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Original

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(Article begins on next page)

Measurement of the LOFAR-HBA beam patterns using an Unmanned Aerial Vehicle in the near-field

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Abstract. An Unmanned Aerial Vehicle (UAV) is exploited to characterize in-situ the High Band Antennas (HBAs) of the LOw Frequency ARray (LOFAR) CS302 station located in Exloo, The Netherlands. The size of an HBA array is about 30 m. The Fraunhofer distance (a few kms) is not reachable in the frequency band (120 - 240 MHz) within the flight regulation limits. Therefore, far-field patterns cannot be directly measured. The UAV, equipped with an RF synthesizer and a dipole antenna, flies in the near-field region of the considered array. Measurement of three different frequencies (124, 150, 180 MHz) is efficiently made during the same UAV flight. The near-field focusing method is exploited to validate the far-field pattern of the array under test within an angular range around the beam axis. Such a technique avoids both the time consuming $\lambda/2$ sampling of the aperture field and the further application of computationally heavy near-field to far-field transformations. The array beam is well reconstructed in the main lobe and first sidelobes within a 2D scan plane sampled with a radial raster. A further post-processing technique is proposed and validated on a subarray of HBAs. It suggests efficient ways for the future characterization of regular aperture arrays for SKA-Mid Phase 2.

Keywords: antenna measurements, unmanned aerial vehicle, near-field focusing, VHF band, large arrays, hybrid beamforming.

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1 Introduction

The LOw Frequency ARray (LOFAR) [1] is a radio telescope composed of 52 stations located in Europe. Each station is composed of two subarrays, one with Low-Band Antennas (LBAs) and one with High-Band Antennas (HBAs). Their operating frequency range is 10 - 90 MHz and 120 - 240 MHz, respectively. LBAs are arranged in a random configuration whereas HBAs are placed in a regular lattice.

LOFAR is a pathfinder for the international Square Kilometre Array (SKA). The SKA will become the biggest and most sensitive radio telescope in the world. Aperture arrays are envisioned for both

38 SKA1-Low (50 - 350MHz, random configuration) [2], [3] and possibly SKA1-Mid Phase 2 (400
39 MHz – 1.45 GHz, regular configuration) [4], [5], [6]. Dishes will be adopted for higher frequencies
40 up to 14 GHz.

41 All these powerful radio telescopes need to be validated and accurately calibrated. Of course,
42 testing these large arrays is not an easy task due to their large size and the low operating
43 frequencies. A few approaches have been proposed exploiting measured data in far or quasi-far
44 field condition. For example, a holographic technique has been applied to the Engineering
45 Development Array 2 of SKA1-LOW [7] and LOFAR [8] to retrieve aperture fields. Other tests
46 on LOFAR have been performed using astronomical calibration sources [9] and RF sources
47 mounted on cranes [10].

48 More recently, thanks to the technological development of Unmanned Aerial Vehicles (UAVs),
49 flying test sources have been developed to test aperture arrays even at element level [11] - [16]
50 with a high signal-to-noise ratio and a huge scan flexibility. Due to the large electrical size of the
51 aperture arrays, the Fraunhofer distance cannot always be reached. Therefore, validation of
52 LOFAR LBA array has been performed comparing measurement and simulation in the near field
53 [17], [18]. All previous papers featured sparse arrays with particular emphasis on the random
54 configuration [19]. In this work, the UAV-based measurement strategy is extended to the LOFAR
55 HBA (Fig. 1) which is a large regular array. Near field focusing [20], [21] is adopted and its
56 validity is assessed by comparison to the far-field simulated data (Section 2). This procedure has
57 been applied on a two-dimensional scan path to provide a more complete characterization (Section
58 3). A first attempt to develop a **far-field reconstruction** strategy (to overcome the artifacts of the
59 near-field focusing) and the corresponding definition of efficient **near-field** scan strategies for
60 regular arrays such as the aperture arrays for SKA-Mid Phase 2 is presented in Section 4.

61 To summarize, the novelty aspects of this paper are:

62 1) The verification of all tiles within a single flight over a LOFAR-HBA substation;

63 2) The application of near-field focusing to an array of tiles pointed in the same far-field direction

64 to provide an end-to-end verification of the system from the antennas to the digitized data;

65 3) The usage of radial raster scans to represent the beam pattern in the u - v plane with a limited set

66 of linear scans, which is an efficient choice in view of the limited UAV flight duration compared

67 to cartesian rasters [11];

68 4) The definition of a **far-field reconstruction strategy to partially overcome** the artifacts of the

69 near-field focusing and its validation on a subarray of the HBA substation.



70

71 **Fig. 1.** The UAV after take-off is reaching the first waypoint to perform the required scan path over a LOFAR HBA

72 array of the CS302 station. The array size is about 30 m.

73

74 *1.1 UAV-mounted test source and the HBA*

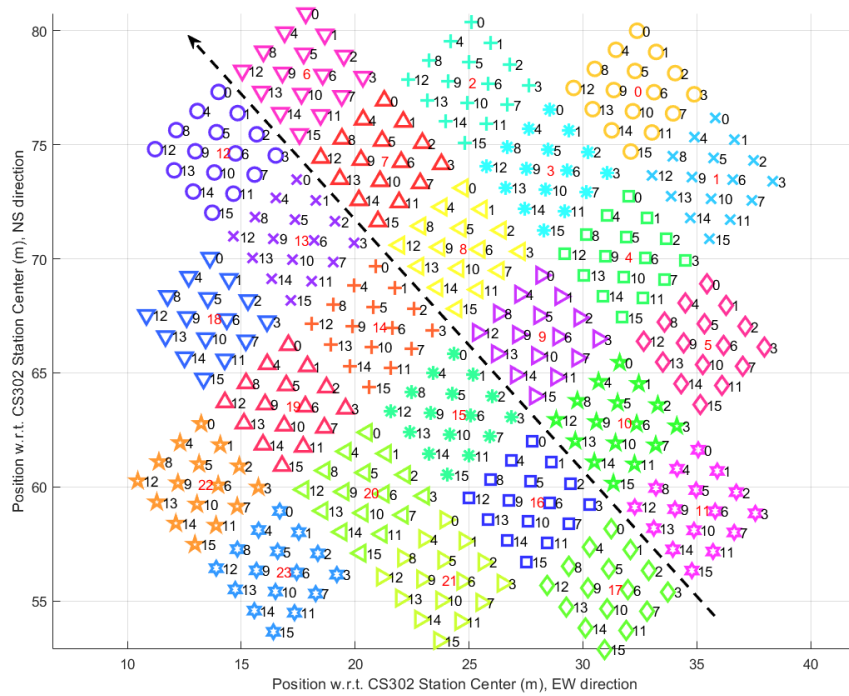
75 The UAV is visible in Fig. 1. It is equipped with a differential Global Navigation Satellite System

76 (GNSS) receiver for accurate positioning within a few centimeters, a dipole antenna and a RF

77 synthesizer [13]. Three higher-order harmonics of the RF synthesizer (i.e., it was operating as a
78 comb generator) have been used during the same flight. In this way, three different frequencies
79 (i.e., 124, 150 and 180 MHz) have been measured simultaneously. This procedure is applicable
80 when the receiver acquisition system can simultaneously record many frequency channels to
81 drastically reduce the flight time of the UAV.

82 Fig.1 also shows the Eastern HBA array of the CS302 LOFAR station located in Exloo. The
83 detailed geometry of this LOFAR HBA subarray is shown in Fig. 2. It is composed of 24 square
84 tiles (red numbers from 0 to 23) with a size of about 5 by 5 m². Each tile is composed of a regular
85 distribution of 4 by 4 dual-polarized elements i.e. thin crossed-bowtie dipoles suspended over a
86 ground plane by means of a polystyrene support structure. The dipole length is about 0.7 m. Within
87 each tile, the element spacing is 1.25 m [1]. The distance between tile centers is 5.15 m, therefore,
88 the spacing between elements of adjacent tiles is slightly larger (1.4 m) than within the tile.
89 Nevertheless, the overall distribution can be considered as very close to a uniform regular array.
90 Through the analog beam forming, each tile can be pointed within a field of view of 60 degrees
91 around zenith. Furthermore, signals from all tiles can be summed together by digital beam forming.

