

## THE 19TH INTERNATIONAL CONFERENCE ON GEOMETRY AND GRAPHICS

SÃO PAULO, BRAZIL JANUARY 18-22, 2021

# BOOK OF ABSTRACTS













#### Catalogação-na-Publicação

International Conference on Geometry and Graphics (19th : 2021 : São Paulo)

ICGG 2020 book of abstracts: livro digital / ed by Liang-Yee Cheng, Rubens Augusto Amaro Junior. -- São Paulo : Epusp, 2021.

ISBN 978-65-89190-00-4

1.Geometria 2.Design graphics I.Cheng, Liang-Yee, 1965- ed II.Amaro Junior, Rubens Augusto, ed

**CDD 516** 

#### **Committees**

#### **International Program Committee**

Ahmad Barari, Ontario Tech University, Canada André Kubagawa Sato, University of São Paulo, Brazil Antonio Álvaro Tordesillas, Universidade de Valladolid, Spain Ashraf Khattab, Ain Shams University, Egypt Aura Conci, Universidade Federal Fluminense, Brazil Baoling Han, Beijing Institute of Technology, China Biljana Jovic, University of Belgrade, Serbia Boris Odehnal, Vienna University of Applied Arts, Austria Cornelie Leopold, TU Kaiserslautern, Germany Daiva Makuteniene, Vilnius Gediminas Technical University, Lithuania Daniel Lordick, Technical University of Dresden, Germany Daniela Velichova, Slovak University of Technology in Bratislava, Slovakia Douglas Dunham, University of Minnesota Duluth, USA Eduardo Toledo Santos, University of São Paulo, Brazil Ema Jurkin, University of Zagreb, Croatia Emiko Tsutsumi, Otsuma Women's University, Japan Frank Maxfield Croft, The Ohio State University, USA Gilson Braviano, Universidade Federal de Santa Catarina, Brazil Gunter Weiss, Technical University of Dresden, Germany Haiyan Yu, Donghua University, China Hans-Peter Schröcker, University of Innsbruck, Austria Hellmuth Stachel, University of Technology Vienna, Austria Hirotaka Suzuki, Kobe University, Japan Hongming Cai, Shanghai Jiaotong University, China José Ignacio Rojas-Sola, Universidad de Jaén, Spain Kensuke Yasufuku, Osaka University, Japan Krassimira Vlachkova, University of Sofia St. Kliment Ohridski, Bulgaria Kunio Kondo, Tokyo University of Technology, Japan Laszlo Voros, University of Pécs, Hungary Leônidas de Oliveira Brandão, University of São Paulo, Brazil Liang-Yee Cheng, University of São Paulo, Brazil Luigi Cocchiarella, Politecnico di Milano, Italy Magdalena Dragovic, University of Belgrade, Serbia Manfred Husty, University of Innsbruck, Austria Marcelo Eduardo Giacaglia, University of São Paulo, Brazil Marco Hemmerling, Cologne University of Applied Sciences, Germany Marcos de Sales Guerra Tsuzuki, University of São Paulo, Brazil Miklós Hoffmann, Esterházy Károly University, Hungary Milena Stavric, Graz University of Technology, Austria Naomi Ando, Hosei University, Japan Norman Wildberger, The University of New South Wales, Australia Otto Röschel, Graz University of Technology, Austria Paul Zsombor-Murray, McGill University, Canada

Peeraya Sripian, Shibaura Institute of Technology, Japan Ren Zuo Wang, National Center for Research on Earthquake Eng., Taiwan Renata Górska, Cracow University of Technology, Poland Roberto Silvio Ubertino Rosso Jr, Santa Catarina State University, Brazil Rogério Yugo Takimoto, University of São Paulo, Brazil Sande Gao, Meisei University, Japan Sergio Gavino, Universidad Nacional de La Plata, Argentina Sonja Krasić, University of Nis, Serbia Ted Branoff, Illinois State University, USA Tomohiro Tachi, The University of Tokyo, Japan Vera Viana, Universidade do Porto, Portugal Xiao Luo, Beijing Institute of Technology, China Yasushi Yamaguchi, The University of Tokyo, Japan Yuanjun He, Shanghai Jiaotong University, China Zhendong Niu, Beijing Institute of Technology, China

