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# Evaluation of the influence of voids on 3D representative volume elements of fiber-reinforced polymer composites using CUF micromechanics 

E. Carrera, M. Petrolo ${ }^{\dagger}$ M.H. Nagaraj ${ }^{\ddagger}$, M. Delicata ${ }^{\S}$<br>MUL ${ }^{2}$ Group, Department of Mechanical and Aerospace Engineering, Politecnico di Torino Turin, Italy

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Author for correspondence:<br>Marco Petrolo<br>MUL ${ }^{2}$ Group, Department of Mechanical and Aerospace Engineering, Politecnico di Torino,<br>Corso Duca degli Abruzzi 24,<br>10129 Torino, Italy,<br>tel: +39 0110906845 ,<br>fax: +39 0110906899 ,<br>e-mail: marco.petrolo@polito.it

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#### Abstract

This paper presents numerical results on the micromechanics linear analysis of representative volume elements ( $R V E$ ) containing voids. The modeling approach is the micromechanical framework within the Carrera Unified Formulation (CUF) in which fibers and matrix are 1D finite elements (FE) with enriched kinematics and component-wise capabilities (CW). RVE models are 3D and consider all six stress components. Such a modeling strategy leads to a twofold reduction of the degrees of freedom (DOF) as compared to 3D FE. The numerical assessments address the influence of the volume fraction and distribution of voids, including comparisons with data from the literature and statistical studies regarding homogenized properties and stress fields. The proposed modeling approach can capture the local effects due to the presence of voids, and, given its computational efficiency, the present framework is promising for nonlinear analysis, such as progressive failure.


Keywords: Voids, micromechanics, CUF, fiber reinforced polymers

## 1 Introduction

Fiber-reinforced composites are increasingly popular in many engineering fields to provide superior performances as compared to metals [1, 2]. In addition to space and aeronautics industries, the automotive and energy sector are making growing use of these materials due to the lightweight and the high specific strength and stiffness [3, 4]. Composites have a multiscale nature, and the proper detection of fundamental mechanical behavior requires modeling of the various scales. The present paper focuses on the microscale in which the differences between constituent properties and the presence of interfaces and defects lead to modeling challenges [5]. Defects stemming from manufacturing can significantly modify the microscale characteristics and lead to various damage mechanisms, such as $[2,6]$ interfacial debonding and sliding, matrix microcracking, delamination, fiber breakage, and fiber micro-buckling.

The present paper deals with the numerical modeling of voids in the matrix. Voids can influence the matrix-dominated mechanical properties and lead to the localization of stresses [7]. Many works have investigated the void formation, growth, morphology, and influence on structural performance. The work of Mehdikhani et al. [8] is a comprehensive guide for the selection of these studies.

Computational micromechanics is a popular tool to study defects and related issues. By the direct modeling of the microscale components and defects, micromechanics can provide the homogenized macroscopic mechanical properties and, via de-homogenization, the stress and strain fields at the microscale. Various numerical approaches, e.g., finite elements (FE), can model the microscale via the use of a representative volume element (RVE) containing the typical architecture of the composite structure in hand [9-18]. Other works investigate the effect of voids in the elastic regime and strength prediction, embedding them into the FE model and considering various loading conditions and failure modes [3, 5, 19-30]. The use of FE models can lead to very high computational costs. Such costs may be prohibitive when the 3D structure of the RVE is of interest, or nonlinear analyses are necessary. The present work falls within the Carrera Unified Formulation (CUF) use for micromechanics [31-33]. One of the advantages of CUF is the possibility of modeling multi-component structures as an ensemble of 1D finite elements with enriched cross-section kinematics [34]. Such a capability significantly reduces the computational costs - as there are no aspect ratio constraints - but retains 3D-like accuracy for all stress and strain components. CUF for linear and nonlinear multiscale problems provided twofold reductions on computational costs as compared to 3D FE [35, 36].

The objective of the present work is to investigate the influence of microscale matrix voids on the macroscopic mechanical properties and the microscopic fields. For the first time, CUF is used to model 3D RVE and voids. The modeling of voids includes their volume fraction and distribution. This paper is organized as follows: Sections 2 and 3 describe the theoretical framework for FE and micromechanics, respectively. The numerical results are in Section 4, and conclusions in Section 5.

