

Point Defects in Two-Dimensional Indium Selenide as Tunable Single-Photon Sources

Mattia Salomone, Michele Re Fiorentin,* Giancarlo Cicero, and Francesca Risplendi*

Cite This: *J. Phys. Chem. Lett.* 2021, 12, 10947–10952

Read Online

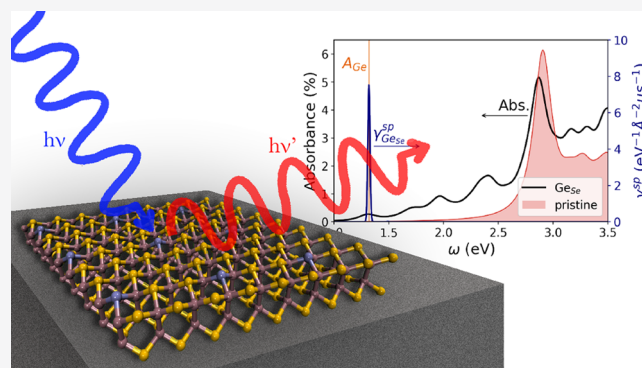
ACCESS |

Metrics & More

Article Recommendations

Supporting Information

ABSTRACT: In the past few years remarkable interest has been kindled by the development of nonclassical light sources and, in particular, of single-photon emitters (SPE), which represent fundamental building blocks for optical quantum technology. In this Letter, we analyze the stability and electronic properties of an InSe monolayer with point defects with the aim of demonstrating its applicability as an SPE. The presence of deep defect states within the InSe band gap is verified when considering substitutional defects with atoms belonging to group IV, V, and VI. In particular, the optical properties of Ge as substitution impurity of Se predicted by solving the Bethe–Salpeter equation on top of the GW corrected electronic states show that transitions between the valence band maximum and the defect state are responsible for the absorption and spontaneous emission processes, so that the latter results in a strongly peaked spectrum in the near-infrared. These properties, together with a high localization of the involved electronic states, appear encouraging in the quest for novel SPE materials.



Photonic technologies are considered the most promising future steps for industrial and scientific innovation. With wide-reaching applications, from sensors for biomedical imaging to superfast computers and ultrasecure communication, photonics may provide solutions to many challenges in our daily lives.^{1–4} In particular, on-demand and truly scalable sources of indistinguishable single photons, otherwise called single-photon emitters (SPEs), represent fundamental building blocks for optical quantum technologies.^{5–8} Given the importance of quantum light in both remote quantum computing and quantum communication, the search for reliable and efficient SPEs is a thriving open field. In fact, existing lasers are inherently unsuitable to generate single photons, and new compact and more reliable single-photon sources that could be easily integrated into quantum optics applications are needed.⁸

Promising structures behaving as SPEs consist of atom-like systems that intrinsically emit one photon at a time. These have been obtained by generating isolated color centers in three-dimensional and two-dimensional semiconductor materials such as diamond,^{9–12} and hexagonal boron nitride h-BN,^{11–13} as well as in one-dimensional materials, such as carbon nanotubes¹⁴ and InP nanowires,¹⁵ and zero-dimensional materials, such as GaAs and InGaAs quantum dots.^{16,17} To achieve efficient single-photon emission, it is mandatory to avoid electron/hole recombination, which ultimately implies that the electron energy levels of the atom-like structure, for example arising from substitutional defects, must be deep in

the host matrix band gap. In this respect, materials with wide energy gaps are the most suitable candidates to be used as matrixes for single-photon emitters. In addition, sharp optical transitions and narrow emission peaks require that the impurity orbitals do not hybridize strongly with the host material¹⁸ orbitals; that is, the impurity states must be flat without showing dispersion in reciprocal space.

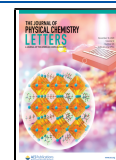
Transition metal dichalcogenides (TMDs) have shown unprecedented features which make them optimal materials for single-photon sources.³ TMDs are characterized by a layered structure held together by weak van der Waals forces. These can be reduced to a single layer by simple exfoliation or other means.^{19–21} The 2D systems obtained in this way have the advantage of exhibiting strong light–matter interaction and large exciton binding energy. Optical confinement and emission can be further tailored either by stacking more than a single layer or by applying external electrostatic²² or strain^{3,23,24} fields. Among the others, single-photon emitters have been obtained with WSe₂^{25,26} and WS₂,²⁷ and narrow emission lines of localized centers have been found in MoSe₂.²⁸

Received: September 3, 2021

Revised: October 18, 2021

Accepted: October 27, 2021

Published: November 4, 2021



too. Recently, single-photon emission was discovered in other metal chalcogenides, such as GaSe. In this compound, local deformations of the crystal trap excitons⁷ are responsible for SP emission.^{3,24,29} These discoveries have stimulated the search for better single-photon sources in other two-dimensional metal chalcogenides.

