forces and generate more
 stable focal adhesion points when migrating over stiffer substrates [16,35–38].
- 159 $H_{shape}(t)$ defines the geometrical attributes of each cell S_s , which are written 160 as elastic potentials as it follows:

161
$$H_{shape}(t) = H_{volume}(t) + H_{surface}(t)$$
$$= \mathop{\bigotimes}_{S_{s}}^{\acute{e}} \mathop{\bigotimes}_{K_{S_{s}}} \left(V_{S_{s}}(t) - V_{C} \right)^{2} + n_{S_{s}}(t) \left(\mathop{s}_{S_{s}}(t) - \mathop{s}_{C} \right)^{2} \mathop{\widecheck{u}}(5)$$

where $v_{S_s}(t)$ and $s_{S_s}(t)$ are the actual volume and surface of the cell S_s , 162 whereas V_c and S_c the corresponding cell characteristic measures in the initial 163 resting condition. k_{S_s} and $n_{S_s}(t)$ are instead two mechanical moduli in units of 164 energy. The former is linked to volume changes and, assuming that cells do not 165 166 significantly grow during migration, is considered constant with a high value (i.e., $k_{S_s} = k_c >> 1$) for any individual S_s . The latter refers to the rigidity of a cell. As 167 we will explain in details later on, for each cell S_s , N_{S_s} is assumed to depend on 168 169 the underneath type of substrate. In particular, each cell decreases its initially high (i.e., >> 1) rigidity, thereby being more able to deform, if it comes in contact with 170 171 a stiff substrate. This assumption is consistent with experimental observations on the fact that cell contact with stiff matrix regions activate downstream 172 intracellular pathways resulting in acto-myosin dynamics and therefore in 173 174 cytoskeletal remodelling [8,39]. More specifically, it seems that certain cells have 175 a binary sensor at their membrane junction sites that allows them to switch from a 176 relaxed and rounded morphology, when the substrate is softer than the cell's elastic modulus [39-43], to a fan-shaped morphology with abundant stress fibres, 177 178 when the substrate is stiffer or as stiff as the cell itself [39]. Further, it has been 179 shown that cells tend to isotropically and poorly spread on soft substrates, 180 whereas they form pseudopodia randomly distributed along the membrane on stiff 181 substrates, resulting in a significant anisotropic spreading [16]. In this respect, 182 according to several experimental observations [16,35–38,44], there exists a linear 183 relationship between the adhesion forces exerted by the cell on the substrate and 184 the spreading area of the cell. More specifically, the larger the contact area 185 between the cell and the substrate, the higher the number of focal adhesion points 186 that can be established. Nonetheless, the sequence of events is still unclear and 187 two main processes may occur when a cell is seeded on a stiff substrate [45]:

- i) the cell adheres because of the stiffness of the substrate, then it significantlyspreads;
- ii) the cell spreads because of the stiffness of the substrate, then it more stronglyadheres.

Such uncertainty is the reason why in the present model both the adhesive
parameters and the cell rigidity directly depend on the substrate stiffness, but are
independent from each other.

The main components and the scales involved in the proposed model are summarized in the diagram in Fig. 1. Finally, all the parameters of the simulations are reported in Table 1, while the Appendix provides a careful explanation of how they have been estimated.

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3. Numerical simulations

201 The characteristic size of each lattice site is 4 μ m and the geometrical domain 202 W is a 70x70x30 regular grid (280 μ m x 280 μ m x 120 μ m) with no-flux 203 boundary conditions in all directions. This choice mimics the situation of a 204 delimited experimental device, where cells are not able to overcome the physical 205 barriers. All our CPM cells are initially a hemisphere of a radius of 20 µm, whose initial position will be specified for each simulation setting. A MCS is set to 206 207 correspond to 2 s of actual unit of time (see the Appendix for a comment on this aspect), which results in simulations covering time intervals between 16 min to 208 209 5.5 h. This choice enables cells to migrate over sufficiently long paths in order to 210 compare numerical results and proper experimental observations. We have tested 211 several cell-matrix settings, which are presented in the followings. The resulting 212 simulations were performed on a modified version of the open source package 213 CompuCell3D (downloadable at www.compucell3d.org). In particular, a Phyton 214 script was specifically developed to account for substrate-dependent cell rigidity.

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3.1 Cells preferentially crawl over stiff substrates

217 We first consider a substrate split into a soft and a stiff region, i.e., t = S and $t = S_2$ (see Fig. 2a). A cell S_1 is then seeded at the centre of the substrate and it 218 is allowed to move for 500 MCS (approximately 16 minutes). The rigidity of S_1 , 219 n_{S_1} , has initially a high value $\nu_{\Sigma_1} = \nu_C = 25 \cdot 10^{-3} \text{ Kg/s}^2 \text{m}^2$. However, it is allowed 220 to decrease, of 10^{-3} Kg/s²m² for MCS until a threshold value n_t equal to 10^{-2} 221 Kg/s^2m^2 , while the cell is in contact with the stiff region S₂, thereby leading to a 222 223 flattening of the initially rigid cellular hemisphere. In mathematical terms, we 224 indeed have that

$$\nu_{\Sigma_{1}}(t) = \begin{cases} \max(\nu_{\Sigma_{1}}(t-1) - 10^{-3}; \nu_{t}) \text{ if } \exists (x, x' \in \Omega'_{x}): x \in \Sigma_{1} \text{ and } x' \in S_{2}; \\ \nu_{\Sigma_{1}}(t-1) & \text{else,} \end{cases}$$
(6)

for each MCS.

226 We then study how cell behaviour is affected by variations in the ratio between the adhesive affinity of the cell with either the soft or the stiff substrate region. In 227 particular, we keep fixed $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ while decreasing the 228 value of J_{C,S_2} from $25 \cdot 10^{-15}$ Kg/s² to $1 \cdot 10^{-15}$ Kg/s² (which is equal to J_{stiff} , 229 the lowest value consistent with the case of our interest, see the Appendix). As 230 summarized in Fig. 3c, when J_{C,S_2} decreases, the cell is biased to crawl towards 231 232 the stiff domain, as it is confirmed by the plot of the trajectories of its center of mass deriving from independent simulations. In fact, over a period of 500 MCS (≈ 233 16 minutes), the cell randomly moves around the substrate centre when $\frac{J_{C,S_1}}{J_{C,S_2}} = 1$ 234 (Fig. 3a) while, when $\frac{J_{C,S_1}}{J_{C,S_2}} = 25$, the cell trajectories dramatically shift over the 235 stiff part of the substrate (Fig. 3b). Our numerical results are sustained and 236 consistent with the experimental observations according to which cells (i.e., 237 238 fibroblasts, smooth muscle cells, Mesenchymal Stem Cells (MSCs)) crawl from 239 soft (1 to 5 kPa) to stiff (34 to 80 kPa) substrates (i.e., gels or polyacrylamide sheets) [9-11,46]. Notably during motion towards the stiff substrate, our CPM 240 241 cell is also allowed to increase its remodeling ability, as its rigidity 242 ν_{Σ_1} progressively decreases upon contact with substrate S₂, according to Eq. (6). 243 In this respect, a further set of simulations evaluates cell morphological 244 differences due to the underneath type of substrate. Keeping the same domain as in Fig. 2a, two cells, i.e., S_1 and S_2 , are initially seeded in the middle of the soft 245 246 and the stiff regions, respectively. The rigidity of the two cells is then regulated by Eq. (6). As reproduced in Fig. 4 (in particular, panel (a) represents the final cell 247 248 morphologies as resulted from a single representative simulation, whereas panel 249 (b) gives the mean final cell morphologies, as the plain ellipsoids derive from an 250 interpolation procedure of the cell adhesive areas coming from independent 251 simulations, see the Appendix for further details), both individuals do not 252 significantly move across the domain during a time lapse of 500 MCS (approximately 16 min). However, the adhesive area of the cell located over the 253 254 soft region is almost 30% lower than the adhesive area of the cell that crawls over the stiff substrate (Fig. 4c). Such a cell behaviour is consistent with the 255 256 experimental data by Lo and co-workers on 3T3 fibroblasts cultured on flexible polyacrylamide sheets coated with type I collagen, where a transition in rigidity 257 258 was introduced by a discontinuity of the bis-acrylamide cross-linker, that resulted in two substrate regions with Young's modulus equal to either 14 kPa and 30 kPa 259 260 [46]. In particular, on one hand, the value of the adhesive area of our CPM cell 261 seeded on the soft substrate is not surprisingly similar to the corresponding data by Lo and co-workers [46], since we used such an experimental quantification for 262 263 our parameter estimate (see the Appendix). On the other hand, the adhesive area 264 of the CPM cell seeded on the stiff region is instead a completely independent and self-emerging model outcome: therefore its consistency with the measurements by 265 266 Lo and colleagues [46] is relevant point of our work.

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3.2 Stiff vs soft substrate in the presence of an external cue

For the second series of simulations we consider again a domain split into a soft ($t = S_1$ such as $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$) and a stiff ($t = S_2$ such as $J_{C,S_2} = J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$) region, but an additional external potential is introduced. This results in an imposed artificial bias in the spin flip rate that is able to affect the direction of cell migration. Entering more in details, the expression of the Hamiltonian function presented in Eq. (3) is modified as it follows

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$$H(t) = H_{adhesion}(t) + H_{shape}(t) + H_{potential}$$
(7)

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277 where $H_{potential} = -v_{ext} \left(\mathbf{x}_{target} - \mathbf{x}_{source} \right)$ and v_{ext} is a vector whose components 278 determine the direction of the potential and whose modulus gives the relative 279 importance in the overall system energy. For the sake of simplicity, we assume 280 that the potential is constant in time and homogeneous throughout the entire 281 domain. As we will see later, it is in fact an artificial term that simply helps cells 282 to maintain a sustained directional movement. In this respect, what is relevant is 283 only its modulus, i.e., $|\mathbf{v}_{ext}|$. We then test two configurations:

286 b) the same cell Σ_1 placed at the south-west corner of the substrate and the 287 external potential directed towards the north-east corner.

