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# Dry Friction Discontinuous Computational Algorithms

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**Abstract** —*The design of high position accuracy servo mechanisms (such as an aircraft primary command EHA), involves the deep knowledge of their behavior, markedly affected by the Coulomb friction. The proper evaluation of the friction forces and torques is usually necessary when an accurate simulation of the servomechanisms dynamic behavior is requested in order to perform a suitable design of the system itself. To the purpose, the authors consider a servomechanism consisting of a hydraulic motor element (translational or rotary) coupled with an electro-hydraulic servovalve as a controller; the dynamic behavior of these elements may be strongly dependent on the dry friction forces or torques acting on the moving parts, particularly of the motor element.*

**Index Terms**— Actuator, Algorithm, Coulomb, Friction.

## I. INTRODUCTION

The present work compares the abilities of different friction computational methods selected as the most common discontinuous ones, such as Sign function (usually called SIGN), hyper viscous, Karnopp [1], Quinn [2] and the friction model proposed by the authors in [3] and [4]. In fact, the Coulomb friction may greatly affect the behavior of high position accuracy servomechanisms, as the flight controls are. To perform a suitable design of the system, an adequate friction model must be employed, having the following abilities. The dry friction acting on a movable mechanical element must be generally considered as a force, opposing the motion, having a value depending on the speed. In the most of the applications however the relationship between friction force and speed can be represented by the following model (classical Coulomb friction):

- in standstill conditions the friction force can assume any value lower or equal in module to the so said static friction value, opposing the active force and depending on it;
- Otherwise the force module has a constant value equal to the so said dynamic friction value, opposing the motion.

This highly nonlinear relationship (discontinuous and undefined in null velocity conditions) gives rise to difficulty in numerical simulation of friction phenomena for the abovementioned purposes. The friction models can be mainly classified into two types: discontinuous and continuous. In discontinuous models, the friction force is discontinuous at zero velocity (i.e., in sticking regime) and acts to balance the other forces to maintain zero velocity, if possible. Continuous models consider small elastic displacement (presliding displacement) in the sticking regime and are particularly interesting in the study of specific problems around the null

velocity condition, having no further abilities in slipping conditions. Advantages of discontinuous models are their high performance to simplicity ratio and their wide application field in the classical applied mechanics. However, the conception of the related numerical algorithms is not so simple because their two formulations in conditions of zero and nonzero velocity are completely different; some of the discontinuous friction models most often used are the basic Coulomb (usually implemented by means of a Sign function), the hyper viscous, the Quinn and Karnopp models, which provide alternative tradeoffs amongst the desirable characteristics of a friction model. In order to overcome the shortcomings characterizing the abovementioned friction models, the authors devised an original numerical discontinuous friction algorithm, developed by the classical Coulomb model (as reported in [3] and [4]), requiring no specific skill by the user and able to describe the behavior of mechanical elements affected by friction, distinguishing between the four possible conditions as follows:

- Mechanical element initially stopped which must persist in standstill condition;
- Mechanical element initially stopped which must break away;
- Mechanical element initially moving which must persist in movement;
- Mechanical element initially moving which must stop.

This ability is important especially in order to point out some specific behaviors concerning the moving parts of whatever mechanical system characterized by dry friction, large displacement and speed, forward – backward movements and eventual standstill or stick-slip conditions. According to these considerations, the ability to select the correct friction force sign as a function of the actuation rate sense, to distinguish between the sticking condition (static) and the slipping (dynamic) one, to evaluate the eventual stop of the previously running mechanical element, to keep correctly in a standstill condition the previously still mechanical element or to evaluate the eventual break away of the previously still element itself must be considered as the most relevant merit. In aeronautical field, such problems are strictly inherent in servomechanism behavior analysis and so it is particularly interesting to employ these numerical methods in the simulation of their dynamics.

## II. AIMS OF WORK

Aims of the present work are the detailed analysis of the proposed friction computational algorithm structure and the

comparison between its abilities related to those of the most common discontinuous ones, such as Sign function (SIGN), hyper viscous, Quinn and Karnopp. To the purpose, the authors consider a generic electrohydraulic servomechanism consisting of a Power Control and Drive Unit (PCDU), mainly containing, besides a control computer, a hydraulic piston and an electrohydraulic servovalve as a controller; the dynamic behavior of these elements (particularly the piston) is strongly dependent on the dry friction forces acting on their moving parts, so a dynamic simulation program of the entire system has been prepared containing the friction model of the hydraulic piston, having the main responsibility in the system undesirable behaviors. The friction model is alternatively represented by the previously reported different computational method (SIGN, hyper viscous, Quinn, Karnopp and authors' one). Several simulations have been run to verify the different behaviors of the various computational algorithms; particularly, some proper analysis of the stop, standstill and breakaway conditions put in evidence the specific characteristics of each type of algorithm. The analysis is interesting both from the science and engineering point of view, because both the methodological and operative critical comparisons between the different models are performed, to put in evidence their related merits and shortcomings.