In this Letter, we propose the use of InSe as SPE and show how to tailor its optical emission by introducing substitutional defects in its monolayer structure. The focus on this material has been stimulated by experimental evidence that as-grown InSe presents selenium vacancies at its surface and that these defects can be passivated³⁰ by introducing different types of heteroatoms (Se substitutional defects, X_{Se}). Further, several studies^{3,31} have evidenced that 2D InSe, whose structure and band diagram are reported in Figure 1, is characterized by a

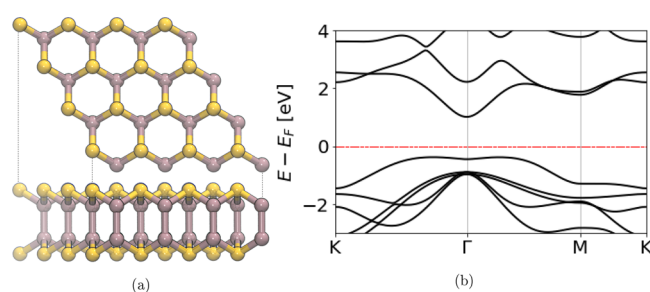


Figure 1. Left panel: top and side views of an InSe monolayer. Se atoms are represented in yellow, while In atoms are in gray. Right panel: InSe band structure calculated at the DFT-PBE level.

reduced valley hybridization and a relatively large band gap. These features are expected to give rise to little dispersion of impurity states and consequently to originate single-atom-like behavior of substitutional defects. As such, the InSe monolayer presents some important prerequisites required to effectively function as an SPE host matrix. The strong light–matter interaction reported³² for InSe may further boost optical SPE efficiency. In this study we consider the passivation of selenium vacancies with atomic species of the IV, V, and VI group of the periodic table (namely Ge, As, P, N, S, and O) and calculate the optoelectronic properties of the resulting structures by means of *ab initio* simulations. Our results highlight that some of the proposed structures show sharp optical transitions involving flat atom-like impurity states, which could be stimulated on demand, for example by coupling the two-level system to a resonant cavity.^{33–36} Further, it is shown that the emitted frequency can be tuned by changing the depth and localization of the defect level by changing the atomic species used to saturate the vacancy sites.

Calculations are based on spin-polarized DFT as implemented in the Quantum Espresso package.^{37,38} We employ ultrasoft pseudopotentials³⁹ to describe the electron–ion interaction and the gradient-corrected Perdew–Burke–Ernzerhof (PBE) functional⁴⁰ to describe the exchange–correlation effects. Computational details can be found in the Supporting Information. To overcome the limitations of DFT in the estimation of the electronic band gap and optical properties, we apply many-body perturbation theory (MBPT) to systems that appear most promising after the DFT screening. The band structure is corrected within the G_0W_0 approximation, and the optical absorption is studied by solving the Bethe–Salpeter equation (BSE).⁴¹ All post-DFT calculations are performed by means of the YAMBO code.⁴² Details

on the MBPT convergence procedure and parameters are reported in the Supporting Information.

We first compare the impurity defect formation energies with the vacancy formation energy, E_{Form} , computed in the low-concentration limit as defined in the Supporting Information. All X_{Se} species considered in this study, except for germanium and nitrogen, yield E_{Form} values smaller than the vacancy formation energy along the whole range of variability of the In and Se chemical potentials (*cf.* the Supporting Information). The E_{Form} of Ge_{Se} and N_{Se} defects are comparable to the cost of generating a vacancy in the lattice. Because vacancies are widely observed in experimental samples,^{43–45} the obtained E_{Form} values point at technologically achievable substitutions. As a general trend we observe that E_{Form} decreases along the columns of the periodic table (from the second to the third row) and decreases along the rows (from right to left): impurities with dimensions closer to Se are more favorable (see Figure S1 of the Supporting Information). Interestingly, O and S substitutions show negative formation energies confirming the experimentally observed tendency of InSe to spontaneously incorporate oxygen when exposed to air.^{30,43,44}

The modifications of the electronic properties of InSe induced by vacancies and substitutional impurities are analyzed in terms of band structure, density of states (DOS), projected density of states (pDOS), and spatial distribution of the charge densities associated with defect states. In addition, we report the positions of defect levels (E^d) referred to the Fermi level.

InSe containing selenium vacancies presents fully occupied defect states (*i.e.*, donor states) in the energy gap, as also shown in the band diagram reported in Figure 2a (left panel). These one-electron states have predominantly P_{Se} character with some hybridization with In p orbitals, while the lower conduction band has mainly S_{In} and P_{In} character. Considering the total DOS and the projections on Se and In species, also reported in Figure 2a, it is worth noting that both Se and In atoms contribute to the defect states. Moreover, Figure 2a (right panel) shows that the charge density associated with these states is spatially localized around the Se vacancy and equally distributed around surrounding atoms (both Se and In). In this structure, the defect state coincides with the highest occupied state, and it is localized below the Fermi energy. The corresponding lowest electronic transition has defect level–conduction band minimum (D-CBm) character, and it occurs at approximately 1 eV.