In both cases, we set $|v_{ext}| = 7 \cdot 10^{-21} \text{Kg} \cdot \text{m/s}^2$, which results in plausible cell velocities (see later) and the simulations last 10000 MCS (approximately 5.5 h). Further, cell rigidity is again regulated by Eq. (6).

In system configuration a) (see Movie 1 and Fig. 5a), the external cue guides the cell towards the north-west corner of the domain. In particular, when a part of the cell comes into contact with the stiffer substrate, it becomes the leading edge. Further, the moving individual clearly accelerates as soon as it crosses the boundary between the two matrix regions (3.6 μ m/s versus 4.5 μ m/s, Fig. 5c), as experimentally observed in [8] for fibroblasts crawling over polyacrylamide 297 sheets. An increment of the adhesive area is observed as well when the cell shifts298 over the stiff region.

299 In the case b), the external potential forces the cell to move towards the north-300 east corner of the domain (see Movie 2 and Fig. 5b). However, as soon as the 301 individual approaches the soft region, it changes orientation, and starts moving 302 and elongating parallel to the boundary between the two substrate regions. These 303 outcomes may be compared to the experimental observations obtained by Lo et al. 304 in [46], who cultured fibroblasts on the already described substrate system, i.e., 305 characterized by two areas with different Young's modulus. In particular, Lo and 306 colleagues seeded cells at low density to minimize the effects of intercellular 307 interactions and to avoid that pulling or pushing forces from neighbours 308 individuals may alter cell substrate probing processes (thereby impeding cells to 309 freely move across the soft and the stiff regions). Then, cell migration was 310 recorded over a time span of 10 h. Similarly to our numerical outcomes, the 311 authors found that as cells move towards a stiffer substrate, new lamellipodia are 312 formed in the direction of migration, thereby resulting in the dominant front end 313 of the individuals. On the opposite, local retractions occur when cells approach a 314 soft region, inducing therefore a change of direction. In a second series of 315 experiments, Lo and co-workers showed that mechanical inputs triggered by 316 substrate deformations might also control formation and retraction of 317 lamellipodia. In particular, they externally pulled or pushed the substrate away or 318 towards the cells centre to find that, due to the centripetal forces exerted by the 319 3T3 fibroblasts on the substrate [46], in the first case less motion is produced, 320 since cells experience a softening of the substrate, whereas in the second case the overall motion is increased, since cells perceive the substrate as stiffer. In the 321

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CPM model proposed here, the matrix substrates are not deformable, therefore the numerical simulations are unable to capture the experimental observations coming from this second set of assays.

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3.3 Two stiff stripes embedded in a soft substrate

The third configuration that has been tested includes a soft substrate (again 327 $t = S_1$ with $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ with two embedded stiff stripes (again 328 $t = S_2$ with $J_{C,S_2} = J_{stiff} = 1.10^{-15} \text{ Kg/s}^2$, which are both 28 µm-wide (Fig. 2b). 329 A cell S_1 is initially seeded at the south-west corner, whose rigidity is allowed to 330 decrease following the constitutive law (Eq. (6)). An external potential is then 331 332 introduced towards the north-east corner of the domain: its intensity $|v_{ext}|$ is allowed to vary from a minimal value of $7 \cdot 10^{-21}$ Kg·m/s² to a maximal value of 333 28.10⁻²¹ Kg·m/s². All simulations last 10000 MCS, which correspond to nearly 5.5 334 h. In the case of a low $|\boldsymbol{v}_{ext}| = 7 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ (see Fig. 6a and Movie 3), the cell 335 336 typically migrates towards the first stiff substrate stripe: then it remains stuck over 337 it and goes on migrating along such a matrix region. Furthermore, its morphology, due to the dependency of its elasticity on the underneath type of substrate, 338 339 changes as the crawling individual acquires an elongated shape. Such a behaviour 340 is due to the fact that the external potential is too low to overcome the adhesive 341 interactions between the cell and the stiffest substrate: in particular, the individual 342 has not energetic benefits (deriving from the external bias) to move further in the domain, i.e., to pass the first stiff stipe. The outcomes of our CPM are consistent 343 344 to that observed for cells (i.e., endothelial cells or fibrosarcoma cells) seeded on

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2D substrates (i.e., maleic acid copolymer surfaces) structured with fibronectin stripes which orient their actin fibres along the stripe direction [47–49].

347 On the other hand, if the modulus of the external potential increases, we have a 348 higher percentage of cells that are able to cross the entire domain (Fig. 6b). In particular, when $|\boldsymbol{v}_{ext}|$ is maximal (i.e., 28·10⁻²¹ Kg·m/s², Fig. 6c and Movie 4), 349 the cells constantly migrate at the north-east corner of the domain passing also the 350 351 second stiff stripe. In this case, the cell average velocity increases over the stiff 352 stripes (about 4.4 μ m/s) whereas it varies between 3.6 μ m/s and 3.9 μ m/s over the 353 soft regions (Fig. 6d). With the maximal external potential, cell morphology does 354 not significantly vary, as the moving individuals typically maintain an almost 355 hemispheric shape, without substantial elongation or increments in the adhesive 356 area during the entire motion. They in fact behave as translating rigid bodies, 357 subjected to an external high force. This interesting behaviour is the consequence 358 of the fact that the cells do not need to reorganize (nor have enough time to do it) 359 to be able to crawl, as their motion is mainly due to the external bias: the specific 360 substrate regions are only able to further accelerate (or partially slow down) cell 361 movement, as previously commented. The numerical outcomes in the case of low or intermediate values of $|v_{ext}|$ can be compared to those experimentally tested by 362 363 Choi et al. [50] and Vincent et al. [51], where different cell phenotypes were 364 seeded on micropatterned hydrogels with stiffness gradient. Although no external 365 bias was introduced in such experimental configurations, a similar behaviour may 366 be observed. In the former work [50], the authors proposed two mechanically-367 patterned hydrogels: one constituted by 100 µm stiff (10 kPa) and 500 µm soft (1 368 kPa) stripes and one containing 500 µm stiff (10 kPa) and 100 µm soft (1 kPa). 369 First, Adipose-derived Stem Cells (ASCs) and C2C12 myoblasts were allowed to 370 adhere and both were able to sense the stiffness gradient and to migrate towards 371 the stiffer stripes (i.e., durotaxis) [46]. Such behaviour was also observed when 372 cells were far away from the stripe interface (around 250 µm). Nevertheless, since 373 cells only detect stiffness differences over short distances (around some microns) 374 [52], in this case the authors implied that the phenomenon was mostly due to 375 random walk towards the interface rather than to durotaxis itself. Regarding the 376 morphology of the cells, both ASCS and C2C12 myoblasts aligned in the 377 direction of the long axis of the stripe as we observe in our numerical simulations 378 (Fig. 5a and Movie 3) in the case of low intensity of the external potential. Second, less contractile cells such as neurons were seeded on the hydrogels, 379 380 which did not show any preferential adhesion confirming previous experimental 381 observations according to which they prefer a softer niche [53].

382 In the latter work [51], the authors developed three types of polyacrylamide (PA) hydrogel systems of stiffness gradients: physiological (1 Pa/µm), 383 384 pathological (10 Pa/ μ m) and step (100 Pa/ μ m). The step stiffness gradient, which 385 is the configuration of interest for the simulations presented above in this section, 386 was constituted by 500 μ m wide regions of soft PA alternated with ~100 μ m wide 387 stripes of stiff hydrogel producing a stripped stiffness profile. MSCs were plated 388 and they spread and attached independently of the gradient strength or the 389 stiffness within hours after the seeding, whereas after 3 days they started to 390 migrate towards stiffer regions. Additionally, cells crawled at 18 \pm 0.7 μ m/hr, 391 which is approximately 6-fold faster than on the other gradient configurations 392 discussed in the same paper (i.e. physiological and pathological) and confirms that 393 durotaxis velocity is influenced by gradient strength [11].

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3.4 Stiffness gradient

397 In this section, we present the results for a simulation involving a substrate made of six successive stripes (i.e., t = S, where i = 1, ..., 6, each 46 µm-wide) 398 which are organized to obtain a soft-to-stiff gradient from the left to the right side 399 400 of the domain (from the red to the yellow subdomains). Such substrate regions are characterized by different cell adhesive affinity, i.e., J_{C,S_i} , which vary from 401 $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ to $J_{C,S_6} = J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$, respectively (see 402 Fig. 2c and the corresponding caption for the specific details). A cell S_1 is 403 404 initially seeded at the south-west corner and an external potential is introduced towards the north-east corner of the domain, whose magnitude $|v_{ext}|$ is varied 405 again from a minimal value of $7 \cdot 10^{-21}$ Kg·m/s² (Movie 5) to a maximal value of 406 $28 \cdot 10^{-21}$ Kg·m/s² (Movie 6). The rigidity n_{S_1} of S_1 is allowed to decrease (from 407 the usual initial high value of $\nu_c = 25 \cdot 10^{-3} \text{ Kg/s}^2 \text{m}^2$) with a law analogous with 408 Eq. (6), but which takes into account of the presence of different types of 409 410 substrates, i.e.,

$$v_{\Sigma_1}(t) = \begin{cases} \max(v_{\Sigma_1}(t-1) - v_i; v_t) \text{ if } \exists (x, x' \in \Omega'_x): x \in \Sigma_1 \text{ and } x' \in S_i; \\ v_{\Sigma_1}(t-1) \text{ else,} \end{cases}$$
(8)

411 where *t* is the actual MCS, n_t is the usual threshold value (equal to 10^{-2} Kg/s²m²) 412 and i = 2,...,6. In this respect, $v_i = 0.05 \cdot 10^{-3}$, $0.06 \cdot 10^{-3}$, $0.1 \cdot 10^{-3}$, $0.2 \cdot 10^{-3}$, $1 \cdot 10^{-3}$ 413 Kg/s²m² while the cell is in contact with substrate S_2, S_3, S_4, S_5, S_6 , respectively. 414 n_{S_1} remains indeed constant and equal to v_c if the cell is located over the softest 415 substrate S_1 . All the resulting simulations last 10000 MCS (5.5 h). As reproduced 416 in Fig. 7a, the percentage of cells able to reach the north-east corner increases 417 concomitantly with increments of $|\boldsymbol{v}_{ext}|$. Moreover, by fixing $|\boldsymbol{v}_{ext}| = 28 \cdot 10^{-21}$ 418 Kg·m/s², it is possible to observe that the cell average velocity increases from 3.6 419 µm/s to 4.4 µm/s as they move from softer to stiffer substrates (Fig. 7b). This 420 result is coherent with the model outcomes of the previous set of simulations (i.e., 421 see Fig. 6c and d), where we have observed that in the case of very high external 422 potential cells accelerate while crossing on stiffer matrix regions, even if they do 423 not significantly undergo morphological transitions.