#### **Local Organizing Committee**

Ana Lucia Camargo Harris, University of Campinas Arivaldo Leão Amorim, Universidade Federal da Bahia Aura Conci, Universidade Federal Fluminense Brenda Chaves Coelho Leite, University of São Paulo Eduardo Toledo Santos, University of São Paulo Elsa Vásquez Alvarez, University of São Paulo Fabiano Rogerio Corrêa, University of São Paulo Fabio Kenji Motezuki, University of São Paulo Fernando Akira Kurokawa, University of São Paulo Gilson Braviano, Universidade Federal de Santa Catarina João Roberto Diego Petreche, University of São Paulo Liang-Yee Cheng, University of São Paulo Marcelo Eduardo Giacaglia, University of São Paulo Marco Antonio Rossi, São Paulo State University Maria Antonia Benutti, São Paulo State University Rovilson Mafalda, Federal University of ABC Sergio Leal Ferreira, University of São Paulo Zulind Luzmarina Freitas, São Paulo State University

#### **Organizing staff**

Cezar Augusto Bellezi, Lucas Soares Pereira, Matheus Kenji Kubo, Pedro Luis Rufato de Jesus, Yuri Confessor Castilho Fernandes

#### **Editor**

Liang-Yee Cheng

#### Co-editor

Rubens Augusto Amaro Junior

#### **Contents**

#### Part I Theoretical Graphics and Geometry

String Constructions of Quadrics Revisited	3
Hellmuth Stachel	
Space Kinematics and Projective Differential Geometry Over the Ring of Dual Numbers Hans-Peter Schröcker, Martin Pfurner and Johannes Siegele	s 5
Examples of Isoptic Ruled Surfaces	7
A One-Parameter Family of Triangle Cubics	9
Vermeer's Specific Ratio	11
Perspective and Illusion in Four-dimension: Droste-effect in Four-dimension Based on Es	scher's
Work	13
Hidden Structures in Tessellations of Convex Uniform Honeycombs	15
Geometry and Proportion: Materialization of an Architectural Carpentry Project	17
Factorization of Locus Polynomials using DGS  Pavel Pech	19
A Spatial Generalization of Wallace–Simson Theorem on Four Lines	21
Interactive 4-D Visualization of Stereographic Images from the Double Orthogonal Proj	
Michal Zamboj	23

The M-Points Related to the Perfect Circles in any Triangle ABC as the Next the Generalized Soddy-line and About "Square Root Angle"	
Michael Sejfried	
Part II Applied Geometry and Graphics	
Assessment of Light Transmission for Comfort and Energy Efficient Insola	
Tetiana Tkachenko and Viktor Mileikovskyi	
Cyclographic Model of Generation of Families of Parallel Curves to a Mul	
Konstantin Leonidovich Panchuk, Tatyana Mikhailovna Myasoedova, and Evger Lyubchinov	nij Vladimirovich
Cyclographic Model of Automotive Road Surface Form Design	33
Konstantin Leonidovich Panchuk, Evgenij Vladimirovich Lyubchinov, and Taty	ana Mikhailovna
Myasoedova	
Development of Data-Driven Agent Model for Consumer Shopping Behavior	r in Commercial
Facility	35
Kensuke Yasufuku, Junichi Izumoto and Hirokazu Abe	
A Curved Surface Flattening Computing Method Combined with Machining l	<b>Process</b> 37
Peng-Fei Zheng, Jing-Jing Lou, Da-Jun Lin, Qi An	
Research on Reverse Engineering for Free-form Surfaces	39
Sande Gao and Loulin Huang	
The Language of Geometry, the Icosahedron as a Case Study	41
Dina Rochman	
Interactive Creation of Voronoi Diagrams for Origami Tessellation	43
Yohei Yamamoto and Jun Mitani	
Teeth Mesh Segmentation Through Curvature Analysis	45
Lucas K. Miyazaki, Rogerio Y. Takimoto, André K. Sato, Hiromasa Suzuki and Mar	
Biomimetic Approach to Parametric Flower Modeling	47
Biljana Jovic, Aleksandar Cucakovic, Marija Markovic and Katarina Cvijic	

