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Method and system for generating channel codes, in particular for a frame-header

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Montorsi et al.

(54) METHOD AND SYSTEM FOR GENERATING CHANNEL CODES, IN PARTICULAR FOR A FRAME-HEADER

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H04J 13/10	(2011.01)
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(45) **Date of Patent:** Jun. 27, 2017

- (58) Field of Classification Search CPC H04L 47/365; H04L 7/042; H04L 1/007; H04L 45/00; H04L 12/28; H04L 29/0653; (Continued)

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(74) Attorney, Agent, or Firm - Workman Nydegger

(57) **ABSTRACT**

A method for generating a channel code, in particular for a frame-header, wherein at least a code-word of the channel code is obtained by means of at least a concatenation of code-words of two constituent codes and such concatenation is performed on subsets of code-words of a first constituent code, having maximum length, with code-words of a second constituent code.

17 Claims, 16 Drawing Sheets



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H03M 13/35	(2006.01)
H04L 29/06	(2006.01)
H04W 72/04	(2009.01)
H03M 13/13	(2006.01)

- (58) **Field of Classification Search** CPC . H04L 2012/5652; H04B 3/54; H04M 13/136 See application file for complete search history.

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$i \cdot N_i$	160	155	150	145	280	270	260	375	360	460	550	630	720	779	882	935	992	1035	1106	1183	1272	1320	1390	1440	1496	1526	1530	1500	1400	LEST	928	$E\{i \cdot N_i\} = 853.226$			
N_i	2	6	ю	ы	10	10	10	15	15	20	25	30	36	41	49	55	62	69	79	01	106	120	139	160	187	218	255	300	350	407	464	$E\{N_i\} = 119$		L	J.
d_T		m	mut	ŧ	ŝ	0	ŝ	ŝ	က	4	ŋ	9	∞	6	12	77 17	18	22	28	35	44	54	68	84	105	131	162	201	247	301	358			Ĺ	Б Б
d_i		0	0	0	, 1	0	0	y	0	,j	,	,i	<u>୧</u> ୨	,	ಲು	¢4	4	4	9	ŀ-	¢,	10	14	16	21	26	31	39	46	54	57				
k_i	ю	və	ю	so.	ю	ю	ю	ю	ю	ю	n	n	ю	ıΩ	n	20	4	4			ব	4	4	4	en	<u></u>	ec.	က 	2	2	in and	0			
n_i	ю	0	0	0	G	0	0	n	0	ŝ	n	in	9	5	8	9	1-	t~-	10	12	10	7 7	10	21	27	쭚	37	54	50	57	51				
SNR_i	15	14	13	12	11	10	6	×	I~	9	s	annie Vici	က	0		0	 1	<u>ণ</u>	က္	7	ų	9	P.	ŝ	6-	-10	-11	-12	-13	-14	-12				
2	33	31	30	29	28	27	26	25	24	33	22	21	20	61	18	17	16	2	4	13	2	1	10	6	×	1~	9	NO.	ব	ಲು	2				

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$i \cdot N_i$	160	155	150	145	280	270	260	375	360	460	550	630	720	622	900	952	1024	1080	1176	1274	1404	1507	1640	1746	1856	1946	1998	2010	1884	1656	1218	$E\{i \cdot N_i\} = 985.968$		
N_i	5	νΩ	ю	υ	10	10	10	15	15	20	25	30	36	7	50	56	64	72	84	98	117	137	164	194	232	278	333	402	471	552	▶ 609	$E\{N_i\} = 149 \ \mathbf{k}$		ر
dT	1			1	2	2	ମ	en	en	4	υ	9	x	0	12	14	18	22	28	35	44	54	68	84	105	131	162	201	247	301	358			Ľ
d_i	-	0	0	0	,	0	0		0	4	,	÷4	2	,	က	0	4	4	9	t;~	6	10	14	16	21	26	31	39	46	54	57			
k_i	5 L	w	ю	ю	ŝ	ю	ŝ	ĸ	ю	ŝ	n	ю	ĥ	ю	ю	ıΩ	4	11.3	4	4	শ	বা	4	শ	es S	က	က	en	5	2	percent.			
n_i	s	0	0	0	ŋ	0	0	ю	0	ю	ŝ	ю	9	ю	6	9	∞	x	12	14	19	20	27	30	38	46	55	69	69	81	57			
SNR_i	15	14	13	12	11	10	6	x	1-	9	ю	4	en	0	,i	0	-1	¢,	က္	Ţ	ဟု	9-	1	ş	6-	-10 0	-11 0	-12 0	-13 0	-140	-15 0			
ż	32	31	30	29	28	27	26	25	24	R	22	21	20	19	18	17	16	15	14	13	12	Ξ	10	6	∞	1~	9	ĸO	r.	ŝ	5			

