

Cost-optimized design of a dual-mode diesel parallel hybrid electric vehicle for several driving missions and market scenarios

*Original*

Cost-optimized design of a dual-mode diesel parallel hybrid electric vehicle for several driving missions and market scenarios / Finesso, Roberto; Spessa, Ezio; Venditti, Mattia. - In: APPLIED ENERGY. - ISSN 0306-2619. - STAMPA. - 177:(2016), pp. 366-383. [10.1016/j.apenergy.2016.05.080]

*Availability:*

This version is available at: 11583/2645376 since: 2021-03-25T17:29:27Z

*Publisher:*

Elsevier

*Published*

DOI:10.1016/j.apenergy.2016.05.080

*Terms of use:*

This article is made available under terms and conditions as specified in the corresponding bibliographic description in the repository

*Publisher copyright*

(Article begins on next page)

1 **Cost-optimized design of a dual-mode diesel parallel hybrid electric vehicle for several**  
2 **driving missions and market scenarios**

---

3 *Roberto Finesso, Ezio Spessa<sup>1</sup> and Mattia Venditti*

4  
5 *IC Engines Advanced Laboratory, Dipartimento Energia, Politecnico di Torino*

6 *c.so Duca degli Abruzzi 24, 10129 - Torino, Italy*

7 [roberto.finesso@polito.it](mailto:roberto.finesso@polito.it), [ezio.spessa@polito.it](mailto:ezio.spessa@polito.it), [mattia.venditti@polito.it](mailto:mattia.venditti@polito.it)

8 **Abstract**

9 The present study has focused on the refinement of a previously developed tool for the optimization of the layout  
10 of hybrid electric vehicles and on its application to a newly proposed non-plug in parallel hybrid vehicle, which  
11 has been equipped with a planetary gear set and a single-speed gearbox positioned between a compression  
12 ignition engine and a permanent magnet electric machine. This vehicle is capable of torque-coupling and speed-  
13 coupling between the engine and the electric machine, and for this reason has been referred to as a “dual-mode  
14 vehicle”.

15 The tool performs a bi-level (nested) coupling of design and control strategy optimization, and is able to identify  
16 the optimal design of each hybrid vehicle by minimizing the powertrain costs over a 10-year time span. The  
17 vehicle design determines the size of battery, engine and electric machine, as well as the values of the speed ratio  
18 of each power coupling device. Different powertrain cost definitions, which account for the production costs of  
19 the components and the operating costs related to fuel consumption and battery depletion over the lifetime of the  
20 vehicle, have been proposed. The latter cost contribution depends directly on the control strategy adopted to  
21 manage the power flow between the electric machine and the engine, as well as on the selection of the

---

<sup>1</sup>Corresponding Author: Tel. +39-011.090.4482; Fax: +39-011.090.4599; e-mail: ezio.spessa@polito.it

22 transmission gear. The optimal control strategy has been identified using a specifically developed fast running  
23 dynamic programming-based optimizer, which minimizes an objective function over a given training driving  
24 mission.

25 The performance of the dual-mode vehicle with the optimal layout has been investigated in detail over several  
26 driving missions and compared with that of more traditional hybrid vehicles equipped with either a speed  
27 coupling device or with a torque coupling device, as well as with a conventional reference vehicle.

28 Moreover, several sensitivity analyses have been carried out in order to investigate the impact of the cost  
29 definition, of the objective function and of the training driving mission on the powertrain design and on its  
30 performance (fuel economy, pollutant emissions, battery management).

31 Finally, different market scenarios have been explored, in terms of fuel price, battery life and battery cost, and  
32 their effects on the identification of the optimal design, as well as on the performance of the resulting vehicles,  
33 have been analyzed.

34 *Key Words: parallel hybrid vehicle; planetary gear; layout; cost-optimized design; market*  
35 *scenario*

## 36 **Nomenclature**

### 37 **Acronyms**

38 AER: All Electric Range

39 AMDC: Artemis Motorway Driving Cycle

40 AUDC: Artemis Urban Driving Cycle

41 BLC: Battery Life Consumption

42 BU: Battery Usage

43 CO<sub>2</sub>: Carbon dioxide

44 DMV: Dual Mode Vehicle

45 DP: Dynamic Programming

- 46 D1: 1.7 L Euro 5 GM diesel engine
- 47 D2: 1.3 L Euro 5 GM diesel engine
- 48 E: Engine
- 49 EGR: Exhaust Gas Recirculation
- 50 EM: Electric Machine
- 51 ES: Engine State
- 52 EV: Electric vehicle
- 53 FC: Fuel consumption
- 54 FD: Final Drive
- 55 GB: Gear Box
- 56 GN: Gear Number
- 57 HEV: Hybrid Electric Vehicle
- 58 J: Objective function
- 59 NOx: Nitrogen oxides
- 60 PF: Power Flow
- 61 PG: Planetary Gear set
- 62 PI: Performance Index
- 63 SC: Speed Coupling
- 64 SCV: Speed Coupling Vehicle
- 65 SOC: State Of Charge
- 66 TC: Torque Coupling
- 67 TCV: Torque Coupling Vehicle
- 68 TM1: Internally-developed Training Mission (1)
- 69 TM2: Internally-developed Training Mission (2)
- 70 TM3: Internally-developed Training Mission (3)
- 71 TR: Transmission

## 72 **Variables**

73 C: Cost [\$]

74  $C_{\text{bat}}$ : Battery capacity [Ah]

75 E: Energy [J]

76  $I_{\text{wh}}$ : Wheel moment of inertia [ $\text{kg m}^2$ ]

77  $I_{\text{bat}}$ : Battery current [A]

78  $\dot{m}_{\text{fc}}$ : Fuel mass flow rate [kg/s]

79  $\dot{m}_{\text{CO}_2}$ : CO2 mass flow rate [kg/s]

80  $P_{\text{fd}}$ : Final drive power [W]

81  $P_{\text{v}}$ : Vehicle power [W]

82  $R_{\text{wh}}$ : Dynamic radius of the wheel [m]

83  $S_{\text{es}}$ : Set of discrete values of the state of the engine

84  $S_{\text{gn}}$ : Set of discrete values of GN

85  $S_{\text{pf}}$ : Set of discrete values of PF

86  $S_{\text{soc}}$ : Set of discrete values of SOC

87 t: Time [s]

88 T: Torque [Nm]

89 u: control strategy

90  $V_{\text{v}}$ : Velocity [m/s]

## 91 **Greek symbols**

92  $\alpha$ : Sub-control variable of PF

93  $\lambda$ : Battery life consumption [Ah]

94  $\lambda_{\text{r}}$ : Battery life residual [-]

95  $\Lambda$ : Battery life [Ah]

96  $\rho$ : Fuel density [kg/m<sup>3</sup>]  
97  $\sigma$ : Severity factor related to battery aging [-]  
98  $\tau_{sc}$ : Speed ratio of the speed coupling device [-]  
99  $\tau_{tc}$ : Speed ratio of the torque coupling device [-]  
100  $\omega$ : Angular speed [rad/s]

## 101 **1. Introduction**

### 102 **1.1 Background**

103 In recent years, the automotive industry has dedicated a great deal of effort to developing innovative  
104 technologies for the realization of green vehicles characterized by low CO<sub>2</sub> and pollutant emissions [1]. Battery  
105 equipped electric vehicles (EV) have only a battery as the energy source, and traction power is provided by one  
106 or several electric machines. These vehicles are highly energy efficient and feature zero tailpipe emissions, while  
107 the well-to-wheel emissions depend on the electric energy production process. If the electric energy is derived  
108 from a renewable source, well-to-wheel emissions can be reduced to a great extent [2, 3]. However, these  
109 vehicles have not been successful so far on the market, because of the higher costs, the added weight of the  
110 batteries, the reduced load capacity, the limited driving range and the lack of recharging infrastructures [4]. Fuel-  
111 cell electric vehicles are still in their early stages of development, as the fuel-cell technology is not yet mature,  
112 but they have shown an interesting long-term potential [2, 5]. Hybrid electric vehicles (HEVs) offer improved  
113 fuel economy and lower emissions than conventional vehicles and they can take advantage of existing fuel  
114 infrastructures. HEVs are provided with two energy sources, i.e., a battery and a fuel tank, and they are equipped  
115 with a conventional thermal engine and one or several electric machines. A significant advantage of HEVs,  
116 compared to battery EVs, is that they offer the possibility of increasing the driving range, due to the presence of  
117 the thermal engine. However, the driving range in pure electric mode is much lower, as a consequence of the  
118 installation of smaller battery packs. HEVs lead to a reduction in fuel consumption (FC) and CO<sub>2</sub> emissions,  
119 compared to conventional vehicles, mainly due to the reduction in engine size, to the possibility of recovering

120 the kinetic energy through regenerative braking, to the implementation of the Stop-Start mode and to the  
121 possibility of optimizing the power flow from the engine and electric machines [6]. Several studies have  
122 demonstrated the capacity of the hybrid technology to reduce CO<sub>2</sub> emissions in developing countries [7, 8],  
123 which are expected to contribute significantly to the greenhouse gas emissions from the transport sector in the  
124 near future. Moreover, a recent study has shown that the life cycles of CO<sub>2</sub> emissions of modern HEVs are  
125 shorter than those of conventional vehicles [9]. HEVs are therefore considered to represent one of the most  
126 promising technologies. A classification of HEVs can first be made considering whether the batteries can be  
127 charged from an electric grid (plug-in HEVs) or not (non plug-in HEVs). Plug-in hybrid electric vehicles use  
128 both electrochemical energy storage and a conventional fuel to overcome the drawbacks of EVs and HEVs.  
129 Plug-in HEVs have the potential of further reducing fuel consumption, as well as pollutant and CO<sub>2</sub> emissions,  
130 compared to non-plug-in HEVs [10-12]. However, they are usually equipped with larger battery packs than non  
131 plug-in HEVs, in order to allow a higher all-electric range (AER) to be obtained. Moreover, the incremental  
132 battery cost of plug-in HEVs might not be counterbalanced by the savings in fuel cost, as was shown in [13].  
133 HEVs can also be classified according to their architecture. Many different hybrid architectures, whether of a  
134 series, parallel or complex series/parallel type [9], have been developed by car manufacturers. The parallel  
135 architecture is currently one of the most frequently adopted ones in hybrid vehicles. In this kind of architecture,  
136 both the engine and electric machine supply mechanical power directly to the driven wheels. The role of the  
137 electric machine is therefore to assist the engine to operate efficiently and to recover energy through regenerative  
138 braking. The main advantages of a parallel configuration over a series configuration are that a generator is not  
139 required, the electric machine used for traction is smaller, and multi-conversion of the power from the engine to  
140 the driven wheels is not necessary. The parallel configuration may have several configurations, which depend on  
141 the connection between the transmission, the electric machines and the engine.

142 The key-aspects that should be considered to fully exploit the capacity of HEVs to reduce CO<sub>2</sub> and pollutant  
143 emissions are the design definition and energy management, i.e., the identification of the optimal control strategy  
144 during vehicle operation. Only a few studies have been found in the literature, which addressed to the co-design  
145 process of hybrid vehicles.

146 Four different types of coupling between the plant and controller optimization problem were examined in [14],  
147 that is, sequential, iterative, bi-level (nested) and simultaneous types. The nested and simultaneous coupling  
148 strategies were found to offer the best performance as they guarantee system-level optimality.

149 A methodology for the optimization of plug-in HEV component sizing, using a parallel chaos optimization  
150 algorithm, is described in [4].

151 Optimization of powertrain component sizing and of the control strategy was studied in [15] for a fuel cell  
152 hybrid electric bus. A higher fuel economy and minimum powertrain costs were achieved using a multi-objective  
153 genetic algorithm with preset design variables and vehicle performance constraints.

154 A combined power management/design optimization problem for the optimization of fuel cell/battery hybrid  
155 vehicles was formulated in [16]. Subsystem-scaling models were utilized to predict the component size and were  
156 integrated into a stochastic-dynamic-programming controller design process.

157 The study in [17], like that in [15], demonstrated the system-control co-design of a fuel cell/battery/super-  
158 capacitor vehicle using a multi-objective genetic algorithm. The optimization process was based on the  
159 minimization of fuel consumption, while preserving the battery state of charge under different driving cycles.

160 A sequential-type co-design for a fuel cell/battery/super-capacitor hybrid electric vehicle was developed in [18].  
161 In this case, the component sizing was first designed to meet the performance constraints of a vehicle. A real-  
162 time optimization of the power flow of the three powertrain components was then carried out.

163 A rule-based control is a technique that is used extensively in hybrid systems to obtain an optimal energy  
164 management [19]. This method is characterized by simple implementation, high computational efficiency and  
165 fast experimental verification. However, it is not suitable for complicated or highly non-linear systems, due to its  
166 inherent drawback, i.e., an engineering intuition-based design. In order to deal with such problems, as well as to  
167 enhance robustness against system uncertainties, the fuzzy logic control method is often applied for various  
168 types of hybrid systems [20]. However, the main problem of these methods is that a system with numerous  
169 control variables could lead to a large number of logic rules.

170 An alternative method for the control strategy optimization of systems equipped with dual energy (or power)  
171 sources is based on the minimization of an equivalent energy [21]. This is also known as a “static optimization



172 method". The simulated results can be organized in the form of multi-dimensional tables, which can be coded  
173 and downloaded directly to a control unit.

174 Dynamic Programming (DP) is a widely-used global optimization method that applies an exhaustive search for  
175 the overall optimal control strategy under a predetermined driving cycle. This methodology was first introduced  
176 by Bellman [22]. Its potentiality has been investigated in detail in several works [23, 24]. It has been found to be  
177 a better candidate for the co-design of an optimal vehicle layout and control strategy than rule-based, fuzzy-  
178 logic-based or static optimization methods. However, the DP-based tools that can be found in literature are very  
179 time consuming. This drawback could represent a major concern for the adoption of such a technique.

## 180 **1.2 Contribution of the present study**

181 The main innovative contributions of this study, with reference to the background illustrated in the previous  
182 section, are:

- 183 1. The refinement of a previously developed tool [25, 26] for the optimization of the layout of hybrid vehicles.  
184 The tool is based on a bi-level (nested) approach, which has been found to offer the best performance when  
185 the aim is to solve plant and controller optimization problems at the same time. Moreover, a DP-based  
186 optimizer has been implemented to identify the optimal control strategy, as it leads to a global optimal  
187 solution, which cannot be guaranteed by static optimizers or rule-based optimizers. However, the DP  
188 optimizers currently available in the literature are very time consuming, and are therefore not suitable for  
189 layout optimization applications, which require the investigation of a large number of possible layouts.  
190 Therefore, specific mathematical techniques have been developed in order to set up a fast running DP-based  
191 optimizer. The optimal control strategy has been identified by minimizing an objective function, which  
192 accounts for fuel consumption, NOx emissions and battery life depletion, over a given mission profile.  
193 The optimal vehicle design tool is based on the minimization of the powertrain cost over the lifetime of the  
194 vehicle. Several cost definitions, which account for the component production costs and for the operating  
195 costs related to fuel consumption and battery depletion, have been introduced. Most of the methodologies  
196 proposed in the literature for vehicle design optimization are based on only fuel consumption minimization.

197 However, this approach may lead to aggressive battery employment, with a consequent impact on the  
198 operating costs.

199 The main novelties with respect to the tool presented in [26] are related to the introduction of new powertrain  
200 cost definitions (OEM cost, user cost, fuel cost, production cost, operating cost) and to the capability of  
201 performing different cost-oriented vehicle design optimizations.

202 2. The application of the refined tool to a newly proposed non-plug-in parallel hybrid electric vehicle, which has  
203 been equipped with a planetary gear set and a single-speed gearbox positioned between a compression  
204 ignition engine and a permanent magnet electric machine. This vehicle is capable of realizing torque-coupling  
205 and speed-coupling functions between the engine and the electric machine, and has therefore been referred to  
206 as a “dual-mode vehicle” (DMV). To the best of the authors’ knowledge, this type of architecture has not yet  
207 been investigated in the literature, and seems highly promising in terms of fuel consumption and emission  
208 reduction. The DMV architecture in fact enables the engine operating point to be shifted either in terms of  
209 speed (via the planetary gear) or in terms of torque (via the single speed gearbox).