"Inversion" of a Pyramid	49
The Mysterious Synergy of Geometry and Art	51
Parametric Otto: Validation of a Visual Programming for the Generation of Minimum	1
Surfaces Conformed by Physical Forces	53
Pedro Oscar Pizzetti Mariano and Janice De Freitas Pires	
Graphic Methodology Based on Funicular and Projective Geometry, in Structural Analysis Historical Constructions	
Javier Suarez, Thomas Boothby and Jose Antonio Gonzalez	
Geometric Modeling of a Topographic Surface Based on a Fractal Coordinate System 5  Elena I. Shangina	57
Inverse Designing Airfoil Aerodynamics in Compressible Flow by Target Pressure Distribut	
Naser Tanabi, Ahmad Barari, Shidvash Vakilipour and Marcos S. G. Tsuzuki	
Framework for Electrical Impedance Tomography Forward Problem with Non-unifor Electrodes Distribution	61
Guilherme C. Duran, André K. Sato, Naser Tanabi, Hossein Nasiri, Rogério Y. Takimoto, Ahn Barari, Thiago C. Martins and Marcos S. G. Tsuzuki	nad
Determination of Open Boundaries in Point Clouds with Symmetry	63
Edson K. Ueda, Ahmad Barari and Marcos S. G. Tsuzuki	
Multi-Objective Topology Optimization using Simulated Annealing Method	65
Hossein R. Najafabadi, Tiago G. Goto, Thiago C. Martins, Ahmad Barari and Marcos S. G. Tsuz	zuki
Study on Space Evaluation using VR and AR6	67
Liu Fan, Hiromitsu Shimizu and Naomi Ando	
Investigation of a Turtle-Shaped Construction Block and its Relationship with other Geomet	tric
Toys	
Daniel W. L. Rodrigues	
From Dynamic Visualization to Designing Sustainable Architecture	71
María Elena Tosello and Santiago Saucedo	

The Geometry of the Ramps in Oscar Niemeyer's Cultural Projects
<b>Research on Geometry of Expandable Portable Building and its Application</b>
Hough Transform Voting Scheme for Detection of Parabolas and Open Conics in Images . 77 Maysa Malfiza Garcia de Macedo, Jordan Salas and Aura Conci
The Use of LEGO® Robots to Visualize the Design Process of High-Performing Heat Exchangers
Kevin Noack, Robert Päßler, Margarete Ketelsen and Daniel Lordick
The Contribution of Great Circles for Building Retractable Polyhedra
Touching and 'Feeling' The Feast of Herod by Benozzo Gozzoli: a Multisensory Communication Strategy Unveiling the Secrets of Painted Spaces to the Blind
Utilization of Nonconvex Shapes as Horizontal Section of Paper Folding Lampshade Constructed with Skew Quadrilateral Elastic Folding
Part III Engineering Computer Graphics
The Gestalt Principle for Building Area Extraction 89  Jie-Xian Zeng, Min Liu, Wei-Ye Li, Jun Chu, Gui-Mei Zhang, Xiao-Yun Yi and Zheng-Xi Wu
<b>Torus and Quadrics Intersection, using GeoGebra</b>
Parametric Modeling of Polyhedron Based on Revit
An Improved Sensitivity Method for Multi-material Topology Optimization
3D Reconstruction of Grabbed Objects Using a Single Image Based on Palletizing Task 97 Lu Lu, Jiong Yang, Jie Liang and Aimei Zhang