## 2 Higher-order 1D structural theories



Figure 1: (a) Beam with arbitrary cross-section oriented along the $y$-axis, and (b) the 9-node bi-quadratic Lagrange expansion element in the natural coordinate system

Considering a beam oriented along the y-axis, as shown in Fig. 1(a), the displacement field in CUF is

$$
\begin{equation*}
\mathbf{u}=F_{\tau}(x, z) \mathbf{u}_{\tau}(y), \tau=1,2, \ldots M \tag{1}
\end{equation*}
$$

Where $\mathbf{u}$ is the displacement field and $F_{\tau}(x, z)$ is the expansion function across the cross-section. $\mathbf{u}_{\tau}$ is the generalized displacement vector, and M is the number of terms in the expansion function. The choice of $F_{\tau}$ and M is arbitrary. The present work utilizes the Lagrange Expansion (LE) class of expansions to enhance the cross-section kinematics, resulting in a Component-Wise (CW) model. In this approach, Lagrange polynomials explicitly discretize the cross-section geometry and displacement field. This work
uses 9-node bi-quadratic expansion elements (L9), see Fig. 1(b), in which the 3D displacement field is

$$
\begin{align*}
& u_{x}=\sum_{\tau=1}^{9} F_{\tau}(x, z) \cdot u_{x_{\tau}}(y) \\
& u_{y}=\sum_{\tau=1}^{9} F_{\tau}(x, z) \cdot u_{y_{\tau}}(y)  \tag{2}\\
& u_{z}=\sum_{\tau=1}^{9} F_{\tau}(x, z) \cdot u_{z_{\tau}}(y)
\end{align*}
$$

The use of Lagrange expansion results in a 1D numerical model that explicitly models the 3D domain without the need of fictitious entities like the reference axis. Furthermore, the displacement field consists of only translational degrees of freedom (DOF), without involving rotations. Further details on the use of Lagrange polynomials as expansion functions can be found in [37].

The stress and strain fields in vector notation are

$$
\begin{array}{r}
\boldsymbol{\sigma}=\left\{\sigma_{x x}, \sigma_{y y}, \sigma_{z z}, \sigma_{x y}, \sigma_{x z}, \sigma_{y z}\right\}^{T}  \tag{3}\\
\boldsymbol{\epsilon}=\left\{\epsilon_{x x}, \epsilon_{y y}, \epsilon_{z z}, \epsilon_{x y}, \epsilon_{x z}, \epsilon_{y z}\right\}^{T}
\end{array}
$$

Assuming linear strains, the displacements are related to the strains as

$$
\begin{equation*}
\epsilon=\mathbf{D} \cdot \mathbf{u} \tag{4}
\end{equation*}
$$

where $\mathbf{D}$ is the linear differentiation operator given by

$$
\mathbf{D}=\left[\begin{array}{ccc}
\frac{\partial}{\partial x} & 0 & 0 \\
0 & \frac{\partial}{\partial y} & 0 \\
0 & 0 & \frac{\partial}{\partial z} \\
\frac{\partial}{\partial y} & \frac{\partial}{\partial x} & 0 \\
\frac{\partial}{\partial z} & 0 & \frac{\partial}{\partial x} \\
0 & \frac{\partial}{\partial z} & \frac{\partial}{\partial y}
\end{array}\right]
$$

The constitutive law, considering an elastic material behavior, is

$$
\begin{equation*}
\sigma=\mathbf{C} \epsilon \tag{5}
\end{equation*}
$$

where $\mathbf{C}$ is the linear elastic material matrix. The structure is discretized in the axial direction using beam elements, interpolated using the nodal shape functions $N_{i}$. The combination of beam elements and cross-section expansions results in a 3D displacement field defined as

$$
\begin{equation*}
\mathbf{u}(x, y, z)=F_{\tau}(x, z) N_{i}(y) \mathbf{u}_{\tau i} \tag{6}
\end{equation*}
$$

where $\mathbf{u}_{\tau i}$ is the nodal displacement field. Based on the principle of virtual displacements,

$$
\begin{equation*}
\delta L_{i n t}=\delta L_{e x t} \tag{7}
\end{equation*}
$$

where $\delta L_{i n t}$ is the virtual variation of the internal strain energy,

$$
\begin{equation*}
\delta L_{i n t}=\int_{V} \delta \boldsymbol{\epsilon}^{T} \boldsymbol{\sigma} \tag{8}
\end{equation*}
$$

$L_{\text {ext }}$ is the work due to the externally applied load,

$$
\begin{equation*}
L_{e x t}=F_{s} N_{j} \delta \mathbf{u}_{s j}^{T} \mathbf{P} \tag{9}
\end{equation*}
$$

where $\mathbf{P}$ is the external force vector. Using Eqs. (5), (6) and (8), the stiffness matrix is defined as

$$
\begin{equation*}
\delta L_{i n t}=\delta \mathbf{u}_{s j}^{T} \mathbf{k}_{i j \tau s} \mathbf{u}_{\tau i} \tag{10}
\end{equation*}
$$

with

$$
\begin{equation*}
\mathbf{k}_{i j \tau s}=\int_{l} \int_{\Omega} \mathbf{D}^{T}\left(N_{i}(y) F_{\tau}(x, z)\right) \mathbf{C D}\left(N_{j}(y) F_{s}(x, z)\right) d \Omega d l \tag{11}
\end{equation*}
$$

$\mathbf{k}_{i j \tau s}$ is the 3 x 3 Fundamental Nucleus (FN), and is invariant with respect to the applied structural theory. $\Omega$ and $l$ represent the cross-section domain and beam length, respectively. A detailed explanation of the fundamental nucleus and the assembly of the global stiffness matrix is found in [34].