92



93
 94 **Fig. 2** Element positions in the LOFAR HBA subarray. Red and black numbers refer to tile number (0-23) and
 95 element number (0-15) inside the single tile, respectively. The black dashed curve shows an example of a UAV path
 96 (its projection to the ground) oriented along the North-West direction.

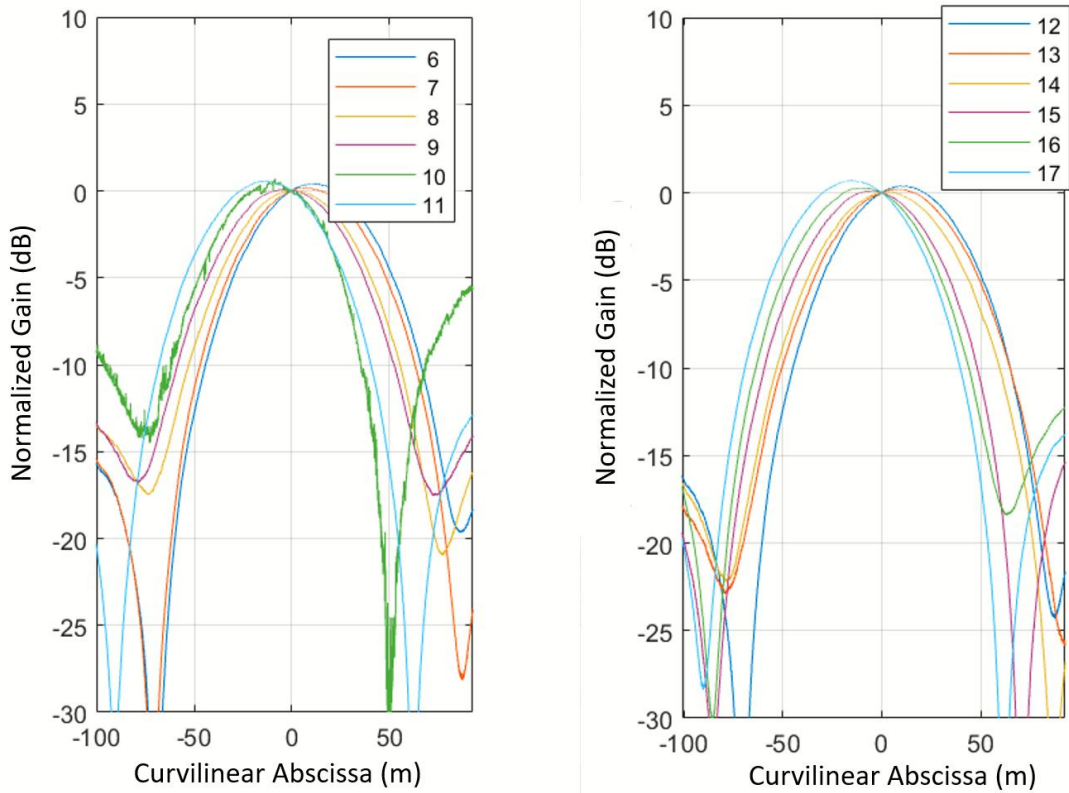
97
 98 The two element polarizations are oriented along the North-West and North-East directions. For
 99 the considered CS302 station, the orientation of the regular array distribution is 48° from North
 100 (see Fig. 2). Hence, there is a 3° rotation between element polarization directions and array lattice
 101 principal directions. Nevertheless, the labels “North-West” and “North-East” will be still adopted
 102 in this paper for both polarization and array principal (periodicity) directions for the sake of
 103 simplicity.

104

105 2 Beam patterns using near-field focusing

106 Several flights with linear trajectories and constant height have been performed. A sketch of a
107 UAV path projected to the ground and oriented North-West is shown in Fig. 2 with the black-
108 dashed line. This section presents the results obtained for a flight where both the UAV speed vector
109 and the onboard dipole are oriented North-West. This corresponds to an E-plane scan of the array
110 elements oriented North-West. **The UAV flight duration to perform this single linear path was**
111 **approximately 1 minute (flight speed was about 3 m/s) whereas 2-3 minutes are necessary for take-**
112 **off and landing.** The flight height has been maintained at 140 m due to regulation limitations. This
113 already satisfies the far-field condition for each tile (Fraunhofer distance is 60 m at 180 MHz) but
114 is not enough for the full array (about 1.1 km at 180 MHz). This fact is confirmed in Fig. 3, where
115 the measured tile beams (E-plane, 124 MHz) are shown for the tiles closest to the projection of the
116 UAV path (dashed black line in Fig. 2), i.e., tiles 6-11 and 12-17. The effect of UAV pattern and
117 path loss has been removed as in [22]. All beams are reported with respect to the curvilinear
118 abscissa on the UAV path. The origin of the curvilinear abscissa is set where the UAV path
119 projection is closest to the center of the HBA array. The analog beam formers were programmed
120 to point the tile beams at zenith. However, because of the low altitude of the UAV, the maxima of
121 the tile beams occur at different values of the curvilinear abscissa. In particular, the maxima of
122 tiles 11 and 17 occur at about -13 m, whereas the maxima of tiles 6 and 12 occur at +13m. This is
123 consistent with the distance between tile centers of about 26 m. The successful comparison with
124 simulations at tile level was already reported in [23]. In this work, the tile beams are instead used
125 to estimate the full array pattern by means of a near-field focusing method [20]. However, it
126 should be mentioned that, differently from [17], the presence of analog beam-formers at tile level
127 prevents the application of the required parabolic phase shifts across the array aperture i.e., to each

128 array element. Such near-field focusing can only be applied on the tile signals. In other words, the
129 tile beams are pointed to zenith (far-field) whereas the array of tiles will be focused in near-field.
130 All the tile beams in Fig. 3 are normalized in magnitude and phase at the origin of the curvilinear
131 abscissa to produce the near-field focusing for the array of tiles. The parabolic phase shifts for the
132 various tiles are automatically produced by the different electrical distances with respect to the
133 UAV-mounted source placed in the near-field.
134



135
136 **Fig. 3** Normalized E-plane radiation pattern for tiles 6-11 (left) and 12-17 (right) at 124 MHz.

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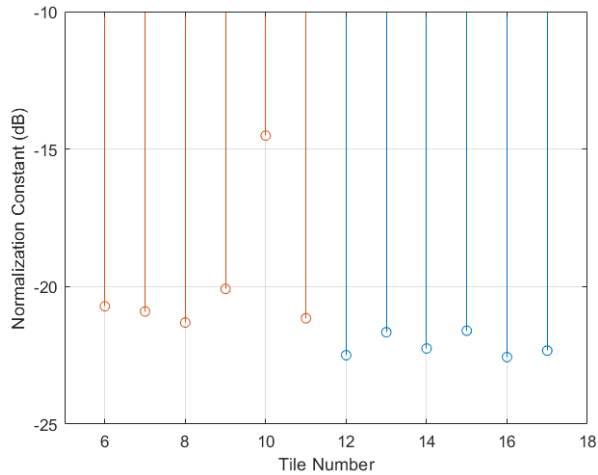
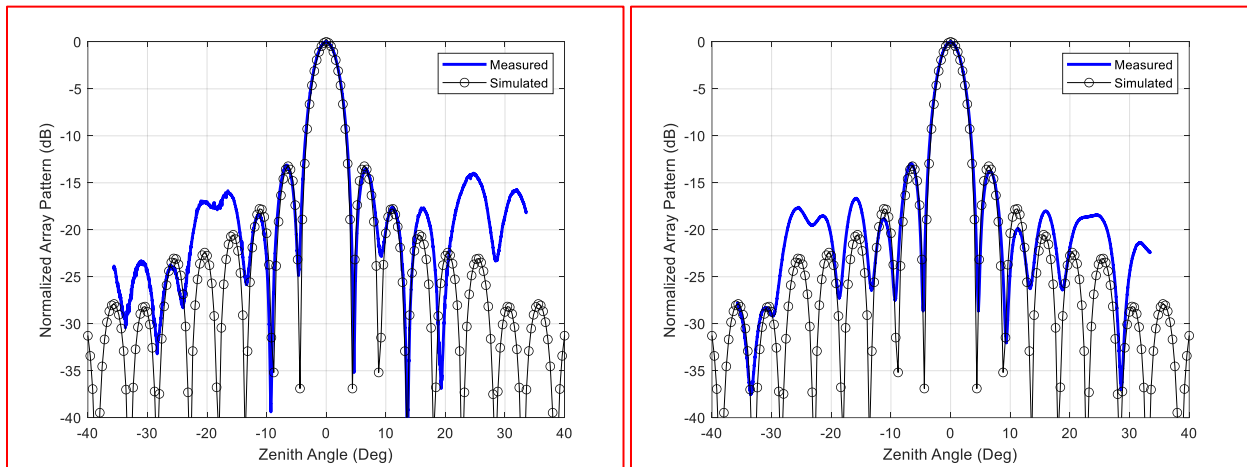