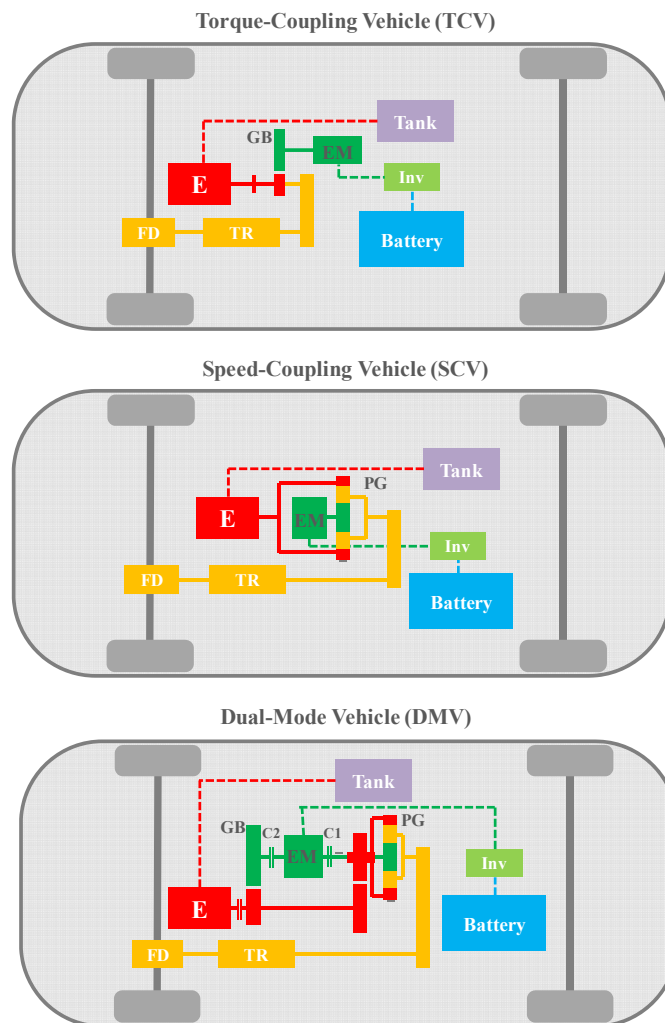
210 3. The comparison of the DMV performance with that of more traditional hybrid vehicles and with that of a  
211 reference conventional vehicle, over different driving missions, including two Artemis Driving Cycles  
212 (AUDC, AMDC) and three internally-developed training missions (TM1, TM2 and TM3). TM1 was  
213 developed to simulate the vehicle in a mountain-like scenario, TM2 to simulate highway-like conditions over  
214 different road slopes, and TM3 was developed in order to include a wide variation of driving conditions taken  
215 from several homologation cycles. Moreover, a study has been carried out to identify the architectures that  
216 show the best performance, in terms of NO<sub>x</sub> emission, CO<sub>2</sub> emission and powertrain cost reductions, in  
217 different driving conditions.

218 4. A detailed sensitivity analysis, which has been conducted in order to investigate the impact of the cost  
219 definition, of the objective function and of the training driving mission on the powertrain design and on its  
220 performance (fuel economy, pollutant emissions, battery management, costs). Moreover, several indicators  
221 have been defined in order to estimate the incremental OEM costs per unit CO<sub>2</sub> emission reduction, per unit  
222 user cost reduction and per unit total powertrain cost reduction over the vehicle lifetime.

223 5. A detailed investigation of different market scenarios, in terms of fuel price, battery life duration and battery  
224 cost, and of their effects on the identification of the optimal design, as well as on the performance of the  
225 resulting vehicles.

## 226 2. Powertrain Design

227 The design optimization procedure has been applied to three different hybrid architectures in this paper. The first  
228 vehicle, whose scheme is reported in Figure 1 (top), is referred to as Torque-Coupling Vehicle (TCV). A single-  
229 speed gearbox (GB) has been installed as a torque-coupling device. The electric machine (EM) is connected to  
230 the second GB shaft, while the engine and the driveline are connected to the first GB shaft.



232 **Figure 1 – Scheme of the hybrid electric vehicles.**

233 The second hybrid vehicle (Figure 1, middle) has here been referred to as Speed-Coupling Vehicle (SCV). A  
234 planetary gear set (PG) has been installed as a speed-coupling device. The engine is connected to the PG ring,  
235 the EM is connected to the PG sun, and the driveline is connected to the PG carrier.

236 The third hybrid vehicle (Figure 1, bottom) is a newly proposed architecture, which includes SC and TC devices  
237 at the same time, and has here been referred to as a Dual-Mode Vehicle (DMV). A planetary gear set and a  
238 gearbox have been installed as speed-coupling and torque-coupling devices, respectively. The engine (E) is  
239 connected to the first GB shaft and to the PG ring, the EM is connected to the second GB shaft and to the PG  
240 sun, and the driveline is connected to the PG carrier. Two different clutches have been inserted in order to enable  
241 either the speed-coupling mode, if clutch C1 is engaged and clutch C2 is released, or the torque-coupling mode,  
242 if clutch C2 is engaged and clutch C1 is released. The two mechanical connections enable the engine operating  
243 point to be shifted either horizontally (speed) or vertically (torque).

244 The driveline is depicted in yellow for each architecture in the figure, and it consists of the transmission (TR)  
245 and the final drive (FD). The battery is connected to the electric machine through the inverter (Inv).

246 **3. Vehicle Model**

247 The hybrid electric vehicles investigated in this study have been compared to a reference case, i.e., a  
248 conventional vehicle equipped with a compression-ignition engine. The reference vehicle is equipped with a 2.9  
249 L prototype Euro 5 GMPT-E diesel engine (130 kW at 4000 rpm, 356Nm at 1500 rpm). The total vehicle mass is  
250 1536 kg (the chassis mass is 1250 kg), the frontal area  $A_v$  is 2 m<sup>2</sup>, the drag resistance coefficient  $c_x$  is 0.3 and the  
251 tire radius is 0.3247 m. The chassis mass, frontal area, drag resistant coefficient and tire radius have been kept  
252 constant for the different simulated hybrid vehicles. The performance capability of the vehicles has been  
253 measured as a combination of acceleration time, elasticity time and maximum velocity over different uphill  
254 roads, in order to estimate the overall performance index (PI). Each hybrid vehicle layout obtained from the  
255 optimal vehicle design tool has had to provide a similar performance to that of the reference vehicle.

256 The kinematic vehicle model has been developed in the Matlab environment [27].

## 257 **3.1 Components**

### 258 **3.1.1 Engine**

259 Two different prototype Euro 5 GM compression ignition engines, with displacements of 1.7 L and 1.3 L,  
260 respectively, have been employed in this study. The first engine, which is here referred to as D1, provides a  
261 maximum power of 97 kW at 3700 rpm and a maximum torque of 304 Nm at 2400 rpm. The second engine,  
262 referred to as D2, provides a maximum power of 70 kW at 4000 rpm and a maximum torque of 206 Nm at 1800  
263 rpm. The adoption of different engines is of fundamental importance in order to be able to investigate the impact  
264 of the degree of hybridization on the performance of the hybrid vehicle.

265 The performance of the engine was modeled using experimentally-derived look-up tables. The mass flow rate of  
266 both the fuel and NO<sub>x</sub> emissions were evaluated by interpolating a 2D map, which is a function of the engine  
267 power and speed. The corresponding CO<sub>2</sub> emissions were linearly determined as follows [26, 28]:

$$268 \quad \dot{m}_{\text{CO}_2} = 2.65 \cdot \frac{\dot{m}_{\text{fc}}}{\rho} \quad (1)$$

269 where  $\rho$  is the fuel density,  $\dot{m}_{\text{fc}}$  is the fuel mass flow rate and 2.65 represents a conversion factor. The latter was  
270 obtained considering a combustion reaction of diesel oil with air, such as the one presented in [29], and an  
271 average composition of the fuel taken from literature data [30].

### 272 **3.1.2 Electric machine**

273 The electric machine model simulates power conversion from the electric to mechanical form, and vice-versa,  
274 taking into account energy losses by means of efficiency maps, which are functions of the machine power and  
275 speed. The electric machines that have been considered in the present study belong to the brushless permanent  
276 magnet electric motor/generator family, and all the data were taken from the official UQM Technologies website  
277 [31].

### 278 3.1.3 Battery

279 Lithium-ion batteries have been adopted in this study as the secondary power storage device. The battery model  
280 is represented by an equivalent resistance circuit, in which the resistance and the open-circuit voltage of the  
281 battery are SOC-dependent. The SOC represents the electrical status of the battery and depends on the equivalent  
282 battery capacity  $C_{\text{bat}}$  and on the flowing current  $I_{\text{bat}}$ , as follows:

$$283 \text{ SOC} = \text{SOC}_0 - \int \frac{I_{\text{bat}}}{C_{\text{bat}}} \cdot dt \quad (2)$$

284 The battery SOC was limited within the [0.4 – 0.8] range, while the maximum current that may be transferred  
285 through a cell was established as 120A.

286 A phenomenological damage accumulation model, based on the “accumulated Ah-throughput” concept has been  
287 adopted to estimate the depletion of the battery life. The  $\lambda$  parameter, which represents the effective Ah-  
288 throughput, can be computed as follows [32]:

$$289 \lambda = \int \sigma \cdot |I_{\text{bat}}| \cdot dt \quad (3)$$

290 This parameter represents the amount of charge that would have to be exchanged when a nominal cycle is  
291 adopted in order to have the same aging effect as the actual cycle the battery has undergone. The severity factor  
292  $\sigma$  represents the relative aging effect, with respect to the nominal cycle, and it is higher than 1 for severe aging  
293 conditions (i.e. which would lead to a shorter life). The severity factor is estimated as follows [28, 32]:

$$294 \sigma = 1.5 \cdot \left( \frac{I_{\text{bat}}}{C_{\text{bat}}} \right)^2 + 1 \quad (4)$$

295 The residual battery life  $\lambda_r$ , which represents the fraction of charge that could still flow through the battery  
296 before the end of its life, is determined as follows:

$$297 \lambda_r = 1 - \frac{\lambda}{\Lambda} \quad (5)$$

298 where  $\Lambda$  is the battery life, which has here been set to 20000 Ah. The end of life condition is defined as the  
299 instant at which  $\lambda_r = 0$ .

### 300 **3.1.4 Torque-coupling and speed-coupling devices**

301 A single-speed two-shaft gearbox has been used in this study as a mechanical torque-coupling device, as shown  
302 in Fig. 1. It has the function of coupling together the torque from the engine and the electric machine and of  
303 providing the output torque to the transmission shaft.

304 A planetary gear unit, which mechanically connects the power derived from all the power sources, has been used  
305 as a speed-coupling device. It has the function of coupling the speeds of two different power sources that enter  
306 the device separately and of providing the output torque to the transmission shaft. This device consists of three  
307 rotating nodes, namely a sun gear, a ring gear and a carrier gear, as shown in Fig. 1, which are linked by a few  
308 small pinion gears.

309 The equations used to derive the input/output torque and speed of the torque-coupling and speed-coupling  
310 devices are well known and commonly used in the literature [28] and have not been reported here for the sake of  
311 brevity.

### 312 **3.1.5 Transmission**

313 **Table 1 – Transmission speed ratio specifications.**

<b>GN</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
$\tau [-]$	4.17	2.13	1.32	0.95	0.75	0.62

314  
315 The driveline consists of a 6-speed gearbox (which is referred to as “transmission” in this study) and of the front  
316 final drive. The transmission power losses have been estimated by means of an efficiency map, which is a  
317 function of the output shaft speed and torque, as well as of the selected gear number. The transmission inertia  
318 has also been taken into account. The final drive has instead been modeled as a torque multiplier, while power  
319 losses and inertia contributions have been neglected. The transmission speed ratio values are reported in Table 1  
320 for each gear.

## 3.2 Determination of the power and speed of the engine and electric machine

The total vehicle power demand  $P_v$  at the wheel level is the sum of several contributions: the rolling resistance, the grade resistance, the drag resistance and the inertia. The total power demand of the vehicle can be expressed as follows:

$$P_v = \left( m_v \cdot g \cdot r_v \cdot \cos(\alpha_r) + m_v \cdot g \cdot \sin(\alpha_r) + \frac{1}{2} \rho_{\text{air}} \cdot c_x \cdot A_v \cdot V_v^2 + \left( m_v + \frac{I_{\text{wh}}}{R_{\text{wh}}} \right) \cdot \dot{V}_v \right) \cdot V_v \quad (6)$$

where  $m_v$  is the vehicle mass,  $g$  is the gravitational acceleration,  $r_v$  is the rolling resistance coefficient of the vehicle,  $\alpha_r$  is the slope of the road,  $V_v$  is the vehicle velocity,  $A_v$  is the front area of the vehicle,  $\rho_{\text{air}}$  is the air density,  $c_x$  is the aerodynamic drag coefficient,  $R_{\text{wh}}$  is the dynamic wheel radius and  $I_{\text{wh}}$  is the wheel inertia. The working condition of the vehicle may be either of a traction type, if the power is positive, or of a braking type, if the power is negative. The power at the final drive level is therefore determined as follows:

$$P_{\text{fd}} = \begin{cases} P_v, & \text{traction} \\ \gamma_{\text{fr}} \cdot (1 - \gamma_{\text{br}}) \cdot P_v, & \text{braking} \end{cases} \quad (7)$$

where the  $\gamma_{\text{fr}}$  factor represents the power split between the front and the rear wheels of the vehicle during the braking phase, while  $\gamma_{\text{br}}$  represents the power share that has to be managed by the mechanical frictional brakes during braking. The  $\gamma_{\text{fr}}$  value has been kept constant and equal to 0.75 for all of the simulations, while the value of  $\gamma_{\text{br}}$  has been set at 0.1.

The power required at the front powertrain level is obtained as follows:

$$P_f = (P_{\text{fd}} + P_{\text{tr,in}}) \cdot \eta_{\text{tr}}^k + P_{\text{e,in}} + P_{\text{em,in}} \quad (8)$$

where  $P_{\text{tr,in}}$ ,  $P_{\text{e,in}}$  and  $P_{\text{em,in}}$  are the inertial power of the transmission, of the engine and of the electric machine, respectively,  $\eta_{\text{tr}}$  is the transmission efficiency, and exponent  $k$  is equal to 1, if the vehicle is braking, or equal to -1 otherwise.

The angular velocity  $\omega_f$  at the front powertrain level is a function of the control variable  $\tau$  as follows:

$$\omega_f = \tau \cdot \tau_{\text{fd}} \cdot \frac{V_v}{R_{\text{wh}}} \quad (9)$$

where  $\tau_{\text{fd}}$  is the speed ratio of the final drive.



345 The formulation used to determine the power of the engine  $P_e$  and of the electric machine  $P_{em}$  is obtained  
 346 considering the value of the sub-control variable  $\alpha$ :

$$347 \quad P_e = (1 - \alpha) \cdot P_f \quad (10)$$

$$348 \quad P_{em} = \alpha \cdot P_f \quad (11)$$

349 As far as the formulation of the speed of the engine and of the electric machine is concerned, two different  
 350 modes have to be considered.

### 351 **Mode 1 – torque coupling**

352 The engine speed, with reference to the Willis method applied to a planetary gear set [28], is obtained if the sun  
 353 shaft is blocked:

$$354 \quad \omega_{e,t} = \frac{1+\tau_{sc}}{\tau_{sc}} \cdot \omega_f \quad (12)$$

355 where  $\omega_{e,t}$  and  $\omega_f$  are the speed of the engine and of the front powertrain, while  $\tau_{sc}$  is the PG speed ratio. The  
 356 electric machine is now connected to the second GB shaft, and its speed can be defined as follows:

$$357 \quad \omega_{em,t} = \tau_{tc} \frac{1+\tau_{sc}}{\tau_{sc}} \cdot \omega_f \quad (13)$$

358 where  $\omega_{em,t}$  is the speed of the electric machine and  $\tau_{tc}$  is the GB speed ratio.

### 359 **Mode 2 – speed coupling**

360 The engine power, with reference to the torque correlations for the three shafts of the planetary gear set [28], can  
 361 be expressed as follows:

$$362 \quad P_e = (1 - \alpha) \cdot P_f = (1 - \alpha) \cdot T_f \cdot \omega_f = (1 - \alpha) \cdot \frac{1+\tau_{sc}}{\tau_{sc}} \cdot T_e \cdot \omega_f = T_e \cdot \omega_e \quad (14)$$

363 where  $T_e$  and  $T_f$  are the torque at the engine and at the front powertrain level, respectively, while  $\omega_e$  and  $\omega_f$  are  
 364 the speed of the engine and of the front powertrain, and  $\tau_{sc}$  is the PG speed ratio. The engine speed is therefore  
 365 obtained as:

$$366 \quad \omega_{e,s} = (1 - \alpha) \cdot \frac{1+\tau_{sc}}{\tau_{sc}} \cdot \omega_f \quad (15)$$

367 In a similar way, the power of the electric machine can be written as follows:

$$368 \quad P_{em} = \alpha \cdot P_f = \alpha \cdot T_f \cdot \omega_f = \alpha \cdot (1 + \tau_{sc}) \cdot T_{em} \cdot \omega_f = T_{em} \cdot \omega_{em} \quad (16)$$

369 where  $T_{em}$ ,  $\omega_{em}$  are the torque and the speed of the electric machine, whose speed is calculated as follows:

370  $\omega_{em,s} = \alpha \cdot (1 + \tau_{sc}) \cdot \omega_f$  (17)

371 The aforementioned equations describe the vehicle model for DMVs. The TCV model equations can be obtained  
 372 from the DMV model if the speed ratio  $\tau_{sc} \rightarrow \infty$ . The SCV model equations can instead be obtained from those  
 373 of the DMV, if the speed ratio  $\tau_{tc}$  is set at 1.

