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Optimized Management of Ultra-wideband Photonics Switching Systems Assisted by Machine Learning

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Abstract: Recent years have seen an unprecedented growth of data traffic driven by a continuous increase of connected devices and new applications. This trend will tend to saturate transparent optical networks that are the backbone of the whole telecommunication infrastructure. To improve the capacity of already deployed network infrastructures and maximize operators CAPEX returns, band-division multiplexing (BDM) has emerged as a promising solution to expand the fiber bandwidth beyond the existing C-band. Along with this, the demand for flexible and dynamically reconfigurable functionalities in each network layer is increasing. In this regard, optical networking is fast evolving towards the applications of the software-defined networking (SDN) paradigm down to the physical layer. The implementation of optical SDN requires the full abstraction and virtualization of each network element in order to enable complete control by a centralized network controller. To pursue this objective, photonics transmission components and their transmission functionalities must be abstracted to allow the definition of the control states and a real-time quality-of-transmission (QoT) evaluation of transparent lightpaths (LP). In this work, we propose an SDN based model of a photonic switching fabric that allows determining the control state and evaluating QoT degradation. Our investigations present a wideband optical switch design based on photonic integrated circuits (PICs), where QoT degradation is abstracted using a structure-agnostic approach based on machine learning (ML). The ML engine training and testing datasets are generated synthetically by software simulation of the photonic switch architecture. Results show the potential of the proposed technique to predict QoT impairments with high accuracy, and we envision its application in a real-time control plane.

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1. Introduction

The continuous rise of global internet traffic and the latest evolving technologies such as 5G and internet of things (IoT) will require an increase of optical network capacity together with a demand for flexible and dynamic network functionalities at every layer. State-of-the-art optical transport networks are based on wavelength-division multiplexing (WDM) in the standard spectral window of ≈ 4.8 THz defined as C-band. An increase in network capacity can be obtained by adopting one of the two unique solutions; (i) exploiting the residual capacity of already installed infrastructure, (ii) deploying new network infrastructures. The initial solution of exploiting the residual capacity of already installed infrastructure is more valuable for network operators from a techno-economic viewpoint. In this scenario, a technique like BDM appears as a promising technology to exploit the residual capacity of existing WDM optical network infrastructure throughout the whole low-loss spectrum of optical fibers (e.g., ≈ 54 THz in ITU G.652.D fiber) [1].

The demand for flexible and dynamic network functionalities in each layer can be provided by implementing the SDN paradigm down to the physical layer [2, 3]. At this level, the SDN is

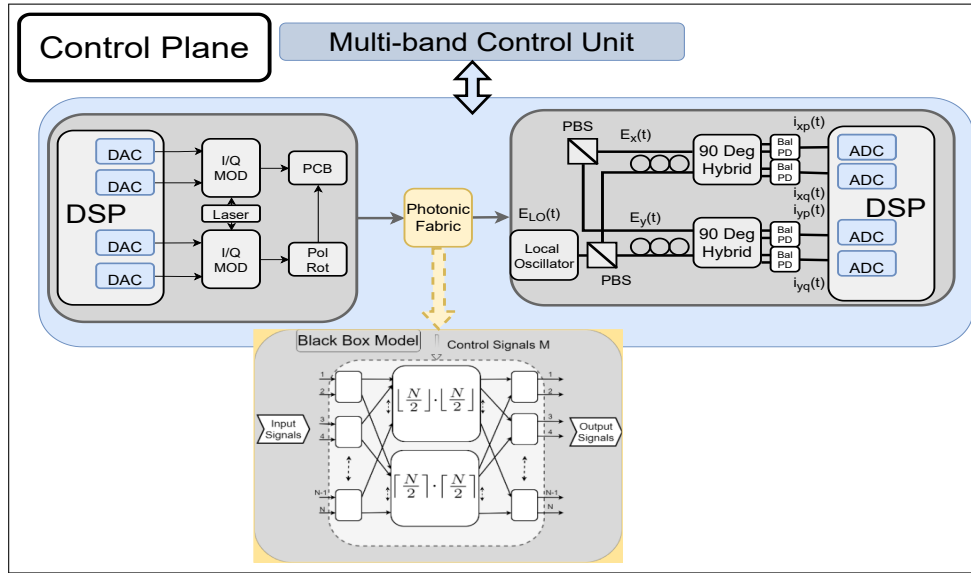


Fig. 1. Abstraction of the optical switching fabric for the control-plane of a SDN-controlled photonic transmission system.

45 based on a network controller that manages physical links and controls switching elements to
 46 optimize performance, i.e., to maximize transmission capacity. SDN needs an open interface for
 47 each transmission element with a model for its transmission impairment.

48 For physical channels, the SDN application requires the capability to summarize the QoT of
 49 links in a unique QoT meter, given by the availability of a QoT estimator (QoT-E) to compute it.
 50 The application of QoT-E to the WDM optical transport has been made easier by introducing
 51 transceivers (TRXs) based on dual-polarization multilevel modulation formats exploiting DSP
 52 technologies for spectral shaping and coherent detection. The advent of coherent TRXs has
 53 been a game-changer in link design: it allowed the introduction of the uncompensated approach,
 54 removing the need for dispersion compensating units that needed specific optimization. Exploiting
 55 this transmission technology in transparent LP within the system simplifies the QoT evaluation
 56 as the non-linear propagation impact can be easily modeled as an additive white Gaussian noise
 57 (AWGN) [4]. This AWGN-like approach defines the requested minimum optical-signal-to-noise ratio
 58 (OSNR) of TRXs in a back-to-back characterization and then uses it for determining LP
 59 deployment and feasibility. This property enables the full abstraction of the optical transport
 60 system through a QoT-E that computes the OSNR of each LP and compares it to the minimum
 61 OSNR requested by the coherent TRX [5]. Each transparent LP can be dynamically set from
 62 source to destination by setting the traversing switching elements. Consequently, models to
 63 evaluate the QoT degradation of each crossed switching element are also needed to compute
 64 the overall OSNR. Besides quantifying the QoT degradation due to the switching element, the
 65 optical network controller must define the control state for them. To this end, we need models to
 66 set operational modes minimizing the QoT degradation, defining the selected transparent LP by
 67 properly configuring the switching elements.

68 Optical network elements currently exploit PICs to carry out most of the complex functions at
 69 the photonic level; specifically, optical networks and data centers progressively utilize large-scale
 70 photonic switches and wavelength selective switches due to their wide-band abilities together
 71 with low latency and low power consumption. PIC-based photonic switches primarily work on
 72 the principle that the flow of light can be maneuvered by 2×2 electrically controlled elements,

73 like mach-zehnder interferometers (MZI) [6] or optical micro-ring resonators (MRRs) [7].
74 Before the development of PIC technology, various switching machinery has been proposed,
75 such as 3D micro-electro-mechanical systems (MEMS) [8] and beam-steering techniques [9].
76 These technologies offer stable optical switching and a satisfactory level of scalability, but the
77 requirement to calibrate and install discrete components makes them considerably more costly
78 and massive. Cost and size make it challenging to implement these technologies in the future
79 UWB system. Consequently, it boosts the trend of using PICs-based modules. Moreover, this
80 increased use of PICs-based switching systems creates a demand for a generic software-based
81 management model for photonic switches enabling complete control in the optical SDN context.

82 In this work, we focus on the definition of an SDN model of a photonic switching fabric
83 for both control and QoT degradation as pictorially shown in Fig. 1. The principal aim of this
84 investigation is to present the design of a wideband optical switch based on PICs and then
85 model this $N \times N$ ultra-wideband (UWB) switching system at two different levels of abstraction:
86 the routing behavior and the QoT relation to the applied control signals. The routing problem
87 is solved by considering the black-box abstraction of the 2×2 cross-bar switching units on a
88 simplified version of the circuit, taking only into account the ideal link between the elements and
89 the binary control state of each fundamental switch. For the QoT, an ML-based framework is
90 proposed to predict the QoT degradation due to the real switching element. This method is a
91 topological and technological agnostic *blind* approach which exploits neural network methods to
92 model the QoT impairments of the $N \times N$ photonic switch. The introduced data-driven structure
93 is trained on a dataset obtained by considering a $N \times N$ photonic switch. The training dataset can
94 either be obtained experimentally or *synthetically* by using a software simulator for components.
95 The trained ML model provides the QoT impairments in real-time as ML models only require
96 time during the initial training; once the model is substantially trained, it can provide results in
97 real-time for the given application.