When Se vacancies are saturated with group VI species (O and S), vacancy defect states are pushed down in energy and become degenerate with states of InSe valence band (VB). This is an indication that the bonds between these atoms and the nearby In atoms are somewhat similar to that of In–Se bonds, thus resulting in a complete saturation of the dangling bonds around the vacancy site. Indeed, in this case the highest occupied state is delocalized on the whole 2D layer and does not show localization typical of impurity states. This is clearly visible in the first panel of Figure 2b. Further, this finding shows that even when present as residual impurity after InSe growth or when used to saturate possible residual vacancy sites, group VI species do not have detrimental effects on InSe optical properties because they do not originate trap states in the gap but rather eliminate them.

Figure 2c shows the DOS/pDOS, the band diagram (left panel), and the electron density of the highest occupied state (right panel) when phosphorus substitutes selenium atoms.

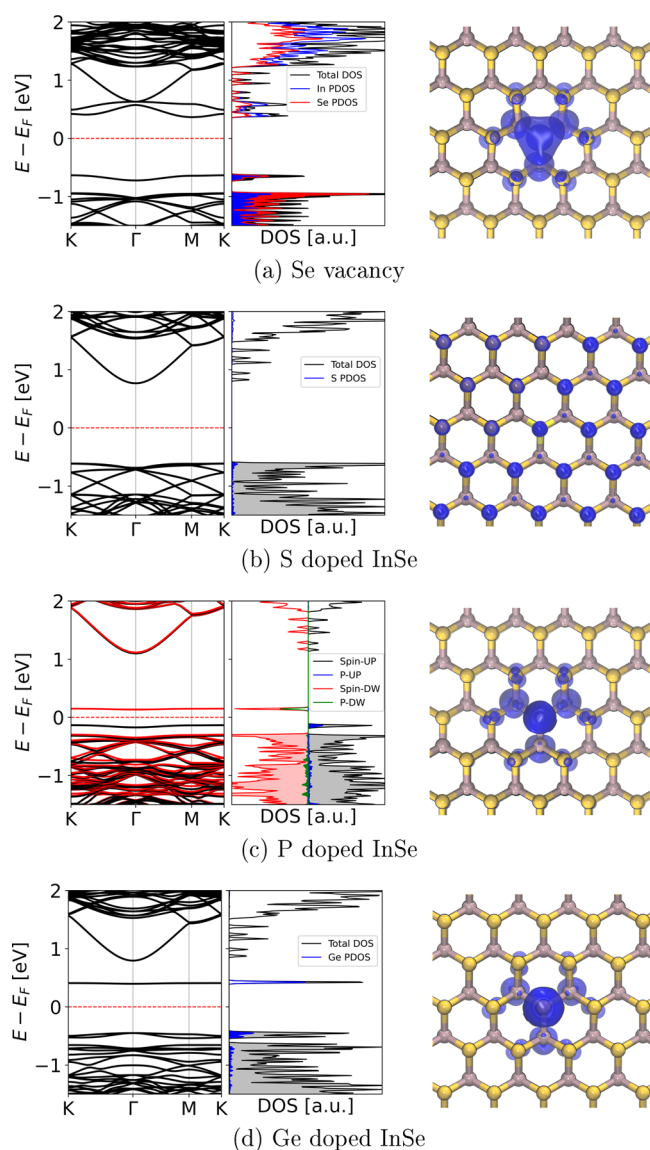


Figure 2. Band structures, density of states, and defect level spatial localization of InSe monolayer computed in 4×4 supercells with different lattice modifications: In panel (a) it is possible to see a purely donor defect state. In panel (d) the defect level is completely empty (acceptor state), whereas in panel (c) the defect level is split because of spin polarization. In panel (b), instead, the defect level is degenerate with the VB.

Other group V species yield similar results in terms of electronic structure (see the values reported in Table 1). In particular, P originates defect states in the InSe band gap characterized by different spin. The unoccupied state results at ~ 1.3 eV below the bottom of the conduction band, whereas the occupied state is ~ 0.4 eV above the valence band. Two low-energy transitions can be defined in this case, one corresponding to D-CBm and the other one related to VBM-D, which are characterized by $E_{\text{Trans}} = 1.29$ and 0.45 eV, respectively.