### 374 **3.3 Control/state variables and their discretization**

375 The gear number, GN, and the power flow, PF, have been chosen as the control variables in this study. The GN  
 376 variable determines the speed ratio of the transmission,  $\tau$  (see Table 1). The GN domain is defined by the  $S_{gn} =$   
 377  $\{1, 2, \dots, 6\}$  set, since a 6-speed transmission has been adopted on the front axle. The PF variable is related to the  
 378 management of the power of the engine and of the electric machine. In particular, it controls the sub-control  
 379 variable  $\alpha$ , which quantifies the power contribution provided by the battery through the front axle, with respect  
 380 to the front vehicle power demand (see Eqs. (10-11)). The PF domain is defined by the  $S_{pf} = \{1, 2, \dots, N_{pf}\}$  set,  
 381 where  $N_{pf}$  stands for the number of different power flow types. The default size of  $S_{pf}$  has been set equal to 4 for  
 382 the TCV and SCV architectures and to 7 for DMV.

383 All the different values of the PF control variable are listed in Table 2, where **pe** stands for pure electric mode,  
 384 **pt** for pure thermal mode, **ps** for power split mode and **bc** for battery charge mode, while **tc** stands for torque-  
 385 coupling and **sc** for speed-coupling.

386 Two different pure-electric modes are possible for the dual-mode vehicle: the electric machine can in fact drive  
 387 the vehicle either in torque-coupling mode (**pe.tc**) or in speed-coupling mode (**pe.sc**). Its speed is expressed  
 388 either by Eq. (17) or by Eq. (13), according to which mode is selected, while engine speed is null. Only one  
 389 pure-thermal mode, in which both the electric machine clutches are disengaged and the engine is connected to  
 390 the driveline in the torque-coupling mode, is possible for this vehicle powertrain.

391 **Table 2 – Working modes of the TCV, SCV and DMV architectures.**

PF	1	2	3	4	5	6	7	
<b>description</b>	pe.tc	pe.sc	pt.tc	ps.tc	bc.tc	ps.sc	bc.sc	$N_{pf}$
<b><math>\alpha</math></b>	1	1	0	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	

<b>TCV</b>	✓		✓	✓	✓			<b>4</b>
<b>SCV</b>		✓	✓			✓	✓	<b>4</b>
<b>DMV</b>	✓	✓	✓	✓	✓	✓	✓	<b>7</b>

392

393 Finally, the electric machine can work either to assist the engine or to charge the battery, and it can be connected  
394 either in speed-coupling mode or in torque-coupling mode. The power of each component is identified according  
395 to the value of the sub-control variable  $\alpha$  (see Eqs. (10-11)). The speeds of the engine and of the electric machine  
396 are obtained by means of Eq. (15) and Eq. (17), respectively, if the speed-coupling mode is enabled, otherwise  
397 by means of Eq. (12) and Eq. (13), respectively, if the torque-coupling mode is selected.

398 A set of constraints has been introduced in order to identify the feasible combinations of the GN and PF control  
399 variables at each time instant, according to the vehicle driving conditions.

400 With reference to the state variables, the state of the engine, which can be equal to 0 if the engine is off, or equal  
401 to 1 otherwise (the related discrete set is therefore  $S_{es} = \{0, 1\}$ ), was chosen as the first variable. The battery  
402 SOC was chosen as the second state variable. It can vary in the  $S_{soc} = \{0.4, 0.4001, \dots, 0.8\}$  discrete set, since  
403 4000 discretization steps have been considered. While the evolution of the battery SOC depends on the time-  
404 history of the two control variables, the engine state is obtained directly as a function of the instantaneous value  
405 of the power flow.

## 406 **4 Identification of the optimal control strategy**

### 407 **4.1 Objective function**

408 The optimal policy or control strategy  $u^*(t)$  is determined by minimizing an objective function,  $J$ , while the  
409 constraint on the final SOC and  $NO_x$  emissions has to be guaranteed. The mathematical formulation of the  
410 problem is:

$$411 \quad u^*(t) = \min_{u(t) \in S^*(t)} J(u(t)) \quad (18)$$

$$412 \quad SOC_{end} \geq SOC_0 \quad (19)$$

413  $M_{\text{nox}} \leq M_{\text{nox,ds}}$  (20)

414 where  $u(t)$  is the generic policy or control strategy and  $S^*(t)$  is the set of feasible combinations of control

415 variables for each time interval  $t$ .  $\text{SOC}_{\text{end}}$  is the battery SOC at the end of the mission,  $\text{SOC}_0$  is its initial value,

416  $M_{\text{nox}}$  is the cumulated  $\text{NO}_x$  emission mass of the hybrid vehicle at the end of the mission and  $M_{\text{nox,ds}}$  is the

417 cumulated  $\text{NO}_x$  emission mass of the conventional reference vehicle equipped with the same downsized engine

418 as that of the hybrid vehicle.  $S^*(t)$  is a subset of all the combinations of the control variables.

419 The battery SOC at the end of the mission has to be higher or equal to that at the beginning, as the architecture is

420 of the non-plug-in type.

421 If the after-treatment devices are not sufficient to meet the emission limits, the engine-out  $\text{NO}_x$  levels could be

422 controlled directly by means of the control strategy. Similarly, the cost related to battery life depletion might

423 become extremely significant if a control strategy optimization is completely oriented toward a reduction in fuel

424 consumption. The objective function  $J$  has therefore been defined to include not only fuel consumption, but also

425  $\text{NO}_x$  emissions and battery aging effects, as follows:

426 
$$J = \alpha_1 \frac{\text{FC}}{\text{FC}_{\text{rv}}} + \alpha_2 \frac{M_{\text{nox}}}{M_{\text{nox,ds}}} + \alpha_3 \frac{\text{BP}}{\text{FP} \cdot \text{FC}_{\text{rv}}} \cdot \frac{\lambda}{\Lambda}$$
 (21)

427 where  $\text{FC}$  is the cumulated mass of fuel consumed over the mission (kg),  $\text{FC}_{\text{rv}}$  is the cumulated mass of fuel

428 consumed by the reference vehicle (kg),  $\text{BP}$  is the cost related to battery replacement (\$),  $\text{FP}$  is the fuel price

429 (\$/kg),  $\lambda$  is the effective battery life consumption (Ah) and  $\Lambda$  is the battery life (Ah). Three weighting factors

430 have been introduced, namely  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$ , in order to adjust the relative importance of the related terms. This

431 formulation allows the fuel consumption, the  $\text{NO}_x$  emissions and the battery life depletion effects to be taken into

432 account at the same time.

433 Whenever the  $\text{NO}_x$  emissions are not taken directly into account in the optimization process, Eq. (20) still has to

434 be satisfied.

## 435 **4.2 Dynamic programming**

436 A fast running dynamic programming (DP) algorithm has been developed and implemented in the vehicle design

437 tool in order to identify the control strategy.

438 Several computational techniques were introduced in order to reduce the simulation time as much as possible.  
439 One of these techniques is based on the splitting of the vehicle model evaluations and of the DP-based  
440 optimization stage. The model evaluations are pre-processed a-priori for all the possible combinations of the  
441 control variables of the problem and the results of the simulations are indexed. In this way, the DP-based  
442 algorithm can rely on pre-calculated data to extract the optimal policy, instead of continuously running the  
443 vehicle model, which is the main cause of the high computational time [26].  
444 Furthermore, the state grid that has to be generated for the battery SOC has also been exploited for other state  
445 variables (such as the NOx emissions), in order to manage multiple constraints of the optimization problem, such  
446 as those expressed in Eq. (19) and Eq. (20).  
447 A third technique has been adopted in order to simulate the vehicle performance over a more sparse time grid,  
448 without compromising the accuracy of the result. In the present study, the time domain has been discretized  
449 uniformly with a time step of 3 s in order to create the corresponding time grid of equispaced intervals.  
450 This algorithm allows all the different vehicle designs to be compared on an equal basis, while rule-based tools  
451 may promote some designs because of biasing tuned rules. Specific vehicle control units can be developed in the  
452 subsequent step, when the design has been obtained and the DP-algorithm has established the vehicle design  
453 benchmark.

## 454 **5 Optimal vehicle design**

455 The tool that has been used to identify the optimal design of each hybrid vehicle is a refined version of that  
456 shown in [25, 26]. Basically, the tool is based on the generation of a large number of different layouts (in terms  
457 of engine size, electric machine size and speed ratios of the TC/SC devices and of the final drive) for each  
458 vehicle architecture. A preliminary selection of the feasible layouts was carried out, considering performance  
459 and emission constraints. The optimal control strategy was then identified for each feasible layout and the  
460 overall powertrain cost was then calculated. The latter includes the production costs and the operating costs  
461 related to fuel consumption and to battery life depletion. Finally, the layouts that led to the minimum powertrain  
462 cost were selected as optimal.

## 463 5.1 Cost definition

464 The optimal layout  $x^*$  has been selected for each hybrid vehicle architecture by minimizing the total powertrain  
465 cost  $C_{pt}$ . The identified layout must guarantee specific performance and emission constraints. The mathematical  
466 formulation of the problem is defined as follows:

$$467 \quad x^* = \min_{x \in X^*} C_{pt}(x) \quad (22)$$

$$468 \quad PI(x) \leq PI_{rv} \quad PI_e(x) \leq 1.4 \cdot PI_{rv} \quad AER(x) \geq 2.5 \text{ km} \quad M_{nox}(x, y) \leq M_{nox,ds}(y) \quad (23)$$

469 where  $x$  is the vector that contains the parameters that univocally define the layout of each vehicle,  $x^*$  is the  
470 optimal layout,  $PI(x)$  and  $PI_e(x)$  represent the performance index of the hybrid vehicle, whose design is defined  
471 by  $x$  itself, in hybrid mode and in pure-thermal mode, respectively,  $PI_{rv}$  is the performance index of the  
472 reference vehicle (see Eq. (37)),  $AER$ , namely the all-electric range, represents the distance that the vehicle has  
473 to cover in pure electric mode, using 60% of the battery energy content,  $M_{nox}(x, y)$  is the cumulated nitrogen  
474 oxide mass emission of the hybrid vehicle with the  $x$  layout over the  $y$  mission, while  $M_{nox,ds}(y)$  is the  
475 cumulated nitrogen oxide mass emission of the reference vehicle equipped with the same downsized hybrid  
476 vehicle engine over the same mission  $y$ .

477 The  $X^*$  set contains a large number of layouts that have been found to be feasible over several driving missions.  
478 The total powertrain cost  $C_{pt}$  may be defined in several ways, according to the specific requirements and/or  
479 targets of the design procedure. In this study, six different definitions have been taken into account:

- 480 1. **Production** ( $C_{pr}$ ): the cost of the powertrain components.
- 481 2. **OEM** ( $C_{oem}$ ): the cost that the OEM has to deal with. It consists of the production costs and a fraction of  
482 the costs due to battery replacement. It has been speculated that the OEM might be interested in partially  
483 financing the purchase of additional batteries, if they are required over the lifetime of the vehicle. This is  
484 a reasonable policy that could be adopted by the OEM in order to promote the introduction of hybrid  
485 vehicles onto the market.
- 486 3. **Fuel** ( $C_{fc}$ ): the cost of the fuel required to drive the vehicle.
- 487 4. **Operating** ( $C_{op}$ ): the fuel cost and the cost due to any battery replacement.

488 5. **User** ( $C_{usr}$ ): the cost concerning the user, i.e. the fuel cost and a fraction of the battery replacement costs  
 489 (this is basically an operating cost-oriented definition, as it does not include the cost required to purchase  
 490 the vehicle and the costs related to insurance/taxes).

491 6. **Total** ( $C_{tot}$ ): the sum of the production cost and the operating cost.

492 The production cost  $C_{prod}$  takes into account the cost of the engine  $C_e$ , of all the electric machines  $C_{em}$  and of  
 493 the battery pack  $C_{bat}$ :

$$494 C_{prod}(x) = C_e + C_{em} + C_{bat} \quad (24)$$

495 which can be broken up into:

$$496 C_e(x) = 12 \cdot P_{e,max} + 424 \quad (25)$$

$$497 C_{em}(x) = 21.7 \cdot P_{em,max} + 425 \quad (26)$$

$$498 C_{bat}(x) = 350 \cdot E_{bat,tot} + 680 \quad (27)$$

499 where  $P_{e,max}$  is the maximum engine power [kW],  $P_{em,max}$  is the maximum power of the electric machine [kW]  
 500 and  $E_{bat,tot}$  is the energy content of the battery [kWh]. The method used to estimate the cost of the components  
 501 was derived from [33], but the battery cost has been updated, considering more recent data [34].

502 As far as the operating cost evaluation is concerned, it is first necessary to evaluate the fuel consumption and the  
 503 battery life over a given driving mission. These quantities depend on the control strategy to a great extent.

504 The minimum achievable fuel cost  $C_{fc}^*$  is then estimated as follows:

$$505 C_{fc}(x, u) = \frac{FP \cdot D \cdot I}{\rho \cdot N \cdot d} \cdot FC(u^*) \quad (28)$$

506 where FP is the fuel price (\$/kg),  $D = 250000$  km is a reasonable distance covered by the vehicle during its  
 507 lifetime,  $N = 10$  represents the time horizon (year),  $d$  is the distance of the specific mission the vehicle is trained  
 508 over. FC is the cumulated fuel consumption mass (kg), while  $u^*$  is the optimal policy obtained with DP that  
 509 minimizes the objective function J, defined in Eq. (21), over that vehicle mission. The I term is related to the  
 510 inflation phenomena and is estimated as follows:

$$511 I = \sum_{j=1}^N (1 + i)^j \quad (29)$$

512 where  $i$  is the inflation index.

513 The cost related to the battery replacement requires the calculation of the number of batteries that have to be  
514 employed during the life of the vehicle. To this aim, the battery usage BU has been introduced as follows:

$$515 \quad BU = \frac{\lambda}{\Lambda} \cdot \frac{D}{d} \quad (30)$$

516 where  $\lambda$  is the effective life consumption of the battery (Ah) and  $\Lambda$  is the battery life (Ah).

517 The battery replacement cost  $C'_{br}$  has been calculated as follows:

$$518 \quad C'_{br} = C_{bat} \cdot \frac{1}{N} \cdot (BU - 1) \quad (31)$$

519 However, since the first battery is part of the initial vehicle, it has not been included in the operating costs. A  
520 second definition has therefore been taken into account:

$$521 \quad C_{br} = \max(0, C_{bat} \cdot \frac{1}{N} \cdot (BU - 1)) \quad (32)$$

522 The OEM costs have instead been estimated as follows:

$$523 \quad C_{oem} = C_{pr} + C_{br}/2 \quad (33)$$

524 while the user cost has been estimated as:

$$525 \quad C_{usr} = C_{fc} + \min(C'_{br}, C_{br}/2) \quad (34)$$

526 The operating costs have been defined as follows:

$$527 \quad C_{op} = C_{fc} + C_{br} \quad (35)$$

528 Finally, the total costs are the sum of the three terms, namely the production, the fuel consumption and battery  
529 replacement costs:

$$530 \quad C_{tot} = C_{pr} + C_{fc} + C_{br} \quad (36)$$

## 531 **5.2 Vehicle performance constraint**

532 The performance index of each vehicle has been estimated taking into account:

- 533 1. The time necessary to cover 1 km at the maximum velocity of the vehicle  $V_{v,max}(\alpha)$  over five uphill  
534 climbing roads with different slopes  $\alpha$ .
- 535 2. The response time to increase the velocity over a flat road, starting from three different initial speeds.