98 The remainder of the paper is organized as follows. In Section 2, we briefly describe the
99 background and the previous related investigations. Section 3, presents switching structures,
100 topologies and their related performances in a UWB system. In Section 4, the simulation model,
101 together with synthetic data generation and analysis, are reported. In Section 5, the orchestration
102 of the ML engine is presented. Then, in Section 6, we describe the results in detail. Finally,
103 conclusions and future research directions are presented in Section 7.

104 2. Background of the study

105 Research related to the software-based management of photonic switching systems has been sparsely
106 performed and reported. The management model for optical switches is essential because of
107 their path-dependent nature [10] as compared to electronic switches, where the performance of
108 all routes is identical [11]. The variations in performance for optical switches are mainly due to
109 the photonic circuit topology, but they can also depend on mask-level design flaws. Usually, the
110 deterministic routing algorithms presented in literature can efficiently determine the control state
111 of internal switches for any given output permutations. The effectiveness of these algorithms
112 comes from their topology dependent nature, which enables a faster and efficient assessment of
113 the multiple-stage networks. On the contrary, these traditional deterministic routing algorithms
114 do not offer all the equivalent paths for a given channels permutation [12–14]. In contrast with
115 traditional routing algorithms, we propose a routing algorithm that produces all the equivalent
116 paths for a given output permutation. The provided routing scheme is then paired up with an
117 ML-based agent capable of predicting the QoT degradation of each calculated path due to the
118 switching and coupling units, thus allowing for the identification of the best control set.

119 The ML-based approach has already been explored in the area of PIC design and control for
120 different functionalities. An algorithm-driven by the artificial neural network is proposed in [15]
121 to regulate 2×2 dual-ring assisted-MZI switches. In [16] ML is used to assess QoT of PIC in

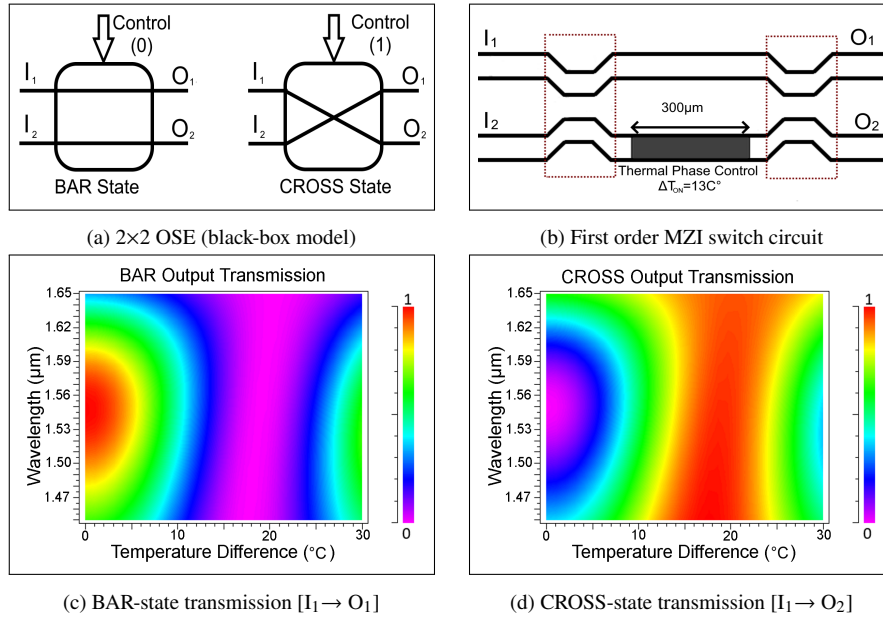


Fig. 2. (a) Optical switching element (OSE) black-box model. (b) MZI switching circuit. (c) and (d) Dependence of transmission properties in BAR and CROSS state on wavelength and temperature.

122 order to reduce the system margin. In [17] ML module is used in SDN enabled optical network to
 123 provide the full abstraction of a PIC. In [18], the authors experimentally demonstrated a complete
 124 self-learning and reconfigurable photonic signal processor based on an optical neural network
 125 chip. The proposed chip executes a variety of functions by self-learning, such as multi-channel
 126 optical switching, optical multiple-input-multiple-output de-scrambling, and tunable optical
 127 filtering. We proposed an ML-based model for modeling the elementary control states of the
 128 PIC $N \times N$ switches in a structural agnostic way in [19, 20]. Similarly, in [21] ML-based model
 129 is used for the accurate prediction of QoT impairments of photonic switches in a SDN context.
 130 In [22], the deep reinforcement learning (DRL) technique is used to reconfigure the silicon
 131 photonic flexible low-latency interconnect optical network switch (Flex-LIONS) giving to the
 132 traffic attributes in high-performance computing systems. Additionally, a novel reinforcement
 133 ML-based framework called DeepConf is presented in [23], for automatically learning and
 134 implementing a range of data center networking techniques.

135 3. Ultra-wideband switching system

136 The device under analysis consists of an electronically controlled integrated transparent photonic
 137 switch, able to perform the routing operation without electro-optical conversion of the transmitted
 138 signals. The two main characteristics of the system are related to the frequency range of operation,
 139 allowing switching in the spectral range covering S+C+L bands, as well as the logical routing
 140 requirement, as every permutation of the input signal must be achievable at the egress stage of
 141 the device, referred as non-blocking switching.

142 Different solutions have been described in the literature, with $N \times N$ multistage switching
 143 networks being one of the most widespread implementations. In this class of devices, the routing
 144 operation is achieved by cascading various stages of elementary 2x2 switches, referred to as
 145 optical switching elements (OSE), arranged in different topologies depending on the required

146 properties of the routing operation. Each OSE of the network can be controlled independently
147 through an electrical signal. In this work, we apply the proposed approach to an 8×8 switching
148 device, with MZI-based OSEs, analyzed in Section 3.1, interconnected through the Beneš
149 network topology, described in Section 3.2. The switching network size $N = 8$ has been chosen
150 as a trade-off between realistic implementation sizes for photonic integrated circuits, circuit
151 complexity and data-set size. The chosen size acts as a reasonable simulation test-bed to verify
152 the proposed control scheme and abstraction, while providing a large enough component cascade
153 to highlight the physical devices behavior.

154 3.1. Optical switching element

155 The OSE is the fundamental block required for the switching action, introducing limitations
156 on the operating frequencies and imposing some QoT degradation. At the logical level, the
157 OSE 2×2 cross-bar switch can be modelled as a black-box (see Fig. 2a) with two available
158 routing states: the BAR configuration ($[I_1, I_2] \rightarrow [O_1, O_2]$) and the CROSS configuration
159 ($[I_1, I_2] \rightarrow [O_2, O_1]$) which can be appropriately toggled by a given binary control signal. The
160 OSE can be implemented with two main solutions described in the literature: the MRR filter and
161 the MZI. Due to the bandwidth limitations of the MRR solutions, we propose in this paper a
162 device based on the MZI principle.

163 The most straightforward MZI device is structured as shown in Fig. 2b: the signal is divided
164 into the two waveguides by the first 3 dB coupling section and recombined in the egress 3 dB
165 coupler, with the thermally-controlled phase shift region acting as the control section for the
166 routing state. The routing state is controlled electrically by increasing the temperature of the
167 phase control waveguide in the MZI arms. This increase in temperature introduces a phase
168 shift in the propagating signal, changing the output recombination waveguide in the egress
169 coupler. The signal transmission is depicted in Fig. 2(c) and Fig. 2(d) as a function of the signal
170 wavelength as well as the temperature shift between the MZI arms. In the OFF state ($\Delta T = 0^\circ\text{C}$)
171 the bandwidth limitation of the device is clear, with the range of operation covering roughly half
172 of the S+C+L band. The bandwidth limitation is due to the 3 dB coupling regions where phase
173 velocity dispersion of the physical waveguides causes asymmetry in the signal propagation, with
174 uneven power splitting and recombination, leading to significant crosstalk with the incorrect
175 output port.