### III. EXAMINED FRICTION MODELS

In order to simulate the dynamic behavior of mechanical systems affected by friction forces, several algorithms have been conceived; a part of the abovementioned algorithms are strictly based upon the Coulomb friction model and characterized by a discontinuous arrangement. The classical Coulomb friction model can be generally represented by the following relationships, taking into account the difference between sticking and slipping conditions:

$$FF = \begin{cases} h & \text{if } v = 0 \wedge |h| \leq FS \\ FS \cdot \text{sgn}(h) & \text{if } v = 0 \wedge |h| > FS \\ FD \cdot \text{sgn}(v) & \text{if } v \neq 0 \end{cases} \quad (1)$$

Where  $FS$  and  $FD$  represent the friction force in sticking and slipping conditions respectively,  $h$  is the active force and  $v$  represents the relative slipping velocity. Difficulty in implementing the above mentioned friction model in numerical algorithm is rooted in the definition of  $FF$  vs.  $v$  relationship around  $v = 0$  and joined computational criteria; in fact, this function is discontinuous with respect to  $v$  in standstill condition and depends on  $h$  exclusively when  $v = 0$ . In order to overcome the computational troubles deriving from the function discontinuity a smart measure can be employed. The discontinuity is replaced by a linear relationship between  $FF$  and  $v$ , characterized by a properly high viscous coefficient and having an absolute value limited to the dynamic friction force  $FD$ . The so said hyper viscous friction algorithm can be described as follow:

$$FF = \begin{cases} F \cdot v / \varepsilon & \text{if } |v| \leq \varepsilon \\ F \cdot \text{sgn}(v) & \text{otherwise} \end{cases} \quad (2)$$

This model is characterized by a simple mathematical form, because it is continuous, but its behavior at  $v = 0$  is completely different from that of the Coulomb friction model. In fact, in this condition, the friction force, necessarily computed as null, is no able to balance the external force  $h$ . In order to remove the discontinuities while maintaining consistency with the Coulomb friction assumption, Quinn proposed the following model:

$$FF = \begin{cases} F \cdot \bar{v} / \varepsilon & \text{if } |\bar{v}| \leq \varepsilon \\ \text{sgn}(\bar{v}) \cdot F & \text{if } |\bar{v}| > \varepsilon \end{cases} \quad (3)$$

Where

$$\bar{v} = \begin{cases} v + \varepsilon \cdot h / F & \text{if } |h| \leq F \\ v + \text{sgn}(h) \cdot \varepsilon & \text{if } |h| > F \end{cases} \quad (4)$$

The Quinn friction model overcomes the shortcomings concerning the sticking and breakaway conditions of hyper viscous one, but, in case of  $h$  opposing the motion, the value of  $FF$  may have surprisingly the same sense of the velocity; this event, occurring when the absolute value of the diminishing velocity  $v$  is lower than  $\varepsilon$ , is clearly in contrast to the Coulomb friction model and physical laws. Karnopp overcomes the aforesaid problems by introducing a dead band, having half-width equal to  $\varepsilon$ , centered on  $v = 0$ . This method can be described as follows:

$$FF = \begin{cases} \text{MIN}(\text{MAX}(-FS, h), FS) & \text{if } |v| \leq \varepsilon \\ v = 0 & \text{if } \varepsilon > |v| > -\varepsilon \\ FD \cdot \text{sgn}(v) & \text{if } |v| > \varepsilon \end{cases} \quad (5)$$

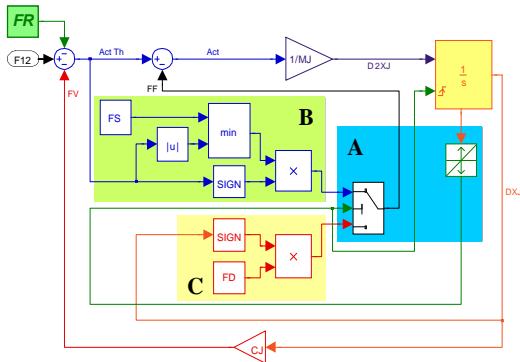
Where  $\varepsilon$  is a small velocity below which  $v$  is imposed equal to zero. Unfortunately, also this method is strongly dependent on the choice of the value  $\varepsilon$  and, moreover, the threshold velocity has no physical meaning. It must be noted that all the above mentioned algorithms are influenced by the value of  $\varepsilon$  and, unfortunately, its optimal choice<sup>1</sup> is not provided.

### IV. AUTHORS' FRICTION MODEL AND RELATED ALGORITHM

The computational algorithm, originally implemented in FORTRAN environment (as shown in Table I), have been also developed in Matlab-Simulink language (one of the most

<sup>1</sup> The proper value to give to the velocity bandwidth  $\varepsilon$ , occurring both in viscous models and Karnopp one, is the consequence of two opposite requirements: the value must be small enough to reproduce at the best the discontinuous function, but not so small to produce numerical instabilities related to sudden reversions of the friction force sign within the same computational step; the proper minimum value of  $\varepsilon$  is a function of the time-characteristics of the system and of the selected integration step. Nevertheless, an excessive value of  $\varepsilon$  fails in the simulation of the very low speed dynamic behavior.

commonly used languages in engineering applications) and it is shown in Fig. 1. Both these algorithms are conceived according to the aforesaid physical friction model and to a general layout not so different from the Karnopp's structure; in fact, both of them are divided in two alternative procedures related to the sticking or slipping condition. In sticking conditions, the friction force/torque is considered equal to the sum of the active forces/torques and opposing it, but its absolute value must be not greater than its limit represented by the static value of friction ( $FS$ ) as in statement 3 of the computational routine (Table I) and in block B of Simulink diagram shown in Fig. 1. The result is, through the statement 4, an acceleration value  $D2XJ$  proportional to the excess of  $Act\_Th$  with respect to  $FS$ , having the sense of  $Act\_Th$ . Therefore, according to the statements 3 and 4, the breakaway occurs (in  $Act\_Th$  sense) only if  $Act\_Th$  exceeds  $FS$  and the consequent value of velocity  $DXJ$  (statement 6) is no longer null, so defining a slipping condition at the input of the following computational step; otherwise the sticking condition persists.