Fig. 6



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$i \cdot N_i$	1248	1209	1170	1131	1092	1053	1014	975	936	897	858	819	780	741	702	663	3456	3240	3024	2808	2592	2376	2160	1944	2120	2275	2958	2465	2824	2118	1582	$E\{i\cdot N_i\}=1717.1$
N_i	39	39	39	39	39	39	39	39	39	39	39	39	39	39	39	39	216	216	216	216	216	216	216	216	265	325	493	493	706	706	162	$E\{N_i\} = 216$
dT	19	19	19	19	61	19	19	19	19	19	19	19	19	19	19	19	113	113	113	113	113	113	113	113	141	175	271	271	413	413	498	
d_i	10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	94	0	0	0	0	0	0	0	28 28	34	96	0	142	0	85	
k_i	ŝ	ល	w	ນ	ю	ю	ນດ	ĸ	ю	ю	ю	ທ	ю	ю	ĸ	ю	4	ব	বা	ন্যা	4	4	7	4	ŝ	က	က	က	e)	3		
n_i	39	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	177	0	0	0	0	0	0	0	49	60	168	0	213	0	85	
SNR_i	15	4	13	12	11	10	6	×	t	0	10	4	က	c)		0	i 1	9	ကု	÷.	မဂ္	9-	<u>-</u>	ş	6-	-10 0	-11.0	-12 0	-13 0	-14 0	-150	
į.	32	31	30	29	28	27	26	25	24	23	22	21	20	19	18	5	16	15	14	13	21	Π	10	с,	∞	1-	9	ю	4	3	63	

Fig. 8





	71		1
$\left \frac{j}{n} \right $	18j 20	Cj 1111000000001111010010101001011001001	
	39	111100000001111010010110100001111100	
		0101001010101111100000010000101000	
4	39		
	20		
** E	90		
6	- 33		
-7	- <u>33</u>		
8	35		
0	90		
2	90		
10			
10	39	3100110001300100110001101001001000	
12	- 33		
14	20		
1.4	- 39		
10	016	00000001111100000000001111111111	
1.0	210	10100001111000100010101101010000101010	
17	216		
1.1	210	111100000010101011010000000000000000000	
		1000000001110111011001000100110111110000	
18	216	1010010110100700110101001010101010101	
1.0		01101010010110110010100101110011100110011001100011000110011010	
		00110000110011101101010100101110011110011001100110000	—
19	216	00111100001111000111111000001111110000	Ľ,
		001111110000000111111110000000000111111	
		111111000000000011111111000000000111111	
20	216	11000011110000110011001100110011001	60
		10011001100110010100110011111000011110010000	:
		00001111000011110011011001100110111110000	
21	216	01011010010110111001100110011001100	
		11001100110001100111100113000111110000111111	
		1100001111000001100111100110000111100001111	
22	216	1001011010010110101011010101010101010	
		01010110101010101010101010101001100110	
00	010		
23	216		
04	000		
24	205		
		1910011010010110100010110130111110011000011001111001111000111101010	
25	205		
1.0	112.17	111001110011110000111100011111110000000	
		001111111100000111100001111000011111111	
		011110001111000111100011110001111100001111	
		01111110000011110001111000111100011110000	
26	493	10101010101010101010011010011010011010	
		011010011010101010101010110101100111100110000	
		1100111100110010110100101101010101001111	
		101101010101010101010101010101011001110011100	
		1010110101010101010101010101010101010101	
		10110101010101010101010101010101010101	
		1111001100101101010101010101010101010101	

j	N_j	c_j
27	493	001100110011001211001111001111
		00111100111100011113000011111000000111111
		0000001111111100011110000111100000011111
		0001111000111100011110001111000000011111
		0000011111100011110001111000111100011110001111
		0001111000111100011110001111000000111111
		001111111100011110001111000111100011110000
28	706	110011001100110100110100110100110
		1001101001101100110011001101111000011110000
		11110000111100110011001100110111100001111
		11001101100110110011011001101101100001111
		1101001101011001101100110110011011001101111
		1100110110011011003101100110110011011110000111100110011011
		00001111001100110110011011001101100110
		111111111111111111111111111111111111111
		000000000000000000000000000000000000000
29	706	0101010101010101110011110011110011
		110011110011011001300110011110000111100001111000011110130011001300110011110000111100-
		0011110000111101100110011001100111100001111
		011001101100110110011011001100110011110000
		011110011110110011011001101100110110011001111
		01100110110011011001101100110110011001
		11000011110110011011001101100110110011001100110000
00	-	
30	791	
		·



			١																	
k=9	3584	2816	2304	1792	1536	1280	1024	768	768	512	512	512	256	256	256	256	256	256	256	256
k=8	3456	2688	2176	1792	1408	1152	896	768	640	512	384	384	256	256	256	128	128	128	128	128
k=7	3200	2560	2048	1664	1280	1024	832	640	512	448	320	256	256	192	128	128	128	64	64	64
k=6	3072	2432	1952	1536	1248	992	768	640	512	416	320	256	224	160	128	128	96	64	64	64
k=5	2928	2320	1840	1472	1168 <	928	736	592	464	368	304	240	192	160	128	96	80	64	48	48
k=4	2776	2200	1752	1392	1104	880	696	560	440	352	280	224	176	144	112	88	72	56	48	40
k=3	2608	2072	1644	1308	1040	824	656	520	416	328	264	208	168	132	104	84	68	52	44	36
k=2	1854	1473	1170	930	738	588	468	372	294	234	186	150	117	93	22	60	48	39	30	24
k=1	1130	898	713	567	450	358	284	226	180	143	113	90	72	52	45	36	29	23	18	15
SNR	-20.0	-19.0	-18.0	-17.0	-16.0	-15.0	-14.0	-13.0	-12.0	-11.0	-10.0	-9.0	-8.0	-7.0	-6.0	-5.0	-4.0	-3.0	-2.0	-1.0
	L					ă				******										