536 The formulation is:



537 
$$PI(x) = \sum_{\alpha} \frac{3600}{V_{v,max}(\alpha)} + t_{0-100} + t_{60-100} + t_{80-120} \quad (37)$$

538 where  $t_{0-100}$  is the 0-100 km/h acceleration time (free gear shift strategy),  $t_{60-100}$  is the 60-100 km/h  
 539 acceleration time (5th gear fixed) and  $t_{80-120}$  is the 80-120 km/h acceleration time (6th gear fixed). The  
 540 maximum velocity of the vehicle has been estimated over each uphill road using the following formulation:

541 
$$V_{v,max}(\alpha) \geq V_v | P_{pt}(V_v) = P_v(V_v, \alpha) \quad (38)$$

542 where  $P_v(V_v, \alpha)$  is the resistance power of the vehicle necessary to climb a road with slope  $\alpha$  at velocity  $V_v$  and  
 543  $P_{pt}(V_v)$  is the maximum power that the powertrain is able to provide at that velocity.

544 The acceleration time has been estimated with reference to the following:

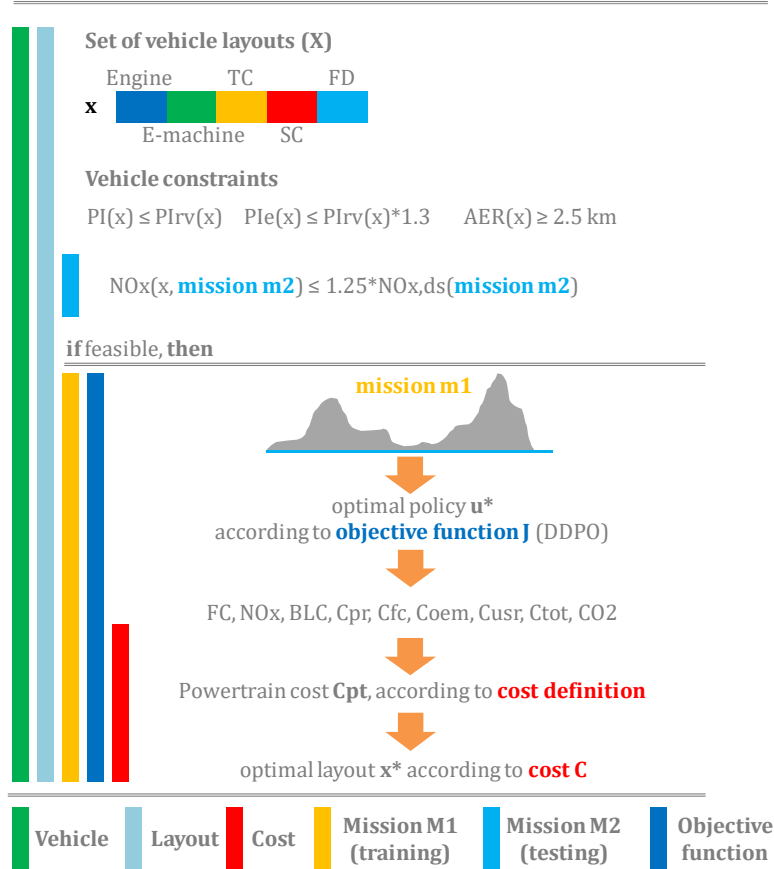
545 
$$\dot{V}_v = \frac{P_{pt}(V_v) - P_v(V_v)}{m_{v,eq} \cdot V_v} \quad (39)$$

546 where the equivalent vehicle mass  $m_{v,eq}$  also takes into account the inertial power contributions of each  
 547 component that is involved in accelerating the vehicle itself.

### 548 **5.3 Toolbox**

549 Figure 2 reports the functional scheme of the bi-level toolbox that has been developed in order to identify the  
 550 optimal layout of each hybrid vehicle. Each colored bar represents a specific phase of the optimization process.  
 551 Six different vehicle types (namely, TCV, SCV and DMV combined with the two engines D1 and D2) have been  
 552 considered in this study (outer green bar in Fig. 2). The tool initially generates a set of different layouts for each  
 553 vehicle type (light cyan bar in Fig. 2). A generic layout is referred to as  $x$ , which is an array that stores the  
 554 information related to the maximum engine power, maximum electric machine power and the speed ratio of the  
 555 TC device (for the TCV and DMV), of the SC device (for the SCV and DMV) and of the final drive (FD). The  
 556 generic  $x$  layout is shown at the top of Fig. 2.

### Optimal vehicle design toolbox



557

558

**Figure 2 – Scheme of the Optimal vehicle design toolbox.**

559

The vehicle performance of the  $x$  layout is then estimated in terms of performance index (PI) and all-electric

560

range (AER) (see section 5.1 for more details) and the NO<sub>x</sub> emissions are calculated over the M2 set (cyan bar in

561

Fig. 2) of the test missions (TM1, TM2, TM3, AUDC and AMDC in this study). If all the constraints are

562

satisfied, the layout is marked as feasible.

563

The optimal policy is then elaborated by means of DP for each feasible layout over each m1 mission of the M1

564

set (yellow bar in Fig. 2) of the training missions (TM1, TM2, TM3 in this study) using objective function J (FC-

565

BLC-oriented, see Eq. (21)). This phase is represented by the blue bar in Fig. 2. The main outcomes of the

566

different layouts, namely the fuel consumption (FC), the NO<sub>x</sub> emissions and the battery life consumption are

567

then derived using the optimal policy  $u^*$  that was identified in the previous step. The powertrain cost  $C_{pt}$  is

568 obtained according to a given cost definition  $C$  (red bar in Fig. 2, see Section 5.1 for the cost definitions), and the  
569 optimal layout  $x^*$  is then identified for the given cost definition.

570 In short, the toolbox first evaluates the set of feasible layouts for each vehicle architecture on the test missions,  
571 and then evaluates the powertrain costs, adopting a fast-running DP-based algorithm to identify the optimal  
572 control strategy over the training missions.

573 A set of 30k layouts have been generated in this study for the DMV architecture, while a much smaller set (5k)  
574 has been generated for the TCV and SCV ones. Since the former architecture is equipped with two mechanical  
575 coupling devices, the design domain is much larger. The toolbox then estimates the performance and the NOx  
576 emissions for each layout over the M2 set of missions, using a pure-thermal strategy, with the aim of identifying  
577 the feasible layouts that satisfy the constraints expressed by Eq. (23). The total number of simulations that are  
578 necessary to estimate NOx emissions over the M2 set is  $(30 + 5 + 5) \cdot 1000 \cdot 5 \approx 200k$  (40000 layouts x 5  
579 missions). In addition,  $(30 + 5 + 5) \cdot 1000 \approx 40k$  simulations are required to test the capability of the vehicle,  
580 in terms of maximum vehicle velocity and acceleration, with respect to the reference vehicle. This procedure  
581 requires a computational time of about 1 h, if several Matlab servers are run on a computer that features an Intel  
582 i7 processor (8 CPUs at 2.8 GHz) and 16 GB of RAM. This first stage is of fundamental importance to reduce  
583 the number of layouts that have to be investigated in the subsequent stage. This stage (yellow bar in Fig. 2),  
584 which in fact computes the optimal control strategy, is much more time consuming than the first stage. It has  
585 been found that the number of feasible layouts is of the order of 200, 100 and 1000 for the TCV, SCV and DMV  
586 architectures, respectively (starting from original domains of 5k, 5k and 30k layouts). The total number of  
587 simulations that has to be carried out in the control strategy optimization phase is therefore  $(200 + 100 +$   
588  $1000) \cdot 3 \cdot 3 \cdot 6 \approx 70k$ , since three training missions, three objective functions and six powertrain cost  
589 definitions have been considered. This procedure requires an overall computational time of about 40 h, which  
590 can be considered low, compared to the total number of simulations that have to be carried out. A great  
591 advantage, in terms of computational time (but also memory demand) reduction, has been obtained using a  
592 specific numerical accelerator technique, which shifts the evaluation of the vehicle model to the pre-processing  
593 stage. Moreover, since each simulation task is not only fast, but also light, in terms of CPU and memory usage,

594 several Matlab servers can be launched simultaneously. Another advantage, in terms of computational time  
595 reduction, is obtained from the time grid discretization, which allows a large time step (3s) to be used, while  
596 maintaining at the same time a good accuracy in the results.

## 597 **6. Model validation and driving mission specifications**

### 598 **6.1 Validation of the vehicle model**

599 The models of the different components, i.e., the engine, the electric machine and the battery, were assessed by  
600 means of experimental tests carried out on a diesel mild hybrid powertrain, equipped with a belt-alternator  
601 starter, installed at the dynamic test bed of the ICEAL-PT (Internal Combustion Engine Advanced Laboratory,  
602 Dipartimento Energia, Politecnico di Torino). The model was validated by comparing the predicted and  
603 experimental fuel consumption and NOx emission values over NEDC for warm and cold start operations. It was  
604 found that the inaccuracy resulted to be within  $\pm 1$  % for the fuel consumption and  $\pm 6$  % for the cumulated NOx  
605 emissions.

606 For further details on the test rig specifications, the reader can refer to [35], and for further details on the  
607 assessment of the model, the reader can refer to [36, 37].

### 608 **6.2 Specifications of the considered driving missions**

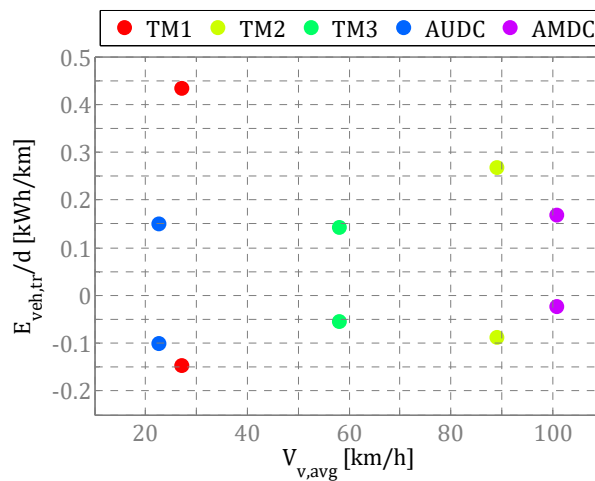
609 The performance of the hybrid vehicles analyzed in this study has been evaluated over a set of five driving  
610 missions. The main specifications of the driving cycles are shown in Table 3, which reports the duration  $T$ , the  
611 covered distance  $D$ , the global average velocity  $\bar{V}_v$ , the effective average velocity  $\bar{V}_v'$ , the maximum velocity  
612  $V_{v,max}$ , the maximum vehicle powers  $P_{tr,max}$  and  $P_{br,max}$  for the traction and braking stages, respectively, the  
613 average vehicle powers  $\bar{P}_{tr}$  and  $\bar{P}_{br}$ , as well as the total energy demands  $E_{tr}$  and  $E_{br}$  for the traction and braking  
614 stages. Figure 3 reports the coordinates of each driving mission, where the x-axis indicates the average speed,  
615 while the y-axis represents the ratio of the traction/braking energy demand to the covered distance. The dots that  
616 lie in the positive quadrant refer to traction, while those in the negative part refer to braking. This picture

617 provides useful information to help understanding which driving missions are more demanding in terms of  
 618 energy and velocity.  
 619 TM1 has been developed to simulate the vehicle in a mountain-like scenario, TM2 to simulate highway-like  
 620 conditions over different road slopes, while TM3 has been built in order to include an extensive variation of  
 621 driving conditions extracted from several homologation cycles.

622 **Table 3 – Main specifications of the set of driving cycles.**

	TM1	TM2	TM3	AUDC	AMDC
T [min]	96	108	171	993	1068
D [km]	0.72	2.67	2.76	4.86	29.53
$\bar{V}_v$ [km/h]	27	89	58	17.6	99.5
$\bar{V}_v'$ [km/h]	27	89	58	22.5	100.7
$V_{v,max}$ [km/h]	50	140	108.4	57.2	148.3
$P_{tr,max}$ [kW]	33	51.7	40.5	27	49.3
$P_{br,max}$ [kW]	-48	-100	-51.5	-40.4	-81.5
$\bar{P}_{tr}$ [kW]	15.6	28.7	11.6	6.7	20.6
$\bar{P}_{br}$ [kW]	-15.8	-46.2	-11.1	-4.5	-13.1
$E_{tr}$ [kWh]	0.31	0.72	0.4	0.74	5.01
$E_{br}$ [kWh]	-0.11	-0.23	-0.15	-0.48	-0.67

623



624

625 **Figure 3 – Traction/braking energy demand, with respect to the covered distance, and average velocity**

626

for the set of driving cycles.

## 627 **7. Results and Discussion**

628 A summary of this section is reported hereafter. Section 7.1 reports the main results obtained from the toolbox  
629 application to the vehicle design optimization proposed in this study. Three hybrid vehicles were considered (the  
630 speed-coupling architecture, the torque-coupling architecture, and the newly proposed dual-mode architecture),  
631 and their performance was compared with that of a conventional reference vehicle, in terms of CO2 emission  
632 reduction, NOx reduction and incremental costs. A detailed sensitivity analysis is provided in section 7.2, in  
633 order to investigate the impact of the cost definition, of the objective function and of the training driving mission  
634 on the optimal design of the vehicle and on its performance with respect to the conventional vehicle. Finally,  
635 section 7.3 reports a simulation of different market scenarios, in terms of fuel price, battery life duration and  
636 battery cost, and of their effects on the identification of the optimal design, as well as on the performance of the  
637 resulting hybrid vehicles.

638 The results are related to simulations in which each mission was repeated in order to cover a total distance of  
639 250000 km.

### 640 **7.1 Identification of the optimal layout and analysis of the vehicle** 641 **performance over different driving missions**

642 Table 4 reports the specifications of the layouts of the different vehicles, in terms of maximum engine power,  
643 battery and EM power (kW), as well as of the speed ratios of the TC/SC devices and of the final drive, obtained  
644 from the application of the toolbox proposed in this study.

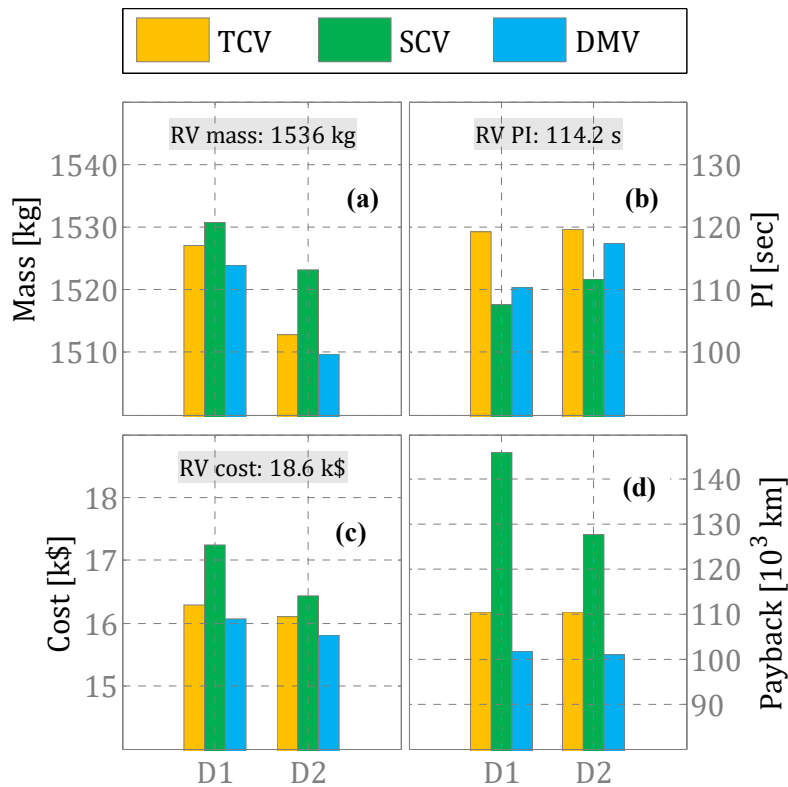
645 **Table 4 - Default design of each vehicle, in terms of maximum power of the engine, battery and EM (kW) and**  
646 **of the TC, SC and FD speed ratios.**

		<b>Engine power (kW)</b>	<b>Battery power (kW)</b>	<b>EM power (kW)</b>	<b>TC speed ratio</b>	<b>SC speed ratio</b>	<b>FD speed ratio</b>
<b>D1</b>	<b>TCV</b>	100	30	30	0.59		3.25

	SCV	100	32.5	32.5		2.7	2.5
	DMV	100	27.5	27.5	0.5	4.5	2.5
D2	TCV	70	42.5	42.5	0.91		3.25
	SCV	70	50	50		3	2.5
	DMV	70	40	40	0.5	4.2	2.5

647

648 The main specifications of each vehicle, in terms of total mass, performance index (PI), total powertrain cost  
649 over the lifetime and payback distance (estimated over the TM3 mission) are instead reported in Fig. 4.



650

651 **Figure 4 - Main specifications of the default design of each considered hybrid vehicle, estimated over the**  
652 **TM3 mission.**

653 The optimal design of each vehicle has been obtained over the TM3 mission, using the total powertrain costs  
654 definition (i.e., Eq. (36)) and the FC-BLC-oriented optimization. These choices are explained in the following  
655 subsections.