## 3 Component-wise micromechanics framework


(a)

(b)

Figure 2: Modelling the RVE using the CW approach. (a) 3D domain of a square-packed RVE and its individual constituents, and (b) 1D-CUF model

The CW micromechanics framework adopts 1D CUF models with Lagrange expansion functions. In this approach, an RVE is modeled, as shown in Fig. 2. Beam elements are used in the RVE thickness direction, and Lagrange expansion elements explicitly model the individual constituents of the RVE crosssection. The formulation is based on the assumption of a periodic microstructure, and periodic boundary conditions (PBC) are applied to the RVE. Such a process ensures the energy equivalence between the heterogeneous material and the effective homogenized medium [9]. The periodic boundary conditions, applied on opposite boundary surfaces, are formulated as

$$
\begin{equation*}
u_{i}^{j+}(x, y, z)-u_{i}^{j-}(x, y, z)=\bar{\epsilon}_{i k}\left(x_{k}^{j+}-x_{k}^{j-}\right) \tag{12}
\end{equation*}
$$

where $\bar{\epsilon}_{i k}$ is the applied macroscopic strain, indices $j+$ and $j$ - represent the positive and negative directions, respectively, along $x_{k}$. Two PBC sets can thus be distinguished, which are applied in the cross-section edges and the beam ends, respectively, as shown in Fig. 3. The homogenized stress ( $\bar{\sigma}_{i j}$ )


Figure 3: Application of the PBC on a square-packed RVE (a) on the opposite edges of the cross-section and (b) at the beam end nodes
and strain $\left(\bar{\epsilon}_{i j}\right)$ response is obtained by volume averaging the microscopic fields ( $\sigma_{i j}, \epsilon_{i j}$ ) [9],

$$
\begin{align*}
& \bar{\epsilon}_{i j}=\frac{1}{V} \int_{V} \epsilon_{i j} d V  \tag{13}\\
& \bar{\sigma}_{i j}=\frac{1}{V} \int_{V} \sigma_{i j} d V \tag{14}
\end{align*}
$$

where $V$ is the RVE volume. The constitutive relation for the homogenized medium reads as

$$
\begin{equation*}
\bar{\sigma}_{i j}=\bar{C}_{i j k l} \bar{\epsilon}_{i j} \tag{15}
\end{equation*}
$$

where $\bar{C}_{i j k l}$ is the homogenized elastic material matrix. A detailed explanation of the micromechanics framework using the CW approach is given in [31].

Voids are modeled in the matrix constituent of the RVE by selecting a set of Gauss points (GP) within the matrix domain and assigning them arbitrarily low elastic moduli. Such a process creates voids with a domain equal to the volume associated with the selected GP. Matrix GP are iteratively selected as void candidates until the void volume fraction, given as an input, is satisfied. Furthermore, the matrix GP can be selected either randomly throughout the RVE, or be biased in the RVE thickness direction. The former results in voids that are randomly and equally distributed within the RVE, while the latter
results in voids clustered towards one end of the RVE. This methodology thus allows for the development of a fully 3D cubic RVE with matrix voids of a required volume fraction as well as morphology. As an example, a multi-fiber RVE with $1 \%$ randomly distributed voids has been schematically shown in Fig. 4. Such a technique enables the efficient development of multiple configurations of the RVE for a given void volume fraction, which is an important requirement for statistical studies on the influence of voids.


Figure 4: A multi-fibre RVE with $1 \%$ voids randomly distributed within the matrix

## 4 Numerical results

### 4.1 Pristine RVE

The RVE has 22 randomly distributed fibers, and the material system is carbon/epoxy with $60 \%$ of fiber volume fraction. Figure 5 shows the randomly distributed fibers; the blue cylinders represent the carbon fibers, and the white portion indicates the matrix. The side of the cross-section is $38.5 \mu \mathrm{~m}$. The thickness along the y -axis is $19.25 \mu \mathrm{~m}$. The radius of the fiber is $3.6 \mu \mathrm{~m}$. The material properties are in Table 1 and retrieved from Sevenois et al. [38] through a reverse engineering approach. The longitudinal direction of the fiber coincides with the y-axis, see Fig. 2. This section aims to evaluate the influence of the cross-

Table 1: Properties of the constituent materials [38], the units of the elastic moduli are GPa

| Material | $E_{11}$ | $E_{22}=E_{33}$ | $G_{12}=G_{13}$ | $G_{23}$ | $\nu_{12}=\nu_{13}$ | $\nu_{23}$ |
| :--- | ---: | :---: | :---: | :---: | :---: | :---: |
| Fiber | 223.987 | 18.534 | 36.898 | 7.232 | 0.258 | 0.282 |
| Matrix | 3.700 | 3.700 | 3.700 | 3.700 | 0.400 | 0.400 |

section modeling on the homogenized properties and select the discretization for all subsequent analyses.