Fig. 13





		ц С																		
	4608	3584	2816	2304	1702	1536	0821	1024	2 <u>8</u> 2	<u>36</u>	N D	2 2 2	N 10	922 7	226	256	256	336	256	256
k=8	4352	3456	2688	2176	705	1408	22	88	38	660	20	Š	72 22 22	536 53	ŝ	288	12%	128	28	128
1	4096	3264	2624	244	1664	1344	1088	832	704	576	448	384	320	256	361	S	128	128	28 28	ŝ
k=6	3968	3168	2496	1984	-1600	1280	₩7.0	800	640	9 E	<u>–</u>	320	236	224)]	128	128	96	ţ	nonia C
10	3824	3040	9 1 57	020	15204	1216	990	768	608	<u>4</u> 80	384	304	236	3	60	128	90	88	Q4	48
1	3664	2012	2312	1840	terrer CC States T	1160	928	736	55	464	368	296	232	184	S D	120	90	8	Ğ	ŝ
k=3	3500	2780	2208	176	1396	1108	880	700	556		222	280	224	Ş	Ş	2	88	2	ŝ	Ş
2	2523	2004	ŝ	1266	1005	7 <u>0</u> 8	936:	25	402	ŝ	5 S S	201	162	120	102	x	Ş		9	R
<u>k</u> -1	22	1251	Too	200	627	498	3965	lo R	220 520	<u>100</u>	22	126	160	2	Ś	ß	and the second s	ŝ	ŝ	R
SNR	-20.0	0.01*	-18,0	° Ľ	-16.0	-15.0	-14.0	-13.0	-12.0	0.	-10,0	0.0-	-8.0	ç	-6.0	ç	<u> </u>	<u>ං</u> ද	0. ?	0. 1

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Fig. 15

METHOD AND SYSTEM FOR GENERATING CHANNEL CODES, IN PARTICULAR FOR A FRAME-HEADER

FIELD OF THE INVENTION

The present invention relates to a method and a system for generating channel codes, in particular channel codes for a frame-header in an ACM ("Adaptive Coding and Modulation") communication system.

DESCRIPTION OF THE PRIOR ART

Real-time adaptation of transmission parameters according to the channel conditions is highly desirable feature in the communication systems where the channel parameters may change in time or from one receiver to another.

Time and/or user varying channel condition is an important characteristic of most communication systems such as 20 satellite, network and broadcast systems.

According to the prior art, adaptive coding and modulation schemes have been proposed in such systems to provide significant capacity gains by real-time adaptation of the FEC ("Forward Error Correction") code rate/length and modula- 25 tion constellation.

The main idea of an ACM scheme is to increase the capacity of a system communication by avoiding the waste of resources caused by adopting a fixed physical layer scenario by which the spectral efficiency must be sacrificed ³⁰ to guarantee a good performance for the user with the worst channel conditions.

By employing an ACM scheme, the transmitter is able to switch between several constellations and codes choosing the largest available modulation and code rate which ensures 35 a target DER ("Detection Error Rate"), therefore insuring maximum spectral efficiency for each user. At the receiver, to successfully decode the message, each user should be able to decide whether the message is intended to him and/or to recognize the parameters of the constellation and code 40 which has been used by the transmitter.

In general, each packet sent by the transmitter consists of two main parts.

The first part is called frame-header, or simply header, and contains the informations regarding the modulation and 45 coding, hereinafter called ACMI ("Adaptive Coding and Modulation Indicator").

The second part contains the message which is encoded using the corresponding ACMI parameters.

Therefore each user should first decode the information in 50 the frame-header in order to be able to decode the rest of the message.

In applications such as satellite broadcasting, the coding strategy is not trivial due to the wide dynamic range of the SNR ("Signal to Noise Ratio"), typically from -15 dB to 15 55 dB. Only the use of an ACM scheme may not be sufficient to ensure the radio link, a good spectral efficiency and a target probability of error to the receiver.

It is therefore important to improve the spectral efficiency through a generation of a code which allows to minimize the 60 average and maximum length of a frame-header.

In the patent application no. US 2010/0128661, the code generation procedure is based on heuristic considerations without any attempt to minimize the frame-header length. The variable length code consists in the repetition of a single 65 strong Reed-Muller code to cope with the different signal to noise ratio conditions.

However, such patent application does not teach to minimize a length of a frame-header. It is the main object of the present invention to indicate a method and a system for generating channel codes, in particular for a frame header, able to minimize an average and a maximal length of a frame-header of a data packet.

It is a further object of the present invention to indicate a method and a system for generating channel codes, in particular for a frame header, able to maximize the spectral efficiency of a communication system.