656 The total mass of the hybrid vehicles resulted to be the same as that of the conventional vehicle (Fig. 4a) because  
657 of the power density of the battery, which is significantly high for non-plug-in hybrid vehicles (i.e., twice the

658 specific power of a conventional vehicle engine). The SCV, equipped with the D1 engine, was the heaviest,  
659 while DMV-D2 was the lightest.

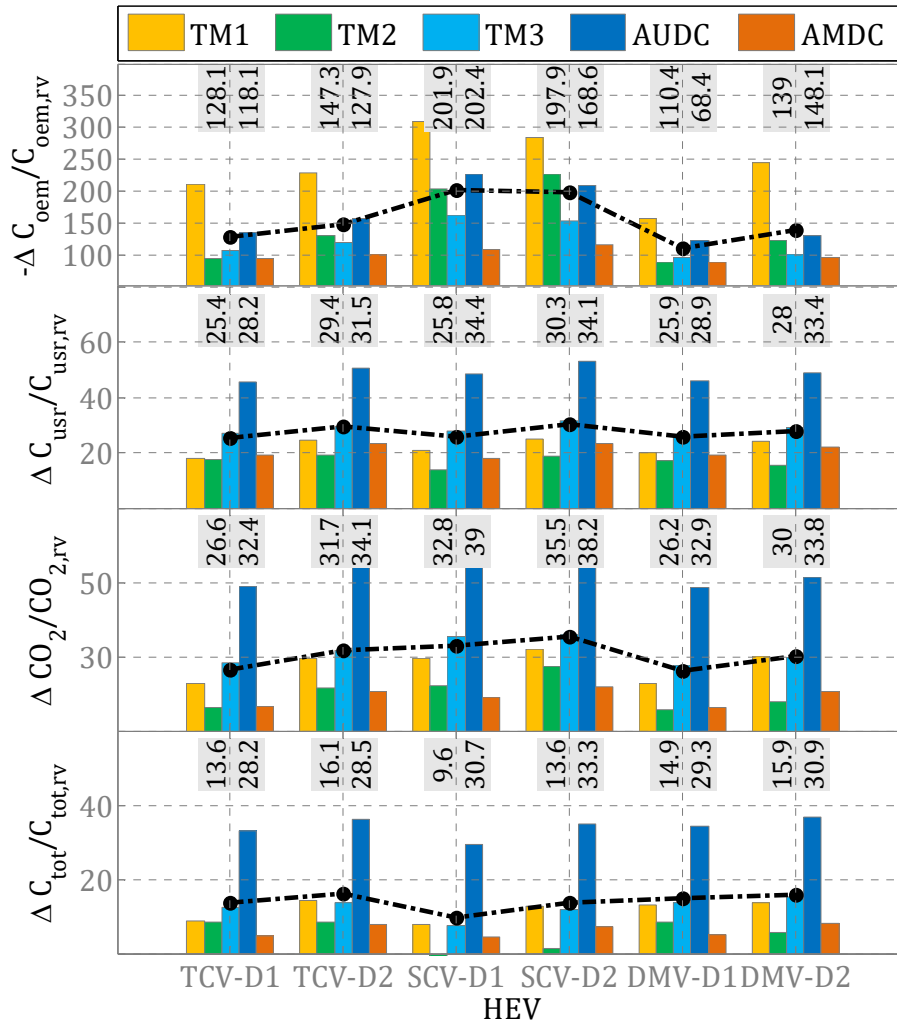
660 As far as the total costs are concerned (Fig. 4c), the vehicles equipped with the D2 engine are capable of  
661 reducing the total costs by 2.5%, compared to the corresponding vehicles equipped with the D1 engine, except  
662 for SCV-D2, which shows a reduction of 5%. The maximum cost reduction, with respect to the reference  
663 vehicle, is obtained for DMV-D2 (17.7%).

664 The cost savings also depend on the distance covered by the vehicle over a certain period: the longer the  
665 distance, the greater the operating cost reduction. The break-even point represents the distance that each vehicle  
666 has to cover to counterbalance the initial investment. A significant result is that the proposed dual-mode vehicle  
667 leads to the lowest powertrain costs and to the shortest payback distance.

668 Figure 5 reports the increase in the OEM cost (first row), as well as the decrease in the user cost (second row), in  
669 the CO<sub>2</sub> emissions (third row) and in the total costs (fourth row), for the hybrid vehicles with the optimal  
670 baseline layout tested over each mission of the M2 set (TM1, TM2, TM3, AUDM, AMDC).

671 Each black dashed line in the figure shows the average variation in the corresponding quantity over the set of  
672 driving cycles for the different vehicles. Each textbox in the chart reports instead the average (left) and the  
673 difference between the maximum and minimum values (right) over the five driving cycles. It can be observed  
674 that DMV-D1 is the most convenient vehicle in terms of OEM costs, since the average increment over the test  
675 missions is 110%. It is worth recalling that the OEM cost consists of the production costs and a fraction of the  
676 costs due to battery replacement. The different values of the OEM cost increase over different missions for a  
677 given layout reported in Fig. 5 are related to different battery replacement costs. In general, TM1 is the most  
678 critical mission in terms of battery usage, due to its severe accelerations over both uphill and downhill roads and  
679 due to its short distance, which justifies the highest OEM cost when the hybrid vehicle performance is simulated  
680 over that mission.





681

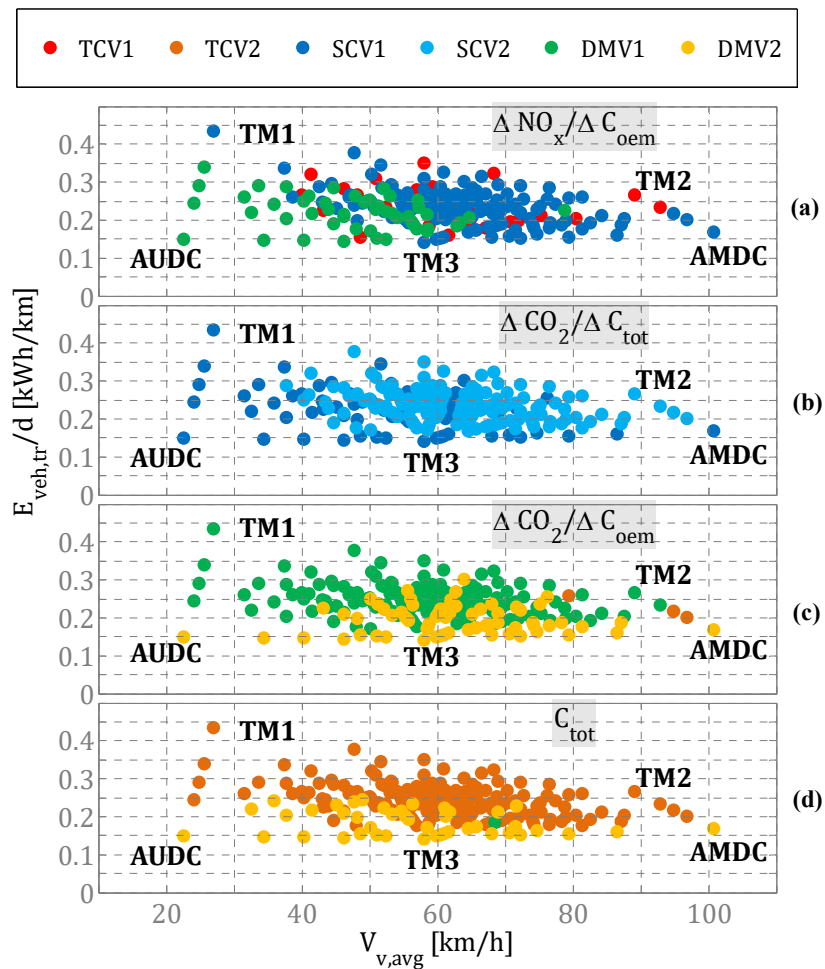
682 **Figure 5 –Increase in OEM costs (first row), user cost reduction (second row), CO2 emissions reduction (third**  
 683 **row) and total cost reduction (fourth row), with reference to the reference vehicle, for different test missions**  
 684 **and for each vehicle. The optimal layout has been used for each vehicle.**

685 A significant result is that DMV-D1 is the least expensive architecture from an OEM point of view, but its  
 686 average performance, in terms of user cost reduction and CO2 emission reduction over the vehicle lifetime, is in  
 687 line with that of the other vehicles. The SCV-D1 leads to the best CO2 emission reduction (32.8%), but this is  
 688 obtained at the expense of the OEM costs, which are the highest.

689 In general, the vehicles equipped with the D2 engine outperform the corresponding vehicles equipped with the  
 690 D1 engine, in terms of user costs, CO2 emissions and total costs. However, they also lead to higher OEM costs,

691 except for the SCVs, which are characterized by similar OEM costs, regardless of what type of engine is  
 692 considered.

693 An additional investigation has been carried out in order to understand which hybrid architectures are the most  
 694 convenient, considering the testing mission specification and different target functions. The results are reported  
 695 in Fig. 6. Each point represents a specific driving condition, in terms of average speed (x-axis) and the ratio of  
 696 the traction energy demand to the covered distance (y-axis). A large set of missions with different specifications  
 697 was generated for this analysis. The color of each point indicates the best architecture that minimizes the target  
 698 function over the considered mission. Four different target functions were defined, namely the ratio of the NOx  
 699 emission reduction to the OEM cost variation (Fig. 6a), the ratio of the CO2 emission variation to the total cost  
 700 variation (Fig. 6b), the ratio of the CO2 emission variation to the OEM cost variation (Fig. 6c) and the total costs  
 701 (Fig. 6d). The points corresponding to the TM1, TM2, TM3, AUDC and AMDC missions are also reported.



703 **Figure 6 – Optimal hybrid architectures over several driving scenarios, for different target functions.**

704 First, it can be noted, from Fig. 6a, that the best architectures selected to reduce NO<sub>x</sub> emissions are those  
705 equipped with engine D1. This is a consequence of the fact that the D2 engine is smaller than the D1 engine, and  
706 it generally operates at higher relative load levels, where high NO<sub>x</sub> emissions occur (the calibration maps of the  
707 engines considered in this study were in fact optimized for a conventional vehicle). In order to avoid this issue, a  
708 comprehensive optimization tool, which is capable of identifying not only the optimal control strategy of the  
709 hybrid powertrains over the mission, but also the optimal values of the main engine parameters (i.e., EGR rate,  
710 start of injection), is currently being developed. This tool will incorporate specifically developed low-throughput  
711 models that simulate the combustion and emission formation processes in the engine (see [35, 38-40]). The  
712 results of this research will be presented in the near future.

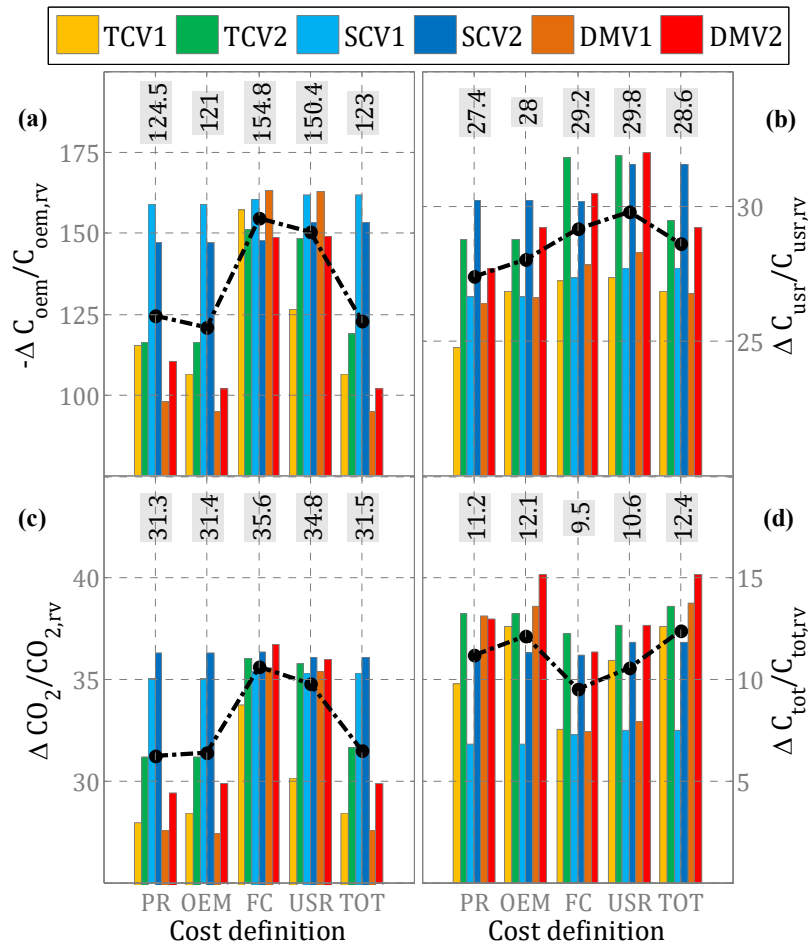
713 Moreover, Fig. 6a indicates that the DMV-D1 is convenient, in terms of NO<sub>x</sub> emission reduction per unit OEM  
714 cost reduction, for driving cycle specifications in the AUDC-TM1-TM3 region, while TCV-D1 is convenient in  
715 the TM1-TM3-AMDC-TM2 region. Fig. 6b shows that the speed-coupling architectures lead to the highest  
716 potential, in terms of CO<sub>2</sub> emission reduction per unit total cost reduction. However, it was found that this result  
717 was achieved after an intense exploitation of the battery, which leads to high battery replacement costs (i.e., high  
718 OEM and user cost). Fig. 6c shows that SCV is in fact not convenient, in terms of NO<sub>x</sub> emission reduction per  
719 unit OEM cost reduction. In this case, DMVs represent the best choice. The employment of the D1 engine with  
720 the smallest battery pack (27.5 kW, see Table 5) is more advisable in the upper region (higher energy demand),  
721 while the D2 engine with the largest battery pack (40 kW, Table 5) is advisable in the lower region. Finally, Fig.  
722 6d indicates that DMV-D2 is the best choice, in terms of total powertrain cost, over missions that feature a  
723 relatively low specific traction energy demand, while TCV-D2 is better for higher values. It was verified that the  
724 total cost reduction for DMV-D2 is mainly due to the reduction in the battery replacement costs, while the TCV-  
725 D2 layout shows the best potential to reduce the fuel consumption cost. Missions with a high energy demand,  
726 such as TM1 and TM2, favor the choice of TCV-D2, since fuel costs rather than battery replacement costs are  
727 the predominant contributions. On the other hand, DMV-D2 is the best choice for driving missions in which  
728 battery life depletion is a major concern.

## 729 **7.2 Sensitivity analyses**

730 Several sensitivity analyses have been carried out, in order to understand the impact of the cost definition  
731 (section 7.2.1), of the objective function (section 7.2.2) and of the training mission (section 7.2.3) on the optimal  
732 layout and on the performance of the related vehicles.

### 733 **7.2.1 Impact of the cost definition**

734 The impact of the powertrain cost definition that was used to identify the optimal design (see section 5.1) has  
735 been investigated, and the results are shown for each vehicle in Figure 7, which reports the reduction in the OEM  
736 cost (Fig. 7a), in the user cost (Fig. 7b), in the CO<sub>2</sub> emissions (Fig. 7c) and in the total costs (Fig. 7d), with  
737 respect to the reference vehicle, obtained using different architectures (indicated with different colors) and  
738 optimized using different cost definitions (indicated by the different groups of bars identified with the acronyms  
739 PR, OEM, FC, USR, TOT, i.e., production cost, OEM cost, fuel consumption cost, user cost and total cost,  
740 respectively). The results shown in Fig. 7 were obtained using the benchmark optimizer (i.e., DP) and an FC-  
741 BLC-oriented optimization over the TM3 training mission. The three weight factors in Eq. (21) were set as  
742 follows:  $\alpha_1 = 0.5$ ,  $\alpha_2 = 0$ ,  $\alpha_3 = 0.5$ .