Figure 5: RVE with randomly distributed fibers
Figures 6 show two examples of cross-section discretizations. The FE mesh along y is constant and has one B4 element; as shown in previous works [31, 32], such axial mesh is sufficiently accurate. Figure 7


Figure 6: Cross-sections with 314 and 487 L9 elements
shows the homogenized properties for various meshes. The reference value to compute the error is the one provided by the most refined discretization, 3144 L 9 . The coarsest discretization has the highest error. However, such errors are lower than $2 \%$. Given that the use of the 314 L 9 leads to a considerably reduced computational cost for the statistical studies, the following numerical examples will use the same discretization. A further assessment focuses on the verification of the results via a comparison with [38],


Figure 7: Effect of the cross-section discretization on the homogenized properties of the pristine RVE
see Table 2. The results show a good match. Figures 8 and 9 show stress distributions given by an applied strain of $0.2 \%$.

Table 2: Homogenized properties for the pristine RVE via 314 L9 and results from [38], the units of the elastic moduli are GPa

| Model | 1D-CUF | FE ref. [38] |
| :---: | :---: | :---: |
| $\mathrm{E}_{11}$ | 135.88 | 135.74 |
| $\mathrm{E}_{22}$ | 9.96 | 9.66 |
| $\mathrm{E}_{33}$ | 9.91 | 9.66 |
| $\mathrm{G}_{12}$ | 5.19 | 5.31 |
| $\mathrm{G}_{13}$ | 5.02 | 5.31 |
| $\mathrm{G}_{23}$ | 3.15 | 3.23 |
| $\mathrm{\nu}_{12}$ | 0.31 | 0.31 |
| $\mathrm{\nu}_{13}$ | 0.31 | 0.31 |
| $\mathrm{~V}_{23}$ | 0.47 | 0.48 |



Figure 8: Axial stress contours, $\sigma_{x x}, \sigma_{z z}$, and $\sigma_{y y}$, with applied $\epsilon_{x x}, \epsilon_{z z}$, and $\epsilon_{y y}$, respectively, pristine RVE

### 4.2 RVE with voids

The analysis of voids considers two RVE configurations. The first one - referred to as RVE-1, has the same material and geometrical characteristics seen in the previous section. The second one, RVE-2, differs only for the dimension along y; that is, $38.5 \mu \mathrm{~m}$. From the modeling standpoint, the cross-section discretizations are the same, whereas two B4 are employed in RVE-2. Figure 10 shows both RVE and the beam meshes in which the reported mesh over the matrix is not representative of the numerical model, but it serves postprocessing purposes. o Table 3 summarizes the main characteristics of the models. The shape and void percentages considered in this paper are consistent with those from the literature [8]. The analysis considers two void distributions as follows


Figure 9: Shear stress contours, $\sigma_{x z}, \sigma_{x y}, \sigma_{y z}$, with applied $\epsilon_{x z}, \epsilon_{x y}$, and $\epsilon_{y z}$, respectively, pristine RVE


Figure 10: RVE-1 and RVE-2 and beam meshes

- The first distribution - referred to as VD-1 - is random within the RVE. Figure 11 shows an example of this void arrangement for the RVE-2.
- The second distribution - referred to as VD-2 - is random along the cross-section but follows a linear distribution of the void percentage along y. By considering Fig. 12, the first segment along y has $5 \%$ of the total voids, while the last one has some $30 \%$. The aim is to simulate a configuration with moderate clustering.

In both cases, 100 distributions per each void volume fraction were considered to evaluate statistical parameters. Table 4 presents the main characteristics of each distribution. VD-2 was applied only to RVE-2 due to the small $y$-dimension of RVE-1. Furthermore, VD-2 considers the random variation of the slope of the distribution; that is, the maximum of voids can be either on the last segment or the first


Figure 11: Random distributions of voids with increasing contents, VD-1


Figure 12: Clustering of voids, VD-2

Table 3: Structural and FE modeling of RVE-1 and RVE-2

|  | Discretization | DOF |
| :---: | :---: | :---: |
| RVE-1 | 314 L9 on the cross-section, <br> one B4 along y | 15876 |
| RVE-2 | 314 L9 on the cross-section, <br> two B4 along y | 27783 |

one. The results consider homogenized properties and local distributions of stress. For the latter, all six

Table 4: Summary of VD-1 and VD-2

| VD-1 |  |
| :---: | :---: |
| RVE considered | RVE-1 and RVE-2 |
| Void volume fractions | $1,2,3,4,5 \%$ |
| Subcases per void volume fractions | 100 |
| VD-2 | RVE-2 |
| RVE considered | $1,2,3,4,5 \%$ |
| Void volume fractions | 100 |

strains were applied separately, and, in each case, the strain is $0.2 \%$. The statistical parameters employed are the following [39, 40]: mean value $\bar{x}$, median $q_{2}$, standard deviation $s$, minimum value min, maximum value $\max$, first quartile $q_{1}$, third quartile $q_{3}$. Such parameters were computed on the maximum values of stress components of a given void distribution and content.