176 3.1.1. Higher order coupling regions

177 The critical component for achieving the UWB range of operation is the coupler region, required
178 before and after the thermal phase control section. While the coupler has a 3 dB power ratio for
179 the centre design frequency, the waveguide dispersion causes increasing asymmetry as the signal
180 frequency moves away from the center point. One of the simplest solutions to compensate for
181 this effect is cascading two identical couplers while introducing a constant phase shift between
182 the two waveguides ($\Delta\phi = 90^\circ$), as shown in Fig. 3. This solution reduces the dispersion effect
183 on the power ratio, leading to a larger and flatter bandwidth near the design frequency while also
184 reducing the overall asymmetry at the limits of the chosen bandwidth, depicted in Fig. 3d. More
185 advanced solutions, like a complex waveguide, tapered structures or advanced 3D structure [24]
186 can still enlarge the bandwidth of the 3 dB coupling region. For the intended applications
187 of a multi-stage switching structure, the rapid increase in circuit complexity and production
188 requirements may become prohibitive as the scale of the overall network increases, which leads to
189 a trade-off between the cost and effectiveness of the solution. The analyzed device, implemented
190 through the second-order coupling structure, is depicted in Fig. 4a: the bandwidth of operation
191 covers the target transmission windows, with increases in crosstalk and penalty observed only at
192 the edges of the operating region, as shown for both routing states in Fig. 4b-Fig. 4c.

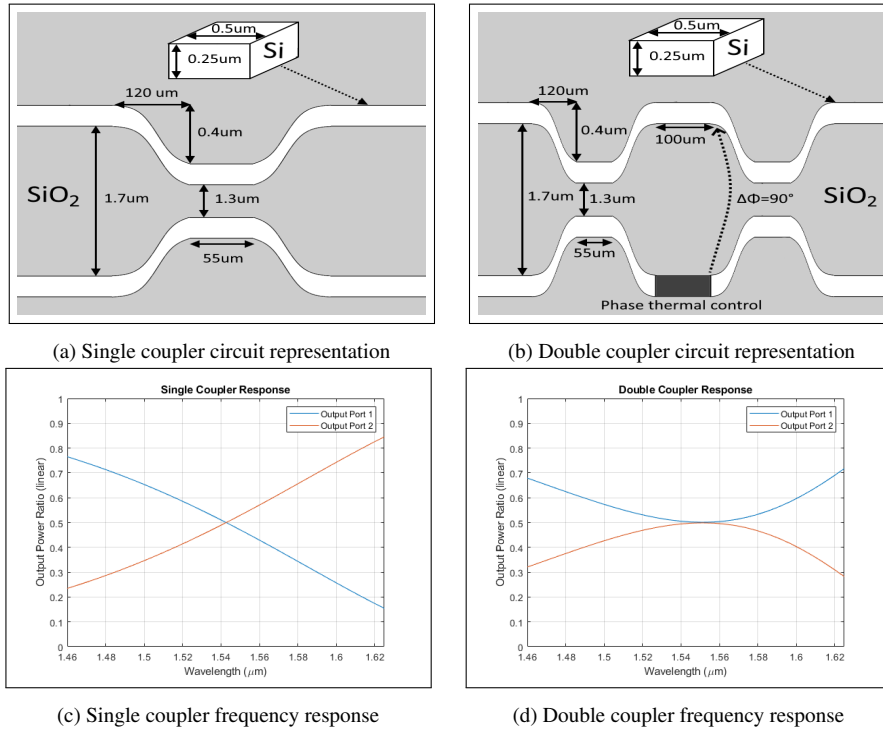


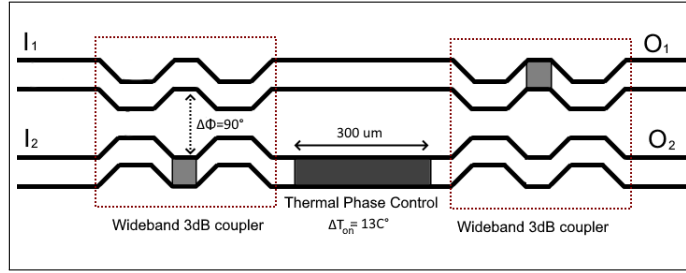
Fig. 3. (a)-(b) MZI switch structures: single coupler vs. double coupler. (c)-(d) Corresponding transmission bandwidth properties.

193 3.2. Beneš topology

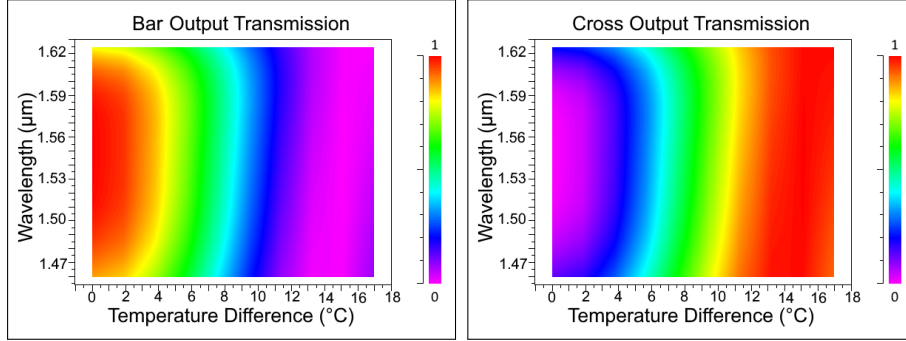
194 After defining the fundamental 2×2 OSE, any generic $N \times N$ circuit can be modeled following
 195 the topology of choice, for example, the Beneš network. The Beneš network has been chosen
 196 here for various reasons, due to both the target application requirements and minimization of the
 197 circuit footprint. Different classes of switching networks exist: topologies based on the Clos
 198 network paradigm, like the Beneš structure, allow both a reduction of the number of switching
 199 elements, as well as guaranteeing non-blocking capabilities, avoiding routing conflict inside
 200 the device mesh [25]. The non-blocking property is fundamental for our target application, as
 201 all possible permutations of the N input signals must be achievable at the egress stage of the
 202 network, allowing full control of the routing component for any given output request. The $N \times N$
 203 Beneš device is characterized by a recursive structure (see Fig. 5a), described in details in [26],
 204 with a number of OSE equal to $N_{sw} = N \times \log_2 N - \frac{N}{2}$ distributed in $2 \log_2 N - 1$ stages, as
 205 depicted for an 8×8 Beneš in Fig. 5b. One important characteristic of this device is the solution
 206 multiplicity for any given target output state: given that the N_{sw} OSEs lead to several control
 207 configurations $N_{conf} = 2^{N_{sw}}$, larger than the number of unique output permutations $N_{out} = N!$,
 208 multiple solutions must exist for each unique output permutation request, whose multiplicity
 209 depends on the specific target output permutation. In Section 5 we propose a ML-based approach
 210 to determine the *best* configuration between the nominally identical ones returned by the proposed
 211 routing algorithm.

212 4. Simulation environment and dataset generation

213 The device is modeled under two different levels of abstraction to characterize the dependence on
 214 the control signals of both the routing behavior and the impact on QoT of the switching operation.



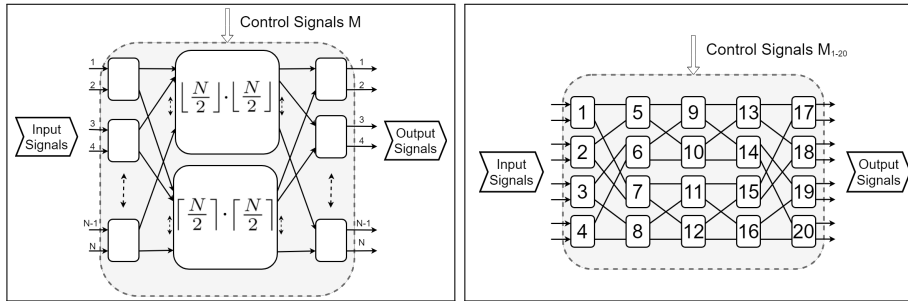
(a) Second order coupling MZI device tested in this study.