743

744 **Figure 7 - Increase in OEM costs (top left), decrease in user costs (top right), in CO2 emissions (bottom left)**  
 745 **and in total costs (bottom right), with respect to the reference vehicle, for the different vehicles whose**  
 746 **layouts have been identified using different powertrain cost definitions (PR, OEM, FC; USR, TOT). The TM3**  
 747 **mission has been used for training.**

748 Fig. 7a shows that if the user or FC cost definitions are selected for the layout optimization process, the resulting  
 749 vehicles are characterized by a higher OEM cost increase than the conventional vehicle (about +150%), mainly  
 750 due to the higher hybridization degree that is required. At the same time, they are capable of providing the best  
 751 performance, in terms of user cost reduction (29-30%, Fig. 7b) and CO2 emission reduction (about 35%, see Fig.  
 752 7c). However, they are also penalized in terms of total powertrain cost over the vehicle lifetime (about 10%, see  
 753 Fig. 7d), mainly as a consequence of the high OEM costs. On the other hand, if the OEM, production or total  
 754 cost definitions are selected, the resulting vehicles are characterized by a lower OEM cost increase (about +121-

755 125%, see Fig. 7a) and a higher total cost reduction than the conventional vehicle (11.2-12.4%, see Fig. 7d), but  
 756 they maintain a good performance in terms of user cost reduction (27.4-28.6%) and CO2 emission reduction (31-  
 757 32%, see Fig. 7c).

758 It should be noted that the OEM costs represent a factor of great importance for car manufactures, and they may  
 759 play a decisive role in promoting a specific vehicle architecture on the market.

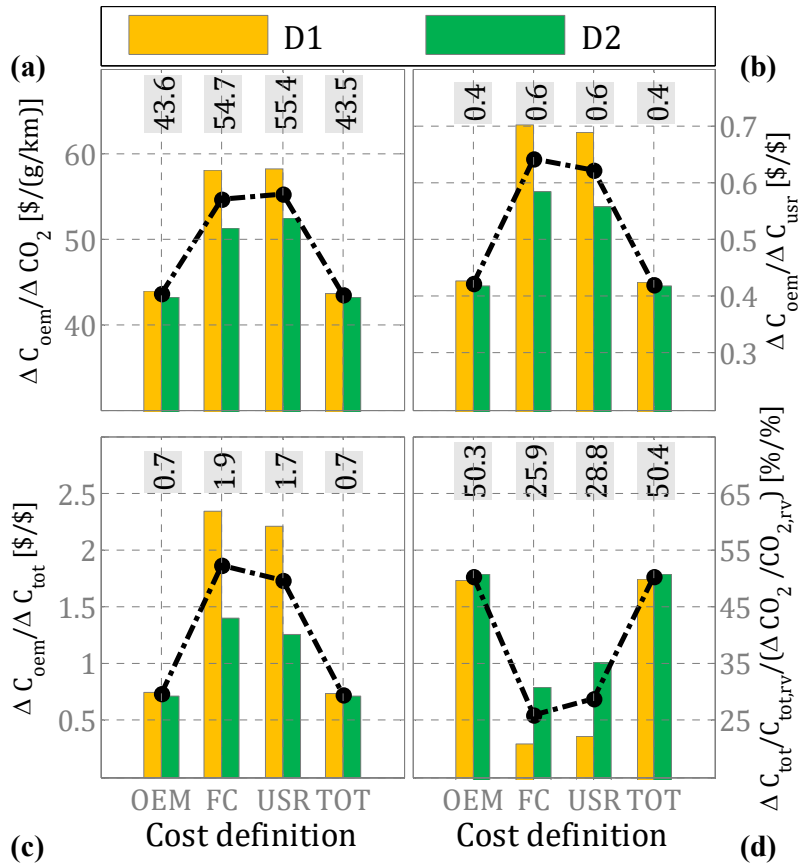
760 The use of the OEM cost definition to identify the optimal layout obviously leads to the lowest OEM cost  
 761 increase, but at the same time also to reductions in the total costs and in the CO2 emissions, which are of the  
 762 same order of magnitude as those obtained using the total cost definition.

763 Table 5 reports the design specifications, in terms of maximum engine, battery and EM power (kW), as well as  
 764 of the speed ratios of the TC/SC devices and of the final drive of the DMVs, whose layouts were optimized  
 765 using two different training cycles (TM1 and TM3) and four cost definitions (fuel, operating, OEM and total).

766 **Table 5 – Main specifications of DMVs for two training cycles and four different cost definitions, in terms of**  
 767 **maximum power of the engine, battery and EM (kW), and of the TC, SC and FD ratios.**

			<b>Engine power (kW)</b>	<b>Battery power (kW)</b>	<b>EM power (kW)</b>	<b>TC speed ratio</b>	<b>SC speed ratio</b>	<b>FD speed ratio</b>
<b>D1</b>	<b>TM1</b>	<b>FC</b>	100	35	35	2	4.5	2.5
		<b>Oper</b>	100	27.5	27.5	0.5	3.3	2.5
		<b>OEM</b>	100	27.5	27.5	0.5	3.9	2.5
		<b>TOT</b>	100	27.5	27.5	0.5	3.3	2.5
	<b>TM3</b>	<b>FC</b>	100	32.5	32.5	2.9	3.9	2.75
		<b>Oper</b>	100	35	35	0.5	3	2.5
		<b>OEM</b>	100	27.5	27.5	0.5	4.2	2.5
		<b>TOT</b>	100	27.5	27.5	0.5	4.5	2.5
<b>D2</b>	<b>TM1</b>	<b>FC</b>	70	40	40	3.2	2.7	2.5
		<b>Oper</b>	70	50	50	1.4	3	2.5
		<b>OEM</b>	70	42.5	42.5	0.8	3.9	2.75
		<b>TOT</b>	70	42.5	42.5	0.8	3.9	2.75
	<b>TM3</b>	<b>FC</b>	70	40	40	2.9	3.3	2.5
		<b>Oper</b>	70	50	50	1.1	3.9	2.5
		<b>OEM</b>	70	40	40	0.5	4.2	2.5
		<b>TOT</b>	70	40	40	0.5	4.2	2.5

769 It should be noted, in the table, that if the OEM and total cost definitions are used to identify the optimal layout,  
770 the maximum power of the electric machine results to be the lowest. It has been verified that this power is the  
771 minimum one that allows the vehicle performance constraint to be satisfied, in terms of vehicle longitudinal  
772 acceleration. The final drive speed ratio is basically independent of the cost definition. A low TC speed ratio has  
773 been chosen when the operating, OEM and total cost definitions have been used (all the definitions take into  
774 account battery aging), while higher values (up to 3) are selected if the fuel consumption cost definition is used.  
775 The latter definition does not take into account battery aging, and the layout is therefore identified in order to  
776 maximize the CO<sub>2</sub> emission reduction, regardless of the battery depletion. A low TC speed ratio in fact limits  
777 the maximum power of the electric machine in both the regenerative braking and electric traction phases. It has  
778 been verified that this determines a limitation of the maximum fraction of recoverable energy during the  
779 regenerative braking phases. This in turn leads to a fuel-economy penalization, but at the same time has a  
780 positive effect on battery life duration, which depends directly on the energy flux across the battery itself.  
781 The results reported in Fig. 7 have suggested the need to investigate what the ratio would be between the  
782 incremental OEM cost of a given hybrid vehicle and the achieved CO<sub>2</sub> emission reduction, in order to  
783 understand how “expensive” a CO<sub>2</sub> emission reduction unit would be in terms of incremental OEM costs. At the  
784 same time, the ratio between the incremental OEM cost and the incremental user and total costs, as well as the  
785 ratio between the reduction in total costs and the achieved CO<sub>2</sub> emission reduction have been investigated. The  
786 results related to the DMVs, equipped with the D1 or D2 engines, are reported in Fig. 8 for each cost definition  
787 used during the layout optimization process.



788

789 **Figure 8 - Ratio between the incremental OEM costs and the CO2 emission reduction (a), user cost reduction**  
 790 **(b) and total cost reduction (c); ratio between the total cost reduction and the CO2 emission reduction (d);**  
 791 **the DMVs equipped with D1 and D2 engines have been considered.**

792 It can be noted, in Fig. 8a, that the incremental OEM cost necessary to reduce the CO2 emissions by 1 g/km is  
 793 about \$ 43.5, if the optimal layout is identified using the OEM or total cost definitions, while it is about \$ 55 in  
 794 the case when the user or FC cost definitions are adopted. The incremental OEM cost increase per unit user cost  
 795 reduction (Fig. 8b) follows the same trends as the CO2 emissions (i.e., fuel consumption), and the user costs are  
 796 closely related to each other. A similar trend can also be observed when the ratio between the incremental OEM  
 797 cost and the incremental cost is considered (Fig. 8c). In addition, it is worth noting (Fig. 8d) that the ratio  
 798 between the relative total cost reduction and the relative CO2 reduction is of the order of 50%, if the OEM or the  
 799 total cost definitions are used to determine the optimal layout, while it is around 26% if the fuel cost or the user

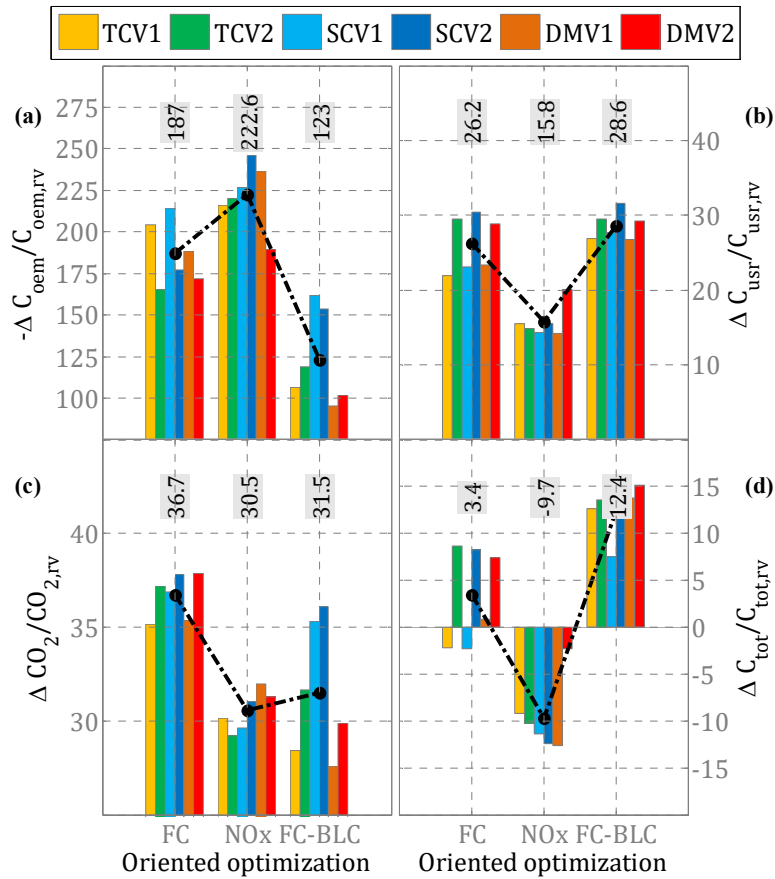


800 cost definitions are adopted. This means that additional CO<sub>2</sub> reductions can be achieved at the expense of higher  
801 overall costs, if the layout is optimized on the basis of the fuel cost or user cost definitions.

802 On the basis of the previous results, the total cost definition can be considered as the best method to identify the  
803 optimal layout, as it leads to the lowest incremental OEM costs per unit CO<sub>2</sub> emission reduction, per unit user  
804 cost reduction and per unit total cost reduction of the hybrid vehicle over its lifetime. However, fuel cost or user  
805 cost definitions could also be used to define the optimal layout if a more intense CO<sub>2</sub> emission reduction is  
806 necessary, regardless of the increment in the powertrain costs. The main reason for the incremental costs related  
807 to the adoption of the fuel or user cost definition is related to the fact that a more aggressive use of the electric  
808 power unit is realized, and this leads to higher battery replacement costs.

### 809 **7.2.2 Impact of the objective function**

810 The impact of the objective function on the optimal design and on its performance and costs has been  
811 investigated and the results for each vehicle are shown in Fig. 9, which reports the increase in the OEM cost  
812 (Fig. 9a), as well as the decrease in the user cost (Fig. 9b), in the CO<sub>2</sub> emissions (Fig. 9c) and in the total costs  
813 (Fig. 9d). The x-axis reports three different oriented optimizations, namely FC ( $\alpha_1 = 1, \alpha_2 = 0, \alpha_3 = 0$  in Eq.  
814 (21)), NO<sub>x</sub> ( $\alpha_1 = 0, \alpha_2 = 1, \alpha_3 = 0$ ) and FC-BLC ( $\alpha_1 = 0.5, \alpha_2 = 0, \alpha_3 = 0.5$ ), which have been used to  
815 define the optimal control strategy. The total cost definition was used to identify the optimal layout over the  
816 TM3 training mission.



817

818 **Figure 9 - Increase in OEM costs (top left), decrease in user costs (top right), in CO2 emissions (bottom left)**  
 819 **and in total costs (bottom right), with respect to the reference vehicle, for different objective functions and**  
 820 **for each type of vehicle. The TM3 mission has been used for layout optimization.**

821 Fig. 9 shows that if the control strategy is identified according to the FC and FC-BLC objective functions, the  
 822 resulting vehicles show a lower OEM cost increase (Fig. 9a) than the reference vehicle (the FC-BLC function is  
 823 the best choice from this point of view), a greater user cost reduction (Fig. 9b), a greater CO2 emission reduction  
 824 (the FC function shows the best potential) and positive total cost reductions (the FC-BLC function leads to the  
 825 maximum benefit). Since each layout must satisfy the constraints expressed by Eq. (23), which also include an  
 826 NOx emission limit, the improvements in CO2 emissions and in cost reductions, using the FC- and FC-BLC-  
 827 oriented optimizations, can be considered consistent.

828 On the other hand, the adoption of the NOx oriented objective function leads to the highest OEM cost increase  
829 (Fig. 9a), to the lowest user cost and CO<sub>2</sub> emission reduction (Figs. 9b, c) and to an unacceptable increase in the  
830 total powertrain costs over the vehicle lifetime (Fig. 9d).

831 This occurs because the NOx-oriented objective function is targeted at reducing pollutant emissions as much as  
832 possible, regardless of the increase in fuel consumption and battery usage (and in their related operating costs). It  
833 has been verified that when the FC-BLC-oriented optimization is adopted, the average NOx emission reduction  
834 is 19% and 11% for the hybrid vehicles equipped with the D1 and D2 engines, respectively (results not reported  
835 in Fig. 9). Instead, this reduction percentage increases to 47% and 60% when the NOx-oriented optimization is  
836 used. However, these promising results are penalized to a great extent by the huge increment in the OEM and  
837 total powertrain costs. An NOx emission reduction would in fact imply an intense use of the electric machine  
838 and of the battery in both the charging and discharging stages, in order to shift the engine operating conditions to  
839 a low NOx emission area, and the battery life would therefore be affected negatively, as would the associated  
840 replacement costs.

841 Finally, it can be noted that if the FC-oriented objective function were adopted instead of the FC-BLC one, an  
842 additional Co<sub>2</sub> emission reduction decrease of 5% could be achieved, but this reduction would lead to higher  
843 OEM and total costs.

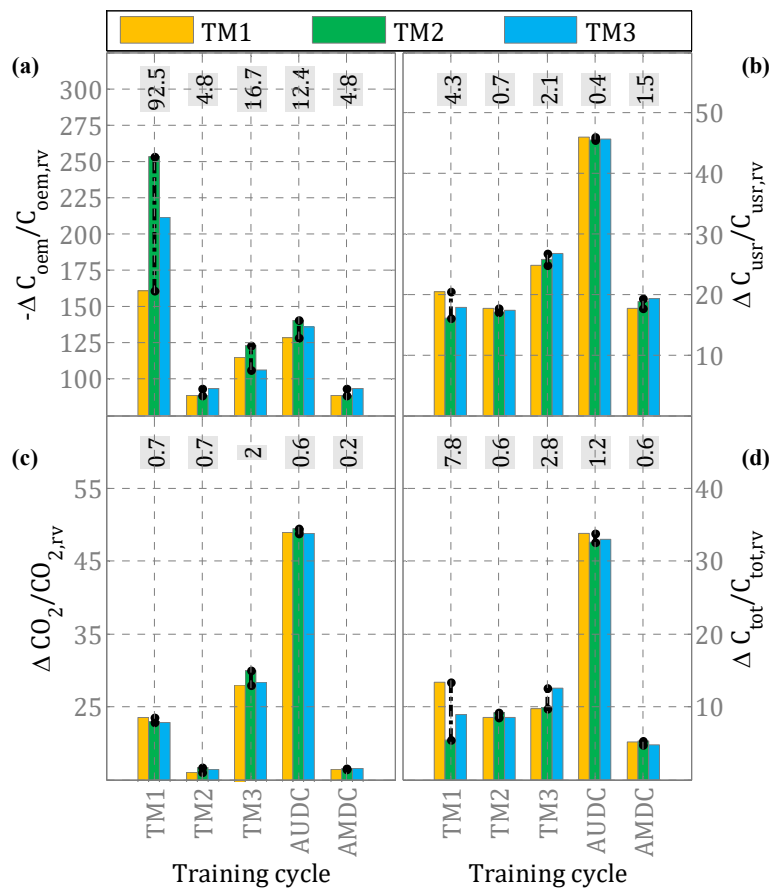
844 The FC-BLC objective function was therefore selected as the best solution, in terms of trade-off between the  
845 incremental OEM cost, CO<sub>2</sub> emission reduction and user/total cost reduction, and was adopted to define the  
846 optimal layout of the vehicles.