**Fig 1: Representation of authors' Matlab- Simulink Friction force/torque algorithm**

The authors' Simulink algorithm implements the aforesaid breakaway detection by means of a switch block that, as a function of instantaneous value of  $DXJ$  (coming from the integrator state port), selects between sticking and slipping condition (by means of a hit crossing block) and, so, gives in output the proper value of static or dynamic friction force  $FF$  (block A in Fig. 1). In slipping conditions, the friction force/torque is the sum of a viscous and a constant term, opposing the motion; the viscous term is computed, by the coefficient  $CJ$ , within  $Act\_Th$  in statement 1, while the constant one is equal to the dynamic value of friction  $FD$ , according to the statement 2 (it must be noted that, in Simulink environment,  $FD$  is computed by means of the routine shown into the block C of Fig. 1). The result is, by the statement 4, an acceleration value  $D2XJ$  proportional to the difference between  $Act\_Th$  and  $FD$ , having the sense coming from the algebraic difference itself. By a numerical integration procedure (as in statement 6, where the simple Euler method is considered), the consequent value of velocity  $DXJ$ , characterizing the step output (considered as input of the following computational step) is computed from the step input value; the eventual velocity reversion, within the

considered computational step (opposite sense between input and output values), must be checked and, if so, the velocity must be imposed equal to zero at the output of the current and so at the input of the following step. In this way, at the input of the following computational step, the considered mechanical element is necessarily seen in a sticking condition; it seems to be a shortcoming of the algorithm but it is not so. In fact, this measure provides a simple but trouble free method to verify the correct condition (sticking or slipping) to select following a velocity reversion by introducing the computational process into the sticking condition algorithm: in fact, in this way, during the velocity reversion, the sticking condition is maintained if  $Act\_Th$  is lower than  $FS$  or converted into a slipping condition if  $Act\_Th$  is greater than it. So no specific procedure is necessary for the velocity reversion, having a very small computational error (due to the stop along half computational step, approximately) and no further algorithm burden.

## V. REFERENCE SERVOMECHANISM DESCRIPTION

The examined servomechanism is a typical electro hydraulic position servo control widely used both in primary and secondary aircraft flight controls.

It consists of the following three subsystems, indicated below:

- A controller subsystem made of a control electronics and a servo amplifier, typically implementing a PID control law (the present work refers to a pure proportional control law)
- An electrohydraulic two stage servovalve
- A piston (symmetrical double acting linear cylinder affected by Coulomb friction), provided by a position transducer, closing the control loop.

The description of the servomechanism employed in the present work and its mathematical model are reported in [4]. The aforesaid servomechanism belongs to the fly-by-wire paradigm: the pilot's command depends upon transducers that express the pilot wishes by an electric or a digital reference signal; this signal is continuously compared via a feedback loop with the actual position of the control surface generating the instantaneous position error as input to the control law. So, the error is processed and transformed into an electric current operating the electro hydraulic servo valve. The servo valve drives an actuator that moves the control surface continuously pursuing, by a proper control law, the reduction of the error between pilot's commanded position and flight surface actual position. The servo valve is a high performance two-stage valve: the corresponding model represents the first stage having a second order dynamics and the second stage as a first order dynamics. The ends of travel of first and second stage are computed. The model of the second stage fluid dynamics takes into account the effects of differential pressure saturations, leakage and variable supply pressure. The hydraulic linear actuator considered in the present paper is double acting symmetrical one: its model includes inertia,

Coulomb and viscous friction and leakage effects through the piston seals developing a not working flow.

## VI. ANALYTICAL MODEL OF THE SERVOACTUATOR

The position error ( $Err$ ), coming from the comparison of the instantaneous value of commanded position ( $Com$ ) with the actual one ( $XJ$ ), is processed by means of a PID logic giving the suitable current input ( $Cor$ ) acting on the servovalve first stage torque generator; the aforesaid engine torque (expressed as a function of  $Cor$  through the torque gain  $GM$ ), reduced by the feedback effect due to the second stage position ( $XS$ ), acts on the first stage second order dynamic model giving the corresponding flapper position ( $XF$ ) (limited by double translational hard stops). The above mentioned flapper position causes a consequent spool velocity and, time-integrating, the displacement  $XS$  (limited by double translational hard stops  $\pm XSM$ ). From  $XS$ , the differential pressure  $P12$  (pressure gain  $GPS$  taking into account the saturation effects) effectively acting on the piston is obtained by the flows through the hydraulic motors  $QJ$  (valve flow gain  $GQS$ ). The differential pressure  $P12$ , through the piston active area ( $AJ$ ) and the equivalent total inertia of the surface-motor assembly ( $MJ$ ), taking into account the total load ( $FR$ ), the viscous (coefficient  $CJ$ ) and dry friction force ( $FF$ ), gives the assembly acceleration ( $D2XJ$ ); its integration gives the velocity ( $DXJ$ ), affecting the viscous and dry frictions and the linear actuator working flow  $QJ$  that, summed to the leakage one, gives the above mentioned pressure losses through the valve passageways. The velocity integration gives the actual jack position ( $XJ$ ) which returns as a feedback on the command comparison element.