Solid Modeling and Artistic Sticker of Sphere-Cone Tangential Combination in Equal Circle
Views 99
Xiaoxian Cui and Xiangbao Meng
Dynamic Target Detection and Tracking in Water for Mobile Robot Based on Deep Learning
Chen Yang, He Xu, Xin Li and Jinwei Huang
Using the contour method from the Theory of Mechanisms to approach a problem of geometry
Iulian Popescu, Marcela Popescu, Alina Duta, Ludmila Sass, Alina Elena Romanescu, and Gabriel Catalin Marinescu
Research on SLAM System Based on Binocular Vision and IMU Information
Soccer Field Lines Determination and 3D Reconstruction
Fernando F. Doria, Felipe B. C. L. Lima, Andre K. Sato, Rogerio Y. Takimoto, Ahmad Barari, Fabio S G. Tsuzuki and Marcos S. G. Tsuzuki
Human Thorax Parametric Reconstruction Using Computer Vision
Flavio A. Nakadaira Filho, Joao V. B. Munhoz, Rogerio Y. Takimoto, Ahmad Barari and Marcos S. G. Tsuzuki
A Kinematics Framing Methodology for Computing Sweep Surfaces using N-dimensional Nurbs Curves
Guilherme C. Duran and Marcos S. G. Tsuzuki
Research on Obstacle Avoidance Motion Planning Technology of 6-DOF Manipulator 113 Baoling Han, Xiao Luo, Qingsheng Luo, Yuting Zhao and Binbin Lin
Robustness Assessment of a Low Poly Modeling Strategy for Performance Simulation of Double-Skin Green Facades
Pierpaolo D'Agostino and Federico Minelli
Computational Graphics and Immersive Technologies Applied to a Ship Maneuvering
Simulator
Humberto S. Makiyama, Edgar Szilagyi, Gabriel H. Pereira, Leanderson R. R. Alves, Brian M.
Kodama, Denis Taniguchi and Eduardo A. Tannuri

#### **Part IV Graphics Education**

An Experience on Short Course of Computational Geometric Modeling in Engineering Design
for High School Students
The Teaching of Geometric Representation Techniques at the Fine Arts School of the Federal University of Rio de Janeiro
Madalena Grimaldi, Maria Helena W. L. Rodrigues, Daniel W. L. Rodrigues
Architectural Geometry Learning Processes Supported by 3D Models and Animations 125  Cornelie Leopold and Viyaleta Zhurava
<b>Studying of MOOC</b> + <b>SPOC teaching mode in Engineering Graphics Course</b>
<b>Education Quality Issues in Engineering Graphics Training</b>
The Evolution of the Descriptive Geometry Course for Architecture Students at a Public University in Northern Paraná
Maria B. Barison and Eduardo Toledo Santos
Research on Graphics Teaching Mode
Ziru Wang, Yuanjun He, Fan Zhang and Bing Qiu
Trends of Spatial Abilities of Students Who Take Graphic Sciences in Recent Undergraduate Curriculum
Kumiko Shiina, Ichiro Tanaka and Nobuhide Nao
Intersecting Architectural Surfaces Between Graphic and Analytic Representations 137  Caterina Cumino, Martino Pavignano and Ursula Zich
Between Geometry and Technical Drawing - Didactic Interactive and Animated Drawing Teaching Tools of the Diad-Tools Project
Monika Sroka Bizon, Piotr Dudzik, Tatjana Sankauskiene, Ewa Terczynska, Jolanta Tofil, Krzysztof Tytkowski and Antanas Vansevicius
<b>Geometrical Thinking: Solving a Problem on Graphic Representation</b>