(b) BAR-state transmission $[I_1 \rightarrow O_1]$

(c) CROSS-state transmission $[I_1 \rightarrow O_2]$

Fig. 4. Transmission dependence on wavelength and thermal tunability for the second order coupling MZI device tested in the paper.



(a) Generic Beneš network recursive structure

(b) 8x8 Beneš network

Fig. 5. Beneš network topologies.

215 4.1. Routing model

216 Given the black-box abstraction of the 2×2 cross-bar OSEs, the routing problem can be solved on
 217 a simplified version of the circuit, taking only into account the logical link between input-output
 218 ports as a function of the binary control state of each fundamental switch. To this end, a virtual
 219 topological structure was generated in MATLAB[®], in order to analyze the routing and then
 220 to evaluate the logical output for the QoT transmission-level simulation. Given the simple
 221 recursive structure of the network, coupled with the non-polynomial increase in the solution
 222 space ($N_{\text{conf}} = O(2^{N \log N})$, $N_{\text{out}} = O(N!)$), brute-force solution together with look-up tables
 223 are not a scalable method to obtain the states configurations for the target output request. This
 224 introduces the need for a scalable deterministic algorithm to tackle the problem complexity and
 225 provide the equivalent paths routing the same output permutation. While it is fundamental to be

Algorithm 1 Beneš routing algorithm

Require: Number of input and output channels N , Input signals labels $\mathcal{I}_{[1:N]}$, Output signals labels $\mathcal{O}_{[1:N]}$

Ensure: A control state, chosen randomly among all the control states giving the requested target output permutation

```
1: Number of switch per stage  $N_{sw/st} = \frac{N}{2}$ 
2: Number of stages  $N_{st} = \log_2 N$ 
3: for layer index  $l = 1$  to  $\frac{N_{st}}{2} - 1$  do
4:   Initialize to -1 the routing matrix  $M_l \in \mathcal{R}^{\frac{N}{2} \times \frac{N}{2}}$ 
5:   Initialize to 0 the label matrix  $T_l \in \mathcal{R}^{\frac{N}{2} \times \frac{N}{2}}$ 
6:   for label index  $j = 1$  to  $N$  do
7:      $SW_I \leftarrow \left\lceil \frac{j}{2} \right\rceil$ 
8:      $SW_O \leftarrow \left\lceil \frac{k}{2} \right\rceil$  with  $k$  such that  $\mathcal{O}_k = \mathcal{I}_j$ 
9:     if  $M_l(SW_I, SW_O)$  is -1 then
10:      if column  $SW_O$  of  $M_l$  contains a 0 then
11:         $M_l(SW_I, SW_O) \leftarrow 1$  %%% 1 i.e. bottom network routing
12:      else if column  $SW_O$  of  $M_l$  contains a 1 then
13:         $M_l(SW_I, SW_O) \leftarrow 0$  %%% 0 i.e. top network routing
14:      else
15:        set randomly  $M_l(SW_I, SW_O)$  to 0 or 1
16:      end if
17:       $T_l(SW_I, SW_O) \leftarrow \mathcal{I}_j$ 
18:    else if  $M_l(SW_I, SW_O)$  is not -1 then
19:       $M_l(SW_I, SW_O) \leftarrow 2$  %%% 2 i.e. same input-output couple request
20:       $T_l(SW_I, 1) \leftarrow T_l(SW_I, SW_O)$ 
21:       $T_l(SW_I, 2) \leftarrow \mathcal{I}_j$ 
22:    end if
23:  end for
24:  check for conflict  $\rightarrow$  Algorithm 2
25:  update  $\mathcal{I}_j, \mathcal{O}_j$  for the evaluated routing
26: end for
```

226 able to generate a single routing solution for a target output permutation, in order to minimize
227 the penalties in a device-agnostic scenario a more general algorithm is needed to evaluate all
228 equivalent routing solutions for each required signal output permutation. The device-agnostic
229 scenario is introduced to generalize the analysis without the need of assuming the QoT behavior
230 to the physical and device-level structure: a simpler approach to the optimization of the QoT
231 could be to minimize the number of interconnecting crossings encountered by each signal, as
232 these elements are typically the leading cause of signal attenuation. However, this relies on a
233 device assumption which could not always be accurate, so to avoid the issue the problem is split
234 into two main sections, under a "divide and rule" paradigm: the routing model is tasked with
235 generating all equivalent routings for the target signal output, without introducing assumptions on
236 the underlying transmission penalty, while the ML agent proposed in the later sections handles
237 the QoT optimizations, selecting between the solution space the best-predicted solution.

238 The proposed solution represents a generalization of the matrix-based algorithm described
239 in [27]. Having defined an $N \times N$ Beneš, with number of switches per stage $N_{sw/st} = \frac{N}{2}$
240 and number of stages $N_{st} = \log_2 N$, the proposed algorithm is divided in the following steps
241 (Algorithm 1-Algorithm 2):

- 242 • For each layer of the network up to the half-point stage, generate two empty matrices
243 $\mathcal{M}, \mathcal{T} \in \mathcal{R}^{\frac{N}{2} \times \frac{N}{2}}$, representing respectively the control states of the OSEs in the layer and
244 the rearranged signal order after the layer.
- 245 • By comparing the input signals order of the ingress layer with respect to the output signals
246 order of the egress layer, for every signal map, the relation between input switch and target
247 output switch. The ingress and egress layers are symmetrical with respect to the middle
248 stage $N_{middle} = \frac{N_{st}}{2}$ (ingress: layer (i), egress: layer ($N_{st} - i$), for $i \in [1 : N_{middle}]$)

Algorithm 2 Routing conflict algorithm

Require: Routing matrix M

Ensure: Balanced conflict-avoiding routing

```
1: conflict=false
2: Conflicts=empty list
3: for row index  $r = 1$  to  $N$  do
4:    $R$ =row  $r$  of  $M$ 
5:   if  $R$  contains two 0s or two 1s then
6:     conflict=true
7:     append  $r$  to Conflicts
8:   end if
9: end for
10: if conflict then
11:    $r^*$  = randomly selected element in Conflicts
12:    $R^*$  = row  $r^*$  of  $M$ 
13:    $c^*$  = randomly selected position of any element of  $R^*$  equal to 0 or 1
14:    $C^*$  = column  $c^*$  of  $M$ 
15:   exchange 0 and 1 in  $C^*$ 
16:   loop to 1
17: else
18:   return → Algorithm 1 (update matrix  $M$ )
19: end if
```

- 249
- 250
- 251
- Fill the matrix \mathcal{M} with $[0, 1]$ using the input-output switch relationship to select the row-column pair respectively. The matrix \mathcal{T} contains the label of the signal corresponding to that input-output switch pair.
- 252
- 253
- 254
- Once the matrix for the layer is compiled, verify that no repetitions occur both row-wise and column-wise. Only one instance of "0" and "1" can occur in any given row or column. If repetitions occur, flip the element column-wise until the conditions are solved.
- 255
- Iterate for all layers $i \in [1 : N_{\text{middle}}]$.

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In the described algorithm the "0" and "1" flags of the \mathcal{M} matrices correspond to the propagation direction of the signal in each switching element, relative to the following stages: considering the recursive structure of the Beneš topology, as well as its symmetry, at every stage, two equivalent paths can be found in the respective top and bottom following sub-network. Two additional flags values are used in the proposed algorithm: every matrix cell is initially set to "-1" to indicate non-allocated requests or empty cells. An additional flag is required in the routing matrix in order to account for equivalent routings in some specific cases: while typically the input signals of an ingress switch must be routed to different egress switches when both input signals are targeting the same output switch, only one single cell of the routing matrix can be targeted: to this end, the flag "2" represents the path equivalence between the top and bottom network, with the implied value of both ("1", "0") and ("0", "1").