It is a further object of the present invention to indicate a method and a system for generating channel codes, in particular for a frame header, able to improve the correction capability of the generated channel code.

It is a further object of the present invention to indicate a method and a system for generating channel codes, in particular for a frame header, able to decrease the computational complexity of a decoder.

It is a further object of the present invention to indicate a method and a system for generating channel codes, in particular for a frame header, able to obtain a fixed length for all code-words in order to have a same complexity of the maximum likelihood decoder of a variable length code.

These and other objects of the invention are achieved by a method and a system for generating channel codes, in particular for a frame header, as claimed in the appended claims, which are intended to be an integral part of the present description.

SUMMARY OF THE INVENTION

In short, it is disclosed a method for generating a channel code, in particular for a frame-header, wherein at least a code-word of said channel code is obtained by means of at least a concatenation of code-words of two constituent codes and such concatenation is performed on subsets of codewords of a first constituent code, having maximum length, with code-words of a second constituent code.

The users are divided, for example, into a smaller set of M types according to their radio link quality. Each user type i is associated with an available signal to noise ratio SNR_i . It is assumed that for any two user types k and m, if k>m, then SNR_k -SNR_m.

A set of maximum ACM modes, ACM_i , are associated to the set of user types. Each user type i must be capable of detecting and decoding all packets encoded with ACM modes j≤i, corresponding to signal to noise ratio SNR lower or equal to that associated to the user type i. Consequently, users of higher types, corresponding to high SNR values, must then be able to detect the ACM mode within a larger set than that of users of lower type.

This corresponds to the generation of a code which admits a sequence of subsets of code-words of such code with very large differences in the correction capabilities.

Further features of the invention are set out in the appended claims, which are intended to be an integral part of the present description.

BRIEF DESCRIPTION OF THE DRAWINGS

The above objects will become more apparent from the following detailed description of a method for generating channel codes, with particular reference to the annexed drawings, wherein:

FIG. 1 shows a block diagram of a communication system;

20

FIGS. **2** and **3** show modes of operation of an ACMI detector for a user type i;

FIG. **4** shows an example of the code generation using a variable length coding;

FIG. **5** shows parameters of codes for a variable length 5 code with thirty-two modes using the method according to the present invention and the Hamming code bound with DER ("Detection Error Rate") equal to 10^{-6} ;

FIG. 6 shows parameters of codes for a variable length code with thirty-two modes using linear codes of the prior art with DER equal to 10^{-6} ;

FIG. 7 shows parameters of codes for a variable length code with forty-eight modes using linear optimal codes of the prior art with DER equal to 10^{-8} ;

FIGS. **8** and **9** show parameters of codes for a variable length code using the method according to the present invention and linear optimal codes of the prior art with DER equal to 10^{-8} with respectively thirty-two and forty-eight modes;

FIG. 10 shows a graph relating to data of FIG. 8;

FIGS. **11***a* e **11***b* show code-words of the code of FIG. **8**; FIGS. **12** and **13** show respectively required header packet length versus minimal signal to noise ratio SNR for some values of k bits when DER is fixed to 10^{-6} and data ²⁵ relating to FIG. **12**, thus corresponding to a straightforward worst case design of frame-header;

FIGS. 14 and 15 show respectively required header packet length versus minimal signal to noise ratio SNR for some values of k bits when DER is fixed to 10^{-8} and data ³⁰ relating to FIG. 14, thus corresponding to a straightforward worst case design of frame-header.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

With reference to FIG. 1, it is shown a communication system 10 used as an example of system scenario to explain the detailed description of the present invention. A plurality of users is served by a gateway 1 through a satellite 40 transponder 2 and the gateway 1 comprises at least one encoder 3 that generate at least a code.

The users are divided into M types, for example M \leq 64, according to their current radio link quality and this subdivision is created by a designer during the design of the 45 communication system **10**.

Each user type i is associated with an available signal to noise ratio SNR_i and it is assumed, with no loss of generality, that $\text{SNR}_i \leq \text{SNR}_{i+1} \leq \ldots \leq \text{SNR}_M$. This latter condition is typical of satellite communication systems. Thus, signal to 50 noise ratio is different for each user type i. Furthermore, each user type i comprises at least one physical user.

A set of maximum ACM modes are associated to each user type i. Each user type i must be capable of detecting and decoding all packets encoded with modes ACM_j with $j \le 1$. A 55 feedback channel, not represented in FIG. 1, allows the gateway 1 to know the type i of each user.

Furthermore, the gateway 1 has the possibility of choosing for each user type i an ACM mode with index $j \le i$. Choosing a value below the maximum allowed i, which in 60 principle is suboptimal for the total system capacity, allows some flexibility at the gateway 1. This additional system flexibility, however, requires that user type i detects and decodes all modes ACM_j with $j \le i$. This requirement then imposes a high detection complexity especially to users 65 associated to high SNR values. In particular, users with the highest user type M must detect and decode all packets from

a satellite. The filtering of the packets, according to the true intended destination, is deferred after the decoding process.