Improving and Measuring Spatial Skills with Augmented Reality and Gamification 143 Róbert Tóth, Marianna Zichar and Miklós Hoffmann
Cultivating Integrated Abilities of Students through Participatory Study in Engineering Graphics Course
Xiu-Zhi Zhang, Yun-Hui Zhang, Li-Ge Wen and Cheng-Ming Zuo
<b>Exploration of Classroom Teaching Methods under Mixed Teaching Mode</b>
Compilation and Application of Graphics Textbook Based on AR technology
Architectural Geometry and Graphics Education some Retrospective Reflections from Italy Across Three Generations
Luigi Cocchiarella, Veronica Fazzina, Matteo Cavaglià and Simone Porro
Analysis of the Application of the Active Teaching-learning Methodology in Graphic Expression Monitoring for UPE Engineering Students
Tutoring as a Tool to Explore New Teaching Methodologies in the Classroom in Engineering Classes of the University of Pernambuco
Part V Geometry and Graphics in History
Elementary Geometry in Staircases Design. The 'City House' of Bernardo Antonio Vittone
Vincenzo Cirillo
Geometric reconstruction of the positioning of the Carceres in the Circus of Maxentius 161 Maria Grazia Cianci and Sara Colaceci
Piero della Francesca's Contribution on the Apparent Contour Perspective
The Geometry as a Decoder of Gravity: Anne G. Tyng's Elementary School in Bucks County P. A. U. S.  165
Juan Manuel Villa Carrero

Geometry, Between History and Shape Configuration
Geometry and Urban Shape of the City of Nola through the Drawings of the De Nola by A.
Leone (1514)
<b>Drawing and Geometric Constructions of Polyhedra in the Art of Escher</b>
Part VI Poster
A Method for Void Inspection in X-Ray CT Images Based on Golden Part Generated from a Set of Accepted Parts
Hiromasa Suzuki, Xiangning Mao and Yutaka Ohtake
<b>Determination of Parameters of an Inaccessible Point of an Object</b>
GeoMotor: Design with Nature. Recognition of Geometries Using a Convolutional Neural-Network Approach (CNN)
3D Animation Applied to Street Art. Physical and Remote Connections Aimed at Inclusion
Maurizio Perticarini and Valeria Marzocchella
Thinking on the Teaching Methods and Contents of Engineering Graphics Courses under the New Engineering Construction
A Class of "Basic Media Design" Based on 3D-CAD for Beginners of Digital Processing 185 Kazuhiro Yamashima and Seiji Hori
3D Scene Reconstruction from a 2D Photo as a Learning Challenge of PBL in Architectural and Engineering
Teaching Architecture and the Modeling Project Associated with Geometric Representation Systems

The Semiotic Context for Learning Engineering Graphics
<b>Isoptic Curves of Cycles on a Hyperbolic Plane of Positive Curvature</b>
Spherical Images: Capture and Visualization Devices. Icons of a Computational Paradigm 195 Federico Alberto Brunetti
Tracing Recognition Through Geometric Analysis: The Search for Federal University of Pelotas Original Coat of Arms Authenticity Features

### INTERSECTING ARCHITECTURAL SURFACES BETWEEN GRAPHIC AND ANALYTIC REPRESENTATIONS

Caterina CUMINO<sup>1</sup>, Martino PAVIGNANO<sup>2</sup> and Ursula ZICH<sup>2</sup>
<sup>1</sup>DISMA, <sup>2</sup>DAD, Politecnico di Torino, Italy