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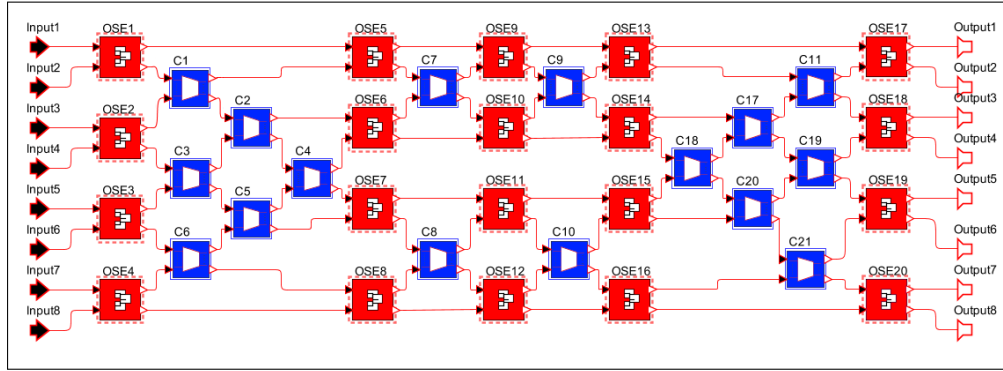
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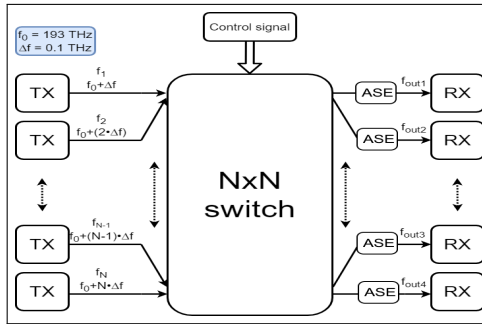
Once the procedure is completed, the state of the switches can be obtained by comparing the order of the signals of each layer, taking into account the interconnects and the top/down direction provided by the compiled \mathcal{M}_i matrices. With a slight modification to the presented algorithm, the evaluation of all equivalent paths in terms of permutation of the output signals becomes trivial: once the output permutation is set, each valid matrix \mathcal{M}_i represents a different equivalent routing possibility. For every routing of the previous layer, the process is iterated, generating a recursive exploration of all switching states for the required output. Using the proposed algorithm, the control unit can generate different solutions depending on the required task: if all equivalent routing solutions are evaluated, the proposed ML agent can optimize the QoT, finally choosing the path with minimum transmission penalty. Suppose a simpler control unit is required; the algorithm can provide a single control configuration for the device, generating



(a) 8×8 Beneš switch schematic in OptSim Photonic Circuit. Crossings are indicated by blue blocks while OSEs are shown as red blocks.



(b) Response of the waveguide crossing



(c) Transmission environment under simulation

Fig. 6. Simulation model schematic and characteristics

278 one random routing compatible with the required signal output permutation without exploring all
 279 equivalent paths.

280 4.2. Transmission model

281 To evaluate the impact of the switching fabric on the QoT, numerical simulations have been
 282 first carried out in the Synopsys OptSim™ Photonic Circuit simulation environment [28],
 283 testing an 8×8 Beneš switch base on an OSE implemented with the second order coupling
 284 MZI previously described. Due to the relative low-loss flat-band behavior of the OSE, the
 285 critical components in the device, especially concerning routing optimization, are the waveguide
 286 crossings, which introduce path-dependent losses and attenuation in the propagating signals. It
 287 must also be remarked that for strict-sense Beneš structures ($N = 2^x$, $x \in \mathcal{N}$) the number of
 288 switches encountered by each signal is equal, independently from the OSE control signals, as
 289 shown in Fig. 6a, highlighting the critical task in characterizing the control states dependent QoT
 290 impairments due to the stages interconnects.

291 The designed waveguide crossing introduces an average 0.2 dB–0.3 dB loss for each instance,
 292 with a small spectral variance, as depicted in Fig. 6b. While the crossings have been accounted
 293 for the penalty evaluation, the interconnect waveguides and bent sections have not, due to their
 294 generally negligible effect in a properly designed layout. The general schematic of the simulated
 295 setup is depicted in Fig. 6c. We assumed eight input signals spaced $\Delta f = 100$ GHz with a central
 296 frequency of $f_c = 193$ THz. The simulated signals consisted of PM-16-QAM modulated streams
 297 at $B_r = 60$ GBaud, which are then demodulated at the receiver side, extracting the Bit-Error
 298 Rate (BER) as a function of the OSNR. These measurements are then expressed as QoT Penalty

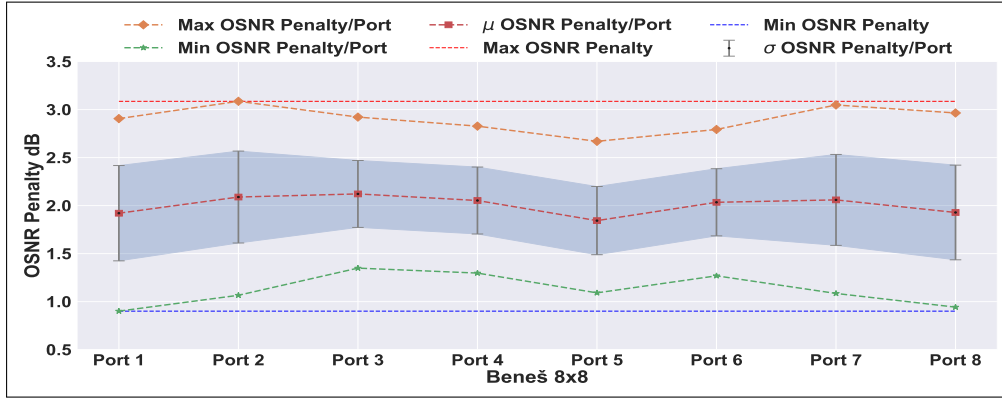


Fig. 7. Statistical analysis of OSNR Penalties for each output port.

299 (in decibel), comparing to the trend of the back-to-back TX/RX system evaluated without the
 300 switching fabric. Due to the previously discussed non-polynomial increase of the solution space,
 301 the characterization of the full system through a look-up table solution is not feasible, especially
 302 at the transmission level, due to the high computational costs of such simulations. In order to
 303 train the proposed ML algorithm, it is necessary to build a dataset of simulated configurations,
 304 measuring the QoT Penalty for a random sub-set of control signals.

305 The simulation dataset has been generated for $N_{sim} = 5000$ random control configurations,
 306 allowing equivalent paths (output permutation) but enforcing individual control states to avoid
 307 erroneous training by repeating the same OSE states. The general distribution of the OSNR
 308 Penalties for the simulated dataset is shown in Fig. 7: as expected, the distribution has a relatively
 309 uniform average value of $\mu = 2$ dB for every output port, with a comparable standard deviation.
 310 To characterize the device in SDN controlled environment, it is important to highlight the
 311 maximum value of the penalty: $\Delta OSNR_{max} \approx 3.1$ dB. Without a control unit capable of a reliable
 312 prediction of the expected penalty in real-time, the impact of switching on QoT must always be
 313 over-estimated to this maximum value, which represents an infrequent worst-case assumption.
 314 To this end, the ML agent allows more flexible control of the device, highlighting the cases
 315 where a higher transmission rate can be applied due to a lower penalty. Furthermore, in Fig. 7
 316 every data-point corresponds to one of the different equivalent solutions, highlighting the average
 317 penalty for all the output ports, as well as the minimum and maximum values. It is clear how a
 318 real-time control strategy can be employed to optimize the performance of such a device. At the
 319 same time, the average port penalties are identical between configurations; the lower variance
 320 solutions offer a better alternative, as the QoT is more uniform between all the output ports of the
 321 configuration.

322 5. Machine learning modeling for QoT impairment

323 This section illustrates the details of the proposed ML framework and explains the complete
 324 workflow of training and testing phases. It also describes the architecture of the main cognitive
 325 engine of the proposed ML module, along with the definition of features, labels, and additional
 326 tuning and control parameters. The final ML module will be integrated as an application program
 327 interface (API) inside the controller.