With reference to FIG. 2, it is shown a mode of operation of a receiver 23 comprising an ACMI detector 21 for a user type i, and an input signal y, in the communication system 10 described in FIG. 1. The ACMI detector 21 delivers an index \hat{j} in the range [1, ..., i] denoting an estimation of an ACM index in the allowed range, or the conventional symbol "0" to denote a failure in the detection, freezing a following decoder 22.

In this example of communication system **10**, the following types of events for an ACMI are:

Detection error: $P_F = P(\hat{j} \neq j | j \le i)$

This refers to the probability that $ACMI_j$, estimated from the ACMI detector 21, is transmitted to the decoder 22 from the ACMI detector 21 and it is not equal to the $ACMI_j$ received from gateway 1, given that index j is less or equal to the index i of the user type. A packet that is potentially intended to the user type i is decoded with an uncorrect ACM mode and consequently not correctly delivered.

Useless decoding: $P_U = P(\hat{j} \neq 0 | j > i)$

This refers to the probability that $ACMI_j$, estimated from ACMI detector **21**, is transmitted to the decoder **22** from the ACMI detector **21** and it is not equal to zero, given that index j is greater than the index i of the user type. A packet that is not intended to users of type j is incorrectly decoded with the wrong format. The only cost is a useless decoding.

From that aforementioned, it is important to design and generate codes for minimizing the probability of the detection error P_E , given that the cost of useless decoding P_U is marginal.

With reference to FIG. 3, it is worthwhile to notice that by removing the flexibility for the gateway 1 of choosing a mode $j \le i$, and thus imposing j=i at the gateway 1, the only function of an ACMI detector 31 is to activate or to freeze a following decoder 32.

An error of the ACMI detector **31** would only cause a useless decoding event. The number of useless decoding in this case can be drastically reduced also for users with good link quality.

In a first example of the present invention it is described a method for generating a channel code for minimizing the aforementioned detection error probability P_E , at which is associated a DER ("Detection Error Rate") of ϵ value, and with variable length code-words.

The set of code-words is generated with variable lengths according to the following algorithm, which is shown in FIG. **4**:

Fixing a set of M ordered SNR values SNR_i corresponding to the desired modes thresholds and a desired DER ε;
 Setting a total distance d_i=0;

3. For all i decreasing from M to 2;

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4. Computing the required incremental distance to achieve the desired DER ϵ at target SNR_i

$$d_i = d_{min}(\epsilon, SNR_i, i) - d_T \tag{1}$$

The minimum distance d_{min} or d_i depends on a signal to noise ratio SNR and on a detection error rate with ϵ value. Furthermore, the minimum distance d_i increases for each generated subset of code and it is computed for each user type i.

5. If $d_i=0$ repeat from step 3.

6. else generating a code with code-words having minimized length n_i , i code-words and minimum distance d_i

7. Setting the total distance $d_T = d_T + d_i$

8. Repeat from step 3.

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9. The set of variable length code-words is finally obtained by concatenating a code-word from each of the constituent codes (see FIG. 4). The code-word of the mode i is then obtained by concatenating code-words of constituent codes from M down to i and have total length N, as follows:

$$N_i = \sum_{m=1}^{M} n_m \tag{2}$$

With reference to FIG. 4. at least a code-word of constituent codes is encapsulated into a code-word of the channel code and at least a code-word of the channel code has length greater than remaining code-words of such channel code. Furthermore, the concatenation is performed on subsets of code-words of a first constituent code, having maximum length, with code-words of a second constituent code.

In the formula (1) it is defined the following function:

$$d_{min}(\epsilon, SNR, M) = \frac{Q^{-1}(\epsilon/(M-1))^2}{2 \cdot SNR}$$
⁽³⁾

where Q is the Q-function, i.e. the complementary cumulative distribution function of the random variable standards.

The formula (3) provides the required minimum distance d_{min} for a channel code with M code-words achieving a detection error rate ϵ at the signal to noise ratio SNR. This ³⁰ formula (3) is obtained by using the upper bound:

$$\leq (M-1)Q\sqrt{2d_{\min}\cdot \text{SNR}}$$
(4)

which is rather accurate for small M and almost perfect 35 codes.

In order to have a lower bound on what can be achieved is used, for example, the Hamming bound

$$M \leq \frac{2^{n}}{\sum_{i=0}^{t} \binom{n}{i}}$$
(5)
$$t = \left\lfloor \frac{d_{min} - 1}{2} \right\rfloor$$
(6)

where t is the maximum weight of error vectors that are surely correct from the minimum distance decoding, to find the minimal length n of a code with M code-words and 50 minimum distance d_{min} required in step 6 of the previous algorithm.

With reference to FIG. 5, it is shown a result of a channel code generation using the previous algorithm for a system with 32 modes, signal to noise ratio SNR ranging from +15 55 to -16 dB in steps of 1 dB, for a target DER $\epsilon = 10^{-6}$.

The columns of the table of FIG. 5 indicate, from left to right, the number of code-words i, that is also the index of the user type, the corresponding signal to noise ratio SNR, the incremental length of code-word n_i of an header with 60 index i, the number of bits k, of code-word of an header at index i, the incremental minimum distance of code-word d_i of an header at index i, the total minimum distance d_T i.e. the sum, at index i, of preceding d_i, the total code-word length N_i of an header i.e. the sum, at index i, of preceding n_i and, in the last column, $i \cdot N_i$ that indicate the complexity of the decoding.