424 A similar configuration was experimentally proposed by Cheung et al. [10] 425 using a microfluidics-based lithography technique, fabricated a who, 426 micropatterned cell-adhesive substrate made of a series of PEG-fibrinogen 427 hydrogels with uniform stiffness ranging from 0.7 to 50 kPa. Human Foreskin 428 Fibroblasts (HFFs) were then plated and their migratory trajectories were analysed 429 over 22 h. The authors found that the cells that were initially seeded on a stiffness 430 frontier tended to migrate towards the stiffer region, while cells plated on uniform 431 stiffness spread in both directions.

432

433

3.5 Role of the characteristic dimension of the gradient stiffness

434 The external potential introduced in most of the previous sets of simulations, is 435 an artificial term that is included in the Hamiltonial to bias and sustain cell 436 movement across the entire matrix substrate. In experimental assays, the directional component in cell motion is typically established by geometrical cues, 437 438 such as microtracks and microchannels [54,55], or gradients of soluble or 439 insoluble chemical substances (chemotaxis and haptotaxis, respectively) or, in the 440 case of our interest, gradients of substrate stiffness [10,51]. However, we have observed from our simulations that the sequence of different types of substrate 441

442 stripes employed in the previous section does not suffice to determine a persistent 443 cell movement across the entire matrix, since a high enough external potential has 444 to be included to allow cells reach the north-east corner of the domain (see the 445 plot in Fig. 7a). The reason of this discrepancy between computational and 446 experimental outcomes relies in the fact that "real cells", once established a 447 direction of movement, are able to dramatically orient their cytoskeleton (via the 448 polarization of actin filaments) and, eventually, start a persistent shape-dependent 449 locomotion. This way, real individuals are able to cross also large portions of 450 substrates without slowing down or changing direction. Such a cell behaviour can 451 not be captured in our approach since we do not include a proper model 452 component reproducing selected intracellular cytoskeletal dynamics (in this 453 respect, the interested reader may refer to [56,57], where polarization processes 454 and the subsequent cell persistent movements are simulated in CPMs either by 455 introducing an asymmetric correction to the Boltzman probability law or by adding a further inertial term in the Hamiltonian). The CPM cells of our model are 456 457 only able to isotropically spread (due to decrements in their rigidity upon contact 458 with stiff substrates) or elongate following the geometry of the underlying matrix 459 region in order to maximize their adhesive interactions with the stiffer areas of the 460 domain (but only when the external potential is substantially low, see Fig. 6a and 461 c). However, the model presented in this paper can be used to predict if a 462 sustained cell motion can be achieved by only varying the geometrical 463 characteristics of the matrix substrate. With this purpose in mind, we employ the 464 same type of domain as in Section 3.4, but we progressively decrease the width of 465 the substrate stripes. We then evaluate the minimal magnitude of the external 466 potential needed by cells to reach the border of the domain opposite to their initial

467	position (again the south-west corner). Cell rigidity follows the law in Eq. [8] and
468	the simulations last 10000 MCS (5.5 h). As summarized in panel (a) of Fig. 8, we
469	can observe a tri-phasic behaviour. For sufficiently wide stripes (i.e., $>45~\mu m$), a
470	cell sustained movement results only with very high external potentials (i.e.,
471	>25 $\cdot 10^{-21}$ Kg·m/s ²). Then, for lower stripe widths (i.e., in the range of 35-45 μ m)
472	the critical value of the external potential modulus decreases almost linearly.
473	Finally, for low enough stripe widths (i.e., $< 35 \ \mu m$), the potential necessary to
474	have a sustained cell movement significantly drops, until becoming negligible for
475	stripe widths lower than 35 μ m (Movie 7). Summing up, we can state that the
476	characteristic dimension of the stiffness gradient (here determined by the width of
477	the matrix stripes), which allows a persistent cell movement without the artificial
478	help of an external bias, is lower than the mean cell diameter (i.e., that in our
479	simulations is around 40-45 μ m). From a computational viewpoint, the rationale
480	of this behaviour is that when a CPM cell is located on a given substrate stripe it
481	is however able to wandering its close proximity (due to the stochastic Metropolis
482	algorithm) which, if the stripe width is low enough, includes the neighbouring
483	matrix region. In this respect, the CPM cell simultaneously experiences the
484	adhesive affinity with a couple of neighbouring substrate stripes and then it moves
485	towards the stiffer one, thereby advancing across the domain. Such a process is
486	reiterated for all pairs of substrate stripes, thereby resulting in a sustained
487	directional movement. These results can be interpreted from an experimental
488	viewpoint as a prediction on the fact that cells may exhibit a persistent motion
489	also without an intracellular polarization, i.e., by only maintain an amoeboid
490	movement, if the substrate stiffness gradient is sufficiently fine-grained.

491 We finally conclude this section by analysing how cell velocity is affected by the 492 wide of the substrate stripes, in the range of values sufficiently low to have a 493 sustained cell crawling in the absence of an external potential (i.e., $< 35 \ \mu m$). As it 494 is possible to see in panel (b) of Fig. 8, lower widths of the substrate regions 495 (which means, as previously seen, more fine-grained stiffness gradients) results in 496 increments in cell average velocity. From the computational viewpoint, this is due 497 to the fact that the more the different stripes of the matrix are small, the more the 498 previously described cell probing mechanism is facilitated and accelerated, 499 thereby resulting in higher cell average velocities.

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501

3.6 Soft squares embedded in a stiff substrate

502 As a final simulation, we test the substrate configuration in Fig. 2d, where four soft squares ($t = S_1$ with $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$) are embedded in a stiff 503 substrate ($t = S_2$ with $J_{C,S_2} = J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$) at its three corners (north-504 west, north-east and south-east) and at the centre. A cell S_1 is initially seeded at 505 the south-west corner and an external potential is introduced towards the north-506 507 east corner of the domain, whose magnitude $|v_{ext}|$ has been set equal to an intermediate 14.10⁻²¹ Kg·m/s². As usual, cell rigidity is allowed to decrease 508 according to Eq. (6) and the observation time is 10000 MCS (i.e., nearly 5.5. h). 509 510 The cell starts moving in the direction determined by the potential with a trajectory of approximately 45° but, as soon as it encounters the central soft 511 512 square, the cell avoids and circumvents it. As the original path is recovered, the 513 cell needs to squeeze between the north-east square and the substrate frontier in 514 order to achieve the target corner of the domain (Movie 8 and Fig. 9). The choice 515 of the migration track may depend on the initial position of the cell. In the present 516 simulation, the cell is seeded along the substrate diagonal, thus the probability of 517 circumventing the central soft square counter clockwise (as it happens here) or 518 clockwise are the same. However, if the cell is seeded slightly downward and/or 519 right, it will most certainly employ a counter clockwise trajectory, whereas if it is 520 plated upward, it will probably follow a clockwise path. It is useful to notice that with a significantly higher modulus of the external potential the cell would have 521 522 been able to pass across the soft regions, without deforming to avoid them, 523 coherently with the simulations proposed in Fig. 6c.

524 This configuration is similar to that proposed in [23] where the cell must 525 avoids two slipping regions in order to reach the external cue placed at 45°. 526 Although the employed numerical approaches are substantially different, taken 527 together the outcomes confirm the tendency of the cell to migrate over stiffer 528 substrates where the higher adhesion forces may be developed.

529

530 **4.** Conclusions

531 In this paper we have proposed a three-dimensional CPM approach to simulate 532 single cell migration over matrix domains in which soft and stiff regions are 533 combined.

The CPM method is becoming an increasingly common technique for the mathematical modelling of a wide range of biological phenomena, including avascular and vascular tumor growth [58–61], gastrulation [62], skin pigmentation [63], yeast colony growth [64], stem cell differentiation [65], fruiting body formation of Dictyostelium discoideum [66], epidermal formation [67], hydra regeneration [66], retinal patterning [68], wound healing [69,70], biofilms [71],

540 chick limb-bud growth [72-74], cellular differentiation and growth of tissues, 541 blood flow and thrombus development [75-77], angiogenesis [70,78-81], 542 dynamics of vascular cells [82-85], cell scattering [86], cell migration on and 543 within matrix environments [56,57,87]. Notably, in [88] the authors introduced a 544 compartmentalized approach to subdivide a Myxococcus Xanthus into strings of 545 subcellular domains with different rigidity, this in order to give the bacterium a 546 particular geometry and to control its overall length. Further, in [89] a keratocyte 547 has been represented with a set of undifferentiated hexagonal subunits, which has 548 allowed to reproduce its polarization during motion. In this respect, it is useful to 549 underline that, as commented in [25], although these approaches are correct, the 550 fact that the proposed subcellular compartments do not have an immediate or 551 direct correspondence with real subcellular elements, has limited the practicality 552 and the usefulness of the relative models. The most accurate way of realistically 553 reproducing different and extremely complex cell morphologies is to 554 compartmentalize them according to the compartmentalization "suggested in 555 nature", and thus to explicitly represent for instance the plasmamembrane (PM), 556 the cytosolic region, the nucleus, and other intracellular organelles (e.g., 557 mitochondria, ribosomes, Golgi apparatus, and secretory granules). This way is in 558 fact possible, for example, to localize within the proper cell compartment selected 559 biochemical pathways and/or to study the role play by the nucleus in cell 560 movement, given its higher rigidity with respect to the surrounding cytoplasm 561 [56,57,87].