## VII. RESULTS ANALYSIS

Some simulations have been run to put in evidence merits and shortcomings of the considered algorithms. The examples suited to the purpose are a run having no load and a small step position command (case 1) and a no load actuation following a very slow ramp position input (case 2). In both cases fluid compressibility, supply pressure variations and leakage are neglected.

**Case 1:** the step command has a null initial position and final value 0.001 m. As the step command is small, the displacement  $XS$  of the servovalve spool from its null position (related to the feedback spring action) is lower than its end of travel. The spool displacement produces a piston actuation rate  $DXJ$  almost proportional to  $XS$  itself (only slightly delayed), having the piston low inertia and no load  $FR$ . As a consequence of the reduction of the position error  $Err$ , the control system progressively bring back the spool towards its null position and the piston reduces its actuation rate till to a standstill condition, following some damped oscillations; when the system stops, the negative position error produces a spool back displacement but the Coulomb friction is able to keep it stopped. The above described actual behavior of the system is, in different ways, reproduced by the following

models. Particularly, in Fig. 2, no dry friction is considered, so no final system stop can occur. In Fig. 3, the SIGN friction model is unable to produce the complete stop condition (upper detail), so a particular type of velocity oscillation (due to periodic reversions of  $FF$ ) occurs (lower detail), having a not null mean value, so incorrectly producing a slow position error decrease to the commanded position. In Fig. 4, the hyper viscous friction model shows, in some way, a similar problem (detail), without any velocity oscillation, if a proper value of  $\epsilon$  has been selected; the position error decrease is slightly quicker than in SIGN case. In Fig. 5, the Quinn friction model overcomes the aforesaid troubles (detail), been able to lead the mechanical element to an asymptotical (and so incomplete) stop. The general arrangement of the previous algorithms is not conceived to consider a static value of  $FF$  greater than the dynamic one, as the FF time history shows; to the purpose, further improvements (Stribeck, etc) are necessary, though possible. In Fig. 6, the Karnopp friction model shows the capability of completely stopping the piston (upper detail) when  $h$  is not greater than  $FD$  and preventing the breakaway when  $h$  is not greater than  $FS$ , so selecting the proper static or dynamic condition; nevertheless, the breakaway is delayed (lower detail and time history of  $FF$ ) whit respect to the time in which  $h$  exceeds  $FS$ , owing to the velocity band. All these troubles are completely overcome by the authors' model (Fig. 7), which, in addition, lets the operator free from any type of velocity bandwidth selection, evaluation of results reliability and so on; the behavior of the system, according to Fig. 7, is quite as expected.

**Case 2:** the ramp command has a null initial position and slope value equal to 0.25 mm/s.

The response of the piston does not reproduce the input ramp but, following an initial time delay (resolution), it develops a step sequence divided by a time interval depending on the slope of the command ramp and the characteristics of the system (in particular friction, viscous damping and position stiffness). This stick-slip phenomenon is a direct consequence of the dry friction acting on the piston and, particularly, of the greater value of the friction forces in static than in dynamic conditions. In fact, when the system stops, the friction (passive) forces overcome the growing active ones, preventing the movement till to the breakaway. A brief and quick movement follows, so reducing the error and stopping the system again. The considered models reproduce in different ways the above described actual behavior of the servomechanism as follows. The SIGN model has no chance in this type of simulation, as the hyper viscous (Fig. 8(a)), been, further, incapable of taking correctly into account the breakaway event and of evaluating the "resolution" of the servomechanism. The Quinn model (Fig. 8(b)) is slightly more efficient in the breakaway evaluation, but as no chance in the tick-slip estimation as the two previous model, been unable to distinguish between static and dynamic conditions.

The stick-slip phenomenon is, in general, well reproduced both by Karnopp (Fig. 9(a)) and authors' (Fig. 9(b)) models; nevertheless, in the Karnopp model, as a consequence of the velocity band, the breakaway is delayed after the time in

which  $h$  overcomes  $FS$  and the computed stop precedes the natural event (too small velocities are set equal to zero).