Results for Ge impurity substituting Se are shown in Figure 2d, as representative of the group IV species. The DOS presents a narrow peak within the InSe band gap as a result of an almost perfectly flat defect level. At variance with the cases of Se vacancy and group V impurities, Ge defect states fall closer to the CB and well above the Fermi level, thus behaving

Table 1. DFT Results on Vacancy and Substitutional Defects in Monolayer InSe^a

defect type	E^d (eV)	transition type	E_{Trans} (eV)
Se vac.	−0.64	D-CBm	1.00
Ge _{Se}	0.42	VBM-D	0.86
N _{Se}	−0.21/0.23	VBM-D/D-CBm	0.50/1.29
P _{Se}	−0.14/0.15	VBM-D/D-CBm	0.45/1.29
As _{Se}	−0.11/0.13	VBM-D/D-CBm	0.40/1.27
O _{Se}		VBM-CBm	1.31
S _{Se}		VBM-CBm	1.45

^a E^d reports the position of the defect state with respect to the Fermi energy. In the case of oxygen and sulphur, which generate defects hybridized with valence band states, E^d has not been calculated. For group IV atoms, we report the two values given by the splitting of the defect states due to spin-polarization. The third column specifies the lowest-energy electronic transitions: VBM-D (D-CBm) marks a transition from the valence band maximum to the defect level (from the defect level to the conduction band minimum). E_{Trans} represents the corresponding transition energies, computed at the DFT level.

as acceptor states ($E^d = 0.42$ eV). The lower electronic energy transition connects VBM-D states and occurs at $E_{\text{Trans}} \approx 0.86$ eV.

Notably, when group IV species substitute Se atoms in InSe monolayer, the contribution of the X_{Se} atom to the DOS of InSe top VB (tVB) and CB is almost negligible (see left panel of Figure 2c), while, in the case of group V substitutions, the tVB is significantly affected by the presence of the defect (left panel of Figure 2d). In fact, for Ge_{Se} the highest occupied band shows such a large contribution from Ge orbitals and low dispersion in k -space that may be as well considered a Ge-induced defect state. Both for group IV and group V substitutions, the electronic states observed within the band gap show dominant pDOS contributions from the heteroatoms. Moreover, the electron density pertaining to these defects is strongly localized around the impurity site (see right panels of Figure 2c,d). This finding confirms that these impurities in InSe monolayer represent promising structures for SPEs.

Considering the extremely small dispersion in energy of the resulting level, its depth within the band gap, and clear acceptor character of Ge modified InSe monolayer, we make an in-depth analysis of the optical features of this system. The study of the stability of Ge_{Se} in different charge states^{46,47} points out that the most representative germanium substitution in intrinsic InSe is charge neutral (*cf.* the Supporting Information). For this reason, our following investigations focus on neutral Ge_{Se} defects. We first obtain its quasi-particle (QP) band structure within the G_0W_0 approximation and then predict its absorption and emission spectra. In Figure 3a we report the QP bands of the Ge_{Se}-defected monolayer, aligned to the VBM and CBm of the pristine InSe monolayer (red-shaded regions), for comparison. It is possible to notice that VBM-D is widened to 2.11 eV and that the tVB of Ge_{Se} is found at higher energies than the pristine VBM. This result supports the previous pDOS analysis, Figure 2d, suggesting that this low-dispersion top valence band is not bulk-like, but rather another Ge-induced defect level. As a consequence of the upshift in energy of tVB in Ge_{Se}, the gap between the VBM and the conduction band above the defect level is reduced to 2.67 eV, while in pristine InSe the band gap is computed to be 2.92 eV, in very good agreement with the literature.^{48,49} The QP energies obtained within the G_0W_0 approximation are used

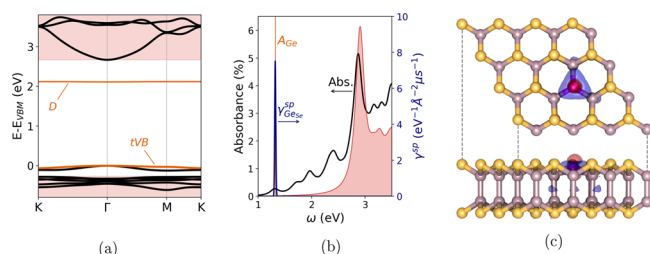


Figure 3. (a) G_0W_0 quasi-particle band structure of the Ge_{Se} defected InSe monolayer in the 4×4 supercell, thick black lines. The shaded red regions mark the valence and conduction bands of pristine InSe monolayer, aligned to the Ge_{Se} VBM. (b) Absorbance of pristine InSe monolayer (shaded region) and Ge_{Se} -defected (thick black line). The vertical line marks the A_{Ge} exciton state. The blue peak represents the spontaneous emission rates $\gamma_{\text{Ge}_{\text{Se}}}^{\text{sp}}$. Absorbance and emission values for Ge_{Se} InSe refer to the simulated 4×4 supercell. (c) Average electron (red) and hole (blue) densities for exciton A_{Ge} in Ge_{Se} InSe.