562 Key benefits of the CPM energetic formalism are its simplicity and 563 extensibility: almost any biological mechanism can in fact be included in the 564 model, simply by adding an appropriate generalized potential term in the

565 Hamiltonian functional. For instance, it is possible to easily comprehend the 566 importance of each mechanism involved in the simulated phenomenon by only 567 altering the relative Potts parameter, so that the other terms in the Hamiltonian 568 scale accordingly. In particular, by equating all the other terms to zero, it is 569 possible to understand whether a mechanism is individually capable of producing 570 the phenomenon of interest or whether it requires cooperative processes. Further critical features of the CPM (compared to alternative cell-based modelling 571 572 approaches that represent biological individuals as point particles, such as Interacting Particle Systems or purely discrete models, or fixed-sized spheres or 573 574 ellipsoids, such as Cellular Automata) is that i) it differentiates between bound 575 and unbound regions of cell membranes and ii) morphological changes can be 576 easily and realistically reproduced. These characteristics have been fundamental 577 in our choice of using a CPM to describe the phenomenon of our interest since 578 they are particularly suitable to implement our two main model assumptions, 579 drawn according to the experimental observations reported in the literature: i) the 580 adhesiveness of cells changes according to the substrate stiffness, that models the 581 fact that higher traction forces and more stable focal points are generated over a 582 stiffer substrate [16,35–38] and ii) each cell adapts its morphology as a function 583 of the substrate stiffness so that over a soft region it maintains a rounded shape, 584 whereas over a stiffer domain a significant spreading occurs [39-43]. The 585 considerations above are in remarkable agreement with the scholarly dissertation 586 proposed by Voss-Böhme in the conclusive section of her article [33]. She in fact 587 argued that the application of CPMs is reasonable when the biological problem of 588 interest involves "considerable variability in cell sizes and shapes", which is the 589 case of the cell morphological transitions due to contact with soft/stiff substrates.

590 On the opposite, when "essentially isotropic, non-polarized cells of uniform size 591 are considered", it would be preferable the use of more coarse-grained modelling 592 approaches, like the already cited Cellular Automata or Interacting Particle 593 Systems, which are better analysed both mechanistically and analytically.

Further, we have opted for a 3D setting since the adhesive interactions between cells and matrix substrates occur *under* the cell body (i.e., they are localized over the contact area between the cells themselves and the underneath substrate). In bidimensional CPMs cell-matrix interactions instead occur only "laterally", as the cells do not move *on* substrates but *within* the same plane as the matrix. Indeed, a three-dimensional domain is more appropriate to reproduce an adhesive-driven cell migration.

601 We have then used our CPM-based approach to test cell behaviour in different 602 domain configurations, where soft and stiff substrates coexisted. In particular, the 603 numerical outcomes have been consistently compared to specific experimental 604 data, in terms of cell morphology, distance covered, spreading/adhesive area and 605 migration speed. In this respect, following the dichotomy proposed in the already 606 cited work by Voss-Böhme [33], we have interpreted our CPM as a 607 phenomenological method. In particular, the resulting remarkable agreement (not 608 only qualitative but also quantitative) between in vitro and in silico data has 609 allowed us to conclude that our approach, although strongly simplified, was able 610 to capture the main mechanisms underlying cell migration in presence of 611 durotaxis. We have finally turned to use our model in a *predictive* manner, with 612 the aim to analyse how the external potential and the critical dimensions of a 613 substrate stiffness gradient (here represented by the width of the different types of 614 matrix stripes) affect cell movement. In this respect, we have found that cells are

able to achieve a sustained cell migration in the absence of an external bias (and
in the absence of intracellular polarization mechanisms) where the underneath
matrix is characterized by a sufficient fine-grained gradient of rigidity.

618 However, our approach is not free of some serious shortcomings. First, it does 619 not reproduce the active and continuous reorganization of the cytoskeleton, which 620 provides the support for cells and mediates their coordinated and directed 621 movements, mainly in response to mechanical tensions and stresses exchanged 622 with the underneath substrate. In this respect, selected geometrical and mechanical properties of the cells, such their elongation and elasticity, should evolve 623 624 according to a model of actin filament dynamics, which are powered, for example, by ATP (adenosine triphosphate) hydrolysis and controlled by inside-out 625 626 signalling mechanisms transmitted from and by the extracellular matrix via focal 627 adhesion points. Further, in our model, the substrates are not deformable and 628 therefore it has not been possible to account how the matrix reacts to the probing 629 processes exerted by crawling cells. Finally, it is useful to underline that our 630 specific CPM application does not suffer of the limitation that Voss-Böhme 631 proved to characterize most CPMs (see again [33]), i.e., cells die out in the long-632 run due to modifications in the original Metropolis algorithm. We have in fact 633 focused on relatively short observation times: our model has indeed worked in a 634 well-behaved parameter regime where the temporal evolution of the simulated 635 system has been still directed towards the minimization of the Hamiltonian 636 functional and the non-controlled, voter-like part of the lattice updates has been 637 negligible.

638 Appendix

639 A.1 Morphological and migratory determinants

640 The *position* of a cell was established by the coordinate of its center of mass 641 (CM). In particular, a cell was assumed to be located on a given type of substrate 642 if its center of mass was located on that matrix region. In this respect, the 643 migratory *trajectory* of a cell was generated by tracking the position of its center 644 of mass at each time step (i.e., at each MCS).

645The *adhesive area* of a cell was defined as the extension of its surface in646contact with the substrate of interest at the final observation time.

647 The *average velocity* of an individual on a given type of substrate was 648 measured as the ratio between the width of the substrate region itself (which is 649 clarified for each simulation setting) and the time needed by the cell to cross it. In 650 this respect, to obtain the amount of time spent by a cell to pass a given matrix 651 region it is sufficient to multiply the corresponding average velocity for the width 652 of the substrate of interest.

- 653
- 654 A.2 Statistics

In the plots, we represented cell trajectories coming from 10 independent and randomly chosen simulations. A number of 10 was chosen since we observed that it was sufficient to have a correct interpretation of the simulation outcomes but it was also low enough to have an acceptable graphical quality, as too many cell paths overlapped one to each other, thereby resulting undistinguishable.

660 Cell average velocity and adhesive area were instead given in the 661 corresponding graphs as mean \pm sd over 100 independent simulations. In the plots representing the cell final distribution on the different types of substrate, the relative frequency was given by the number of individuals that, over 100 independent simulations, were located over each matrix region at the end of the observation time. Indeed, the sum of the relative frequencies is, in all cases, equal to 100.

667Finally, dashed and plain ellipsoids representing, respectively, initial and final668cell morphologies in a given simulation setting were established by interpolating669the cell adhesive areas coming from 10 independent simulations (typically the670ones used to track the cell trajectories for the same simulation setting). Obviously,671the initial cell position was the constant for each simulation setting, whereas the672initial cell shape was the same for all cases (i.e., an hemisphere of 20 μm of673radius).

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- 675

A.3 Parameter estimates

676 Given the energetic nature of the CPM, a direct one-to-one correspondence between model parameters and experimental quantities is not straightforward (as 677 678 commented also in [27] and in [90]). In particular, as explained in details in [33], 679 the CPM parameters can be subdivided in i) directly interpretable and measurable 680 quantities, such as cell geometrical dimensions ii) effective parameters that 681 subsume various cellular and subcellular properties, such as the adhesive strength 682 and the elastic moduli determining cell geometrical attributes iii) "merely technical coefficients", such as the Boltzmann temperature, that has been 683 interpreted in different ways by CPM authors (in this work, we opted to link the 684 685 value of T_C to an intrinsic cell motility, i.e., the amplitude of cell boundary 686 fluctuations: consistently, we therefore added the subscript "C" to the coefficient 687 T_{C}). However, a plausible parameter setting was inferred by a proper comparison 688 with experimental findings, taking also advantage of selected sensitivity analysis performed in other CPM-based works. First, the initial/target dimensions of our 689 690 virtual cells were consistent with the measures of NIH 3T3 mouse fibroblasts used by Lo and colleagues [8] for their assays on durotaxis. Since, as previously seen, 691 692 we did not include in our model any nutrients and therefore cells were not allowed to grow during migration, we set a high $\kappa_c = 25 \cdot 10^{-9} \text{ Kg/(s}^2 \text{m}^4)$ to keep cell 693 volume fluctuations within a few per cent. Such a specific value was taken from 694 other CPMs dealing both with single cell dynamics [82] and with multicellular 695 696 phenomena [91], where it was estimated after some trials. Further, observing from 697 the data by Lo et al. [46] that 3T3 cells seeded on soft enough substrates did not 698 significantly spread or undergo morphological transitions, we set a high value $v_C = 25 \cdot 10^{-3} \text{ Kg/(s^2m^2)}$ also for the intrinsic cell rigidity which, as previously 699 700 seen, can decreases (in our work) only upon cell contact with stiffer substrates. 701 This choice is consistent with other CPM-based approaches [57,70,82,91] that employed similar values (i.e., \geq 15) to model an initially low cell deformability. 702