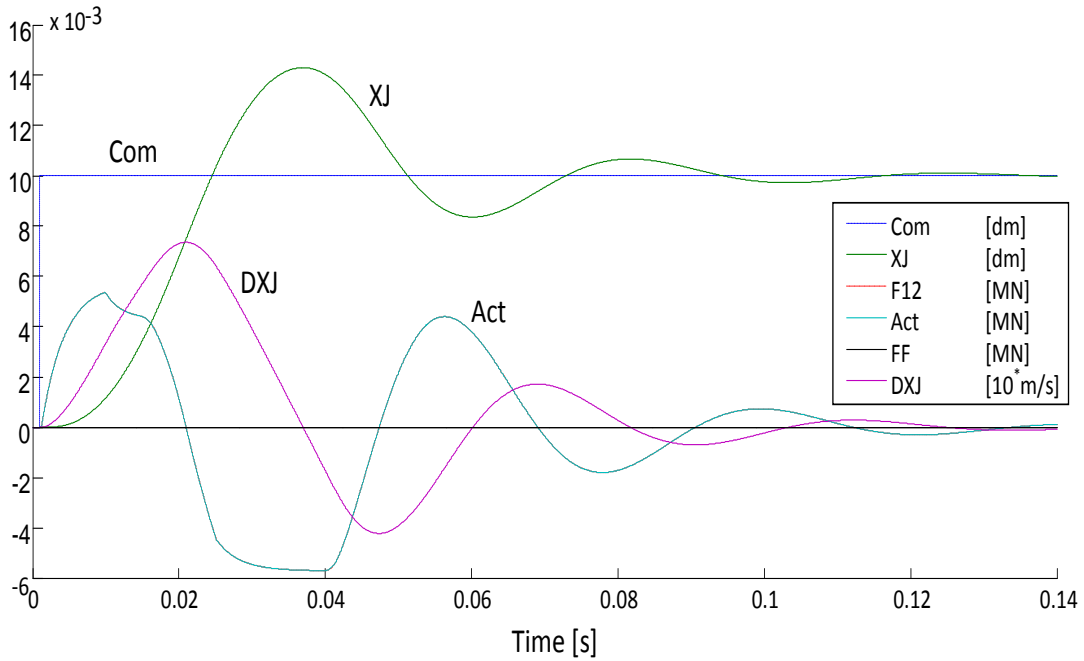


Fig 2: Step Command – No Friction Model

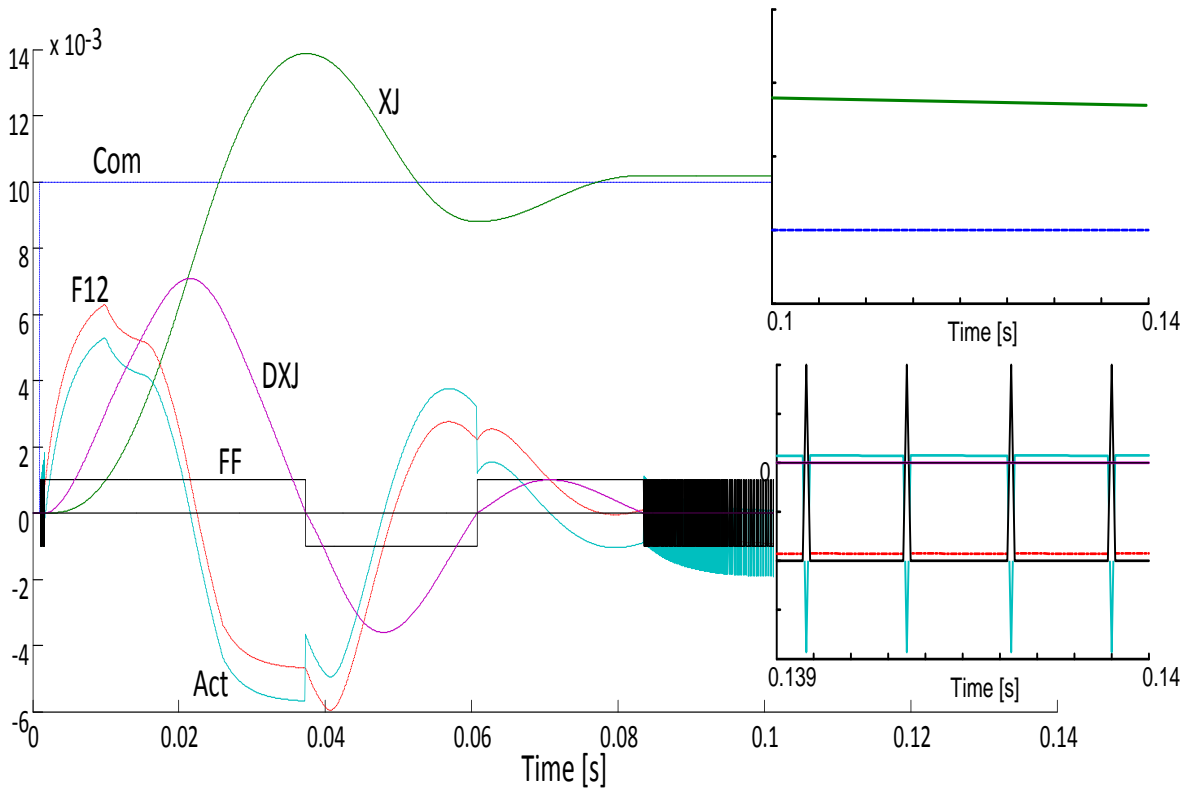


Fig 3: Step Command – SIGN Friction Model

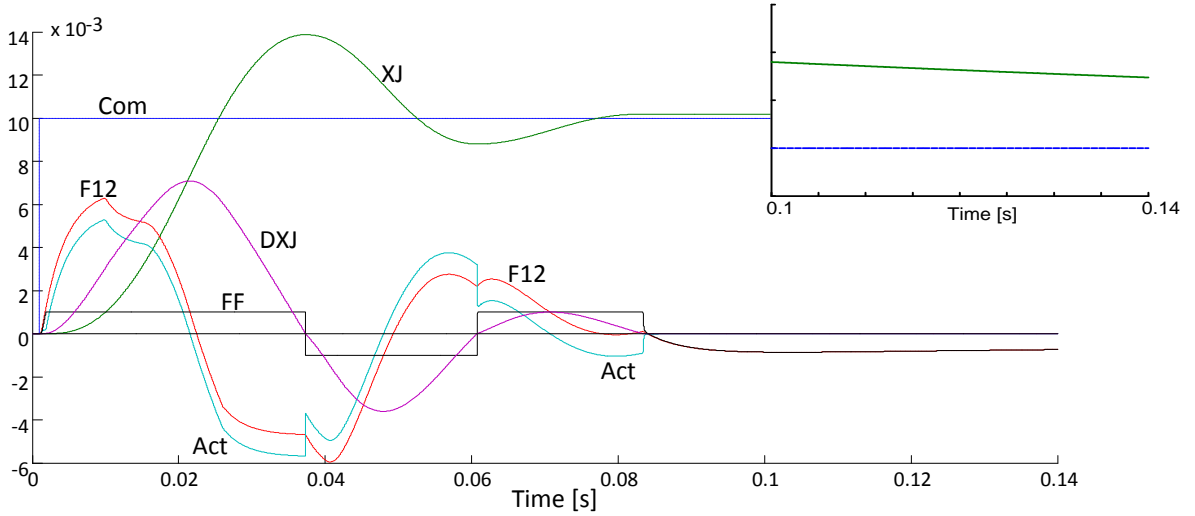


Fig 4: Step Command – Hyperviscous Friction Model

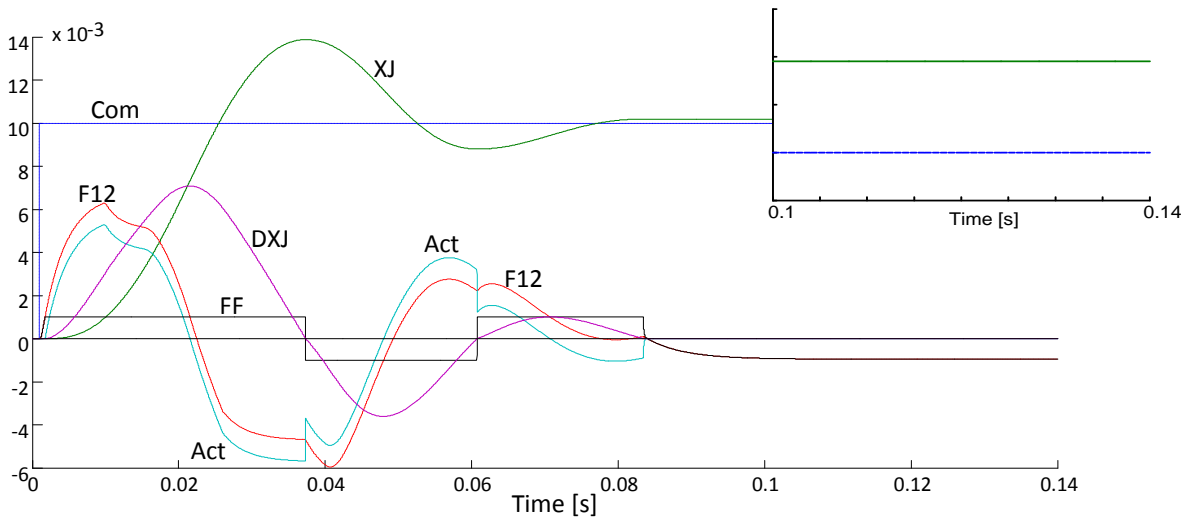


Fig 5: Step Command – Quinn Friction Model

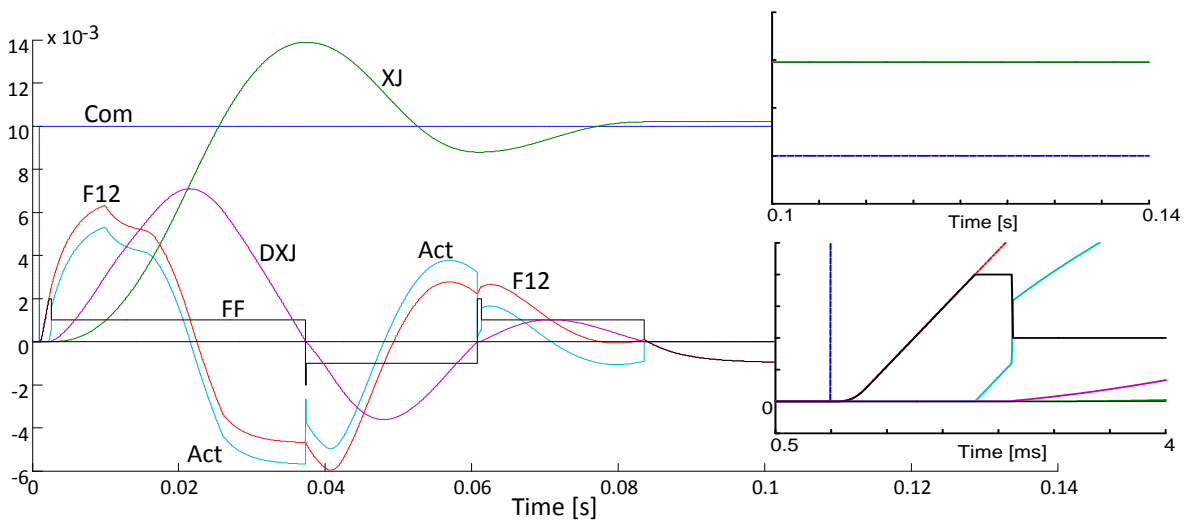


Fig 6: Step Command – Karnopp Friction Model

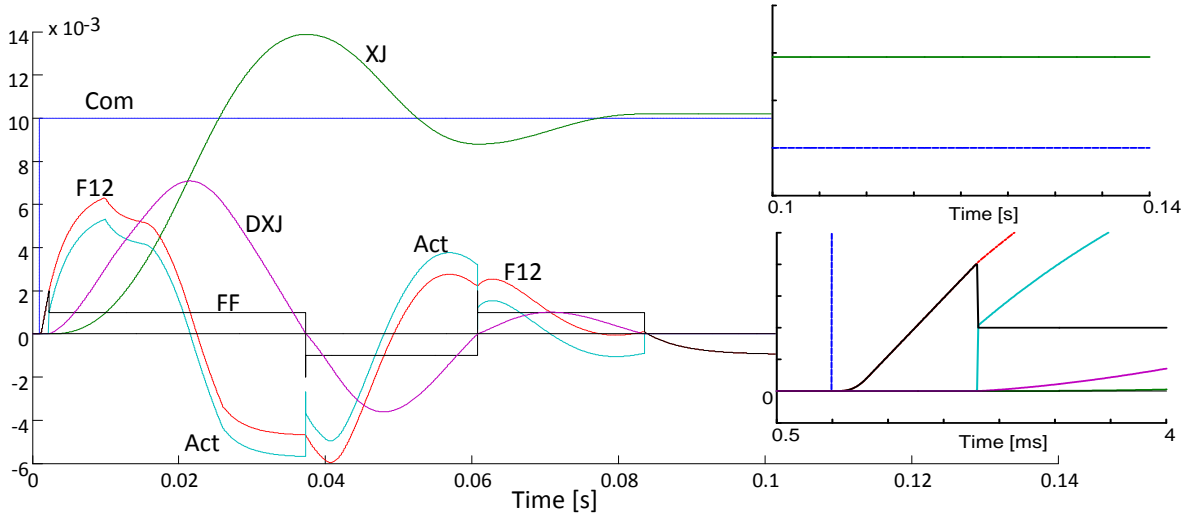


Fig 7: Step Command – Authors' Friction Model

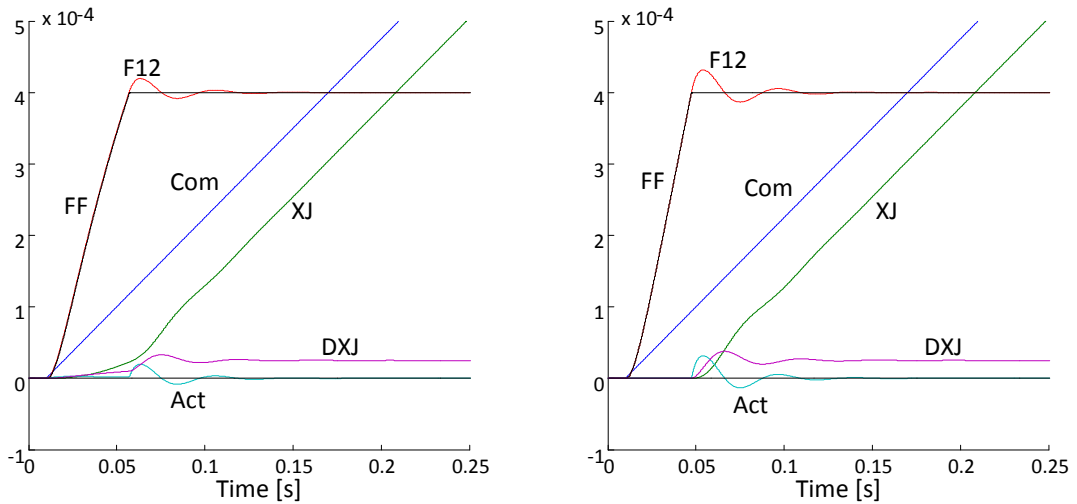


Fig 8: Ramp Command – Hyperviscous (a) and Quinn (b) Friction Models

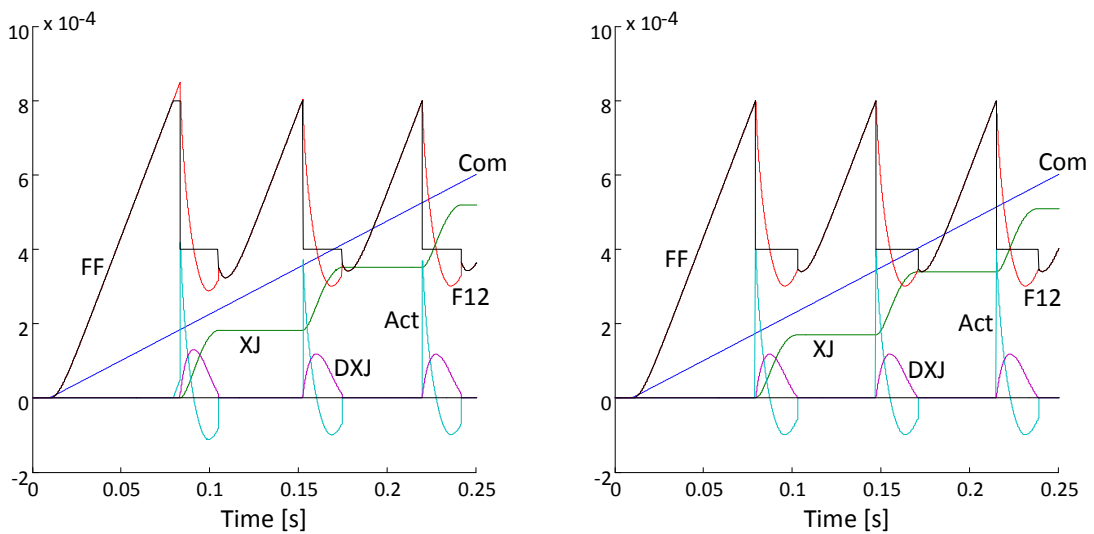


Fig 9: Ramp Command – Karnopp (a) and Authors' (b) Friction Model

### VIII. CONCLUSION

According to these considerations, the ability to select the correct friction force sign as a function of the actuation rate sense, to distinguish between the sticking condition (static) and the slipping (dynamic) one, to evaluate the eventual