Fig. 4 Normalization constants (dB) for tiles 6-17 at 124 MHz.

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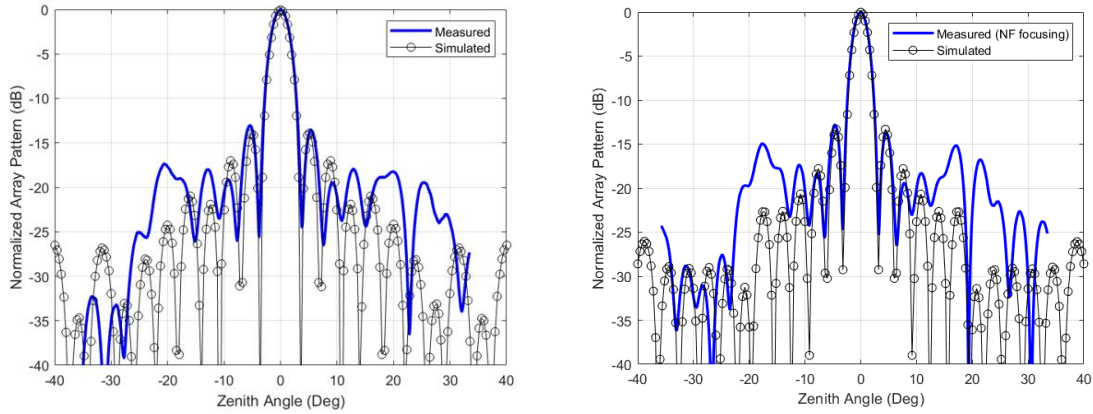
Normalization constants in magnitude are shown in Fig. 4. It is apparent that tile number 10 requires a larger normalization constant with respect to the other tiles to achieve proper equalization. From Fig. 3, it can be also noted that its signal is noisier and the sidelobes are higher with respect to all the other tiles. This can be explained with a fault in the analog beam former of tile 10.



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148
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Fig. 5 Far field pattern (black line) and focused near field (blue line) of tiles 6-11 (left panel) and 12-17 (right panel) at 124 MHz.

150 The equalized (magnitude and phase) signals from the two tile rows 6-11 and 12-17 have been
151 summed together to obtain the radiation patterns at 124 MHz that are shown in Fig. 5 (blue line)
152 as a function of the zenith angle. The zenith angle has been computed using the curvilinear abscissa
153 and the UAV height. A far-field simulation obtained using a combination of WIPL-D and array
154 factor is also shown in Fig. 5 (black solid line with circular markers). **WIPL-D has been used on a**
155 **subarray of 3 by 3 tiles, i.e., 12 by 12 dipoles. This configuration requires neither significant**
156 **computational effort nor specific acceleration methods. However, it allows to estimate the effect**
157 **of mutual coupling on the tile beam. Differences between the nine simulated tile beams in the 3 by**
158 **3 tile array have been found to be negligible with respect to the measured discrepancies [23]. For**
159 **this reason, an array factor approach has been adopted using the simulated tile beam (central tile**
160 **within the 3 by 3 array) as element pattern.** The agreement is satisfactory within $\pm 15^\circ$ from zenith.
161 This is consistent with the near-field focusing method, which guarantees a good agreement
162 between far-field and near-field focused beams only in the proximity of the beam axis [20]. The
163 level of first sidelobes (-13 dB) is consistent with the uniform amplitude excitation. The pattern of
164 the array of tiles 6-11 shows larger discrepancies with respect to simulation because of the faulty
165 tile 10. Almost the same level of agreement has been obtained at 150 and 180 MHz (see Fig. 6,
166 only the array of tiles 12-17 has been reported for brevity). As expected, the angular region with
167 good agreement becomes narrower at higher frequencies ($\pm 10^\circ$ from zenith) because the
168 Fraunhofer condition increases with frequency and all frequencies were measured during the same
169 flight and, hence, at the same height.



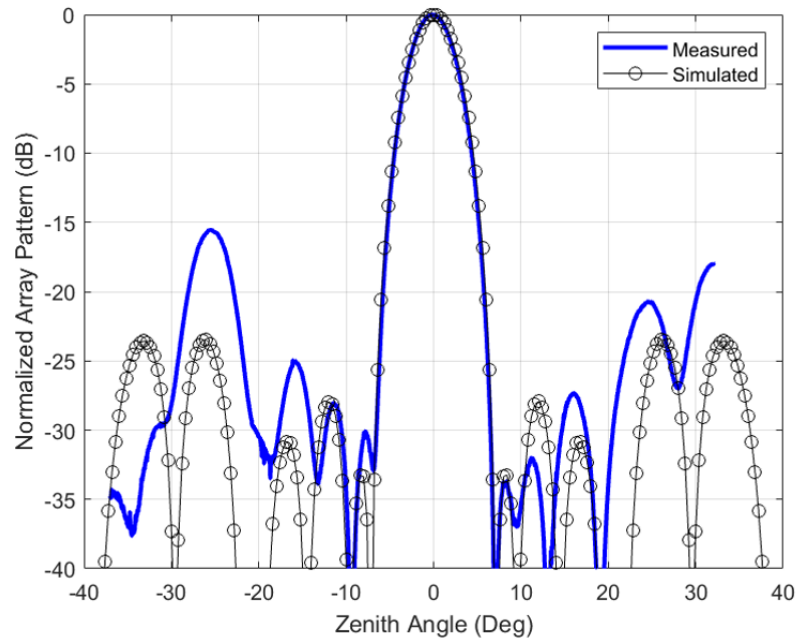
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171 **Fig. 6** Far field pattern (black line) and focused near field (blue line) of tiles 12-17 at 150 MHz (left) and 180 MHz
 172 (right).