703 We then turned to estimate both the Boltzmann temperature T_C and the cellsubstrate adhesiveness, denoted as J_{soft} thoughout the paper, in the case of the 704 705 softest matrix regions considered in this paper (i.e., the ones pseudo-coloured in 706 red in the simulations, typically identified by $\tau = S_1$). In particular, we looked for the couple of coefficients (T_C, J_{soft}) that simultaneously best fitted the *in vitro* 707 708 results by Lo and co-workers in the corresponding experimental setting (i.e., collagen-coated polyacrylamide substrate properly manipulated to obtain a low 709 710 Young's modulus of 14 kPa) in terms of cell adhesive area (which was called by Lo and colleagues "projected area" [46]). As it is possible to observe in Fig. 10, 711

712 there is a quite large range of values that matched experimental and computational 713 data (i.e., the yellow area of the graph): however, we opted for the intermediate couple of coefficients $T_C = 50 \cdot 10^{-27} \text{ Kgm}^2/\text{s}^2$ and $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$. 714 715 Decrements in cell-substrate adhesive strength and in cell rigidity, allowed in our 716 model as a consequence of cell contact with stiffer matrix regions, were then performed until selected threshold values, i.e., $v_t = 10^{-2} \text{ Kg/s}^2 \text{m}^2$ and $J_{stiff} = 1 \cdot$ 717 10^{-15} Kg/s², respectively. In particular, v_t was the lowest value of cell rigidity 718 that permitted to avoid unrealistic (often disconnected) cell shapes. J_{stiff} , i. e., the 719 720 adhesive force between cells and the stiffest substrates (the ones pseudo-coloured in yellow in the simulation snapshots, typically labelled by $\tau = S_2$, except from 721 the case of the simulations dealing with the stiffness gradient) was instead the 722 723 lowest value for which cells did not start to slow down during migration. In fact, 724 as studied in details in [87], a too high cell-substrate adhesiveness partially 725 inhibits cell movement, as CPM cells are not able to detach from the matrix component if the corresponding J-parameter is too low. Finally, the cell-medium 726 contact strength was set equal to J_{soft} (i.e., = $25 \cdot 10^{-15}$ Kg/s²). The rationale of 727 this choice relied in the fact that for lower values of $J_{C,M}$ cells detached from the 728 729 substrate and fluctuate in the middle of the medium, which was obviously an unrealistic situation. On the opposite, too high values of $J_{C,M}$ (i.e., > 30 \cdot 10⁻¹⁵ 730 Kg/s^2) forced cells to completely lay down on the matrix, in order to minimize 731 732 their contact surface with the medium, but also this situation was not plausible. 733 Finally, the correspondence between 1 MCS and 2 seconds of actual time was 734 taken from another CPM reproducing three-dimensional cell migration in matrix environments [87]. Further, we observed that this setting resulted in a remarkable 735 736 accordance, in terms of cell velocity, between computational and experimental

737		results: our CPM cells in fact move at speeds in a range of (3, 5) μ m/s, which is
738		consistent with the values measured by Vincent and colleagues [51] in the case of
739		MSCs plated on polyacrylamide (PA) hydrogels with selected stiffness.
740		Acknowledgements
741		This work was initiated and partially completed while Rachele Allena was a
742		visitor to the Dipartimento di Scienze Matematiche of the Politecnico di Torino
743		funded by the Gruppo Nazionale per la Fisica Matematica (GNFM).
744		Bibliography
745	[1]	R.L. Juliano, S. Haskill, Signal transduction from the extracellular matrix, J. Cell Biol.
746	120 (1993) 577–585.
747		
748	[2]	P. Martin, Wound healingaiming for perfect skin regeneration, Science. 276 (1997)
749	75-81	l.
750		
751	[3]	L.R. Bernstein, L.A. Liotta, Molecular mediators of interactions with extracellular
752	matri	x components in metastasis and angiogenesis, Curr Opin Oncol. 6 (1994) 106–113.
753		
754	[4]	D.A. Lauffenburger, A.F. Horwitz, Cell migration: a physically integrated molecular
755	proce	ss, Cell. 84 (1996) 359–369.
756		
757	[5]	H. Harris, Role of chemotaxis in inflammation, Physiol. Rev. 34 (1954) 529-562.
758		
759	[6]	K.R. Robinson, The responses of cells to electrical fields: a review, J. Cell Biol. 101
760	(1985) 2023–2027.
761		
762	[7]	S. Li, P. Butler, Y. Wang, Y. Hu, D.C. Han, S. Usami, et al., The role of the dynamics
763	of foc	al adhesion kinase in the mechanotaxis of endothelial cells, PNAS. 99 (2002) 3546-
764	3551.	doi:10.1073/pnas.052018099.

765		
766	[8] C.M. Lo, H.B. Wang, M. Dembo, Y.L. Wang, Cell movement is guided by the rigidi	ty
767	of the substrate, Biophys. J. 79 (2000) 144-152. doi:10.1016/S0006-3495(00)76279-5.	
768		
769	[9] M. Raab, J. Swift, P.C.D.P. Dingal, P. Shah, JW. Shin, D.E. Discher, Crawling from	n
770	soft to stiff matrix polarizes the cytoskeleton and phosphoregulates myosin-II heavy chain, J	ſ
771	Cell Biol. 199 (2012) 669–683. doi:10.1083/jcb.201205056.	
772		
773	[10] Y.K. Cheung, E.U. Azeloglu, D.A. Shiovitz, K.D. Costa, D. Seliktar, S.K. Sia,	
774	Microscale Control of Stiffness in a Cell-Adhesive Substrate Using Microfluidics-Based	
775	Lithography, Angewandte Chemie International Edition. 48 (2009) 7188–7192.	
776	doi:10.1002/anie.200900807.	
777		
778	[11] B.C. Isenberg, P.A. DiMilla, M. Walker, S. Kim, J.Y. Wong, Vascular Smooth Muse	ele
779	Cell Durotaxis Depends on Substrate Stiffness Gradient Strength, Biophysical Journal. 97	
780	(2009) 1313–1322. doi:10.1016/j.bpj.2009.06.021.	
781		
782	[12] I.B. Bischofs, U.S. Schwarz, Cell organization in soft media due to active	
783	mechanosensing, PNAS. 100 (2003) 9274–9279. doi:10.1073/pnas.1233544100.	
784		
785	[13] A. Saez, M. Ghibaudo, A. Buguin, P. Silberzan, B. Ladoux, Rigidity-driven growth	
786	and migration of epithelial cells on microstructured anisotropic substrates, PNAS. 104 (2007	7)
787	8281–8286. doi:10.1073/pnas.0702259104.	
788		
789	[14] L. Trichet, J.L. Digabel, R.J. Hawkins, S.R.K. Vedula, M. Gupta, C. Ribrault, et al.,	
790	Evidence of a large-scale mechanosensing mechanism for cellular adaptation to substrate	
791	stiffness, PNAS. 109 (2012) 6933-6938. doi:10.1073/pnas.1117810109.	
792		
793	[15] M. Raab, J. Swift, P.C.D.P. Dingal, P. Shah, JW. Shin, D.E. Discher, Crawling from	n
794	soft to stiff matrix polarizes the cytoskeleton and phosphoregulates myosin-II heavy chain, J	ſ
795	Cell Biol. 199 (2012) 669–683. doi:10.1083/jcb.201205056.	
796		
797	[16] C.A. Reinhart-King, M. Dembo, D.A. Hammer, The dynamics and mechanics of	
798	endothelial cell spreading, Biophys. J. 89 (2005) 676-689. doi:10.1529/biophysj.104.05432	0.

32

799	
800	[17] P. Moreo, J.M. García-Aznar, M. Doblaré, Modeling mechanosensing and its effect on
801	the migration and proliferation of adherent cells, Acta Biomater. 4 (2008) 613-621.
802	doi:10.1016/j.actbio.2007.10.014.
803	
804	[18] B. Harland, S. Walcott, S.X. Sun, Adhesion dynamics and durotaxis in migrating cells
805	Phys Biol. 8 (2011) 015011. doi:10.1088/1478-3975/8/1/015011.
806	
807	[19] I.V. Dokukina, M.E. Gracheva, A Model of Fibroblast Motility on Substrates with
808	Different Rigidities, Biophys J. 98 (2010) 2794–2803. doi:10.1016/j.bpj.2010.03.026.
809	
810	[20] F. Stefanoni, M. Ventre, F. Mollica, P.A. Netti, A numerical model for durotaxis, J.
811	Theor. Biol. 280 (2011) 150–158. doi:10.1016/j.jtbi.2011.04.001.
812	
813	[21] S.A. Sandersius, T.J. Newman, Modeling cell rheology with the Subcellular Element
814	Model, Phys Biol. 5 (2008) 015002. doi:10.1088/1478-3975/5/1/015002.
815	
816	[22] C.W. Harvey, F. Morcos, C.R. Sweet, D. Kaiser, S. Chatterjee, X. Liu, et al., Study of
817	elastic collisions of Myxococcus xanthus in swarms, Phys Biol. 8 (2011) 026016.
818	doi:10.1088/1478-3975/8/2/026016.
819	
820	[23] R. Allena, D. Aubry, "Run-and-tumble" or "look-and-run"? A mechanical model to
821	explore the behavior of a migrating amoeboid cell, J. Theor. Biol. 306 (2012) 15–31.
822	doi:10.1016/j.jtbi.2012.03.041.
823	
824	[24] Graner, Glazier, Simulation of biological cell sorting using a two-dimensional
825	extended Potts model, Phys. Rev. Lett. 69 (1992) 2013-2016.
826	
827	[25] M. Scianna, L. Preziosi, Multiscale Developments of the Cellular Potts Model,
828	Multiscale Model. Simul. 10 (2012) 342–382. doi:10.1137/100812951.
829	
830	[26] A. Balter, R.M.H. Merks, N.J. Popławski, M. Swat, J.A. Glazier, The Glazier-Graner-
831	Hogeweg Model: Extensions, Future Directions, and Opportunities for Further Study, in:
832	D.A.R.A. Anderson, P.M.A.J. Chaplain, D.K.A. Rejniak (Eds.), Single-Cell-Based Models in