Since 2014, we have been dealing with Geometry as a common and shared language between Architecture and Mathematics. In this contribution we focus, from that point of view, on the relationship between the architectural object and its theoretical model by mean of analyzing its Geometry, also bearing in mind the context of first year Bachelor's in Architecture, with the wider goal of improving spatial thinking and visualization abilities. In fact, in architects' training when it comes to analyzing built shapes, there occurs the need to abstract their geometric essences from the real world. It is then important to provide students with instruments to derivate the theoretical object from its built counterpart. We have been focusing on particular architectural/ geometric realities such as compound vaults generated by intersecting surfaces and on the analysis of a variety of approaches for representing them: from the analytical one, which allows rigorous and unambiguous outcomes, to graphical ones, which are consequences of choices (of tools and constructive sequences) leading to only partially rigorous results. To analyze a groin vault with our students, we consider graphical representations of portions of intersecting cones, as outcome of a critical process of data discretization. We compare graphic solutions (obtained via descriptive geometry by CAAD-AutoCAD) and their different levels of approximation with a mathematical formalization (obtained via analytical geometry) and the use of a DGS (GeoGebra), reasoning about subjectivity and objectivity of the respective representations. We chose to use these tools because our students are at their very first year of academic studies, thus they are not comfortable with highly specialized software, with which they will be trained in more advanced courses. There are possible learning difficulties of epistemological nature related to the recognition of geometric objects in space, which involve understanding of concepts, symbols, procedures and different types of representations; even only from a mathematical point of view, indeed, a geometric object can be described by Cartesian equations, or by parametric equations, or even considering it as a set of points that verify the same property; then, students need adequate flexibility to switch from one register to another (in the sense of Duval). Thus we need them to experiment with simple tasks, avoiding possible issues with difficulties in spatial prefiguration capabilities they have might not already developed during their high schools studies. Students are provided with some testing and verification tool: on one side a DGS makes Mathematics accessible to experimentation; on the other side Monge himself, in his 1798 treatise Géométrie descriptive, suggested that one of the purposes of this science is to allow a graphic verification of objects' geometric properties and to suggest new previously unknown features. This remark reveals an aspect of Representation as an experimental science, where reasoning proceeds by adding other entities to the figure or by imagining operations that also have a physical model, such as plane sections. We propose analytical tools to critically verify students' geometric intuitions about built architecture, with the further possibility to highlight relationships between graphic representation sought and analytical properties of surfaces and resulting vaults. Such activities, in the spirit of visual thinking, allow them to visualize relations between surfaces in a more dynamic, manageable and intuitive way and to compare results obtained with a variety of architectural and mathematical tools, by means of implementing the use of the same theoretical concepts using the interdisciplinary language of Geometry.

18-22 JANUARY, 2021, SÃO PAULO, BRAZIL

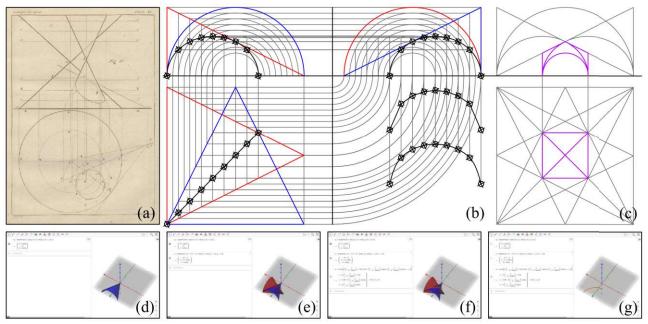


Figure 1. Different approaches to the relationship between cones. (a) Gaspard Monge, *Planche XI*; (b) CAAD orthographic projections of cones cut by a plane, the intersection curve is plotted graphically with the ellipse, polylines and splines tools to visually compare their different outcomes and approximation levels; (c) orthographic projections of a groin vault scheme generated by four cones; (d) - (g), views of related DGS model made by GeoGebra.

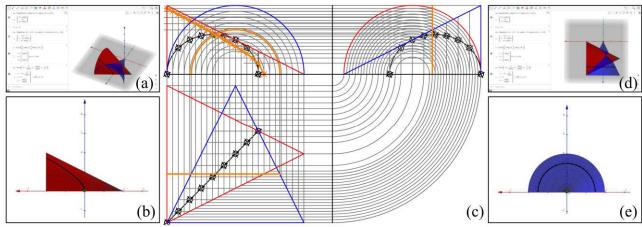


Figure 2. Intersection between two cones by cutting planes: focus on a step of the geometrical sequence. (a), (d) Views of DGS model made by GeoGebra; (b), (e) visualization of the same section on the surface of each cone; (c) orthographic projections of the graphic study of the intersection: in orange hyperbole and circumference defining the intersection point that is one of the possible points to describe the intersection line between the two surfaces.

Keywords: Intersecting Surfaces, Descriptive Geometry, DGS, CAAD, Visual Thinking, Theoretical Form.