328 The proposed supervised ML-based framework works in a complete black-box manner,
 329 requiring only substantial training data to develop a cognitive model without considering the
 330 photonic circuit internal topology. Like all other supervised ML techniques, to complete the
 331 training and prediction procedures, the proposed model requires defining the features and labels

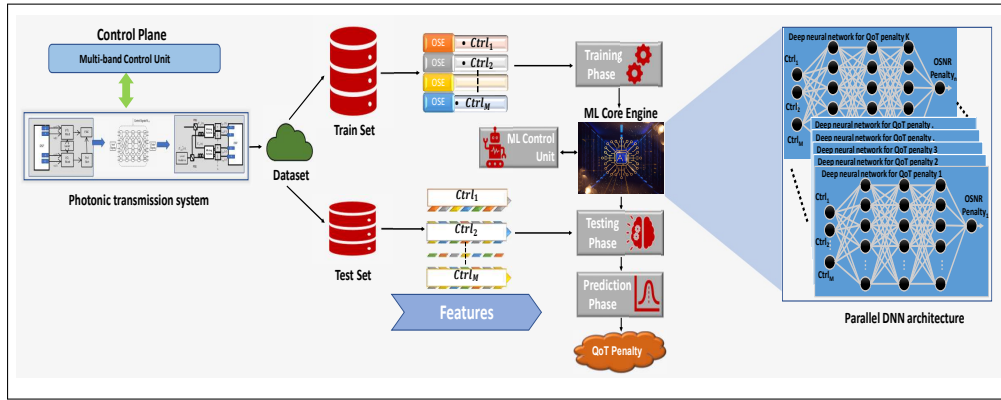


Fig. 8. Schematic of the ML module with Parallel DNN architecture

332 that represent the system inputs and outputs, respectively. The manipulated features include the
 333 different permutations of the OSE control signals ($Ctrl_1, Ctrl_2, Ctrl_3, \dots, Ctrl_M$) at the control
 334 ports of the photonic switch and utilize QoT Penalty of the k -th output port of the considered
 335 photonic switch as labels shown in Fig. 8.

336 A deep neural network (DNN) [29] is considered to develop the cognition in the ML engine
 337 as it is the potential tool that is frequently used in different applications in various fields. The
 338 proposed DNN is built by using a higher-level API of the open-source TensorFlow[®] library [30],
 339 which offers a variety of learning algorithms along with data processing functions to improve the
 340 quality of the generated dataset. The core engine of DNN is configured by various optimized
 341 hyper-parameters such as the *training steps*, set to 1000; the optimizer is loaded with the *adaptive*
 342 *gradient algorithm (ADAGRAD)* Keras optimizer, with a default *learning rate* of 10^{-2} and L_1
 343 regularization is set to 10^{-3} to acquire the computational advantage by avoiding the features with
 344 zero coefficients [31]. Additionally, numerous non-linear activation functions such as *Relu*, *tanh*,
 345 *sigmoid*. have been tested during the model build-up. Later, *Relu* has been selected to feed in
 346 DNN as it outperforms the others in terms of prediction and computational load [32].

347 Furthermore, another essential DNN hyper-parameter is the number of hidden-layers. The
 348 proposed model core engine has been tuned on considerable numbers of hidden-layers and
 349 neurons to reach the best trade-off between accuracy and computational time. Even though an
 350 increase in the number of layers and neurons enhances the accuracy of the DNN up to a certain
 351 level, a further increase in the values of these parameters introduces diminishing returns that
 352 cause over-fitting of the model and, at the same time, increases the computational time. After
 353 this complex trade-off assessment, we decided upon a DNN with three hidden-layers with ten
 354 artificial neurons for each hidden layer optimized for the considered dimension N . To enhance
 355 prediction performance, we propose to use a parallel architecture for the DNN as shown in
 356 Fig. 8. In reality, we have an autonomous DNN to predict the QoT Penalty against each k -th
 357 output port of the considered $N \times N$ photonic switch. The parallel architecture of DNN better
 358 exploits the augmented information in the provided dataset for each output port, which gives
 359 better cognition to the core DNN engine and consequently achieves high efficiency in terms of
 360 prediction. Initially, the core DNN engine training is performed; after that, the trained model is
 361 tested on a separate subset of the dataset: the conventional rule of thumb 70% and 30% have
 362 been opted to split the generated dataset. The train set is 70% while the test set is 30% of the
 363 total generated dataset reported subsection 4.2. Each of the individual DNN modules in the
 364 parallel architecture is provided with the same set of features ($Ctrl_1, Ctrl_2, Ctrl_3, \dots, Ctrl_M$, i.e.,
 365 OSE control signals) as an input during training and retrieves OSNR Penalty $_{i,k}$ for each port k

366 of the proposed UWB Beneš switch as an output label. In order to prevent over-fitting of the
 367 DNN, the *training step* is considered as the stopping factor while the *mean square error* (MSE)
 368 is applied as a loss function, given by

$$\text{QoT MSE} = \frac{1}{n} \sum_{i=0}^n \left(\frac{1}{N} \sum_{k=1}^N \left(\text{OSNR Penalty}_{i,k}^p - \text{OSNR Penalty}_{i,k}^a \right)^2 \right) \quad (1)$$

369 where n is the number of test realizations, N is the total number of input/output ports of the
 370 specific $N \times N$ switching system and $\text{OSNR Penalty}_{i,k}^p - \text{OSNR Penalty}_{i,k}^a$ are the predicted and
 371 actual OSNR Penalties of the k -th output port of the considered topology.

372 6. Results and discussion

373 This section demonstrates the accuracy of proposed ML modules in delivering QoT impairments
 374 predictions for UWB photonics switching architectures. The ML module exploits the deterministic
 375 switch control states to obtain the QoT impairments in terms of $\text{OSNR Penalty}_{i,k}$ for each port k
 376 of the proposed UWB Beneš switch. In addition to this, a complete case study is also analyzed to
 377 reveal the effectiveness of the proposed ML-based QoT Penalty estimation model for the photonic
 378 switching system.

379 The proposed ML cognitive engine manipulates the deterministic control states as input and
 380 exploits the QoT Penalty as an output. The metric utilized to assess the accuracy of the ML
 381 model is defined as:

$$\Delta \text{OSNR}_{i,k} = \text{OSNR Penalty}_{i,k}^a - \text{OSNR Penalty}_{i,k}^p \quad (2)$$

382 where the parameters reported in Eq. 2 have the same meaning as in Eq. 1. The reliability of
 383 the proposed ML-based QoT model is verified by analyzing its performance at each port of the
 384 proposed 8×8 Beneš switch. The distribution of ΔOSNR s of all the ports of the 8×8 Beneš are
 385 shown in Fig. 9, along with their mean (μ) and standard deviation (σ) statistics.

386 In Fig. 9, all the distributions of ΔOSNR s are split up into two slices by the red dotted line
 387 ($\Delta \text{OSNR} = 0$). The portion area where $\Delta \text{OSNR}s \leq 0$ is not critical as $\text{OSNR Penalty}_{i,k}^a \leq$
 388 $\text{OSNR Penalty}_{i,k}^p$ so, in this case we only waste some capacity but the system will never
 389 turn into out-of-service. In contrast the section where $\Delta \text{OSNR}s > 0$ is the critical one as
 390 $\text{OSNR Penalty}_{i,k}^a > \text{OSNR Penalty}_{i,k}^p$. In this case, it is required to deploy some margin on top
 391 of the ML prediction to keep the system working all the time. The maximum required margins
 392 (δ_k) for this case where $\Delta \text{OSNR}s > 0$ are shown as a green line for each port k of the 8×8 Beneš.