- Biology and Medicine, Birkhäuser Basel, 2007: pp. 151–167.
- http://link.springer.com/chapter/10.1007/978-3-7643-8123-3_7 (accessed July 29, 2015).
- 836 [27] J.A. Glazier, A. Balter, N.J. Popławski, Magnetization to Morphogenesis: A Brief
- 837 History of the Glazier-Graner-Hogeweg Model, in: D.A.R.A. Anderson, P.M.A.J. Chaplain,
- 838 D.K.A. Rejniak (Eds.), Single-Cell-Based Models in Biology and Medicine, Birkhäuser
- 839 Basel, 2007: pp. 79–106. http://link.springer.com/chapter/10.1007/978-3-7643-8123-3_4
- 840 (accessed July 29, 2015).
- 841
- 842 [28] N.J. Savill, R.M.H. Merks, The Cellular Potts Model in Biomedicine, in: D.A.R.A.
- 843 Anderson, P.M.A.J. Chaplain, D.K.A. Rejniak (Eds.), Single-Cell-Based Models in Biology
- and Medicine, Birkhäuser Basel, 2007: pp. 137–150.
- http://link.springer.com/chapter/10.1007/978-3-7643-8123-3_6 (accessed July 29, 2015).
- [29] A. Szabó, R.M.H. Merks, Cellular potts modeling of tumor growth, tumor invasion,
 and tumor evolution, Front Oncol. 3 (2013) 87. doi:10.3389/fonc.2013.00087.
- 849

850 [30] E. Ising, Beitrag zur Theorie des Ferromagnetismus, Z. Physik. 31 (1925) 253–258.
851 doi:10.1007/BF02980577.

- 852
- 853 [31] R.B. Potts, Some generalized order-disorder transformations, Mathematical
- 854 Proceedings of the Cambridge Philosophical Society. 48 (1952) 106–109.
- 855 doi:10.1017/S0305004100027419.
- 856
- [32] N. Metropolis, A.W. Rosenbluth, M.N. Rosenbluth, A.H. Teller, E. Teller, Equation of
 State Calculations by Fast Computing Machines, The Journal of Chemical Physics. 21 (1953)
 1087–1092. doi:10.1063/1.1699114.
- 860
- [33] A. Voss-Böhme, Multi-Scale Modeling in Morphogenesis: A Critical Analysis of the
 Cellular Potts Model, PLoS ONE. 7 (2012) e42852. doi:10.1371/journal.pone.0042852.
- 864 [34] M.S. Steinberg, Reconstruction of tissues by dissociated cells. Some morphogenetic
 865 tissue movements and the sorting out of embryonic cells may have a common explanation,
 866 Science. 141 (1963) 401–408.

867	
868	[35] J.P. Califano, C.A. Reinhart-King, Substrate Stiffness and Cell Area Predict Cellular
869	Traction Stresses in Single Cells and Cells in Contact, Cell Mol Bioeng. 3 (2010) 68–75.
870	doi:10.1007/s12195-010-0102-6.
871	
872	[36] J.L. Tan, J. Tien, D.M. Pirone, D.S. Gray, K. Bhadriraju, C.S. Chen, Cells lying on a
873	bed of microneedles: an approach to isolate mechanical force, Proc. Natl. Acad. Sci. U.S.A.
874	100 (2003) 1484–1489. doi:10.1073/pnas.0235407100.
875	
876	[37] C.A. Reinhart-King, M. Dembo, D.A. Hammer, Endothelial Cell Traction Forces on
877	RGD-Derivatized Polyacrylamide Substrata [†] , Langmuir. 19 (2003) 1573–1579.
878	doi:10.1021/la026142j.
879	
880	[38] A.D. Rape, WH. Guo, YL. Wang, The regulation of traction force in relation to cell
881	shape and focal adhesions, Biomaterials. 32 (2011) 2043–2051.
882	doi:10.1016/j.biomaterials.2010.11.044.
883	
884	[39] T. Yeung, P.C. Georges, L.A. Flanagan, B. Marg, M. Ortiz, M. Funaki, et al., Effects
885	of substrate stiffness on cell morphology, cytoskeletal structure, and adhesion, Cell Motil.
886	Cytoskeleton. 60 (2005) 24–34. doi:10.1002/cm.20041.
887	
888	[40] M. Ghibaudo, A. Saez, L. Trichet, A. Xayaphoummine, J. Browaeys, P. Silberzan, et
889	al., Traction forces and rigidity sensing regulate cell functions, Soft Matter. 4 (2008) 1836.
890	doi:10.1039/b804103b.
891	
892	[41] A. Engler, L. Bacakova, C. Newman, A. Hategan, M. Griffin, D. Discher, Substrate
893	compliance versus ligand density in cell on gel responses, Biophys. J. 86 (2004) 617-628.
894	doi:10.1016/S0006-3495(04)74140-5.
895	
896	[42] A.J. Engler, S. Sen, H.L. Sweeney, D.E. Discher, Matrix elasticity directs stem cell
897	lineage specification, Cell. 126 (2006) 677-689. doi:10.1016/j.cell.2006.06.044.
898	
899	[43] N. Zaari, P. Rajagopalan, S.K. Kim, A.J. Engler, J.Y. Wong, Photopolymerization in
900	Microfluidic Gradient Generators: Microscale Control of Substrate Compliance to Manipulate

901	Cell Response, Adv. Mater. 16 (2004) 2133–2137. doi:10.1002/adma.200400883.
902	
903	[44] C.S. Chen, J.L. Alonso, E. Ostuni, G.M. Whitesides, D.E. Ingber, Cell shape provides
904	global control of focal adhesion assembly, Biochem. Biophys. Res. Commun. 307 (2003)
905	355–361.
906	
907	[45] S.J. Han, K.S. Bielawski, L.H. Ting, M.L. Rodriguez, N.J. Sniadecki, Decoupling
908	Substrate Stiffness, Spread Area, and Micropost Density: A Close Spatial Relationship
909	between Traction Forces and Focal Adhesions, Biophys J. 103 (2012) 640–648.
910	doi:10.1016/j.bpj.2012.07.023.
911	
912	[46] C.M. Lo, H.B. Wang, M. Dembo, Y.L. Wang, Cell movement is guided by the rigidity
913	of the substrate, Biophys. J. 79 (2000) 144-152. doi:10.1016/S0006-3495(00)76279-5.
914	
915	[47] S.I. Fraley, Y. Feng, A. Giri, G.D. Longmore, D. Wirtz, Dimensional and temporal
916	controls of three-dimensional cell migration by zyxin and binding partners, Nat Commun. 3
917	(2012) 719. doi:10.1038/ncomms1711.
918	
919	[48] P.P. Girard, E.A. Cavalcanti-Adam, R. Kemkemer, J.P. Spatz, Cellular
920	chemomechanics at interfaces: sensing, integration and response, Soft Matter. 3 (2007) 307-
921	326. doi:10.1039/B614008D.
922	
923	[49] A. Müller, J. Meyer, T. Paumer, T. Pompe, Cytoskeletal transition in patterned cells
924	correlates with interfacial energy model, Soft Matter. 10 (2014) 2444-2452.
925	doi:10.1039/c3sm52424h.
926	
927	[50] Y.S. Choi, L.G. Vincent, A.R. Lee, K.C. Kretchmer, S. Chirasatitsin, M.K. Dobke, et
928	al., The alignment and fusion assembly of adipose-derived stem cells on mechanically
929	patterned matrices, Biomaterials. 33 (2012) 6943-6951.
930	doi:10.1016/j.biomaterials.2012.06.057.
931	
932	[51] L.G. Vincent, Y.S. Choi, B. Alonso-Latorre, J.C. del Álamo, A.J. Engler,
933	Mesenchymal Stem Cell Durotaxis Depends on Substrate Stiffness Gradient Strength,

934 Biotechnol J. 8 (2013) 472–484. doi:10.1002/biot.201200205.

935	
936	[52] A.J. Engler, M.A. Griffin, S. Sen, C.G. Bönnemann, H.L. Sweeney, D.E. Discher,
937	Myotubes differentiate optimally on substrates with tissue-like stiffness: pathological
938	implications for soft or stiff microenvironments, J. Cell Biol. 166 (2004) 877-887.
939	doi:10.1083/jcb.200405004.
940	
941	[53] L.A. Flanagan, YE. Ju, B. Marg, M. Osterfield, P.A. Janmey, Neurite branching on
942	deformable substrates, Neuroreport. 13 (2002) 2411-2415.
943	doi:10.1097/01.wnr.0000048003.96487.97.
944	
945	[54] O. Ilina, GJ. Bakker, A. Vasaturo, R.M. Hofmann, P. Friedl, Two-photon laser-
946	generated microtracks in 3D collagen lattices: principles of MMP-dependent and -
947	independent collective cancer cell invasion, Phys Biol. 8 (2011) 015010. doi:10.1088/1478-
948	3975/8/1/015010.
949	
950	[55] D. Irimia, G. Charras, N. Agrawal, T. Mitchison, M. Toner, Polar stimulation and
951	constrained cell migration in microfluidic channels, Lab Chip. 7 (2007) 1783-1790.
952	doi:10.1039/b710524j.
953	
954	[56] M. Scianna, L. Preziosi, A cellular Potts model for the MMP-dependent and -
955	independent cancer cell migration in matrix microtracks of different dimensions, Comput
956	Mech. 53 (2014) 485–497. doi:10.1007/s00466-013-0944-6.
957	
958	[57] M. Scianna, L. Preziosi, Modeling the influence of nucleus elasticity on cell invasion
959	in fiber networks and microchannels, J. Theor. Biol. 317 (2013) 394-406.
960	doi:10.1016/j.jtbi.2012.11.003.
961	
962	[58] A.L. Bauer, T.L. Jackson, Y. Jiang, A cell-based model exhibiting branching and
963	anastomosis during tumor-induced angiogenesis, Biophys. J. 92 (2007) 3105-3121.
964	doi:10.1529/biophysj.106.101501.
965	
966	[59] B.M. Rubenstein, L.J. Kaufman, The Role of Extracellular Matrix in Glioma Invasion:
967	A Cellular Potts Model Approach, Biophys J. 95 (2008) 5661-5680.
968	doi:10.1529/biophysj.108.140624.