### 847 **7.2.3 Impact of the training driving mission selection**

848 A sensitivity analysis of the impact of the training driving cycle selected for the optimal layout identification has  
849 been carried out in this section.

850 The performance of the generic  $x_{m1}$  layout, which has been optimized over the  $m_1$  training missions of the M1  
851 set (TM1, TM2 or TM3), has been simulated over the  $m_2$  test missions that belong to the M2 set (TM1, TM2,  
852 TM3 AMDC and AUDC).

853 The results are shown in Fig. 10, which reports the increase in OEM cost (Fig. 10a), as well as the reduction in  
 854 the user cost (Fig. 10b), in the CO2 emissions (Fig. 10c) and in the total costs (Fig. 10d), with respect to the  
 855 reference vehicle. The  $i^{\text{th}}$  bar of the  $j^{\text{th}}$  group represents the average performance of the set of the optimal  
 856 vehicle layouts over the  $j^{\text{th}}$  test mission of the M2 set, where each optimal layout was selected over the  $i^{\text{th}}$   
 857 training mission of the M1 set (indicated with different colors). Each black dashed line in the figure and the  
 858 corresponding number in the text box indicate the greatest difference within each bar block, for different training  
 859 cycles. The results shown in Fig. 10 were obtained using DP, an FC-BLC-oriented optimization and a total cost  
 860 definition.



861  
 862 **Figure 10 - Increase in OEM costs (a), reduction in user costs (b), in CO2 emissions (c) and in total costs (d),**  
 863 **with respect to the reference vehicle, for the different training driving cycles used in the layout optimization**  
 864 **process and for each vehicle.**

865 It can be noted, in the above figure, that the OEM costs are the terms that are affected the most by the training  
866 mission selection. For example, considering a layout that has been defined using either the TM1 mission  
867 (mountain-like scenario) or the TM2 driving mission (highway-like scenario), and tested over the TM1 mission  
868 (the two cases are indicated with the yellow and green bars in the first group in Fig. 10a), the differences in  
869 terms of the OEM cost are significant. Additional costs for the OEM are in fact obtained in this case, while the  
870 total costs are less compromised. The performance, in terms of CO<sub>2</sub> emission reduction and user cost reduction,  
871 is in general affected less by the type of training mission used for the identification of the optimal layout.  
872 Finally, it should be noted that the TM3 mission has been designed to include a wide variety of driving  
873 conditions extracted from several homologation cycles, and for this reason it was selected as the best candidate  
874 for the optimal layout identification.

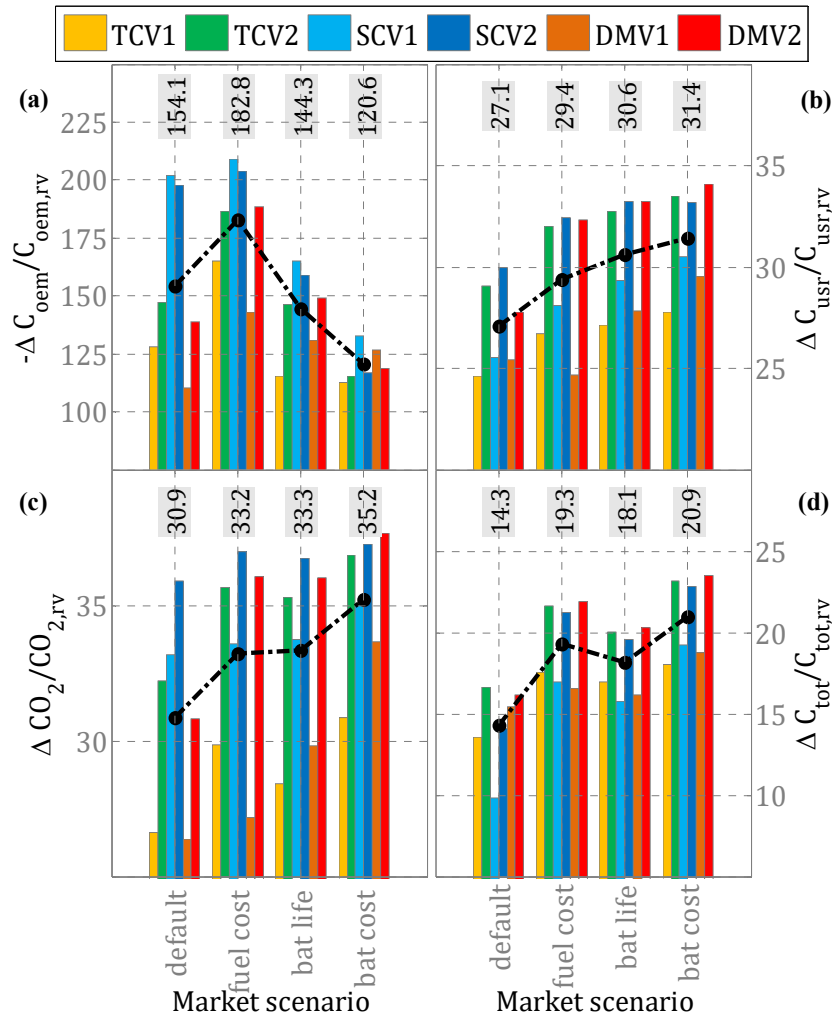
### 875 **7.3 Analysis of different market scenarios**

876 This section reports the results of a detailed investigation of different market scenarios, in terms of fuel price,  
877 battery life duration and battery cost, and of their effects on the identification of the optimal design, as well as on  
878 the performance of the resulting vehicles.

879 Let us set the current market scenario as the default situation, in terms of fuel cost, battery replacement cost and  
880 battery life (case 0). Three additional market scenarios were considered, where the fuel cost increased by 50%  
881 over the lifetime of the vehicle (case 1), the battery life increased by 50% (case 2) and the battery cost was  
882 halved (case 3).

883 The impact of the different market scenarios on the definition of the optimal layout and on the performance has  
884 been investigated, and the results for each vehicle are shown in Fig. 11, which reports the increase in the OEM  
885 cost (Fig. 11a), as well as the decrease in the user cost (Fig. 11b), in the CO<sub>2</sub> emissions (Fig. 11c) and in the  
886 total costs of the powertrain over its lifetime (Fig. 11d), with respect to the reference vehicle. Each black dashed  
887 line and the corresponding numbers in the text box indicate the average reduction over the set of vehicles,  
888 obtained in different market scenarios. The results shown in Fig. 11 were obtained using the benchmark

889 optimizer (i.e., DP) and an FC-BLC-oriented optimization. Moreover, the total costs definition was used to  
 890 identify the optimal layout.



891  
 892 **Figure 11 - Increase in OEM costs (a), decrease in user costs (b), in CO2 emissions (c) and in total costs (d)**  
 893 **for different market scenarios and for each type of vehicle.**

894 In an increasing fuel cost scenario (second group of bars in the charts in Fig. 11), the optimization is in particular  
 895 aimed at reducing CO2 emissions, even though more batteries would be required during the life of the vehicle.  
 896 However, this strategy has an important effect on the OEM costs, which rise to 182.8% (Fig. 11a) compared to  
 897 the reference vehicle. The results obtained for the market scenario in which the battery cost is halved (fourth  
 898 group of bars in Fig. 11) indicate that the battery cost is the most significant factor in promoting the hybrid  
 899 technology. In fact, in this scenario, the average OEM cost increase is the lowest one (120.6%), the average CO2

900 emission reduction is the highest one (35.2%) and the average total cost reduction, with respect to the  
901 conventional vehicle, is the highest one (20.9%). The scenario in which the battery duration is increased (third  
902 group of bars in Fig. 11) also leads to a significant improvement in the performance of the hybrid vehicles.  
903 It is worth observing that each architecture that is equipped with the D2 engine leads to the lowest total costs for  
904 the three speculated market conditions.

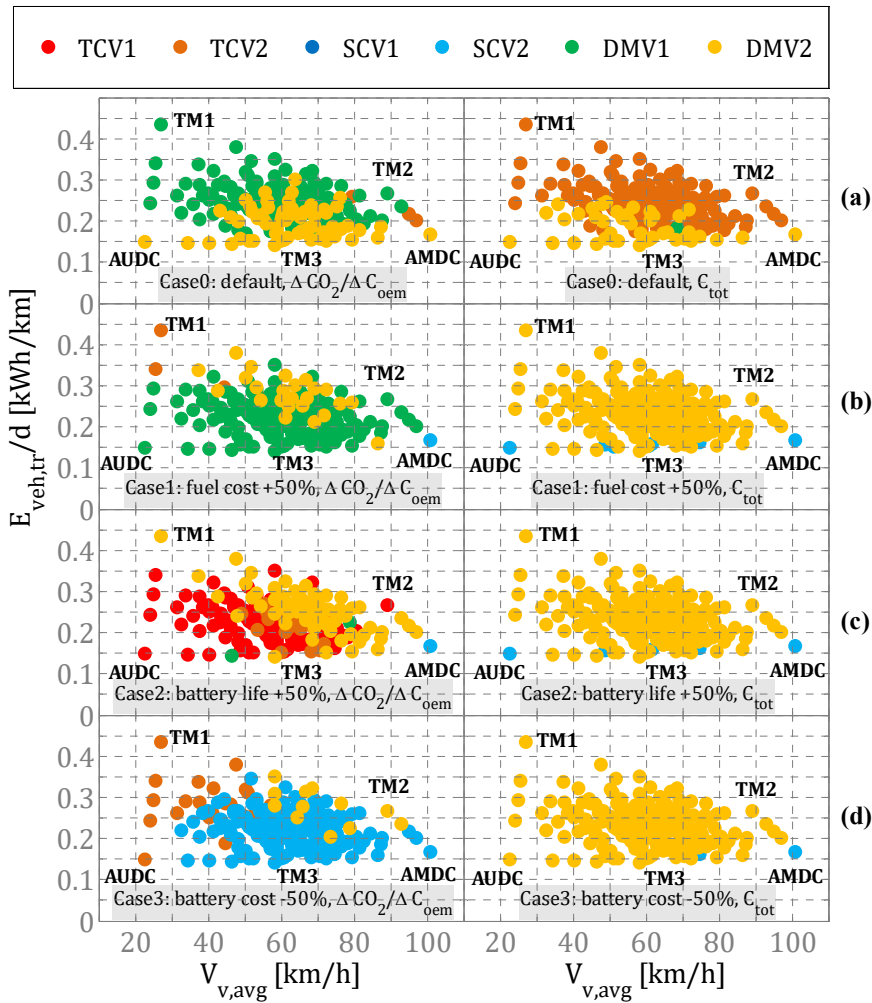
905 In order to conclude the analysis, Figure 12 reports the distribution of the best vehicles that were selected for  
906 different driving-configurations using two target functions (ratio between the CO<sub>2</sub> reduction and OEM cost  
907 increase  $\frac{\Delta CO_2}{\Delta C_{oem}}$  in the left column, total powertrain cost,  $C_{tot}$  in the right column) and exploring the four market  
908 scenarios, namely the default scenario (Fig. 12a), the scenario in which the fuel cost is increased by 50% (Fig.  
909 12b), the scenario in which the battery life is increased by 50% (Fig. 12c) and, finally, the scenario in which the  
910 battery-cost is halved (Fig. 12d).

911 It can be observed that, as far as the  $\frac{\Delta CO_2}{\Delta C_{oem}}$  target function is considered, DMVs are the best architectures in the  
912 incremented fuel-cost scenario, while DMV-D1 is better in the low-medium energy region. TCVs and DMV-D2  
913 are instead better if a battery with a longer life is expected to be available on the market (Fig. 12c).

914 The scenario in which the battery cost is halved suggests choosing the D2 engine and the speed coupling  
915 architecture (Fig. 12d). In particular, SCV-D2 is convenient in the medium-high velocity and low-medium  
916 energy region, while TCV-D2 is convenient in the TM1-TM3-AUDC region.

917 However, if the total cost reduction is the only target (right column in Fig. 12), each market scenario promotes  
918 the selection of DMV-D2 in most of the regions, while SCV-D2 is selected in the low energy demand region.

919 The size of the components of each vehicle is reported in Table 6 for the set of vehicles and for the four market  
920 scenarios.



921

922 **Figure 12 – Optimal hybrid architectures selected over several driving conditions, for different market**  
 923 **scenarios and target functions.**

924 The main outcome concerns the speed ratio of the TC device, which is increased to 1.7 in each new condition for  
 925 DMV-D2, in order to better exploit the battery component for both regenerative braking and pure electric  
 926 traction. Higher TC speed ratios in fact lead to a more intense battery employment, which directly affects the  
 927 battery replacement costs and therefore both the OEM and the total costs. However, in the fuel cost increase  
 928 scenario (case 1), the battery cost contribution is less important, and both the design and the control strategy are  
 929 aimed at the reduction of CO2 emissions.

930 Moreover, if the battery life increases or the battery cost decreases (cases 2 and 3, respectively), the economic  
 931 impact of the battery component is always lower, whatever strategy is defined.



**Table 6 – Design of the set of vehicles for the four market scenarios, in terms of the maximum power of the engine, battery and EM (kW) and of the TC, SC and FD ratios.**

			<b>Engine power (kW)</b>	<b>Battery power (kW)</b>	<b>EM power (kW)</b>	<b>TC speed ratio</b>	<b>SC speed ratio</b>	<b>FD speed ratio</b>
<b>D1</b>	<b>TCV</b>	<b>Default</b>	100	30	30	0.59		3.25
		<b>Fuel cost</b>	100	32.5	32.5	0.8		3.25
		<b>Battery life</b>	100	30	30	0.8		3.25
		<b>Battery cost</b>	100	35	35	0.5		3.25
	<b>SCV</b>	<b>Default</b>	100	32.5	32.5		2.7	2.5
		<b>Fuel cost</b>	100	32.5	32.5		2.7	2.5
		<b>Battery life</b>	100	35	35		2.7	2.5
		<b>Battery cost</b>	100	35	35		2.7	2.5
	<b>DMV</b>	<b>Default</b>	100	27.5	27.5	0.5	4.5	2.5
		<b>Fuel cost</b>	100	27.5	27.5	0.5	4.2	2.75
		<b>Battery life</b>	100	30	30	0.5	3	2.5
		<b>Battery cost</b>	100	35	35	0.8	3.9	2.75
<b>D2</b>	<b>TCV</b>	<b>Default</b>	70	42.5	42.5	0.91		3.25
		<b>Fuel cost</b>	70	47.5	47.5	1.7		3.25
		<b>Battery life</b>	70	45	45	1.7		3.25
		<b>Battery cost</b>	70	45	45	1.7		3.25
	<b>SCV</b>	<b>Default</b>	70	50	50		3	2.5
		<b>Fuel cost</b>	70	47.5	47.5		3	2.5
		<b>Battery life</b>	70	45	45		3	2.5
		<b>Battery cost</b>	70	40	40		2.7	2.5
	<b>DMV</b>	<b>Default</b>	70	40	40	0.5	4.2	2.5
		<b>Fuel cost</b>	70	47.5	47.5	1.7	4.2	2.5
		<b>Battery life</b>	70	45	45	1.7	4.2	2.5
		<b>Battery cost</b>	70	45	45	1.7	3.9	2.5

## 935 **8. Conclusion and future work**

936 This present study has focused on the refinement of a previously developed tool for the definition of the optimal  
937 layout in hybrid vehicles, based on powertrain cost reduction, and on its application to a newly proposed non-  
938 plug-in parallel hybrid architecture that is able to incorporate torque-coupling (TC) and speed-coupling (SC)  
939 functions, and is therefore referred to as a dual-mode vehicle (DMV). The performance of this architecture has  
940 been evaluated in detail in terms of cost and CO<sub>2</sub> emission reduction with respect to a conventional vehicle. Two  
941 different diesel engines, which are here referred to as D1 and D2 (with displacements of 1.7L and 1.3L,  
942 respectively), have been considered for the design optimization process. A bi-level (nested) tool has been  
943 developed for the simultaneous optimization of the vehicle design and control strategy to manage the power flow  
944 of the engine and electric machines. The tool identifies the optimal layout by minimizing the powertrain cost  
945 over the lifetime of the vehicle. Different cost definitions have been considered in this study: production costs  
946 ( $C_{pr}$ ), which account for the production cost required by the OEM; OEM costs ( $C_{oem}$ ), which consist of the  
947 production cost and a fraction of the cost due to battery replacement over the vehicle lifetime; fuel costs ( $C_{fc}$ ),  
948 which are related to the fuel consumed; operating costs ( $C_{op}$ ), which consist of the fuel cost and the battery  
949 replacement cost; user costs ( $C_{usr}$ ), which include the fuel cost and a fraction of the battery replacement costs  
950 (this is basically an operating cost-oriented definition, as it does not include the cost required to purchase the  
951 vehicle and the costs related to insurance/taxes); total costs ( $C_{tot}$ ), which are the sum of the production cost and  
952 the operating cost.