393 Inspecting the required margin, we observe the high level of accuracy achieved operating ML
 394 model for QoT impairments estimation. The proposed 8×8 Beneš, the worst-case prediction
 395 performance is observed on port 5; the δ_5 is less than 0.12 dB. With the availability of such
 396 accurate prediction, we can envision that in practical applications, the OSNR Penalty margin on
 397 top of the ML prediction can be reduced to 0.12 dB for Beneš 8×8 . Furthermore, the prediction
 398 asymmetry between the different port of the device, is due to the intrinsic randomness and limited
 399 size of the provided data-set, leading to better training for the prediction of certain paths. Under
 400 the envisioned case-study, a drastically smaller data-set has been provided by choice to the ML
 401 agent with respect to the complete device configuration set. Even under this limited training
 402 scenario, the asymmetry between the port predictions is still marginal with respect to the QoT
 403 optimization available through this method deployment.

404 The effectiveness of the proposed ML-based QoT impairments estimation model is further
 405 demonstrated by considering the optimality routing issue: the ML agent can be used to optimize
 406 the routing solution in conjunction with the previously described routing algorithm. Taking as
 407 an example a target output request such as $[1, 2, 3, 4, 5, 6, 7, 8] \rightarrow [7, 6, 3, 8, 5, 4, 1, 2]$, we
 408 observe that 32 different combinations of the control states exist leading to the desired output

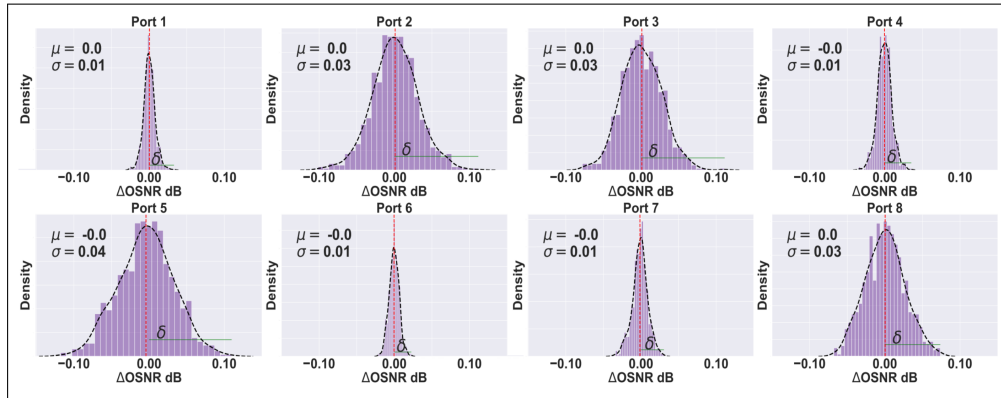


Fig. 9. Probability density functions of ΔOSNR for each port of the 8x8 Beneš switch. Average values μ and variances σ indicated for the individual cases are expressed in decibel.

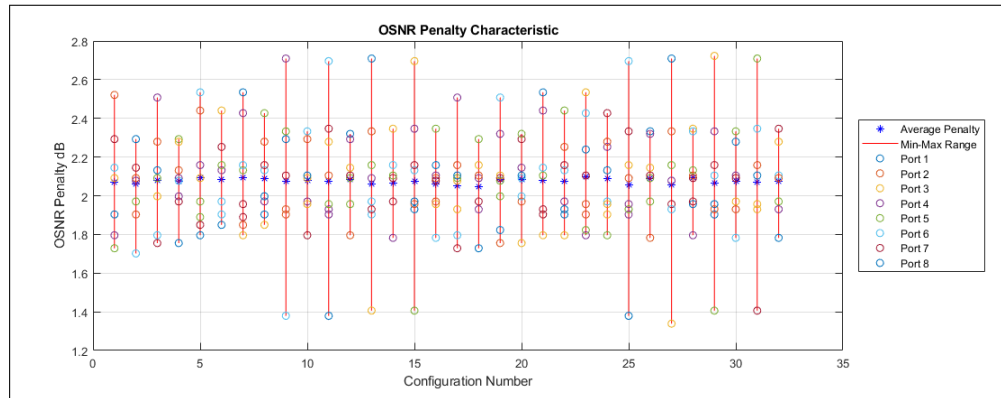


Fig. 10. OSNR Penalty distribution for 32 nominally equivalent control states generating the output pattern [7, 6, 3, 8, 5, 4, 1, 2]. A label from 1 to 32 has been assigned to each control state according to the order it is generated by the proposed algorithm.

409 pattern. The designed routing algorithm is able to evaluate all these nominally equivalent routing
 410 solutions, which have been tested in order to characterize their penalty and statistical distribution,
 411 as shown in Fig. 10. The average penalty for every equivalent configuration is reasonably similar,
 412 while the main difference is found between the standard deviation between the penalty of each
 413 port. The ML agent could provide real-time control optimization for this application, minimizing
 414 the overall penalty and avoiding high deviation solutions. This target goal allows for a similar
 415 penalty factor between all the output signals, minimizing the overall deviation, although different
 416 criteria could provide alternative solutions depending on the overall control goal. The choice of
 417 the *best* control state depends on the selected metric: considering the results introduced in
 418 Fig. 10, configuration number 18 provides the minimal deviation between the alternative routings,
 419 while solution number 27 could be selected if only the minimum penalty is considered as the
 420 optical metric.

421 7. Conclusions

422 Optical network elements currently exploit PICs to carry out most of the complex functions at
423 the photonic level; specifically, optical networks and data centers progressively utilize large-scale
424 photonic switches and wavelength selective switches due to their wide-band abilities together
425 with low latency and low power consumption. This increased use of photonic switching systems
426 creates a massive demand for a generic management model that works in an entirely topological
427 and technological agnostic way.

428 This work introduced the concept of a softwarized and autonomous management of PIC-based
429 UWB optical switches for software-defined open optical networks. The proposed method can
430 model any $N \times N$ UWB switching system at two different levels of abstraction: the routing and
431 the QoT levels related to the applied control signals. The routing level problem is solved by
432 considering the black-box abstraction of the 2×2 cross-bar switching units. At the same time, for
433 the QoT, an ML-based framework is proposed to predict the QoT degradation due to the switching
434 element. The proposed model works in a topological and technological agnostic *blind* way,
435 exploiting neural network to model the QoT impairments of any $N \times N$ UWB photonic switch.

436 The operated data-driven technique is easily scalable to larger input dimensions N as a high
437 level of accuracy can be achieved with limited-size datasets. Besides this, the proposed two-level
438 abstraction scheme can be further expanded to evaluate the performance of any $N \times N$ optical
439 switch on the network layer metrics. Furthermore, the model achieved promising results in
440 predicting QoT degradation; the error in predicting QoT degradation is less than 0.12 dB. With
441 the availability of such accurate prediction, we can envision that in practical applications, the
442 required QoT margin on top of the ML prediction can be reduced to 0.12 dB for the considered
443 Beneš 8x8 architecture.

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448 **Data Availability Statement.** Data underlying the results presented in this paper are not publicly available
449 at this time but may be obtained from the authors upon reasonable request.