969	
970	[60] A. Shirinifard, J.S. Gens, B.L. Zaitlen, N.J. Popławski, M. Swat, J.A. Glazier, 3D
971	multi-cell simulation of tumor growth and angiogenesis, PLoS ONE. 4 (2009) e7190.
972	doi:10.1371/journal.pone.0007190.
973	
974	[61] S. Turner, J.A. Sherratt, Intercellular adhesion and cancer invasion: a discrete
975	simulation using the extended Potts model, J. Theor. Biol. 216 (2002) 85-100.
976	doi:10.1006/jtbi.2001.2522.
977	
978	[62] D. Drasdo, G. Forgacs, Modeling the interplay of generic and genetic mechanisms in
979	cleavage, blastulation, and gastrulation, Dev. Dyn. 219 (2000) 182-191. doi:10.1002/1097-
980	0177(200010)219:2<182::AID-DVDY1040>3.0.CO;2-A.
981	
982	[63] J. Moreira, A. Deutsch, Pigment pattern formation in zebrafish during late larval
983	stages: a model based on local interactions, Dev. Dyn. 232 (2005) 33-42.
984	doi:10.1002/dvdy.20199.
985	
986	[64] T. Walther, H. Reinsch, A. Grosse, K. Ostermann, A. Deutsch, T. Bley, Mathematical
987	modeling of regulatory mechanisms in yeast colony development, J. Theor. Biol. 229 (2004)
988	327–338. doi:10.1016/j.jtbi.2004.04.004.
989	
990	[65] V.P. Zhdanov, B. Kasemo, Simulation of the growth and differentiation of stem cells
991	on a heterogeneous scaffold, Physical Chemistry Chemical Physics. 6 (2004) 4347-4350.
992	doi:10.1039/b407371c.
993	
994	[66] A.F.M. Marée, P. Hogeweg, How Amoeboids Self-Organize into a Fruiting Body:
995	Multicellular Coordination in Dictyostelium discoideum, Proceedings of the National
996	Academy of Sciences of the United States of America. 98 (2001) 3879-3883.
997	
998	[67] N.J. Savill, J.A. Sherratt, Control of epidermal stem cell clusters by Notch-mediated
999	lateral induction, Dev. Biol. 258 (2003) 141-153.
1000	
1001	[68] A. Mochizuki, Pattern formation of the cone mosaic in the zebrafish retina: a cell
1002	rearrangement model, J. Theor. Biol. 215 (2002) 345-361. doi:10.1006/jtbi.2001.2508.

1003	
1004	[69] P.K. Maini, L. Olsen, J.A. Sherratt, Mathematical models for cell-matrix interactions
1005	during dermal wound healing, Int. J. Bifurcation Chaos. 12 (2002) 2021–2029.
1006	doi:10.1142/S0218127402005674.
1007	
1008	[70] M. Scianna, An extended Cellular Potts Model analyzing a wound healing assay,
1009	Comput. Biol. Med. 62 (2015) 33-54. doi:10.1016/j.compbiomed.2015.04.009.
1010	
1011	[71] N.J. Popławski, A. Shirinifard, M. Swat, J.A. Glazier, SIMULATION OF SINGLE-
1012	SPECIES BACTERIAL-BIOFILM GROWTH USING THE GLAZIER-GRANER-
1013	HOGEWEG MODEL AND THE COMPUCELL3D MODELING ENVIRONMENT, Math
1014	Biosci Eng. 5 (2008) 355–388.
1015	
1016	[72] R. Chaturvedi, C. Huang, J.A. Izaguirre, S.A. Newman, J.A. Glazier, M. Alber, A
1017	Hybrid Discrete-Continuum Model for 3-D Skeletogenesis of the Vertebrate Limb, in: P.M.A
1018	Sloot, B. Chopard, A.G. Hoekstra (Eds.), Cellular Automata, Springer Berlin Heidelberg,
1019	2004: pp. 543-552. http://link.springer.com/chapter/10.1007/978-3-540-30479-1_56
1020	(accessed July 29, 2015).
1021	
1022	[73] R. Chaturvedi, C. Huang, B. Kazmierczak, T. Schneider, J Izaguirre, T. Glimm, et
1023	al., On multiscale approaches to three-dimensional modelling of morphogenesis, J R Soc
1024	Interface. 2 (2005) 237–253. doi:10.1098/rsif.2005.0033.
1025	
1026	[74] N.J. Popławski, M. Swat, J.S. Gens, J.A. Glazier, Adhesion between cells, diffusion of
1027	growth factors, and elasticity of the AER produce the paddle shape of the chick limb, Physica
1028	A. 373 (2007) 521–532. doi:10.1016/j.physa.2006.05.028.
1029	
1030	[75] C. Xue, A. Friedman, C.K. Sen, A mathematical model of ischemic cutaneous
1031	wounds, PNAS. 106 (2009) 16782-16787. doi:10.1073/pnas.0909115106.
1032	
1033	[76] Z. Xu, J. Lioi, J. Mu, M.M. Kamocka, X. Liu, D.Z. Chen, et al., A multiscale model of
1034	venous thrombus formation with surface-mediated control of blood coagulation cascade,
1035	Biophys. J. 98 (2010) 1723–1732. doi:10.1016/j.bpj.2009.12.4331.
1036	

1037	[77] Z. Xu, N. Chen, M.M. Kamocka, E.D. Rosen, M. Alber, A multiscale model of	
1038	thrombus development, J R Soc Interface. 5 (2008) 705-722. doi:10.1098/rsif.2007.1202.	
1039		
1040	[78] R.M.H. Merks, J.A. Glazier, Dynamic mechanisms of blood vessel growth,	
1041	Nonlinearity. 19 (2006) C1-C10. doi:10.1088/0951-7715/19/1/000.	
1042		
1043	[79] R.M.H. Merks, S.V. Brodsky, M.S. Goligorksy, S.A. Newman, J.A. Glazier, Cell	
1044	elongation is key to in silico replication of in vitro vasculogenesis and subsequent remodeling	g,
1045	Dev. Biol. 289 (2006) 44–54. doi:10.1016/j.ydbio.2005.10.003.	
1046		
1047	[80] R.M.H. Merks, E.D. Perryn, A. Shirinifard, J.A. Glazier, Contact-Inhibited	
1048	Chemotaxis in De Novo and Sprouting Blood-Vessel Growth, PLoS Comput Biol. 4 (2008).	
1049	doi:10.1371/journal.pcbi.1000163.	
1050		
1051	[81] M. Scianna, L. Munaron, L. Preziosi, A multiscale hybrid approach for vasculogenesi	is
1052	and related potential blocking therapies, Prog. Biophys. Mol. Biol. 106 (2011) 450-462.	
1053	doi:10.1016/j.pbiomolbio.2011.01.004.	
1054		
1055	[82] M. Scianna, A multiscale hybrid model for pro-angiogenic calcium signals in a	
1056	vascular endothelial cell, Bull. Math. Biol. 74 (2012) 1253-1291. doi:10.1007/s11538-011-	
1057	9695-8.	
1058		
1059	[83] A. Szabo, E.D. Perryn, A. Czirok, Network Formation of Tissue Cells via Preferentia	1
1060	Attraction to Elongated Structures, Phys. Rev. Lett. 98 (2007) 038102.	
1061	doi:10.1103/PhysRevLett.98.038102.	
1062		
1063	[84] A. Szabó, R. Unnep, E. Méhes, W.O. Twal, W.S. Argraves, Y. Cao, et al., Collective	
1064	cell motion in endothelial monolayers, Phys Biol. 7 (2010) 046007. doi:10.1088/1478-	
1065	3975/7/4/046007.	
1066		
1067	[85] A. Szabó, A. Czirók, The Role of Cell-Cell Adhesion in the Formation of	
1068	Multicellular Sprouts, Math Model Nat Phenom. 5 (2010) 106. doi:10.1051/mmnp/20105105	5.
1069		
1070	[86] M. Scianna, R.M.H. Merks, L. Preziosi, E. Medico, Individual cell-based models of	

1071	cell scatter of ARO and MLP-29 cells in response to hepatocyte growth factor, J. Theor. Biol.
1072	260 (2009) 151–160. doi:10.1016/j.jtbi.2009.05.017.
1073	
1074	[87] M. Scianna, L. Preziosi, K. Wolf, A Cellular Potts Model simulating cell migration on
1075	and in matrix environments, Math Biosci Eng. 10 (2013) 235-261.
1076	
1077	[88] J. Starruß, T. Bley, L. Søgaard-Andersen, A. Deutsch, A New Mechanism for
1078	Collective Migration in Myxococcus xanthus, J Stat Phys. 128 (2007) 269–286.
1079	doi:10.1007/s10955-007-9298-9.
1080	
1081	[89] A.F.M. Marée, A. Jilkine, A. Dawes, V.A. Grieneisen, L. Edelstein-Keshet,
1082	Polarization and movement of keratocytes: a multiscale modelling approach, Bull. Math. Biol.
1083	68 (2006) 1169–1211. doi:10.1007/s11538-006-9131-7.
1084	
1085	[90] R.M.H. Merks, P. Koolwijk, Modeling Morphogenesis in silico and in vitro :
1086	Towards Quantitative, Predictive, Cell-based Modeling, Mathematical Modelling of Natural
1087	Phenomena. 4 (2009) 149–171. doi:10.1051/mmnp/20094406.
1088	
1089	[91] M. Scianna, E. Bassino, L. Munaron, A cellular Potts model analyzing differentiated
1090	cell behavior during in vivo vascularization of a hypoxic tissue, Comput. Biol. Med. 63
1091	(2015) 143–156. doi:10.1016/j.compbiomed.2015.05.020.
1092	
1093	
1094	
1095	
1096	
1097	Figures, Movies and Tables
1009	Eis 1. Call behaviour is determined by a modified Materialic also ithm, which is based on a
1020	rig. 1 Cen benaviour is determined by a modified Metropolis algorithm, which is based on a
1099	iterative and stochastic minimization of the cell-matrix system energy, defined by a Hamiltonian
1100	functional H. In particular, it includes energetic contributions for cell geometrical attributes and
1101	cell-substrate adhesive affinity. A Boltzmann-like law finally controls the likelihood of the