953 A sensitivity analysis has been carried out in order to verify the impact of the cost definition, of the objective  
954 function and of the training mission typology on the resulting optimal layout and its performance, in terms of  
955 CO<sub>2</sub> and pollutant emission reduction, as well as in terms of cost reduction. In addition, different market  
956 scenarios, which consider a fuel price increment (+50%), a longer battery life (+50%) and a battery cost  
957 decrement (-50%), have been explored individually in terms of optimal layout and the resulting performance.

958 The main findings of this study can be summarized as follows:

- 959 1. Vehicle architectures: The dual-mode vehicle equipped with the smallest engine D2 (i.e., DMV-D2)  
960 shows the best potential to reduce the total costs (an average 15.9% reduction) with limited penalties in  
961 terms of incremental OEM costs with respect to the conventional vehicle (139%), and a good  
962 performance in terms of CO<sub>2</sub> reduction (30%). The speed-coupling vehicle equipped with the D2 engine  
963 (i.e, SCV-D2) shows a higher CO<sub>2</sub> reduction potential (35.5%), but at the expense of a higher increment  
964 in the OEM costs (197.9%).
- 965 2. Sensitivity analysis on the powertrain cost definition: The total powertrain cost definition  $C_{tot}$  was  
966 selected as the best choice when defining the optimal layout of the hybrid vehicle, as it leads to the  
967 lowest incremental OEM costs per unit CO<sub>2</sub> emission reduction, per unit user cost reduction and per unit  
968 total powertrain cost reduction. However, fuel cost or user cost definitions could also be used to define  
969 the optimal layout if a more intense CO<sub>2</sub> emission reduction is necessary, regardless of the increment in  
970 the powertrain costs. If the  $C_{tot}$  definition is selected for layout optimization, the average powertrain  
971 cost reduction is about 12.4%, CO<sub>2</sub> emissions are reduced by 31.4%, and the OEM cost increase is  
972 123%. If the  $C_{oem}$  definition is used, the resulting HEV layouts provide similar results to those obtained  
973 with total cost approach. If  $C_{usr}$  or  $C_{fc}$  are minimized, the resulting HEV layout shows the best potential  
974 to reduce the CO<sub>2</sub> emissions (by as much as 35%), but at the expense of a higher battery usage and the  
975 related costs (the  $C_{tot}$  reduction is limited to 10-11%). An interesting indicator that was investigated is  
976 the ratio between the incremental  $C_{oem}$  and the achieved CO<sub>2</sub> emission reduction unit. It was found that  
977 the increased OEM cost, due to a reduction of 1g/km of CO<sub>2</sub> emissions, was estimated to be around \$44  
978 per vehicle, if the layout was selected using the OEM cost definition, while it was around \$55 per  
979 vehicle, if the layout was selected using the user cost definition.
- 980 3. Sensitivity analysis of the objective function: the objective function oriented toward fuel consumption  
981 and battery depletion resulted to be the most balanced choice to define the vehicle control strategy  
982 during the layout optimization process. If an NO<sub>x</sub>-oriented objective function is used, the layout results  
983 to be optimized for the extensive use of the electric power unit, in order to shift the engine operating  
984 point to a low NO<sub>x</sub> emission region. However, this leads to high battery depletion.

985 4. Analysis of the different market scenarios: in a scenario in which the fuel cost increases by 50% with  
986 respect to the nominal value adopted in this study, the layout optimization is in particular aimed at  
987 reducing CO2 emissions, even though more batteries would be required during the lifetime of the  
988 vehicle. However, this strategy has a drastic effect on the OEM cost increase, which rises to 182.8%  
989 (against a nominal value of 154.1%). The battery cost resulted to be the most significant factor in  
990 promoting the hybrid technology. In the scenario in which the battery cost is halved, the average OEM  
991 cost increment is in fact the lowest (120.6%), the average CO2 emission reduction is the highest (35.2%)  
992 and the average total cost reduction is the highest one (20.9%). The proposed DMV architecture was  
993 found to be the best choice to reduce the overall powertrain costs, for all the considered scenarios related  
994 to fuel price increase, battery life increase and battery cost decrease.

995 Finally, some topics and ideas for future investigations have emerged from this study and they will be  
996 investigated in detail in the near future. For example, the optimal vehicle design toolbox is intended to also be  
997 applied to complex plug-in and non-plug-in hybrid electric vehicles. Moreover, a new algorithm for an  
998 equivalent consumption minimization strategy (ECMS) that takes into account the battery life consumption is  
999 currently under investigation for DMVs. A comprehensive optimization tool, which is capable of identifying not  
1000 only the optimal control strategy of the hybrid powertrains over the mission, but also the optimal values of the  
1001 main engine parameters (i.e., EGR rate, start of injection), is currently being developed. This tool will  
1002 incorporate specifically developed low-throughput models that simulate the combustion and emission formation  
1003 processes in the engine.

## 1004 **Acknowledgements**

1005 General Motors PowerTrain Europe is gratefully acknowledged for the technical support.

1006 **References**

- 1007 [1] K. D. Huang, K. V. Quang, K.-T. Tseng, Study of the effect of contraction of cross-sectional area on flow  
1008 energy merger in hybrid pneumatic power system, *Applied Energy* 86 (10):2171–2182, 2009,  
1009 doi:10.1016/j.apenergy.2009.03.002.
- 1010 [2] M. Hannan, F. Azidin, A. Mohamed, Hybrid electric vehicles and their challenges: A review, *Renewable and*  
1011 *Sustainable Energy Reviews* 29:35–150, 2014, doi: 10.1016/j.rser.2013.08.097.
- 1012 [3] W. Liu, W. Hu, H. Lund, Z. Chen, Electric vehicles and large-scale integration of wind power—the case of  
1013 inner mongolia in china, *Applied Energy* 104:445–456, 2013, doi: 10.1016/j.apenergy.2012.11.003.
- 1014 [4] X. Wu, B. Cao, X. Li, J. Xu, X. Ren, Component sizing optimization of plug-in hybrid electric vehicles,  
1015 *Applied Energy* 88 (3):799–804, 2011, doi:10.1016/j.apenergy.2010.08.018.
- 1016 [5] K. Ç. Bayindir, M. A. Gözükcük, A. Teke, A comprehensive overview of hybrid electric vehicle:  
1017 Powertrain configurations, powertrain control techniques and electronic control units, *Energy Conversion and*  
1018 *Management* 52 (2):1305–1313, 2011, doi: 10.1016/j.enconman.2010.09.028.
- 1019 [6] L. Damiani, M. Repetto, A. P. Prato, Improvement of powertrain efficiency through energy breakdown  
1020 analysis, *Applied Energy* 121:252–263, 2014, doi: 10.1016/j.apenergy.2013.12.067.
- 1021 [7] S. Saxena, A. Phadke, A. Gopal, Understanding the fuel savings potential from deploying hybrid cars in  
1022 china, *Applied Energy* 113:1127–1133, 2014, doi: 10.1016/j.apenergy.2013.08.057.
- 1023 [8] S. Zhang, Y. Wu, H. Liu, R. Huang, L. Yang, Z. Li, L. Fu, J. Hao, Real-world fuel consumption and CO2  
1024 emissions of urban public buses in Beijing, *Applied Energy* 113:1645–1655, 2014, doi:  
1025 10.1016/j.apenergy.2013.09.017.
- 1026 [9] T. Hutchinson, S. Burgess, G. Herrmann, Current hybrid-electric powertrain architectures: Applying  
1027 empirical design data to life cycle assessment and whole-life cost analysis, *Applied Energy* 119: 314–329, 2014,  
1028 doi: 10.1016/j.apenergy.2014.01.009.
- 1029 [10] T. Kutrašnik, Impact of vehicle propulsion electrification on well-to-wheel CO2 emissions of a medium  
1030 duty truck, *Applied Energy* 108:236–247, 2013, doi: 10.1016/j.apenergy.2013.03.029.

- 1031 [11] B. M. Al-Alawi, T. H. Bradley, Analysis of corporate average fuel economy regulation compliance  
1032 scenarios inclusive of plug in hybrid vehicles, *Applied Energy* 113:1323–1337, 2014, doi:  
1033 10.1016/j.apenergy.2013.08.081.
- 1034 [12] R. T. Doucette, M. D. McCulloch, Modeling the prospects of plug-in hybrid electric vehicles to reduce CO<sub>2</sub>  
1035 emissions, *Applied Energy* 88 (7):2315–2323, 2011, doi: 10.1016/j.apenergy.2011.01.045.
- 1036 [13] X. Wu, J. Dong, Z. Lin, Cost analysis of plug-in hybrid electric vehicles using GPS-based longitudinal  
1037 travel data, *Energy Policy* 68 :206–217, 2014, doi: 10.1016/j.enpol.2013.12.054.
- 1038 [14] H. K. Fathy, J. Reyer, P. Y. Papalambros, A. Ulsov, et al., On the coupling between the plant and controller  
1039 optimization problems, in: *American Control Conference, 2001. Proceedings of the 2001, Vol. 3, IEEE, 2001,*  
1040 pp. 1864–1869, doi: 10.1109/ACC.2001.946008.
- 1041 [15] M. Jain, C. Desai, S. S. Williamson, Genetic algorithm based optimal powertrain component sizing and  
1042 control strategy design for a fuel cell hybrid electric bus, in: *Vehicle Power and Propulsion Conference, 2009.*  
1043 *VPPC'09. IEEE, IEEE, 2009,* pp. 980–985, doi: 10.1109/VPPC.2009.5289740.
- 1044 [16] M.-J. Kim, H. Peng, Power management and design optimization of fuel cell/battery hybrid vehicles,  
1045 *Journal of power sources* 165 (2): 819–832, 2007, doi: 10.1109/TCST.2003.815606.
- 1046 [17] Z. Yu, D. Zinger, A. Bose, An innovative optimal power allocation strategy for fuel cell, battery and  
1047 supercapacitor hybrid electric vehicle, *Journal of Power Sources* 196 (4) : 2351–2359, 2011, doi:  
1048 doi:10.1016/j.jpowsour.2010.09.057.
- 1049 [18] V. Paladini, T. Donato, A. De Risi, D. Laforgia, Super-capacitors fuel-cell hybrid electric vehicle  
1050 optimization and control strategy development, *Energy Conversion and Management* 48 (11) : 3001–3008, 2007,  
1051 doi: doi:10.1016/j.enconman.2007.07.014.
- 1052 [19] K.-B. Sheu, Simulation for the analysis of a hybrid electric scooter powertrain, *Applied energy* 85 (7):589–  
1053 606, 2008, doi: doi:10.1016/j.apenergy.2007.09.002.
- 1054 [20] S.-C. Tzeng, K. D. Huang, C.-C. Chen, Optimization of the dual energy-integration mechanism in a  
1055 parallel-type hybrid vehicle, *Applied Energy* 80 (3): 225–245, 2005, doi: doi:10.1016/j.apenergy.2004.04.010.

- 1056 [21] G. Paganelli, Y. Guezennec, G. Rizzoni, Optimizing control strategy for hybrid fuel cell vehicle, Tech. rep.,  
1057 SAE Technical Paper 2002-01-0102, 2002, doi:10.4271/2002-01-0102.
- 1058 [22] R. Bellman, R. E. Kalaba, Dynamic programming and modern control theory, Academic Press New York,  
1059 1965.
- 1060 [23] W. L. Winston, J. B. Goldberg, Operations research: applications and algorithms, Vol. 3, Duxbury press  
1061 Boston, 2004.
- 1062 [24] O. Sundström, L. Guzzella, A generic dynamic programming matlab function, in: Control  
1063 Applications,(CCA) & Intelligent Control,(ISIC), 2009 IEEE, IEEE, 2009, pp. 1625–1630, doi:  
1064 10.1109/CCA.2009.5281131.
- 1065 [25] Finesso, R., Spessa, E., & Venditti, M., Optimization of the Layout and Control Strategy for Parallel  
1066 Through-the-Road Hybrid Electric Vehicles, SAE Technical Paper 2014-01-1798, 2014, doi:10.4271/2014-01-  
1067 1798.
- 1068 [26] Finesso, R., Spessa, E., & Venditti, M., Layout design and energetic analysis of a complex diesel parallel  
1069 hybrid electric vehicle, Applied Energy, 134: 573-588, 2014, doi:10.1016/j.apenergy.2014.08.007.
- 1070 [27] MathWorks, MatLab - The Language Of Technical Computing,  
1071 <http://www.mathworks.com/products/matlab/>, [Online; accessed 04-May-2016] (2016).
- 1072 [28] Finesso, R., Spessa, E., & Venditti, M., An Unsupervised Machine-Learning Technique for the Definition  
1073 of a Rule-Based Control Strategy in a Complex HEV, SAE Int. J. Alt. Power. 5(2):2016, doi:10.4271/2016-01-  
1074 1243.
- 1075 [29] S. d'Ambrosio, R. Finesso, E. Spessa, Calculation of mass emissions, oxygen mass fraction and thermal  
1076 capacity of the inducted charge in SI and diesel engines from exhaust and intake gas analysis, Fuel 90 (1):152–  
1077 166, 2011, doi:10.1016/j.fuel.2010.08.025.
- 1078 [30] J. B. Heywood, Internal combustion engine fundamentals, Vol. 930, Mcgrawhill New York, 1988.
- 1079 [31] U. Technologies, <http://www.uqm.com>, [Online; accessed 04-May-2016] (2016).

1080 [32] Serrao, L., Onori, S., Sciarretta, A., Guezennec, Y., & Rizzoni, G. (2011, June). Optimal energy  
1081 management of hybrid electric vehicles including battery aging. In American Control Conference (ACC), 2011  
1082 (pp. 2125-2130). IEEE, 10.1109/ACC.2011.5991576.

1083 [33] Golbuff, S., Design Optimization of a Plug-In Hybrid Electric Vehicle, SAE Technical Paper 2007-01-  
1084 1545, 2007, doi:10.4271/2007-01-1545.

1085 [34] Fischer, R., Fraidl, G., Hubmann, C., Kapus, P., Kunvemann, R., Sifferlinger, B., & Beste, F, Range  
1086 Extender Module - Enabler for Electric Mobility, ATZ autotechnology, 9, 2009.

1087 [35] Catania, A. E., Finesso, R., & Spessa, E., Predictive zero-dimensional combustion model for DI diesel  
1088 engine feed-forward control. Energy Conversion and Management, 52(10): 3159-3175, 2011,  
1089 doi:10.1016/j.enconman.2011.05.003.

1090 [36] Morra, E. P., Spessa, E., & Venditti, M. (2012, May). Optimization of the operating strategy of a BAS  
1091 hybrid diesel powertrain on type-approval and real-world representative driving cycles. In ASME 2012 internal  
1092 combustion engine division spring technical conference (pp. 557-568). American Society of Mechanical  
1093 Engineers, doi: doi:10.1115/ICES2012-81093.

1094 [37] Morra, E., Spessa, E., Ciaravino, C., & Vassallo, A., Analysis of various operating strategies for a parallel-  
1095 hybrid diesel powertrain with a belt alternator starter, SAE Int. J. Alt. Power. 1(1):231-239, 2012,  
1096 doi:10.4271/2012-01-1008.

1097 [38] Catania, A., Finesso, R., Spessa, E., Catanese, A., & Landsmann, G., Combustion prediction by a low-  
1098 throughput model in modern diesel engines, SAE Int. J. Engines 4(1):2106-2123, 2011, doi:10.4271/2011-01-  
1099 1410.

1100 [39] Catania, A., Finesso, R., & Spessa, E., Real-time calculation of EGR rate and intake charge oxygen  
1101 concentration for misfire detection in diesel engines, SAE Technical Paper 2011-24-0149, 2011,  
1102 doi:10.4271/2011-24-0149.

1103 [40] Finesso, R., & Spessa, E., Real-Time Predictive Modeling of Combustion and NO<sub>x</sub> Formation in Diesel  
1104 Engines Under Transient Conditions (No. 2012-01-0899). SAE Technical Paper 2012-01-0899, 2012,  
1105 doi:10.4271/2012-01-0899.