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It is to be noted that in this case the maximal code-word length N_i is 464 symbols, indicated with the reference 51, and the average header length $E\{N_i\}$, assuming that all modes have the same probability, is only 119 symbols, indicated with the reference 52. Hamming bound is an upper bound to the number of code-words and there are few codes that achieve it.

With reference to FIG. 6, it is reported a result of a channel code generation using optimal constituent linear codes noted in the prior art, taken from the tables found on M. Grassl, "Bounds on the minimum distance of linear codes and quantum codes", available online at http://www. codetables.de, published in 2007.

These constituent linear codes, noted in the prior art, have the additional constraint of having a number of code-words that is a power of two, i.e. 2^k , wherein k is the number of information bits. The use of these linear codes requires a maximal code-word length of 609 symbols, indicated with ₂₀ the reference 61, and an average header length $E\{N_i\}$ of only 149 symbols, indicated with the reference 62.

By comparing FIG. 5 and FIG. 6, it is therefore clear that the channel code, generated using the previous algorithm according to the present invention, is able to minimize the average and the maximal length of a frame-header of a data packet.

With reference to FIG. 7, it is compared an example of the generated code length according to the present invention for 48 modes with the required header length for the signaling scheme specified in D. Becker, N. Velayudhan, A. Loh, J. O'Neill, and V. Padmanabhan, "Efficient control signaling over shared communication channels with wide dynamic range", described in the U.S. patent application Ser. No. 12/621,203. The DER is fixed into $\epsilon = 10^{-8}$.

It can be noticed that the channel code generation proposed according to the present invention allows to reduce considerably the header length for all modes. The average of header length $E\{N_i\}$ according to the U.S. patent application Ser. No. 12/621,203 is 750 (reference 71), while the average of the header length $E\{N_i\}$ (reference 72) is reduced to 301 according to this example of the present invention; in the same way the maximum header length is reduced from 4416 (reference 73) to 1285 (reference 74).

Therefore, using the method according to the present invention, by evaluating the average length $E\{N_i\}$, an improvement of about 60% is obtained.

The aforementioned algorithm, when applied to constituent linear codes, shows some weaknesses in the channel code length. This is mainly due to the fact that the number of code-words of a constituent linear code is always a power of 2.

In this case, for example, all modes from 32 to 17 in FIG. 6 share the same size. In such cases, it is useful to generate a single constituent code which guarantees a good minimum distance instead of using a completely incremental approach as described above.

It is therefore proposed an example of modified code generation algorithm as follows:

- 1. Fixing a set of M ordered SNR values SNR, corresponding to the desired modes thresholds and a desired DER ϵ .
- 2. Setting $d_{T,M+1}=0$ and $N_{T,M+1}=0$.
- 3. For all i decreasing from M to 2
- 4. Setting k=[log₂ i]
- 65 5. Computing the required minimum distance

 $d_{T,i} = d_{min}(\epsilon, SNR_{i}, i)$

6. For all $i \le j \le 2^k$ (modes with the same code dimension) 7. Computing the incremental distance

 $\delta_{i,j} = d_{T,i} - d_{T,j}$

8. Generating a $(n_{i,j}, k, \delta_{i,j})$ linear code with minimal length 5

 $n_{i,j}$. Notice that when the distance increment $\delta_{i,j}$ is zero, the code has length 0. In this case, k is the number of information bits and not the number of code-words.

9. Repeat from 6.

10. Picking from the previous set of codes the one with the minimal total length corresponding to $j^*=\arg \min_{j} n_{i,j} + N_{T,j}$ 11. Setting $N_{T,j}=n_{T,j^*}$ and $d_{T,j}=d_{T,i}$, for all $i \le j \le j^*$

12. Repeat from 3.

13. The set of variable length code-words is finally obtained 15 by concatenating code-words from each of the constituent codes (see FIG. 4).

It can be noticed that, in this example, at each step are considered all the possible constituent codes with the same dimension k guaranteeing the minimum distance $d_{T,i}$. This 20 generation allows at steps i of the iteration to change the codes generated in previous steps $j \ge i$, provided that $j < 2^{\lceil \log_2 i \rceil}$.

With reference again to the case of FIG. 4, at least a code-word of constituent codes is encapsulated into a codeword of the channel code and at least a code-word of the 25 channel code has length greater than remaining code-words of such channel code. Furthermore, the concatenation is performed on subsets of code-words of a first constituent code, having maximum length, with code-words of a second constituent code.

The result of this new generation of codes are reported in FIG. 8 and FIG. 9 and the latter is compared with FIG. 7. It is important to notice that this new generation of codes allows to slightly reduce both the average and the maximum length of header.

In fact, the maximum length of header of FIG. 9 is 1239 symbols, indicated with the reference 91, which is lower than the maximum length of 1285 symbols of the header of FIG. 7, indicated with the reference 74; while the average length of header $E\{N_i\}$ is reduced from 301 symbols, 40 the required header length Rn achieved setting a DER indicated with the reference 72, to 285 symbols, indicated with the reference 92.