### 4.2.1 Influence of void distribution on homogenized properties

The first numerical assessment focuses on the homogenized properties. Tables 5 and 6 presents the results regarding VD-1 and both RVE. Table 7 shows the results for RVE-2 and considering VD-2. The results suggest the following:

- As expected, the void content affects the mechanical properties with the degradation that can reach $4 \%$. The standard deviation is very low in all cases.
- The use of a deeper RVE does not affect the mean values; that is, there is no significant influence on the homogenized properties. Likewise, the adoption of different void distributions does not lead to significant modifications of the properties.
- The influence of RVE and void content on the standard deviation is more evident, but, in all cases, $s$ is low.

Table 5: Mean value $(\bar{x})$ and standard deviation $(s)$ of the homogenized properties, RVE-1 and VD-1

|  |  | Void content (\%) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 |
| $\bar{x}$ (GPa) | $E_{11}$ | 135.846 | 135.809 | 135.771 | 135.734 | 135.697 |
|  | $E_{22}$ | 9.887 | 9.818 | 9.747 | 9.679 | 9.609 |
|  | $E_{33}$ | 9.836 | 9.765 | 9.695 | 9.625 | 9.555 |
|  | $G_{12}$ | 5.156 | 5.127 | 5.098 | 5.069 | 5.040 |
|  | $G_{13}$ | 4.993 | 4.964 | 4.935 | 4.906 | 4.877 |
|  | $G_{23}$ | 3.125 | 3.102 | 3.080 | 3.057 | 3.034 |
| $s$ (MPa) | $E_{11}$ | 0.744 | 1.100 | 1.056 | 1.258 | 1.460 |
|  | $E_{22}$ | 2.641 | 3.425 | 3.480 | 3.755 | 4.471 |
|  | $E_{33}$ | 2.264 | 2.735 | 3.388 | 4.493 | 3.960 |
|  | $G_{12}$ | 1.869 | 2.132 | 2.508 | 2.733 | 3.039 |
|  | $G_{13}$ | 1.496 | 1.956 | 2.502 | 2.923 | 2.828 |
|  | $G_{23}$ | 0.571 | 0.953 | 0.887 | 1.026 | 1.316 |

Table 6: Mean value ( $\bar{x}$ ) and standard deviation $(s)$ of the homogenized properties, RVE-2 and VD-1

|  |  | Void content (\%) |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  | 1 | 2 | 3 | 4 | 5 |
| $\bar{x}(\mathrm{GPa})$ | $E_{11}$ | 135.846 | 135.809 | 135.772 | 135.734 | 135.697 |
|  | $E_{22}$ | 9.887 | 9.818 | 9.749 | 9.679 | 9.609 |
|  | $E_{33}$ | 9.836 | 9.766 | 9.696 | 9.625 | 9.555 |
|  | $G_{12}$ | 5.156 | 5.127 | 5.098 | 5.069 | 5.040 |
|  | $G_{13}$ | 4.993 | 4.964 | 4.935 | 4.906 | 4.878 |
|  | $G_{23}$ | 3.125 | 3.103 | 3.080 | 3.057 | 3.034 |
| $s(\mathrm{MPa})$ | $E_{11}$ | 0.508 | 0.680 | 0.784 | 0.850 | 0.963 |
|  | $E_{22}$ | 1.470 | 2.174 | 2.231 | 2.910 | 3.108 |
|  | $E_{33}$ | 1.307 | 2.036 | 2.761 | 2.405 | 3.127 |
|  | $G_{12}$ | 1.064 | 1.673 | 1.835 | 1.979 | 2.064 |
|  | $G_{13}$ | 0.969 | 1.304 | 1.894 | 1.790 | 2.165 |
|  | $G_{23}$ | 0.456 | 0.580 | 0.647 | 0.790 | 0.868 |

Table 7: Mean value $(\bar{x})$ and standard deviation $(s)$ of the homogenized properties, RVE-2 and VD-2

|  |  | Void content (\%) |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  | 1 | 2 | 3 | 4 | 5 |
| $\bar{x}(\mathrm{GPa})$ | $E_{11}$ | 135.846 | 135.809 | 135.772 | 135.734 | 135.697 |
|  | $E_{22}$ | 9.887 | 9.818 | 9.749 | 9.679 | 9.610 |
|  | $E_{33}$ | 9.836 | 9.766 | 9.696 | 9.625 | 9.555 |
|  | $G_{12}$ | 5.156 | 5.127 | 5.098 | 5.069 | 5.040 |
|  | $G_{13}$ | 4.994 | 4.964 | 4.936 | 4.906 | 4.877 |
|  | $G_{23}$ | 3.125 | 3.103 | 3.080 | 3.057 | 3.034 |
| $s(\mathrm{MPa})$ | $E_{11}$ | 0.511 | 0.682 | 0.686 | 0.825 | 0.919 |
|  | $E_{22}$ | 1.566 | 1.955 | 2.330 | 2.680 | 2.527 |
|  | $E_{33}$ | 1.540 | 2.047 | 2.339 | 2.692 | 2.794 |
|  | $G_{12}$ | 1.120 | 1.448 | 1.765 | 1.824 | 1.921 |
|  | $G_{13}$ | 1.064 | 1.194 | 1.585 | 1.816 | 1.970 |
|  | $G_{23}$ | 0.417 | 0.573 | 0.658 | 0.771 | 0.936 |