stop of the previously running mechanical element, to keep correctly in a standstill condition the previously standstill mechanical element or to evaluate the eventual break away of the previously standstill element itself are fundamental characteristics. The authors' algorithm has all these abilities without any problem in low velocity conditions, concerning possible numerical troubles (SIGN in stopped conditions, hyper viscous, Quinn, Karnopp having too small or too large value of bandwidth, delay breakaway and early stop in Karnopp). In aeronautical field, the user friendly authors' method is particularly suitable for the real time monitoring proposes, particularly in friction compensation and prognostics.

**Table I: FORTRAN Listing of the Authors' Coulomb Friction Algorithm**

N°	Statement
1	Act_Th = F12-FR-FV
2	FF = SIGN(FD,DXJ)
3	IF(DXJ.EQ.0.) FF = MIN(MAX(-FS,Act_Th),FS)
4	D2XJ = (Act_Th-FF)/MJ
5	Old = DXJ
6	DXJ = DXJ+D2XJ*DT
7	IF (Old-DXJ.LT.0) DXJ = 0

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### LIST OF SYMBOLS

<i>Act_Th</i>	sum of active forces	[N]
<i>AJ</i>	piston active area	[m <sup>2</sup> ]
<i>CJ</i>	rod dimensional viscous coefficient	[N·s/m]
<i>Com</i>	command signal	[m]
<i>Cor</i>	SV piloting current	[mA]
<i>Err</i>	position error	[m]
<i>D2XJ</i>	acceleration of the piston rod	[m/s <sup>2</sup> ]
<i>DXJ</i>	velocity of the piston rod	[m/s]
<i>F12</i>	hydraulic force acting on piston rod	[N]
<i>FR</i>	external load acting on piston rod	[N]
<i>FV</i>	viscous force acting on piston rod	[N]
<i>GPS</i>	pressure gain of the SV 2° stage	[Pa/m]
<i>GQS</i>	flow gain of the SV 2° stage	[m <sup>2</sup> /s]
<i>h</i> =	<i>Act_Th</i>	[N]
<i>P12</i>	differential pressure acting on piston areas	[Pa]
<i>QJ</i>	working flow	[m <sup>3</sup> /s]
<i>XF</i>	SV 1° stage displacement	[m]
<i>XS</i>	SV 2° stage displacement	[m]
<i>XSM</i>	hard stop position of SV 2° stage	[m]
<i>XJ</i>	real position of the flight surface	[m]

### AUTHOR BIOGRAPHY



**Lorenzo Borello** received the M.Sc. from the Politecnico di Torino in 1973. He is a retired full professor and continues to cooperate with other researchers of the Department of Mechanics and Aerospace Engineering. His research activity is mainly focused on aeronautical systems engineering and, in particular, is dedicated to design, analysis and numerical simulation of on board systems, study of secondary flight control system and conception of related monitoring strategies and developing diagnostic algorithms for aerospace servomechanism and flight controls



**Matteo D. L. Dalla Vedova** received the M.Sc. and the Ph.D. from the Politecnico di Torino in 2003 and 2007, respectively. He is currently assistant researcher at the Department of Mechanics and Aerospace Engineering. His research activity is mainly focused on the aeronautical systems engineering and, in particular, is dedicated to design, analysis and numerical simulation of on board systems and developing of prognostic algorithms for flight control systems and aerospace servomechanism.