to build and solve the BSE and obtain the optical properties of the Ge_{Se} -defected monolayer. In Figure 3b we report the absorbance of the defected monolayer (thick black line) and of the pristine InSe monolayer (red-shaded region), as defined in the Supporting Information. The highest absorbance peak of the defected monolayer falls in the close proximity of the absorption peak of pristine InSe (~ 2.88 eV), but several new peaks appear at lower energies. Clearly, the intensities of these additional peaks depend on the simulated defect concentration, *i.e.*, one substitutional defect per 4×4 supercell, corresponding to a defect surface density of ~ 0.45 nm $^{-2}$. However, we have checked that the chosen supercell ensures the suppression of long-range interactions between periodic replicas of the defect, so that the positions of the additional peaks are not affected by finite-size effects. The first absorption peak is due to a bright exciton, A_{Ge} , at $E_{A_{\text{Ge}}} = 1.31$ eV, whose electronic transitions involve the tVB and the defect state D , marked in orange in Figure 3a. A_{Ge} binding energy, $E_{A_{\text{Ge}}}^{\text{b}} = 0.79$ eV, is particularly high, as is common in low-dimensional materials.^{50–52}

Following the excitation, we expect the defected system to relax to the lowest-energy exciton state, so that the zero-phonon line (ZPL)⁵³ of the emission spectrum of Ge_{Se} will originate from the radiative recombination of A_{Ge} . We can gain some insight into this process by computing the spontaneous emission rate γ^{sp} (per unit energy, per unit surface) exploiting the Roosbroeck–Shockley relations,⁵⁴ neglecting exciton–phonon coupling. In Figure 3b, with the blue line, we report the spontaneous emission spectrum of the 4×4 Ge_{Se} supercell, $\gamma_{\text{Ge}_{\text{Se}}}^{\text{sp}}$. Because of the gap in energy between higher-energy exciton states and the lowest-energy one, only exciton A_{Ge} contributes to the ZPL. As in the case of the absorption spectrum, the emission peak intensity depends on the chosen defect concentration, while its position is not affected by the finite-size effect. Independently of the defect density, these results point out that Ge_{Se} monolayers will present an emission of photons with energy $E_{A_{\text{Ge}}} = 1.31$ eV (neglecting exciton–phonon coupling), originating from spatially isolated sources. Indeed, in Figure 3c the red and blue isosurfaces report the average densities of the electron and hole, respectively, bound in A_{Ge} , *cf.* the Supporting Information. It is possible to notice that exciton A_{Ge} is spatially localized around the defect,

ensuring that the studied Ge substitutions are promising candidates of isolated single-photon emitters.

In conclusion, in this Letter, we studied the properties of point defects in InSe obtained through the substitution of selenium atoms with species belonging to groups IV (Ge), V (N, P, and As), or VI (O and S) of the periodic table. The computed formation energies and the analysis of the corresponding band structures show that S and O substitutions can be exploited to saturate dangling bonds (Se vacancy defects) spontaneously present in the experimental sample and cure the 2D layer in a way that does not modify the optical emission or absorption of the pristine monolayer. N, P, As, and Ge substitutions of Se generate defect levels that are well distinct both from the VB and the CB of InSe and allow for new electronic sharp transitions. We have applied MBPT to Ge_{Se} defected monolayer and obtained its absorbance and spontaneous emission spectrum by solving the BSE. We have shown that the defect states in this material realize a single-atom-like system with a low-energy absorption peak due to electronic transitions between the tVB and the defect state. Our results highlight that the proposed Se substitutions, in particular Ge_{Se} , can be attractive for SPE because they possess strong spatial localization; their formation energies are not prohibitive for their employment; and, in particular, the depth of the obtained defect levels guarantees their thermal stabilities and enables electronic transitions which result in emission spectra, which may be stimulated on demand.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpclett.1c02912>.

Details on the DFT, G_0W_0 , and BSE calculations; absorbance and emission rate definitions (PDF)

■ AUTHOR INFORMATION

Corresponding Authors

Francesca Risplendi – Dipartimento di Scienza Applicata e Tecnologia, Politecnico di Torino, 10129 Torino, Italy;

✉ orcid.org/0000-0002-1277-6733;

Email: francesca.risplendi@polito.it

Michele Re Fiorentin – Center for Sustainable Future Technologies, Istituto Italiano di Tecnologia, 10144 Torino, Italy; ✉ orcid.org/0000-0002-1074-0411;

Email: michele.refiorentin@iit.it

Authors

Mattia Salomone – Dipartimento di Scienza Applicata e Tecnologia, Politecnico di Torino, 10129 Torino, Italy;

✉ orcid.org/0000-0002-2689-6138

Giancarlo Cicero – Dipartimento di Scienza Applicata e Tecnologia, Politecnico di Torino, 10129 Torino, Italy;

✉ orcid.org/0000-0002-2920-9882

Complete contact information is available at: <https://pubs.acs.org/doi/10.1021/acs.jpclett.1c02912>

■ ACKNOWLEDGMENTS

The authors acknowledge CINECA for the availability of high-performance computing resources under the Iskra-B initiative, as well as the computational support provided by HPC@POLITO (<http://www.hpc.polito.it>).

