Green’s function based simulation of trap-induced device variability

Original

Availability:
This version is available at: 11583/2497863 since:

Publisher:
Associazione gruppo italiano di elettronica

Published
DOI:

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Green’s function based simulation of trap–induced device variability

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OUTLINE

- MOS Variability
  - Random Telegraph Noise (single trap)
    - also in conjunction with Random Doping Fluctuation (RDF)
- Green’s function vs. incremental approach
- Case study
  - 32 nm MOS for FLASH applications
  - Varying trap position
- Green’s function approach Validation
  - static case
- Variability analysis
Device scaling

Moore’s law

- **RTN** (Random Telegraph Noise)
- **RDF** (Random Dopant Fluctuation)
Variability: Random Telegraph Noise

Capture/Emission of single electrons by oxide/interface traps

Due to reduced device dimensions, fluctuations in the device terminal properties become important
Single Trap Analysis

- Worst case difference of the drain current with full-empty trap
How to evaluate Single Trap Effect?

- **Incremental**
  - Simulations at the possible traps positions
  - Time consuming
  - High computing resources

\[
\Delta I_{D,inc}(x) = I_{D,full}(x) - I_{D,empty}(x)
\]
How to evaluate Single Trap Effect?

- **Green’s function**
  - Well established tool for variability analysis e.g. RDF Synopsis model
  - One simulation to evaluate the Green’s function
  - Single trap effect amounts to a small variation of charge → linear response through Poisson equation Green’s function

**Evaluate Green’s function**
(computation time ~ SS analysis at 0 f.)

Convolution integral for single trap reduces to 1 product

\[ \Delta I_{D,ifm}(x) = q_{trap} \times G_\phi(x) \]
Simulation setup for RTN

- Advanced MOS 32nm [1]
  - European MODERN Project
  - Bando Alta Formazione – Regione Piemonte

- Traps positions
  - Si/SiO₂ interface
  - Si channel
  - SiO₂
- No traps dynamics

Figure 1: 2D cross-section of the 32 nm MOSFET device obtained by eliminating the floating gate from the template non-volatile memory device used in MODERN
Model Validation: RTN

Figure 2: Comparison between the incremental (symbols) and Green’s function (line) estimation of (minus) the relative drain current variation $\Delta I_D/I_D$. Trap placed at the interface between SiO$_2$ and Si.

Threshold voltage variability found from drain current $1 \times 10^{-7}$ A/mm exploiting Y21 SS parameter at zero freq.

Figure 3: Comparison between the incremental (symbols) and Green’s function (line) estimation of (minus) the relative drain current variation $\Delta I_D/I_D$. Trap placed near the interface at the SiO$_2$ side.
Randomize traps position at Si–SiO₂ interface
  ◦ Uniform distribution
  ◦ Evaluate Green’s function at the interface
Device fabricated in large numbers

Differences in the number and exact placement of dopant atoms

Induced fluctuations (noise-like) at the device terminal

Figure 4: Synopsis NMOS structure with (left) continuum doping and (right) randomized doping profile
Green’s functions statistical RTN + RDF analysis

- Ongoing work
  - Green’s function statistical RTN
  - Linearity Uncorrelated

- Synopsis demonstrated statistical RDF
Variability analysis: RTN

- Extraction of the slope $\lambda$ [mV/dec] of the statistical distribution of the single trap RTN (1000 random position on Si/SiO2 interface)

Figure 5 Statistical distribution of the RTN on the threshold voltage
Variability analysis: RTN + RDF

- Dependence of $\lambda$ [mV/dec] on Gate length considering both the RTN and RDF

Figure 6 Statistical distribution of the RTN on the threshold voltage
Further work

- Validation of the Green’s function approach on a MOS 3D template
- Study of other 3D structures
Thanks for the attention

Riccardo Tisseur