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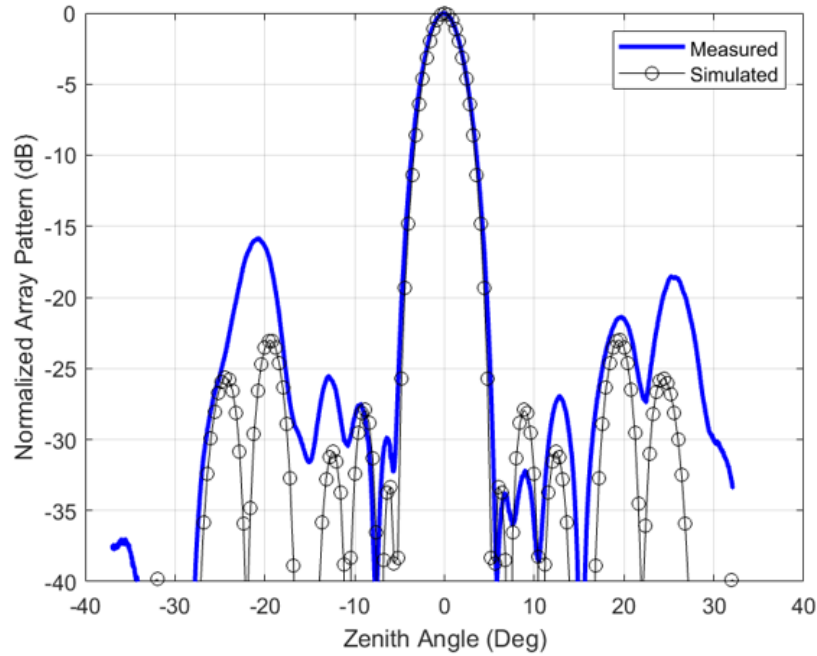
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175 The same near-field focusing procedure has been applied to the full HBA array in Fig. 2. No further
 176 faulty tile has been found besides number 10 (it should be noted that all the tiles in Fig. 2 have
 177 been verified in such a single flight). Figs. 7, 8 and 9 show the measured (near-field focused) and
 178 the simulated (far-field) radiation patterns at 124, 150 and 180 MHz. The angular region showing
 179 good agreement is again ranging from $\pm 15^\circ$ to $\pm 10^\circ$ at lower and higher frequencies, respectively.
 180 The Full Half Power Beamwidths are 5.2° , 3.9° and 3.4° at 124, 150 and 180 MHz, respectively.
 181 The low level of the first sidelobes is due to the array geometry. It should be noted that all the tiles
 182 in Fig. 2 contribute to the array pattern. The number of tiles along the direction that is orthogonal
 183 to the UAV scan i.e. the number of tiles along North-East direction is six in the array center and
 184 two at its edges. As far as the North-West cut reported in Figs. 7, 8 and 9 is concerned, this is
 185 equivalent (in the far-field) to a linear array with edge tapering, which in turn explains the low
 186 sidelobes. This fact can be easily demonstrated by computing the array factor along the North-
 187 West cut.



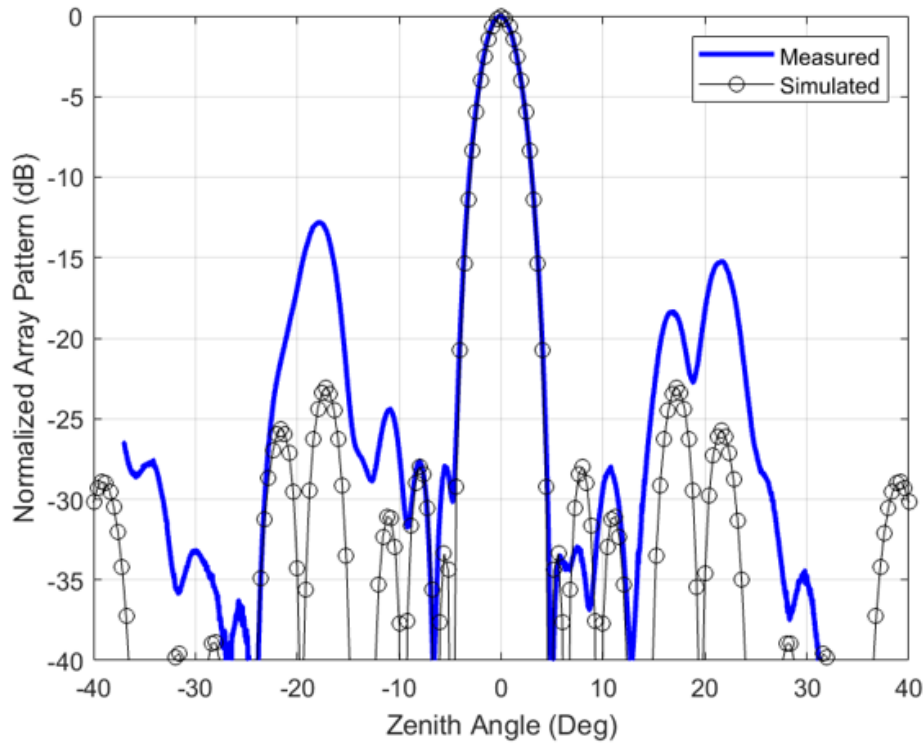
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189 **Fig. 7** Far field pattern (black line) and focused near field (blue line) of tiles 1-24 (full HBA subarray) at 124 MHz.



190

191 **Fig. 8** Far field pattern (black line) and focused near field (blue line) of tiles 1-24 (full HBA subarray) at 150 MHz.



192

193 **Fig. 9** Far field pattern (black line) and focused near field (blue line) of tiles 1-24 (full HBA subarray) at 180 MHz.

194

195

196 **3 Radial Rasters as an efficient scan strategy**

197 The results in section 2 concern a single linear scan performed along the North-West direction.

198 Additional linear scans were performed with an angular offset of 22.5° to achieve a more complete

199 coverage of the u - v plane (directional cosines). All angular steps were performed with two

200 orientations of the UAV-mounted dipole i.e., parallel and orthogonal to the speed vector to sample

201 both the θ - and ϕ -components of the radiation patterns. Each raster has been split as two flights for

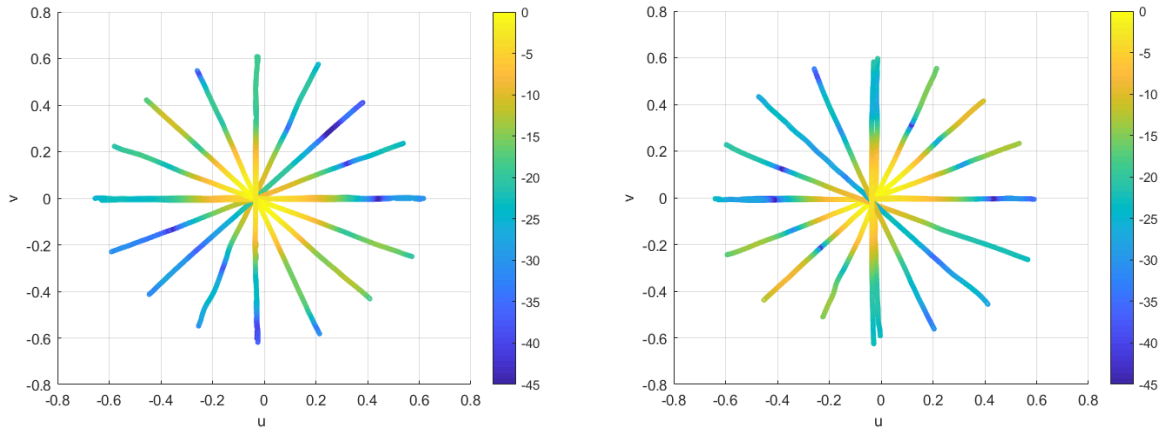
202 each field component i.e. a total of four flights. **The duration of each flight has been approximately**

203 **10 minutes. The full flight duration capability of the UAV has not been exploited due to the severe**

204 **wind condition observed during the campaign. A larger margin on the battery charge has been**

205 maintained for safety reasons. Longer flight durations up to 40 minutes are now available with
 206 modern UAVs operating in calm wind condition. The measured results for the North-West
 207 polarized elements of tile number 9 (see Fig. 2) are shown in Fig. 10.

208



209

210 **Fig. 10** Measured θ - (left) and φ - (right) components of the radiated pattern in dB of tile 9 at 180
 211 MHz (Elements polarized along North-West, i.e. $+135^\circ$ from u axis).