REFERENCES

- (1) Aspuru-Guzik, A.; Walther, P. Photonic quantum simulators. *Nat. Phys.* **2012**, *8*, 285–291.
- (2) Lodahl, P.; Mahmoodian, S.; Stobbe, S. Interfacing single photons and single quantum dots with photonic nanostructures. *Rev. Mod. Phys.* **2015**, *87*, 347–400.
- (3) Chakraborty, C.; Vamivakas, N.; Englund, D. Advances in quantum light emission from 2D materials. *Nanophotonics* **2019**, *8*, 2017.
- (4) Lo, H.; Curty, M.; Tamaki, K. Secure quantum key distribution. *Nat. Photonics* **2014**, *8*, 595–604.
- (5) Darquié, B.; et al. Controlled Single-Photon Emission from a Single Trapped Two-Level Atom. *Science* **2005**, *309*, 454–456.
- (6) Knill, E. G.; Laflamme, R.; Milburn, A. A scheme for efficient quantum computation with linear optics. *Nature* **2001**, *409*, 46–52.
- (7) Tonndorf, P.; Schwarz, S.; Kern, J.; Niehues, I.; Pozo-Zamudio, O. D.; Dmitriev, A. I.; Bakhtinov, A. P.; Borisenko, D. N.; Kolesnikov, N. N.; Tartakovskii, A. I.; et al. Single-photon emitters in GaSe. *2D Mater.* **2017**, *4*, 021010.
- (8) Eisaman, M. D.; Fan, J.; Migdall, A.; Polyakov, S. V. Invited Review Article: Single-photon sources and detectors. *Rev. Sci. Instrum.* **2011**, *82*, 071101.
- (9) Aharonovich, I.; Zhou, C.; Stacey, A.; Orwa, J.; Castelletto, S.; Simpson, D.; Greentree, A. D.; Treussart, F. m. c.; Roch, J.-F.; Prawer, S. Enhanced single-photon emission in the near infrared from a diamond color center. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2009**, *79*, 235316.
- (10) Aharonovich, I.; Neu, E. Diamond Nanophotonics. *Adv. Opt. Mater.* **2014**, *2*, 911–928.
- (11) Sipahigil, A.; Jahnke, K. D.; Rogers, L. J.; Teraji, T.; Isoya, J.; Zibrov, A. S.; Jelezko, F.; Lukin, M. D. Indistinguishable Photons from Separated Silicon-Vacancy Centers in Diamond. *Phys. Rev. Lett.* **2014**, *113*, 113602.
- (12) Grosso, G.; Moon, H.; Lienhard, B.; et al. Tunable and high-purity room temperature single-photon emission from atomic defects in hexagonal boron nitride. *Nat. Commun.* **2017**, *8*, 705.
- (13) Re Fiorentin, M.; Kiprono, K. K.; Risplendi, F. Substitutional impurities in monolayer hexagonal boron nitride as single-photon emitters. *Nanomater. Nanotechnol.* **2020**, *10*, 1847980420949349.
- (14) Ma, X.; Hartmann, N.; Baldwin, J.; et al. Room-temperature single-photon generation from solitary dopants of carbon nanotubes. *Nat. Nanotechnol.* **2015**, *10*, 671–675.
- (15) Dalacu, D.; Poole, P. J.; Williams, R. L. Nanowire-based sources of non-classical light. *Nanotechnology* **2019**, *30*, 232001.
- (16) Hours, J.; Varoutsis, S.; Gallart, M.; Bloch, J.; Robert-Philip, I.; Cavanna, A.; Abram, I.; Laruelle, F.; Gérard, J. M. Single photon emission from individual GaAs quantum dots. *Appl. Phys. Lett.* **2003**, *82*, 2206–2208.
- (17) Rakhlin, M.; Belyaev, K.; Klimko, G.; et al. InAs/AlGaAs quantum dots for single-photon emission in a red spectral range. *Sci. Rep.* **2018**, *8*, 5299.
- (18) Sajid, A.; Ford, M. J.; Reimers, J. R. Single-photon emitters in hexagonal boron nitride: a review of progress. *Rep. Prog. Phys.* **2020**, *83*, 044501.
- (19) Sánchez Royo, J. F.; Muñoz-Matutano, G.; Brotons-Gisbert, M.; Martínez-Pastor, J.; Segura, A.; Cantarero, A.; Mata, R.; Canet-Ferrer, J.; Tobias, G.; Canadell, E.; et al. Electronic structure, optical properties, and lattice dynamics in atomically thin indium selenide flakes. *Nano Res.* **2014**, *7*, 1556.
- (20) Sang, D.; Wang, H.; Qiu, M.; Cao, R.; Guo, Z.; Zhao, J.; Li, Y.; Xiao, Q.; Fan, D.; Zhang, H. Two Dimensional β -InSe with Layer-Dependent Properties: Band Alignment, Work Function and Optical Properties. *Nanomaterials* **2019**, *9*, 82.
- (21) Kandemir, A.; Sahin, H. Janus single layers of In₂SSe: A first-principles study. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2018**, *97*, 155410.
- (22) Song, X.-X.; Liu, D.; Mosallanejad, V.; You, J.; Han, T.-Y.; Chen, D.-T.; Li, H.-O.; Cao, G.; Xiao, M.; Guo, G.-C.; et al. A gate defined quantum dot on the two-dimensional transition metal dichalcogenide semiconductor WSe₂. *Nanoscale* **2015**, *7*, 16867–16873.