450 References

- 451 1. A. Ferrari, A. Napoli, J. K. Fischer, N. Costa, A. D'Amico, J. Pedro, W. Forysiak, E. Pincemin, A. Lord, A. Stavdas,
452 J. P. F.-P. Gimenez, G. Roelkens, N. Calabretta, S. Abrate, B. Sommerkorn-Krombholz, and V. Curri, "Assessment
453 on the achievable throughput of multi-band ITU-T G.652.D fiber transmission systems," *J. Light. Technol.* **38**,
454 4279–4291 (2020).
- 455 2. C.-S. Li and W. Liao, "Software defined networks," *IEEE Commun. Mag.* **51**, 113–113 (2013).
- 456 3. M. Jinno, T. Ohara, Y. Sone, A. Hirano, O. Ishida, and M. Tomizawa, "Elastic and adaptive optical networks: possible
457 adoption scenarios and future standardization aspects," *IEEE Commun. Mag.* **49**, 164–172 (2011).
- 458 4. V. Curri, A. Carena, A. Arduino, G. Bosco, P. Poggiolini, A. Nespola, and F. Forghieri, "Design strategies and merit
459 of system parameters for uniform uncompensated links supporting Nyquist-WDM transmission," *J. Light. Technol.*
460 **33**, 3921–3932 (2015).
- 461 5. V. Curri, "Software-defined wdm optical transport in disaggregated open optical networks," in *2020 22nd International
462 Conference on Transparent Optical Networks (ICTON)*, (2020), pp. 1–4.
- 463 6. K. Suzuki, R. Konoike, J. Hasegawa, S. Suda, H. Matsuura, K. Ikeda, S. Namiki, and H. Kawashima, "Low-insertion-
464 loss and power-efficient 32×32 silicon photonics switch with extremely high- δ silica plc connector," *J. Light.
465 Technol.* **37**, 116–122 (2019).
- 466 7. Q. Cheng, L. Y. Dai, N. C. Abrams, Y.-H. Hung, P. E. Morrissey, M. Glick, P. O'Brien, and K. Bergman,
467 "Ultralow-crosstalk, strictly non-blocking microring-based optical switch," *Photon. Res.* **7**, 155–161 (2019).
- 468 8. J. Kim, C. Nuzman, B. Kumar, D. Lieuwen, J. Kraus, A. Weiss, C. Lichtenwalner, A. Papazian, R. Frahm,
469 N. Basavanthally, D. Ramsey, V. Aksyuk, F. Pardo, M. Simon, V. Lifton, H. Chan, M. Haueis, A. Gasparyan,
470 H. Shea, S. Arney, C. Bolle, P. Kolodner, R. Ryf, D. Neilson, and J. Gates, "1100 x 1100 port MEMS-based optical
471 crossconnect with 4-dB maximum loss," *IEEE Photonics Technol. Lett.* **15**, 1537–1539 (2003).
- 472 9. A. N. Dames, "Beam steering optical switch," (2008). US Patent 7,389,016.

- 473 10. Y. Huang, Q. Cheng, Y.-H. Hung, H. Guan, X. Meng, A. Novack, M. Streshinsky, M. Hochberg, and K. Bergman,
474 "Multi-stage 8×8 silicon photonic switch based on dual-microring switching elements," *J. Light. Technol.* **38**,
475 194–201 (2020).
- 476 11. D. Opferman and N. Tsao-Wu, "On a class of rearrangeable switching networks part I: Control algorithm," *The Bell*
477 *Syst. Tech. J.* **50**, 1579–1600 (1971).
- 478 12. M. Ding, Q. Cheng, A. Wonfor, R. V. Penty, and I. H. White, "Routing algorithm to optimize loss and IPDR for
479 rearrangeably non-blocking integrated optical switches," in *2015 Conference on Lasers and Electro-Optics (CLEO)*,
480 (2015), pp. 1–2.
- 481 13. Y. Qian, H. Mehrvar, H. Ma, X. Yang, K. Zhu, H. Fu, D. Geng, D. Goodwill, P. Dumais, and E. Bernier, "Crosstalk
482 optimization in low extinction-ratio switch fabrics," in *2014 Optical Fiber Communication (OFC)*, (2014), pp. 1–3.
- 483 14. Q. Cheng, Y. Huang, H. Yang, M. Bahadori, N. Abrams, X. Meng, M. Glick, Y. Liu, M. Hochberg, and K. Bergman,
484 "Silicon photonic switch topologies and routing strategies for disaggregated data centers," *IEEE J. Sel. Top. Quantum*
485 *Electron.* **26**, 1–10 (2020).
- 486 15. W. Gao, L. Lu, L. Zhou, and J. Chen, "Automatic calibration of silicon ring-based optical switch powered by machine
487 learning," *Opt. Express* **28**, 10438–10455 (2020).
- 488 16. I. Khan, M. Chalony, E. Ghillino, M. U. Masood, J. Patel, D. Richards, P. Mena, P. Bardella, A. Carena, and V. Curri,
489 "Effectiveness of machine learning in assessing QoT impairments of photonics integrated circuits to reduce system
490 margin," in *2020 IEEE Photonics Conference (IPC)*, (2020), pp. 1–2.
- 491 17. I. Khan, M. Chalony, E. Ghillino, M. U. Masood, J. Patel, D. Richards, P. Mena, P. Bardella, A. Carena, and V. Curri,
492 "Machine learning assisted abstraction of photonic integrated circuits in fully disaggregated transparent optical
493 networks," in *2020 22nd International Conference on Transparent Optical Networks (ICTON)*, (2020), pp. 1–4.
- 494 18. H. Zhou, Y. Zhao, X. Wang, D. Gao, J. Dong, and X. Zhang, "Self-configuring and reconfigurable silicon photonic
495 signal processor," *ACS Photonics* **7**, 792–799 (2020).
- 496 19. I. Khan, L. Tunesi, M. Chalony, E. Ghillino, M. U. Masood, J. Patel, P. Bardella, A. Carena, and V. Curri, "Machine-
497 learning-aided abstraction of photonic integrated circuits in software-defined optical transport," in *Next-Generation*
498 *Optical Communication: Components, Sub-Systems, and Systems X*, vol. 11713 (SPIE, 2021), p. 117130Q.
- 499 20. I. Khan, L. Tunesi, M. U. Masood, E. Ghillino, P. Bardella, A. Carena, and V. Curri, "Automatic management of
500 $N \times N$ photonic switch powered by machine learning in software-defined optical transport," *IEEE Open J. Commun.*
501 *Soc.* **2**, 1358–1365 (2021).
- 502 21. I. Khan, L. Tunesi, M. U. Masood, E. Ghillino, P. Bardella, A. Carena, and V. Curri, "Machine learning assisted
503 model of qot penalties for photonics switching systems," in *Photonics in Switching and Computing 2021*, (Optical
504 Society of America, 2021), p. M2A.3.
- 505 22. R. Proietti, X. Chen, Y. Shang, and S. J. B. Yoo, "Self-driving reconfiguration of data center networks by deep
506 reinforcement learning and silicon photonic Flex-LION switches," in *2020 IEEE Photonics Conference (IPC)*, (2020),
507 pp. 1–2.
- 508 23. S. Salman, C. Streiffer, H. Chen, T. Benson, and A. Kadav, "DeepConf: Automating data center network topologies
509 management with machine learning," in *Proceedings of the 2018 Workshop on Network Meets AI & ML*, (Association
510 for Computing Machinery, New York, NY, USA, 2018), NetAI'18, pp. 8–14.
- 511 24. R. Orta, G. Perrone, R. Tascone, A. Fincato, M. Lenzi, S. Lorenzotti, and P. Nugent, "Design technique for wideband
512 optical couplers," in *Fiber Optic Network Components*, vol. 2449 (SPIE, 1995), pp. 375 – 383.
- 513 25. C. Clos, "A study of non-blocking switching networks," *Bell Syst. Tech. J.* **32**, 406–424 (1953).
- 514 26. C. Chang and R. Melhem, "Arbitrary size benes networks," *Parallel Process. Lett.* **7**, 279–284 (1997).
- 515 27. A. Chakrabarty, M. Collier, and S. Mukhopadhyay, "Matrix-based nonblocking routing algorithm for Beneš networks,"
516 in *Future computing 2009*, (IEEE, 2009), pp. 551–556.
- 517 28. E. Ghillino, E. Virgillito, P. V. Mena, R. Scarmozzino, R. Stoffer, D. Richards, A. Ghiasi, A. Ferrari, M. Cantono,
518 A. Carena, and V. Curri, "The Synopsys software environment to design and simulate photonic integrated circuits: A
519 case study for 400G transmission," in *2018 20th International Conference on Transparent Optical Networks (ICTON)*,
520 (2018), pp. 1–4.
- 521 29. C. Bishop, *Pattern Recognition and Machine Learning: All "just the Facts 101" Material*, Information science and
522 statistics (Springer (India) Private Limited, 2013).
- 523 30. <https://www.tensorflow.org/>.
- 524 31. J. Duchi, E. Hazan, and Y. Singer, "Adaptive subgradient methods for online learning and stochastic optimization," *J.*
525 *Mach. Learn. Res.* **12**, 2121–2159 (2011).
- 526 32. C. Nwankpa, W. Ijomah, A. Gachagan, and S. Marshall, "Activation functions: Comparison of trends in practice and
527 research for deep learning," in *2nd International Conference on Computational Sciences and Technology*, (2021), pp.
528 12–133.