212

213

214 The North-West radiation pattern cut ($+135^\circ$ from u axis) for the (radial) θ - component (on the left

215 panel of Fig. 10) corresponds to the E-plane co-polar pattern for the tile elements polarized along

216 the North-West direction (same cut that is discussed in both section 2 and [23]), where both main

217 lobe and sidelobes are visible. The cut oriented North-East (θ - component, left side of Fig. 10)

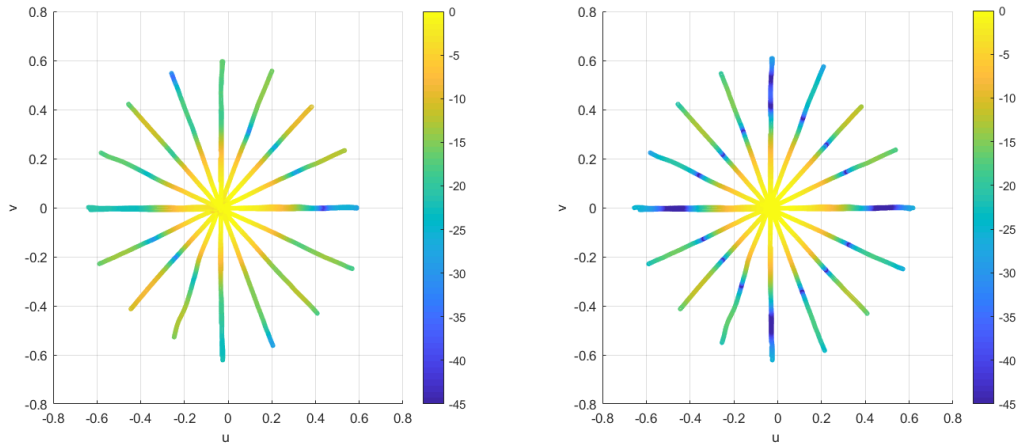
218 instead represents a cross-polar H-plane pattern, which is quite low in magnitude as expected. The

219 H-plane co-polar pattern is visible in the right panel of Fig. 10 where the (azimuthal) φ -component

220 is shown. The North-East cut shows again both main lobe and first sidelobes. This is consistent

221 with the square geometry of the tiles.

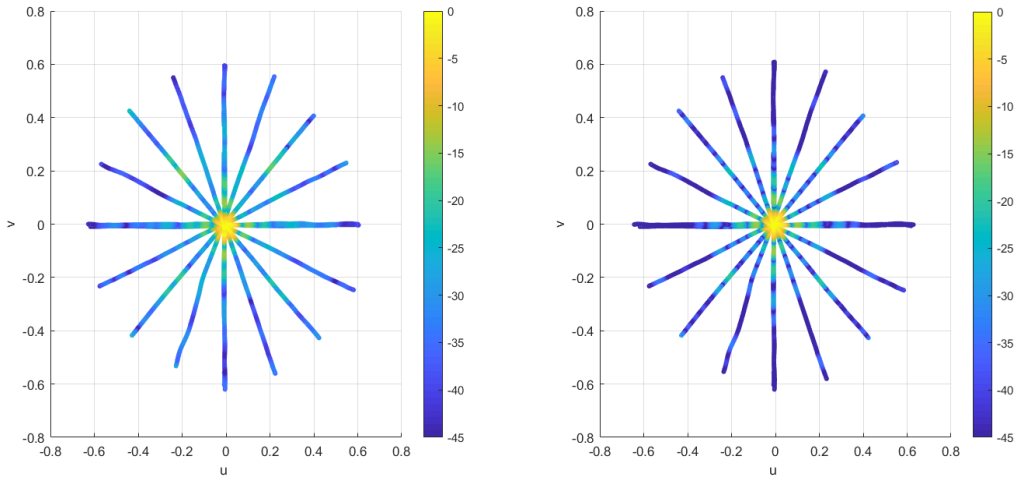
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Fig. 11 Measured (left) an simulated (right) beam patterns in dB for tile 9 at 180 MHz (North-West polarized elements).

The power pattern, i.e., the combination of the two orthogonal pattern components in Fig. 10, is shown in Fig. 11 (left). Both E-plane and H-plane are now visible on the same plot as North-West and North-East paths, respectively. The symmetry of the beam, which is due to the square geometry of the tiles is clearly visible. The overall pattern is very consistent to the simulated data on the right of Fig. 11. The main difference is the depth of the nulls, which is mainly related to source orientation errors, modeling errors and of course manufacturing and position uncertainties of the real tile. Manufacturing tolerances are neither calibrated nor corrected for in the analog beamformer.



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241

242 **Fig. 12** Measured (left) and simulated (right) beam patterns in dB of the HBA array in Fig. 2 at
243 180 MHz (North-West polarized elements).

244

245 The near-field focusing method described in section 2 has been applied to the full HBA shown in

246 Fig. 2. The result is shown in Fig. 12 (left side) and is in good agreement with the simulation (right

247 side). The beam symmetry and width are consistent. Artifacts are still visible in both the North-

248 West and North-East paths. Nevertheless, these results provide a good in-situ validation of the

249 HBA substitution.

250 For brevity, we have only presented results for the HBA elements polarized along the North-West

251 direction. However, similar results have been achieved for the North-East ones.

252 **4 Far-field reconstruction**

253 This section presents an alternative strategy to partially overcome the artifacts due to near-field

254 focusing method already discussed in section 2. It is based on the consideration that the performed

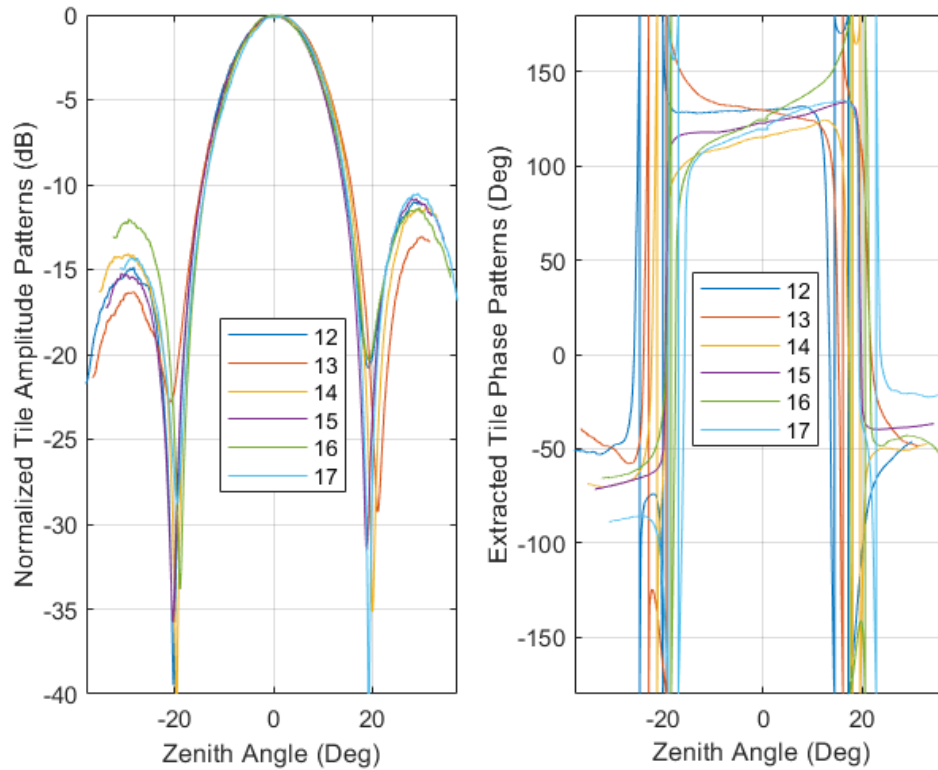
255 UAV flights satisfy the far-field condition for the tiles but not for the array of tiles. For the tiles,

256 both amplitude and phase of the acquired signals are available (complex voltages). The amplitude

257 patterns can be easily obtained by geometrical considerations i.e. the amplitude data for each tile

258 (after removal of UAV pattern and path loss, see for example Fig. 3) are expressed as a function

259 of a local reference system centered on the tile itself, instead of the center of the full array. The
260 resulting patterns for tiles 12-17 are shown in Fig. 13. The frequency of 180 MHz has been selected
261 for this example because it represents a worst case for the near-field focusing artifacts.