### 4.2.2 Influence of void distribution on stress fields

The second numerical assessment concerns the influence of RVE and VD on the stress distributions. Table 8 shows the statistical parameters regarding the maximum values of axial stress found in the RVE- 1 having VD-1 and under various axial strains. The first column indicates the applied strain, the second one the stress component, whereas the last one shows the void content. Similarly, Tables 9 and 10 presents the statistical parameters obtained by applying shear strains. The results of RVE-2 with VD-1 are in Tables 11, 12, and 13. Figure 13 shows the box plots of the RVE-1 with VD-1 and applied axial strains. The most relevant stress components are reported. The box plot displays simultaneously several features of the data set [40]. The left side of the box is the first quartile $\left(q_{1}\right)$, and the right side is the third quartile $\left(q_{3}\right)$. The difference $q_{3}-q_{1}$ is the interquartile range (IQR). The vertical line inside the box is the second quartile or median $\left(q_{2}\right)$. The dashed horizontal line on the left of the box connects $q_{1}$ to the smallest data point within 1.5 IQR. Similarly, the one on the right side connects $q_{3}$ to the largest data point within 1.5 IQR. Data points falling beyond these ranges are indicated explicitly. For example, considering the case of $5 \%$ voids and $\epsilon_{x x}$ for RVE-1, the highest maximum stress is $106.8 \mathrm{MPa} . q_{1}, q_{2}$ and $q_{3}$ are $72.6,77.6$ and 84 MPa , respectively. The lowest minimum of stress is 62.8 MPa . Figures 14, 15, and 16 are the box plots with applied shear strains for RVE-1 and both strains for RVE-2. The results of VD-2 are in Tables 14, 15, and 16, and Figures 17 and 18. Figure 19 shows an example of stress distributions over a cross-section of the RVE. The cross-sections are those in which the peak values were found. The results suggest the following

- There is a general increase of stresses moving from RVE-1 to RVE-2 and VD-1 to VD-2. In other words, by considering deeper RVE and clustering, higher stresses were found.
- By considering the locations of stress peaks, they were found in the proximity of voids and at the interfaces between fibers and matrix.
- The increase of void content leads to higher stresses and wider stress ranges. Several box plots show rightward skewness of the data, i.e., quite high-stress peaks as compared to the mean value.
- As expected, by applying a longitudinal strain $\left(\epsilon_{y y}\right)$, most of the load is carried by the fibers. The increase of the void content causes a slight increase in the fiber load as it deteriorates the matrix stiffness.

Table 8: Statistical parameters of the axial stresses (MPa) for various void contents (\%) with applied $\epsilon_{x x}$, $\epsilon_{y y}$, and $\epsilon_{z z}$, RVE-1 and VD-1