1102 acceptance of domain configuration updates, which is further biased by the intrinsic cell motility, 1103 established by parameter T_C . 1104 Fig. 2 Snapshots of the tested substrate configurations: (a) soft (red: $t_{\rm S}$ with $J_{C,S_1} = 25 \cdot 10^{-15}$ Kg/s²) and stiff (yellow: t_{s} with $J_{C,S_2} = 1 \cdot 10^{-15}$ Kg/s²) substrates, (b) soft (red: t_{s} with 1105 $J_{C,S_1} = 25 \cdot 10^{-15} \text{ Kg/ s}^2$ substrate with two stiff (yellow: t_{S_1} with $J_{C,S_2} = 1 \cdot 10^{-15} \text{ Kg/ s}^2$) stripes, 1106 (c) sequence of stripes with different stiffness (red: t_{S} with Kg/s $J_{C,S_1} = 25 \cdot 10^{-15}$, dark orange: 1107 t_{S_1} with $J_{C,S_2} = 20 \cdot 10^{-15}$ Kg/s², orange: t_{S_1} with $J_{C,S_3} = 15 \cdot 10^{-15}$ Kg/s², light orange: t_{S_1} with 1108 $J_{C,S_4} = 10 \cdot 10^{-15}$ Kg/s², dark yellow: t_{s_1} with $J_{C,S_5} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with $J_{C,S_6} = 5 \cdot 10^{-15}$ Kg/s², yellow: t_{s_1} with t_{s_2} with t_{s_1} with t_{s_1} with t_{s_2} with t_{s_1} with t_{s_2} with t_{s_1} with t_{s_1} with t_{s_2} with t_{s_1} with t_{s_1} with t_{s_2} with t_{s_1} with t_{s_2} with t_{s_1} with t_{s_1} with t_{s_2} with t_{s_1} with 1109 $1 \cdot 10^{-15}$ Kg/s²), (d) stiff (yellow: t_{s_1} with $J_{C,s_2} = 1 \cdot 10^{-15}$ Kg/s²) substrate with embedded soft 1110 (red: t_{s} with $J_{C,S_1} = 2510^{-15}$ Kg/s²) squares. 1111 1112 Fig. 3 Simulation for a substrate with soft (red) and stiff (yellow) regions. As the ratio $\frac{J_{c,s,1}}{J_{c,s,2}}$ 1113 1114 increases, the cells are typically biased to migrate towards the stiff region (c). This is also 1115 confirmed by the trajectories of the cell centre of mass, which are relatively close to the centre of the substrate when $\frac{J_{C,S_{1}}}{J_{C,S_{2}}} = 1$ (a), whereas they are substantially shifted on the stiff region when 1116 $\frac{J_{C,S,1}}{J_{C,S,2}} = 25$ (b). 1117 1118 1119 Fig. 4 Two cells are initially seeded on a soft (red) and a stiff (yellow) substrate, respectively. (a) 1120 Simulation snapshot of the final positions (i.e., at MCS = 500 corresponding to nearly 16 minutes) 1121 of the two cells. (b) Initial (dashed) and final (plain) contour shapes give an idea of the position 1122 and the morphology of the two cells. (c) Cell adhesive area as a function of the type of substrate. 1123 The area is about 30% higher in the case of the cell seeded over the stiff substrate, due to the 1124 specific constitutive law given to cell rigidity (i.e., Eq. (6)).

1125

1126Fig. 5 Simulation for a substrate with soft (red) and stiff (yellow) subdomains. The trajectories of1127the cell centre of mass as well as the initial (dashed) and the final (plain) cell contours are traced

1128	respectively for (a) a cell initially seeded at the south-east corner and an external potential
1129	introduced towards the north-west corner and (b) a cell initially seeded at the south-west corner
1130	and an external potential directed towards the north-east corner. (c) Cell average velocity over
1131	either the stiff and soft substrate.
1132	
1133	Fig. 6 Configuration with a soft (red) substrate with two embedded stiff stripes (yellow). (a) and
1134	(c) Simulations with $ \boldsymbol{v}_{ext} = 7 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ and $ \boldsymbol{v}_{ext} = 28 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ respectively.
1135	Representative cell trajectories are plotted together with the initial (dashed) and the final (plain)
1136	cell contours. (b) Relative cell frequency as function of $ v_{ext} $. (d) Cell average velocity over the
1137	different substrate regions in the case of $ \boldsymbol{v}_{ext} = 28 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$.
1138	
1139	Fig. 7 Results for the simulation with a soft to stiff gradient (Sec. 3.4). (a) Relative cell frequency
1140	as $ v_{ext} $ increases. (b) Average cell velocity over the different substrate regions in case of $ v_{ext} $ =
1141	$28 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2.$
1142	
1143	Fig. 8 Results for the simulations with a soft to stiff gradient (Sec. 3.5). (a) $ v_{ext} $ necessary to
1144	allow cells reach the opposite border of the domain vs width of substrate stripes. (b) Average cell
1145	velocity over the different substrate regions for different widths of the matrix stripes in case of a
1146	stiffness gradient sufficient fine-grained to have a cell persistent movement even in the absence of
1147	an external potential.
1148	
1149	Fig. 9 Snapshots from a representative simulation dealing with a domain with four soft squares (red) embedded
1150	in a stiff substrate (yellow). The cell is initially seeded at the south-west corner and migrates in the direction of
1151	an external potential ($ v_{ext} = 14 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$), i.e., towards the north-east corner. Snapshots are taken at 2
1152	min (a), 30 min (b), 1.5 h (c), 2 h (d), 2.5 h (e), 3.5 h (f), 4.5 h (g) and 5.5 h (g).
1153	
1154	Fig. 10 Cell adhesive area at 5.5 h, obtained from CPM simulations for different values both of the Boltzmann
1155	temperature T_C and of the adhesiveness between the cell and the softest substrate, i.e., J_{soft} . Values are given as
1156	the mean over 100 simulations. The experimental value measured by Lo and co-workers in corresponding

1157	conditions is $1.74 \cdot 10^3 \mu m^2$. From this plot, it was indeed possible to observe that the parameter region pseudo-
1158	colored in yellow gave the best fitting couples of coefficients. In particular, we opted for $T_C = 50 \cdot$
1159	10^{-27} Kgm ² /s ² and J _{soft} = $25 \cdot 10^{-15}$ Kg/s ² .
1160	
1161	Movie 1 Simulation of cell migration over a stiff-soft substrate (yellow = stiff region, red = soft
1162	region) in presence of an external potential directed towards the north-west corner (Sec. 3.2). The
1163	cell is initially seeded at the south-east corner.
1164	
1165	Movie 2. Simulation of cell migration over a stiff-soft substrate (yellow = stiff region, red = soft
1166	region) in presence of an external potential directed towards the north-east corner (Sec. 3.2). The
1167	cell is initially seeded at the south-west corner.
1168	
1169	Movie 3. Simulation of cell migration over a soft substrate (red) including two parallel stiff stripes
1170	(yellow) in presence of an external potential ($ \boldsymbol{v}_{ext} = 7 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$) directed towards the north-
1171	east corner (Sec. 3.3). The cell is initially seeded at the south-west corner.
1172	
1173	Movie 4. Simulation of cell migration over a soft substrate (red) including two parallel stiff stripes
1174	(yellow) in presence of an external potential ($ \boldsymbol{v}_{ext} = 28 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$) directed towards the
1175	north-east corner (Sec. 3.3). The cell is initially seeded at the south-west corner.
1176	
1177	Movie 5. Simulation of cell migration over a substrate with a soft-to-stiff gradient from the left to
1178	the right part of the domain (the cell-substrate adhesive affinities vary from $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$
1179	to $J_{stiff} = 1.10^{-15} \text{ Kg/s}^2$) (Sec. 3.4). A low external potential ($ \boldsymbol{v}_{ext} = 7.10^{-21} \text{ Kg} \cdot \text{m/s}^2$) is directed
1180	towards the north-east corner of the substrate, whereas the cell is seeded at the south-west corner.
1181	
1182	Movie 6. Simulation of cell migration over a substrate with a soft-to-stiff gradient from the left to
1183	the right part of the domain (the cell-substrate adhesive affinities vary from $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$
1184	to $J_{stiff} = 1.10^{-15} \text{ Kg/s}^2$ (Sec. 3.4). A high external potential ($ \boldsymbol{v}_{ext} = 28.10^{-21} \text{ Kg·m/s}^2$) is

1185	directed towards the north-east corner of the substrate, whereas the cell is seeded at the south-west
1186	corner.
1187	
1188	Movie 7. Simulation of cell migration over a substrate with a soft-to-stiff gradient from the left to the right part
1189	of the domain (the cell-substrate adhesive affinities vary from $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ to $J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$).
1190	Here, the width of the stripes has been highly reduced (i.e., $= 28 \ \mu m$) and no external potential is introduced
1191	(Sec. 3.5).
1192	
1193	Movie 8. Simulation of cell migration over a stiff substrate (yellow) with four embedded soft
1194	squares (red) (Sec. 3.6). The cell is initially seeded at the south-west corner and an external
1195	potential ($ v_{ext} = 14 \cdot 10^{-21} \text{ Kg·m/s}^2$) is directed towards the north-east corner of the domain.
1196	
1197	Table 1 Main parameters of the model.