Furthermore, it should be noticed that the number of generated codes is reduced. An example of generated code is represented in FIG. 10 and in FIG. 11a and in FIG. 11b are 45 shown relative code-words.

With reference to FIG. 10, there are reported the simulation results relative to FIG. 8. The abscissa of FIG. 10 indicates the gap in dB from the nominal SNR_i of each user type i. In this case many codes actually achieve the target 50 DER with a very large margin.

For example, the curve of user type 32, indicated in the FIG. 10 with the reference number 101, achieves the target DER $\epsilon = 10^{-6}$ with a margin of about 16.3 dB. This is due to the fact that the same code (39,5,19) is used for all types 55 ranging from 32 to 17, and the target DER is achieved with no margin only for the user type 17, corresponding to a nominal SNR of 0 dB.

It is also possible to evaluate the performances of the described above examples, according to the present inven- 60 tion, in term of detection error rate DER with respect to a worst case design.

The worst case design provides a coding example where all users are able to decode all ACMI headers. A Reed-Muller code class is chosen as constituent code and its 65 parameters will be evaluated as a function of the required signal to noise ratio SNR range and number of modes M.

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In the worst case design, the fact that each user type i can be associated to a code with different code-word lengths or protection is not exploited. The code design is such that each user type i is capable to retrieve the ACMI from the header. Remembering that the user type i decides to proceed with decoding only if the detected ACMI; is less than or equal to its type, i.e., $j \le i$. In this case, the channel code generation is rather simple and strictly depends on the minimal signal to noise ratio SNR allowed in the system.

Taking the asymptotic expression of the DER ϵ for a code with minimum distance d_{min}, number of nearest neighbours A and repeating it R times, is achieved:

$$\epsilon = AQ(\sqrt{2d_{min}R \cdot SNR}) \to Rd_{min} = \frac{Q^{-1}(\epsilon/A)^2}{2 \cdot SNR}$$
(7)

It is considered the class of Reed-Muller codes as a solution for worst case design. The Reed-Muller codes have the parameters (n=2^{*m*}, k=m+1), with $d_{min}=2^{m-1}$ and A=2^{*k*}-2.

With reference to FIG. 12 and FIG. 13, there is reported the required header length Rn to achieve a DER $\epsilon 32 \ 10^{-6}$ versus the minimal target SNR. The different curves in FIG. 12 refer to the use of Reed-Muller codes with k=1 to 8. The number of the needed repetitions can be easily computed given the length of the corresponding Reed-Muller. The curve indicated with k=6 is the one that should be considered for a system with 64 ACM modes. It can be noticed that, in order to design a channel code working at -16 dB with 32 modes and DER ϵ =10⁶, a header length of 1168 (reference 131) is required with a worst case design, while the maximum header length of the examples of variable length 35 coding according to the present invention described above is 464 (reference 51) shown in FIG. 5, using Hamming bound, and 609 (reference 61) shown in FIG. 6, using in our construction linear codes of the prior art.

With reference to FIG. 14 and FIG. 15, there is reported $\epsilon = 10^{-8}$. In this latter case, the maximum header length at -16 dB with 32 modes and DER ϵ =10⁻⁸ is 1520 (reference 151), while the maximum header length of the examples of variable length coding of the present invention described above is 791 (reference 81) shown in FIG. 8.

It is clear from this comparison that the header length decreases when using the method according to the present invention.

With reference to FIG. 10, there are shown simulation results using a maximum likelihood decoder, i.e. to maximize the probability $P(\overline{y}|\overline{c})$. It is done by calculating the correlation of a received signal \overline{y} with all the code-words of \overline{c} code and then choosing the code-word with largest correlation. It is important to notice that the user type i needs to calculate the correlation between only the first N, elements of the received signal \overline{y} and only for the i code-words associated to SNR's which are smaller or equal to its nominal SNR (SNR_i).

Therefore, the decoding complexity is different for each user type i and is equal to N_i×i sums and i comparisons. The average decoding complexity can be calculated as $E\{N_i \times i\}$. In FIGS. 5 to 9 the last column shows $N_i \times i$ results with their average values, assuming a uniform distribution over all the users.

Since in the examples described above the linear constituent codes are chosen to be optimal for the given parameters and no other particular structure is assumed, the best optimal decoding strategy is to compute the correlation of the received signal \overline{y} (N_i sums) with all the i candidate code-words.

The complexity of this exhaustive decoder is affordable because it is dealing with small codes and short average 5 lengths.

The complexity of the correlations is further reduced by using constituent codes which admit faster decoding algorithms, as the Hadarmard transform used for Reed-Muller or 10maximal length codes. In particular, for a given set of parameters (n, k, d) where n and k are sufficiently small, repetition of maximal length codes yields codes with almost optimal performances.

The main goal of UEP ("Unequal Error Protection") is to 15 design a code which offer a larger error protection to some bits, symbols or code-words than others. In the literature the same name is used for all three cases.

Hereinafter it is described a further example of the present invention, only addressing the code-word UEP, which uses 20 a modification of the variable length channel code generation described above to generate a fixed length code.

The variable length code also has code-words with different error protection capabilities.