|  |  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\sigma_{x x}^{\max }$ |  | 56.670 | 56.197 | 4.841 | 47.949 | 75.549 | 53.463 | 59.128 | 1 |
|  |  | 63.619 | 62.368 | 6.083 | 53.205 | 83.828 | 59.979 | 67.256 | 2 |
|  |  | 67.209 | 66.043 | 6.359 | 57.859 | 93.672 | 62.654 | 69.749 | 3 |
|  |  | 72.385 | 71.975 | 6.880 | 60.132 | 93.625 | 67.939 | 76.037 | 4 |
|  |  | 78.668 | 77.614 | 8.927 | 62.752 | 106.830 | 72.615 | 84.004 | 5 |
| $\epsilon_{x x}$ | $\sigma_{y y}^{\max }$ | 37.084 | 36.600 | 3.283 | 30.820 | 49.030 | 35.126 | 39.027 | 1 |
|  |  | 41.574 | 40.554 | 4.313 | 34.638 | 56.720 | 38.633 | 44.150 | 2 |
|  |  | 43.947 | 43.016 | 4.106 | 35.976 | 60.923 | 41.084 | 45.546 | 3 |
|  |  | 47.270 | 46.986 | 4.529 | 38.287 | 60.974 | 44.018 | 49.376 | 4 |
|  |  | 51.387 | 50.242 | 6.131 | 40.111 | 71.246 | 47.215 | 55.293 | 5 |
|  | $\sigma_{z z}^{\max }$ | 36.775 | 36.527 | 3.384 | 29.576 | 48.887 | 34.566 | 38.607 | 1 |
|  |  | 41.407 | 40.373 | 4.579 | 34.433 | 58.128 | 37.979 | 44.188 | 2 |
|  |  | 43.690 | 42.999 | 4.356 | 36.284 | 59.424 | 40.579 | 45.822 | 3 |
|  |  | 46.611 | 46.085 | 4.604 | 38.434 | 60.719 | 43.152 | 49.202 | 4 |
|  |  | 50.750 | 49.705 | 6.247 | 39.652 | 71.785 | 46.245 | 54.809 | 5 |
| $\epsilon_{y y}$ | $\sigma_{x x}^{\max }$ | 21.365 | 21.054 | 1.711 | 18.488 | 26.995 | 20.335 | 21.940 | 1 |
|  |  | 24.380 | 23.896 | 2.536 | 20.487 | 33.686 | 22.556 | 25.751 | 2 |
|  |  | 26.259 | 25.687 | 2.712 | 21.732 | 38.296 | 24.671 | 26.999 | 3 |
|  |  | 27.632 | 27.079 | 2.638 | 23.758 | 38.414 | 25.733 | 28.771 | 4 |
|  |  | 30.354 | 29.779 | 3.658 | 23.973 | 45.779 | 27.550 | 32.587 | 5 |
|  | $\sigma_{y y}^{\max }$ | 456.784 | 456.729 | 0.793 | 455.612 | 459.420 | 456.152 | 457.119 | 1 |
|  |  | 457.711 | 457.614 | 1.069 | 456.125 | 461.168 | 456.913 | 458.224 | 2 |
|  |  | 458.522 | 458.341 | 1.130 | 456.457 | 462.539 | 457.818 | 459.155 | 3 |
|  |  | 459.116 | 458.877 | 1.216 | 456.268 | 462.540 | 458.293 | 459.875 |  |
|  |  | 459.767 | 459.580 | 1.315 | 457.277 | 463.191 | 458.828 | 460.451 | 5 |
|  | $\sigma_{z z}^{\max }$ | 21.686 | 21.250 | 1.772 | 18.776 | 26.737 | 20.321 | 22.931 | 1 |
|  |  | 25.415 | 24.498 | 3.936 | 20.010 | 43.822 | 22.755 | 26.549 | 2 |
|  |  | 27.733 | 26.797 | 4.229 | 22.349 | 44.956 | 24.731 | 29.240 | 3 |
|  |  | 29.762 | 28.635 | 4.343 | 23.900 | 44.237 | 26.767 | 31.276 | 4 |
|  |  | 31.531 | 30.300 | 4.508 | 25.207 | 46.899 | 28.297 | 33.226 | 5 |
| $\epsilon_{z z}$ | $\sigma_{x x}^{\max }$ | 37.967 | 37.228 | 3.636 | 30.741 | 49.088 | 35.709 | 39.420 | 1 |
|  |  | 43.580 | 41.379 | 7.155 | 35.145 | 80.370 | 39.059 | 46.015 | 2 |
|  |  | 47.999 | 46.647 | 7.202 | 35.386 | 72.759 | 43.037 | 50.447 | 3 |
|  |  | 51.617 | 48.708 | 8.836 | 39.474 | 81.787 | 45.579 | 55.250 | 4 |
|  |  | 53.271 | 51.648 | 8.195 | 39.851 | 79.988 | 47.618 | 56.238 | 5 |
|  | $\sigma_{y y}^{\max }$ | 38.673 | 38.031 | 3.561 | 32.136 | 50.242 | 36.481 | 40.160 | 1 |
|  |  | 44.237 | 42.425 | 7.075 | 36.116 | 79.411 | 39.652 | 46.604 | 2 |
|  |  | 48.770 | 47.737 | 7.144 | 37.803 | 75.340 | 43.465 | 52.086 | 3 |
|  |  | 52.709 | 50.127 | 8.716 | 41.658 | 79.996 | 47.246 | 55.247 | 4 |
|  |  | 54.410 | 52.991 | 8.124 | 41.642 | 83.652 | 48.430 | 58.174 | 5 |
|  | $\sigma_{z z}^{\max }$ | 59.310 | 58.232 | 5.392 | 50.047 | 76.481 | 56.026 | 61.267 | 1 |
|  |  | 67.781 | 65.093 | 10.457 | 54.467 | 118.228 | 60.751 | 71.349 | 2 |
|  |  | 74.608 | 72.414 | 10.733 | 60.051 | 115.875 | 66.339 | 79.398 | 3 |
|  |  | 80.906 | 77.128 | 13.076 | 61.675 | 122.699 | 73.160 | 84.118 | 4 |
|  |  | 83.825 | 81.378 | 11.946 | 63.852 | 129.370 | 75.342 | 89.852 | 5 |



Figure 13: Box plots of axial stresses with applied axial strains, RVE-1 and VD-1