- (23) Brooks, M.; Burkard, G. Theory of strain-induced confinement in transition metal dichalcogenide monolayers. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2018**, *97*, 195454.
- (24) Linhart, L.; Paur, M.; Smejkal, V.; Burgdörfer, J.; Mueller, T.; Libisch, F. Localized inter-valley defect excitons as single-photon emitters in WSe₂. *Phys. Rev. Lett.* **2019**, *123*, 146401.
- (25) Srivastava, A.; Sidler, M.; Allain, A. V.; Lembke, D. S.; Kis, A.; Imamoglu, A. Optically active quantum dots in monolayer WSe₂. *Nat. Nanotechnol.* **2015**, *10*, 491–496.
- (26) Koperski, M.; Nogajewski, K.; Arora, A.; Cherkez, V.; Mallet, P.; Veuillen, J. Y.; Marcus, J.; Kossacki, P.; Potemski, M. Single photon emitters in exfoliated WSe₂ structures. *Nat. Nanotechnol.* **2015**, *10*, S03–S06.
- (27) Palacios-Berraquero, C.; Barbone, M.; Kara, D. M.; Chen, X.; Goykhman, I.; Yoon, D.; Ott, A. K.; Beitner, J.; Watanabe, K.; Taniguchi, T.; et al. Atomically thin quantum light-emitting diodes. *Nat. Commun.* **2016**, *7*, 12978.
- (28) Branny, A.; Wang, G.; Kumar, S.; Robert, C.; Lassagne, B.; Marie, X.; Gerardot, B. D.; Urbaszek, B. Discrete quantum dot like emitters in monolayer MoSe₂: Spatial mapping, magneto-optics, and charge tuning. *Appl. Phys. Lett.* **2016**, *108*, 142101.
- (29) Zheng, Y. J.; Chen, Y.; Huang, Y. L.; Gogoi, P. K.; Li, M. Y.; Li, L.-J.; Trevisanutto, P. E.; Wang, Q.; Pennycook, S. J.; Wee, A. T. S.; et al. Point Defects and Localized Excitons in 2D WSe₂. *ACS Nano* **2019**, *13* (5), 6050–6059.
- (30) Shi, L.; Zhou, Q.; Zhao, Y.; Ouyang, Y.; Ling, C.; Li, Q.; Wang, J. Oxidation Mechanism and Protection Strategy of Ultrathin Indium Selenide: Insight from Theory. *J. Phys. Chem. Lett.* **2017**, *8*, 4368–4373.
- (31) Mak, K.; Shan, J. Photonics and optoelectronics of 2D semiconductor transition metal dichalcogenides. *Nat. Photonics* **2016**, *10*, 216–226.
- (32) Zhao, Q.; Jie, W.; Wang, T.; Castellanos-Gomez, A.; Frisenda, R. InSe Schottky Diodes Based on Van Der Waals Contacts. *Adv. Funct. Mater.* **2020**, *30*, 2001307.
- (33) Hughes, S.; Franke, S.; Gustin, C.; Kamandar Dezfouli, M.; Knorr, A.; Richter, M. Theory and Limits of On-Demand Single-Photon Sources Using Plasmonic Resonators: A Quantized Quasinormal Mode Approach. *ACS Photonics* **2019**, *6* (8), 2168–2180.
- (34) Broome, M. A.; Fedrizzi, A.; Rahimi-Keshari, S.; Dove, J.; Aaronson, S.; Ralph, T. C.; White, A. G. Photonic Boson Sampling in a Tunable Circuit. *Science* **2013**, *339*, 794–798.
- (35) Kuhn, A.; Ljunggren, D. Cavity-based single-photon sources. *Contemp. Phys.* **2010**, *51*, 289–313.
- (36) Müller, M.; Vural, H.; Schneider, C.; Rastelli, A.; Schmidt, O.; Höfling, S.; Michler, P. Quantum-Dot Single-Photon Sources for Entanglement Enhanced Interferometry. *Phys. Rev. Lett.* **2017**, *118*, 257402.
- (37) Giannozzi, P.; Baroni, S.; Bonini, N. QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials. *J. Phys.: Condens. Matter* **2009**, *21*, 395502.
- (38) Giannozzi, P.; Andreussi, O.; Brumme, T. N. Advanced capabilities for material modelling with quantum espresso. *J. Phys.: Condens. Matter* **2017**, *29*, 465901.
- (39) Schlipf, M.; Gygi, F. Optimization algorithm for the generation of ONCV pseudopotentials. *Comput. Phys. Commun.* **2015**, *196*, 36–44.
- (40) Perdew, J.; Burke, K.; Wang, Y. Generalized gradient approximation for the exchange-correlation hole of many electron system. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1996**, *54* (23), 16533–16539.
- (41) Onida, G.; Reining, L.; Rubio, A. Electronic excitations: density-functional versus many-body Green's-function approaches. *Rev. Mod. Phys.* **2002**, *74*, 601–659.
- (42) Sangalli, D.; Ferretti, A.; Miranda, H.; Attaccalite, C.; Marri, I.; Cannuccia, E.; Melo, P.; Marsili, M.; Perali, F.; Marrazzo, A.; et al.