262

263 **Fig. 13 Reconstructed far-field E-plane radiation patterns for tiles 12-17 at 180 MHz:**
264 magnitude (left) and phase (right). Near field plots are instead shown in Fig. 3.

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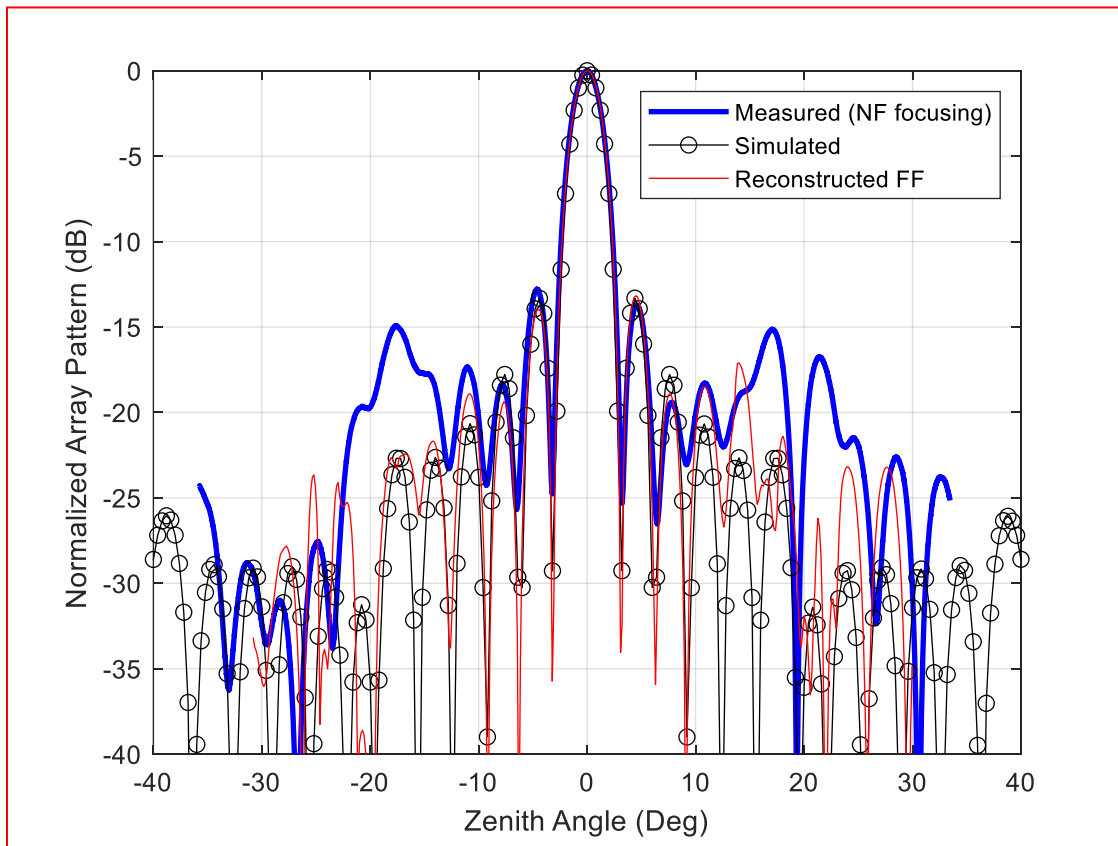
266 As far as far-field phase patterns are concerned, their determination is less straightforward because
267 the UAV-mounted RF source is not phase-locked to the on-ground acquisition system of the
268 telescope. In other words, the relative phase between transmitter and receivers is drifting during
269 the flight in an uncontrolled way. For this reason, only differential phase data can be used [24]. In
270 [25], a reference antenna with known phase pattern was placed in the proximity of the SKA-LOW
271 array prototype to reconstruct a near-field phase pattern. In this campaign, no reference antenna
272 was available. Therefore, one of the central tiles (i.e., tile number 15) is used as reference. This, of

273 course, relies on the knowledge of its phase pattern by simulations (see Fig. 13, right side, violet
274 curve). Under this hypothesis, the phase patterns of all other tiles \emptyset_j can be computed as

$$275 \quad \emptyset_j = \emptyset_i + \varphi_j - \varphi_i + k(r_j - r_i) \quad (1)$$

276 where the time/position dependence of all the terms has been understood, \emptyset_i is the phase pattern
277 of the reference tile ($i = 15$ in our case), φ_j and φ_i are the phase of the acquired complex voltages,
278 k is the wave number and r_j, r_i are the distances between the UAV-mounted source and the centers
279 of tiles j and i , respectively. It should be mentioned that in (1), the direction dependence of the
280 source pattern has been neglected (it is in the order of a few degrees). Moreover, only the co-polar
281 component is considered (transmitter and receiver are matched in polarization). The relative
282 distances r_j and r_i are computed exploiting the UAV position data measured by GNSS and the
283 knowledge of the tile center positions (nominal data have been used, however, an accurate
284 measurement with ground-based instruments such as total station or GNSS is viable). The resulting
285 **reconstructed far-field** phase patterns for tiles 12-14 and 16-17 are shown on the right side of
286 Fig. 13. They are quite similar to each other because local reference systems (centered on each
287 tile) have been adopted. Each of them shows narrow anomalies where the phase rotates of 360°
288 around the zenith angle $\pm 20^\circ$. These anomalies are due to the two nulls on the pattern of the
289 reference tile. At the nulls, the phase exhibits abrupt variations of 180° . In these regions, the
290 accuracy of the models is generally lower and therefore, a perfect cancellation between the terms
291 \emptyset_i and φ_i does not occur in (1). A reference antenna with a smoother behaviour **would be** desirable
292 to avoid such anomalies **(this can be implemented by either activating only one dipole within a tile**
293 **that will be hence used as reference only or exploiting an additional external reference antenna in**
294 **the proximity of the HBA)**. Nevertheless, after summation of the tile patterns in Fig. 13, the
295 resulting beam in Fig. 14 (red curve) is more consistent to the far-field simulation (black curve)