In fact, one way to generate a block UEP code is to extend 25 all the code-words of the code obtained for variable length codes by zero to have a fixed length for all code-words (to equalize the length of all code-words), thus at least a code-word comprises a sequence of bits having values equal to zero. In this case all code-words will have the length equal 30 to the longest code-word in the starting code.

It can be noticed that for this strategy to work, one should not use the all zero code-words in the construction of the starting variable length code.

length coding described above it should be considered the average length as the effective length of the code.

As for the complexity of the maximum likelihood correlator decoder for the generated code by zero padding, it has in principle the same complexity as the corresponding 40 mum distance is computed for each said user type. variable length coding and therefore the aforementioned description about decoding complexity is valid also for these codes.

The features of the present invention, as well as the advantages thereof, are apparent from the above description. 45

A first advantage of the method for generating channel codes according to the present invention is that the average and the maximal length of a frame-header of a data packet is minimized.

A second advantage of the method of the present inven- 50 tion is that the spectral efficiency of a communication system is maximized.

A further advantage of the method of the present invention is that the correction capability of the generated channel code is improved.

A further advantage of the method of the present invention is that the computational complexity of a decoder is decreased.

A further advantage of the method of the present invention is to possibly also obtain a fixed length for all code- 60 words in order to have a same complexity of the maximum likelihood decoder of a variable length code.

The method and the system for generating channel codes in particular for a frame-header described herein by way of example may be subject to many possible variations without 65 departing from the novelty spirit of the inventive idea; it is also clear that in the practical implementation of the inven-

tion the illustrated details may have different shapes or be replaced with other technically equivalent elements.

For example, the method and the system for generating channel codes in particular for a frame-header can be applied in any communication system in which it is possible to vary the spectral efficiency and/or in communication systems that do not use an ACM scheme.

It can therefore be easily understood that the present invention is not limited to a method and a system for generating channel codes in particular for a frame-header, but may be subject to many modifications, improvements or replacements of equivalent parts and elements without departing from the inventive idea, as clearly specified in the following claims.

The invention claimed is:

1. A method for generating a channel code for a frameheader of a packet, the method comprising:

- obtaining a code-word of said channel code, with an encoder, by means of at least a concatenation of codewords of two constituent codes, wherein said concatenation is performed on subsets of code-words of a first constituent code, having maximum length, with codewords of a second constituent code, wherein each of the first constituent code and the second constituent code is associated with a different signal to noise ratio; and
- including the code-word of said channel code in the frame header.

2. The method according to claim 1, wherein said at least a code-word of said constituent codes is encapsulated into a code-word of said channel code.

3. The method according to claim 1, wherein said at least a code-word of said channel code has length greater than remaining code-words of said channel code.

4. The method according to claim 1, wherein a minimum It is important to notice that in the example of variable 35 distance of said constituent codes depends on signal to noise ratios, which are associated with user types and they are different from each said user type, and depends on a detection error rate.

5. The method according to claim 1, wherein said mini-

6. The method according to claim 1, wherein a maximum code-word length of said channel code is obtained by the formula $N_i = \sum_{m=1}^{M} n_m$ where M is the maximum number of said code-words of said channel code corresponding to an highest said signal to noise ratio, m is an integer index varying from one to M and n_m is a length of said code-word of said constituent code at index m.

7. The method according to claim 1, wherein said codewords of said channel code have variable length.

8. The method according to claim 1, wherein said constituent codes are known linear codes.

9. The method according to claim 1, wherein said at least a code-word of said channel code comprises a sequence of bits having values equal to zero to equalize the length of said 55 at least a code-word.

10. The method according to claim 9, wherein said code-words of said channel code have fixed length.

11. The method according to claim 1, wherein said channel code is an UEP code.

12. The method according to claim 1, wherein said channel codes are suitable to be used for a frame-header of a data packet of a communication system.

13. A system for generating channel codes, comprising: at least an encoder configured to generate a channel code for a frame-header, wherein at least a code-word of said channel code is obtained by means of at least a concatenation of code-words of two constituent codes and

said concatenation is performed on subsets of codewords of a first constituent code, having maximum length, with code-words of a second constituent code, wherein each of the first constituent code and the second constituent code is associated with a different 5 signal to noise ratio.

14. The system according to claim 13, wherein said encoder is suitable to be used in a communication system.

15. The system according to claim **14**, wherein said communication system comprises a plurality of user types 10 having different signal to noise ratios.

16. The system according to claim **14**, wherein said communication system is an ACM ("Adaptive Coding and Modulation") communication system.

17. A method for generating a channel code for a frame 15 header broadcast to users associated with different signal to noise ratios, the method comprising:

generating, with an encoder, a set of variable length code-words by concatenating a constituent code word from each of M codes, wherein a code-word for each 20 mode i is obtained by concatenating code-words of constituent codes from M down to i; and

encapsulating, by the encoder, a code word of constituent codes into a code-word of the channel code, wherein the concatenation of the code words of the channel 25 code is performed on subsets of code-words or a first constituent code with code-words of at least a second constituent code, wherein each of the first constituent code and the second constituent code is associated with a different signal to noise ratio. 30

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