Many-body perturbation theory calculations using the yambo code. *J. Phys.: Condens. Matter* **2019**, *31*, 325902.

(43) Hopkinson, D. G.; Zólyomi, V.; Rooney, A. P.; Clark, N.; Terry, D. J.; Hamer, M.; Lewis, D. J.; Allen, C. S.; Kirkland, A. I.; Andreev, Y.; et al. Formation and Healing of Defects in Atomically Thin GaSe and InSe. *ACS Nano* **2019**, *13*, 5112–5123.

(44) Arora, H.; Jung, Y.; Venanzi, T.; Watanabe, K.; Taniguchi, T.; Hübner, R.; Schneider, H.; Helm, M.; Hone, J. C.; Erbe, A. Effective Hexagonal Boron Nitride Passivation of Few-Layered InSe and GaSe to Enhance Their Electronic and Optical Properties. *ACS Appl. Mater. Interfaces* **2019**, *11*, 43480–43487.

(45) Wells, S. A.; Henning, A.; Gish, J. T.; Sangwan, V. K.; Lauhon, L. J.; Hersam, M. C. Suppressing Ambient Degradation of Exfoliated InSe Nanosheet Devices via Seeded Atomic Layer Deposition Encapsulation. *Nano Lett.* **2018**, *18*, 7876–7882. PMID: 30418785.

(46) Freysoldt, C.; Grabowski, B.; Hickel, T.; Neugebauer, J.; Kresse, G.; Janotti, A.; Van de Walle, C. G. First-principles calculations for point defects in solids. *Rev. Mod. Phys.* **2014**, *86*, 253–305.

(47) Komsa, H.-P.; Berseneva, N.; Krashennnikov, A. V.; Nieminen, R. M. Charged Point Defects in the Flatland: Accurate Formation Energy Calculations in Two-Dimensional Materials. *Phys. Rev. X* **2014**, *4*, 031044.

(48) Debbichi, L.; Eriksson, O.; Lebegue, S. Two-Dimensional Indium Selenides Compounds: An Ab Initio Study. *J. Phys. Chem. Lett.* **2015**, *6*, 3098–3103.

(49) Chen, X.; Lin, Z.-Z.; Ju, M. Controllable Band Alignment Transition in InSe–MoS₂ Van der Waals Heterostructure. *Phys. Status Solidi RRL* **2018**, *12*, 1800102.

(50) Cheiwchanchamnangij, T.; Lambrecht, W. R. L. Quasiparticle band structure calculation of monolayer, bilayer, and bulk MoS₂. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2012**, *85*, 205302.

(51) Ramasubramaniam, A. Large excitonic effects in monolayers of molybdenum and tungsten dichalcogenides. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2012**, *86*, 115409.

(52) Re Fiorentin, M.; Risplendi, F.; Palummo, M.; Cicero, G. First-Principles Calculations of Exciton Radiative Lifetimes in Monolayer Graphitic Carbon Nitride Nanosheets: Implications for Photocatalysis. *ACS Appl. Nano Mater.* **2021**, *4*, 1985.

(53) Toth, M.; Aharonovich, I. Single Photon Sources in Atomically Thin Materials. *Annu. Rev. Phys. Chem.* **2019**, *70*, 123–142. PMID: 30735459.

(54) Van Roosbroeck, W.; Shockley, W. Photon-Radiative Recombination of Electrons and Holes in Germanium. *Phys. Rev.* **1954**, *94*, 1558–1560.