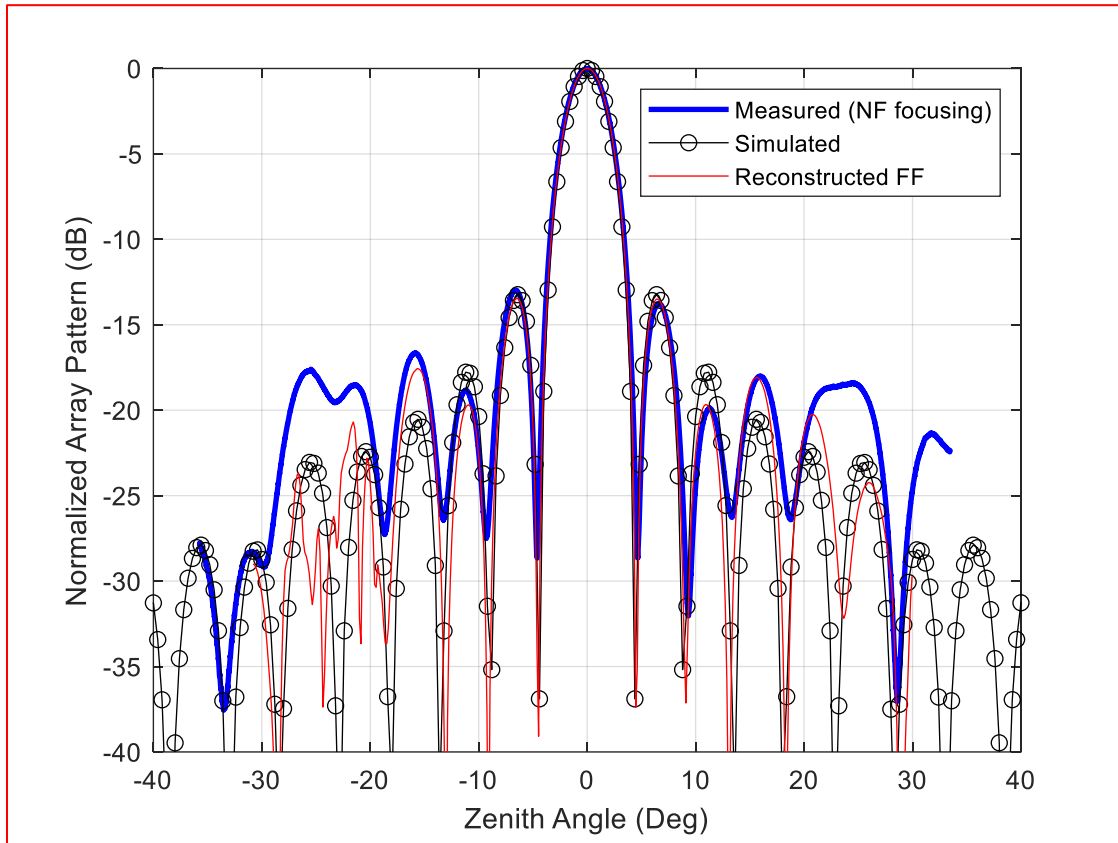
296 than the previous near-field focusing data (blue curve). It should be mentioned that, before
 297 summation, the tile phase patterns in Fig. 13 have been both converted to the same reference
 298 system by exploiting again the knowledge of the tile center positions and equalized at zenith (array
 299 calibration). The angular regions where the discrepancies occur are consistent with the position of
 300 the **reconstructed far-field** phase pattern anomalies in Fig. 13. A **better agreement** has been **also**
 301 achieved at 124 MHz (see Fig. 15) using the same **reconstruction** method. **The overall**
 302 **improvement** has been quantified computing the average (along zenith angle) of the weighted
 303 **logarithmic difference $\Delta_{w,log}$** in [26] with $\beta=0.5$ between measurements and simulation. For the
 304 **near-field focusing (blue curve)**, the quantity $\Delta_{w,log}$ is 0.89 dB and 1.15 dB at 124 and 180 MHz,
 305 **respectively. A smaller $\Delta_{w,log}$ of 0.68 dB has been achieved for the reconstructed far-field case**
 306 **(red curve) at both frequencies.**



307

308
309

Fig. 14. E-plane radiation pattern for the subarray of tiles 12-17 at 180 MHz.



310

Fig. 15. E-plane radiation pattern for the subarray of tiles 12-17 at 124 MHz.

311
312

313 The method presented in this section has only been applied to the linear array of tiles 12-17 which
314 is close to the North-West scan path performed by the UAV (see Fig. 2). The array of tiles 6-11
315 has not been considered because of the faulty tile. The best condition for the presented **far-field**
316 **reconstruction** is a scan path that intersects the maxima of the tile beams, whose pointing is set
317 before the flight. Otherwise, the information of the principal cut of the tile radiation pattern is not
318 available. A linear flight parallel to the array lattice direction (almost North-West in this case) will
319 intersect the maximum number of tile beam maxima. According to these considerations, a cartesian

320 raster with 6 x 6 orthogonal linear scans and a spacing of 5.15 m (distance between tile centers)
321 would have allowed the measurements of all the tile patterns in their principal planes and the
322 subsequent reconstruction of the full array far-field pattern along the North-West and North-East
323 planes by using the method presented in this section. It should be noted that a raster that is suitable
324 for a near-field to far-field transformation would have required a spacing of less than $\lambda/2$ i.e., 0.8 m
325 at 180 MHz, with a strong impact on the UAV flight time requirement. Moreover, a
326 computationally heavy inversion algorithm must be applied [27] to transform the scan paths
327 performed by UAV in the near-field. The presented solution, together with the exploitation of a
328 smoother and well-known reference antenna could be considered for the characterization of the
329 regular arrays of SKA-mid.

330

331 **5 Conclusion and future developments**

332 The application of near-field focusing to an array of LOFAR-HBA tiles pointed in the same far-
333 field direction demonstrated that a useful end-to-end system validation can be performed even
334 considering only a limited angular range around the beam axis. Simulated and measured results
335 are in good agreement as far as beamwidth and first sidelobes are concerned. The method also
336 pointed out the presence of a faulty tile in the Eastern HBA subarray of the CS302 station.

337 The combination of a few linear scans with different orientations has been performed to achieve a
338 radial raster. This procedure confirmed the agreement between measurements and simulations on
339 the full u-v plane, although with limited coverage. The angular step of 22.5° could be reduced at
340 the expense of a longer flight/scan duration.

341 A **far-field reconstruction** method has been proposed and validated on a linear subarray of the HBA
342 **substation. It allows to partially overcome the artifacts of the near-field focusing strategy**

343 exploiting the usage of a known reference antenna and the knowledge of the tile positions. This
344 suggests a validation procedure for regular aperture arrays such as SKA-mid that is based on a
345 cartesian raster in the near-field with a spacing that is equal to the tile spacing, which is several
346 times larger than $\lambda/2$. This efficient scan strategy will provide far-field pattern information on the
347 principal planes only, which could already be satisfactory as far as validating stations in-situ is
348 concerned.

349

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355 *References*

- 356 1. M. P. van Haarlem et al, "LOFAR: The LOw-Frequency ARray", *Astronomy & Astrophysics*, vol.
357 556, A2, 1-53, Aug. 2013.
- 358 2. A. J. J. van Es, M. G. Labate, M. F. Waterson, J. Monari, P. Bolli, D. Davidson, R. Wayth, M.
359 Sokolowski, P. Di Ninni, G. Pupillo, G. Macario, G. Virone, L. Ciorba, F. Paonessa, "A prototype
360 model for evaluating SKA-LOW station calibration," *Proc. SPIE 11445, Ground-based and Airborne*
361 *Telescopes VIII*, 1144589 (13 December 2020); <https://doi.org/10.1117/12.2562391>
- 362 3. P. Bolli et al., "Test-Driven Design of an Active Dual-Polarized Log-Periodic Antenna for the Square
363 Kilometre Array," in *IEEE Open Journal of Antennas and Propagation*, vol. 1, pp. 253-263, 2020, doi:
364 10.1109/OJAP.2020.2999109.

- 365 4. I. Farhat, D. Cutajar, K. Z. Adami, C. Sammut and J. Abela, "Characterization of 36 Meter Square
366 Mid-Frequency Radio Astronomy Prototype Antenna Array," 2018 IEEE Conference on Antenna
367 Measurements & Applications (CAMA), Vasteras, 2018, pp. 1-3, doi:
368 10.1109/CAMA.2018.8530622.
- 369 5. Zhang, Y., El-Makadema, A., de Lera Acedo, E. et al. On the front-end design of mid-frequency
370 aperture array for Square Kilometre Array. *Exp. Astron.*, 46, 357–380 (2018).
371 <https://doi.org/10.1007/s10686-018-9608-z>
- 372 6. G. W. Kant, P. D. Patel, S. J. Wijnholds, M. Ruiter, and E. van der Wal, "EMBRACE: A Multi-Beam
373 20,000-Element Radio Astronomical Phased Array Antenna Demonstrator," *IEEE Trans. Antennas
374 and Prop.*, Vol. 59, no. 6, pp. 1990-2003, June 2011; doi: [10.1109/TAP.2011.2122233](https://doi.org/10.1109/TAP.2011.2122233)
- 375 7. Kiefner, U., Wayth, R. B., Davidson, D. B., & Sokolowski, M. (2021). Holographic calibration of
376 phased array telescopes. *Radio Science*, 56, e2020RS007171. <https://doi.org/10.1029/2020RS007171>
- 377 8. Salas, P., Brentjens, M. A., Bordenave, D. D., Oonk, J. B. R., & Röttgering, H. J. A. (2020). Tied-
378 array holography with LOFAR. *Astronomy and Astrophysics*, 635, A207.
379 <https://doi.org/10.1051/0004-6361/201935670>
- 380 9. S. J. Wijnholds and W. A. van Cappellen, "In Situ Antenna Performance Evaluation of the LOFAR
381 Phased Array Radio Telescope", *IEEE Trans. on Antennas and Propagat.*, Vol. 59, No. 6, June 2011.
- 382 10. A. Nelles, et al, "Calibrating the absolute amplitude scale for air showers measured at LOFAR",
383 *JINST* 10 (2015) no.11, P11005 [arXiv:1507.08932](https://arxiv.org/abs/1507.08932)
- 384 11. E. de Lera Acedo et al., "SKA Aperture Array Verification System: Electromagnetic modeling and
385 beam pattern measurements using a micro UAV", *Experimental Astronomy*, vol. 45, issue 1, pp. 1–
386 20, Mar. 2018. DOI: [10.1007/s10686-017-9566-x](https://doi.org/10.1007/s10686-017-9566-x)
- 387 12. P. Bolli et al., "Antenna pattern characterization of the low-frequency receptor of LOFAR by means
388 of an UAV-mounted artificial test source," *SPIE Ground-based and Airborne Telescopes VI*,
389 Edinburgh, Scotland, United Kingdom, June 26 – July 1 2016. DOI [10.1117/12.2232419](https://doi.org/10.1117/12.2232419)

- 390 13. G. Pupillo et al., “Medicina Array Demonstrator: calibration and radiation pattern characterization
391 using a UAV-mounted radio-frequency source,” *Experimental Astronomy*, vol. 39, issue 2, pp. 405-
392 421, June 2015. DOI: 10.1007/s10686-015-9456-z
- 393 14. P. Bolli et al., “From MAD to SAD: the Italian experience for the Low Frequency Aperture Array of
394 SKA1-LOW”, *Radio Science*, vol. 51, issue 3, pp. 160–175, Mar. 2016. DOI:
395 10.1002/2015RS005922
- 396 15. G. Virone et al., “Strong Mutual Coupling Effects on LOFAR: Modeling and In Situ Validation,”
397 *IEEE Transactions on Antennas and Propagation*, vol. 66, no. 5, pp. 2581-2588, May 2018. DOI:
398 10.1109/TAP.2018.2816651
- 399 16. Paonessa, F., Virone, G., Addamo, G., et al., “UAV-based pattern measurement of the SKALA”.,
400 *IEEE International Symposium on Antennas and Propagation / USNC/URSI National North*
401 *American Radio Science Meeting* Location: Vancouver, CANADA Date: JUL 19-24, 2015
- 402 17. P. Bolli et al., “Near-Field Experimental Verification of the EM Models for the LOFAR Radio
403 Telescope,” *IEEE Antennas and Wireless Propagation Letters*, vol. 17, issue 4, pp. 613–616, Apr.
404 2018. DOI: 10.1109/LAWP.2018.2859828
- 405 18. P. Di Ninni, P. Bolli, F. Paonessa, G. Pupillo, G. Virone, S. J. Wijnholds, “Electromagnetic Analysis
406 and Experimental Validation of the LOFAR Radiation Patterns”, *International Journal of Antennas*
407 *and Propagation*, January 2019, doi:10.1155/2019/9191580
- 408 19. F. Paonessa, L. Ciorba, G. Virone, P. Bolli, A. Magro, A. McPhail, D. Minchin, and R. Bhushan,
409 “SKA-low Prototypes Deployed in Australia: Synoptic of the UAV-based Experimental Results,”
410 *Radio Science Letters*, VOL. 2, 2020, DOI: 10.46620/20-0021.
- 411 20. J. Sherman, "Properties of focused apertures in the Fresnel region," in *IRE Transactions on Antennas*
412 *and Propagation*, vol. 10, no. 4, pp. 399-408, July 1962, doi: 10.1109/TAP.1962.1137900.
- 413 21. P. Nepa and A. Buffi, "Near-Field-Focused Microwave Antennas: Near-field shaping and
414 implementation.," in *IEEE Antennas and Propagation Magazine*, vol. 59, no. 3, pp. 42-53, June 2017,
415 doi: 10.1109/MAP.2017.2686118.

- 416 22. F. Paonessa et al., "UAV-Based Antenna Measurements: Improvement of the Test Source Frequency
417 Behavior," 2018 IEEE Conference on Antenna Measurement and Applications (CAMA 2018),
418 Västerås, Sweden, Sept. 3-6, 2018
- 419 23. G. Virone et al., "Preliminary Results on the Verification of the LOFAR-HBA with a Flying Test
420 Source," 2021 15th European Conference on Antennas and Propagation (EuCAP), 2021, pp. 1-4, doi:
421 10.23919/EuCAP51087.2021.9411311.
- 422 24. F. Paonessa, et al. "Differential phase patterns of the LOFAR LBA array measured in situ", 12th
423 European Conference on Antennas and Propagation, London, UK, 9-13 April 2018
- 424 25. L. Ciorba et al., "Near-Field Phase Reconstruction for UAV-based Antenna Measurements," 2019
425 13th European Conference on Antennas and Propagation (EuCAP), 2019, pp. 1-4.
- 426 26. S. Pivnenko et al., "Comparison of Antenna Measurement Facilities With the DTU-ESA 12 GHz
427 Validation Standard Antenna Within the EU Antenna Centre of Excellence," in *IEEE Transactions on*
428 *Antennas and Propagation*, vol. 57, no. 7, pp. 1863-1878, July 2009, doi: 0.1109/TAP.2009.2021934.
- 429 27. J. L. A. Quijano and G. Vecchi, "Field and Source Equivalence in Source Reconstruction on 3D
430 Surfaces," *Progress In Electromagnetics Research*, Vol. 103, 67-100, 2010.
431 doi:10.2528/PIER10030309

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498

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503

504 **Caption List**

505

506 **Fig. 1** The UAV after take-off is reaching the first waypoint to perform the required scan path over

507 the LOFAR Eastern HBA array of the CS302 station. The array dimension is about 30 m.

508 **Fig. 2** Element positions in LOFAR HBA subarray. Red and black numbers refer to tile number

509 (0-23) and element number (0-15) inside the single tile, respectively. The black dashed curve

510 shows an example of a UAV path (its projection to the ground) oriented along the North-West

511 direction.

512 **Fig. 3** Normalized E-plane radiation pattern for tiles 6-11 (left) and 12-17 (right) at 124 MHz.

513 **Fig. 4** Normalization constants (dB) for tiles 6-17 at 124 MHz.

514 **Fig. 5** Far field pattern (black line) and focused near field (blue line) of tiles 6-11 (left figure) and
515 12-17 (right figure) at 124 MHz.

516 **Fig. 6** Far field pattern (black line) and focused near field (blue line) of tiles 12-17 at 150 MHz
517 (left) and 180 MHz (right).

518 **Fig. 7** Far field pattern (black line) and focused near field (blue line) of tiles 1-24 (full HBA
519 subarray) at 124 MHz.

520 **Fig. 8** Far field pattern (black line) and focused near field (blue line) of tiles 1-24 (full HBA
521 subarray) at 150 MHz.

522 **Fig. 9** Far field pattern (black line) and focused near field (blue line) of tiles 1-24 (full HBA
523 subarray) at 180 MHz.

524 **Fig. 10** Measured θ - (left) and φ - (right) components of the radiated pattern of tile 9 at 180 MHz
525 (North-West polarized elements).

526 **Fig. 11** Measured (left) an simulated (right) beam patterns for tile 9 at 180 MHz (North-West
527 polarized elements).

528 **Fig. 12** Measured (left) an simulated (right) beam patterns of the HBA array in Fig. 2 at 180 MHz
529 (North-West polarized elements).

530 **Fig. 13** E-plane radiation patterns for tiles 12-17 at 180 MHz: magnitude (left) and phase (right).
531

532 **Fig. 14.** E-plane radiation pattern for tiles 12-17 at 180 MHz.

533 **Fig. 15.** E-plane radiation pattern for tiles 12-17 at 124 MHz.