Figure 14: Box plots of stress components with applied shear strains, RVE-1 and VD-1


Figure 15: Box plots of axial stresses with applied axial strains, RVE-2 and VD-1


Figure 16: Box plots of stress components with applied shear strains, RVE-2 and VD-1


Figure 17: Box plots of stress components with applied axial strains, RVE-2 and VD-2


Figure 18: Box plots of stress components with applied shear strains, RVE-2 and VD-2

Table 9: Statistical parameters of stresses (MPa) for various void contents (\%) with applied $\epsilon_{x z}$, RVE-1 and VD-1

|  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\sigma_{x x}^{\max }$ | 30.805 | 30.050 | 3.415 | 25.565 | 46.629 | 28.635 | 32.427 | 1 |
|  | 34.537 | 33.835 | 4.170 | 26.272 | 48.472 | 31.461 | 36.653 | 2 |
|  | 38.093 | 37.324 | 5.138 | 28.982 | 54.148 | 34.863 | 40.916 | 3 |
|  | 39.908 | 39.397 | 4.557 | 31.828 | 53.213 | 36.679 | 42.068 | 4 |
|  | 42.705 | 41.544 | 5.721 | 32.111 | 60.232 | 38.208 | 46.298 | 5 |
| $\sigma_{y y}^{\max }$ | 22.234 | 22.371 | 2.278 | 18.175 | 31.514 | 20.228 | 23.627 | 1 |
|  | 25.130 | 24.513 | 2.889 | 20.277 | 35.152 | 23.448 | 26.018 | 2 |
|  | 27.535 | 27.161 | 3.586 | 21.789 | 38.993 | 25.277 | 29.220 | 3 |
|  | 29.044 | 28.498 | 3.446 | 22.878 | 39.533 | 26.713 | 30.997 | 4 |
|  | 31.553 | 30.680 | 4.652 | 23.472 | 46.079 | 28.268 | 34.002 | 5 |
| $\sigma_{z z}^{\max }$ | 27.696 | 27.621 | 2.648 | 21.492 | 36.014 | 26.165 | 29.158 | 1 |
|  | 31.258 | 30.426 | 3.326 | 25.948 | 41.815 | 29.317 | 32.955 | 2 |
|  | 33.543 | 32.692 | 4.062 | 27.929 | 48.693 | 30.819 | 35.393 | 3 |
|  | 35.801 | 34.934 | 4.262 | 28.906 | 48.680 | 32.539 | 39.023 | 4 |
|  | 39.403 | 37.604 | 6.398 | 30.211 | 57.848 | 34.744 | 42.619 | 5 |
| $\sigma_{x z}^{\max }$ | 23.332 | 22.787 | 1.310 | 22.086 | 30.339 | 22.477 | 23.749 | 1 |
|  | 25.533 | 24.852 | 2.831 | 22.225 | 35.063 | 23.441 | 26.449 | 2 |
|  | 25.883 | 25.173 | 2.420 | 22.469 | 33.916 | 24.117 | 27.093 | 3 |
|  | 27.396 | 26.760 | 3.137 | 23.077 | 38.418 | 24.836 | 28.798 | 4 |
|  | 28.870 | 28.518 | 3.390 | 23.295 | 39.246 | 26.260 | 31.173 | 5 |



Figure 19: Cross-section distributions of stresses in which peak values were found, void content $5 \%$, applied $\epsilon_{z z}$, RVE-2 and VD-2

Table 10: Statistical parameters of stresses (MPa) for various void contents (\%) with applied $\epsilon_{x y}$ and $\epsilon_{y z}$, RVE-1 and VD-1

|  |  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\epsilon_{x y}$ | $\sigma_{y y}^{\max }$ | 21.784 | 21.118 | 6.195 | 11.855 | 45.525 | 17.085 | 24.162 | 1 |
|  |  | 30.693 | 30.031 | 6.467 | 19.520 | 49.347 | 25.708 | 34.987 | 2 |
|  |  | 36.921 | 35.692 | 6.793 | 25.062 | 56.996 | 32.120 | 40.700 | 3 |
|  |  | 43.298 | 40.832 | 8.730 | 30.106 | 70.883 | 36.463 | 47.364 | 4 |
|  |  | 49.871 | 48.275 | 8.511 | 34.598 | 71.430 | 43.836 | 53.535 | 5 |
|  | $\sigma_{x y}^{\max }$ | 63.376 | 61.813 | 3.844 | 60.111 | 79.480 | 60.825 | 65.998 | 1 |
|  |  | 65.501 | 63.685 | 4.896 | 59.892 | 82.703 | 61.322 | 68.995 | 2 |
|  |  | 67.107 | 65.933 | 4.863 | 60.415 | 80.350 | 62.924 | 69.972 | 3 |
|  |  | 68.973 | 68.214 | 5.266 | 59.588 | 85.396 | 65.391 | 71.999 | 4 |
|  |  | 69.565 | 69.412 | 5.191 | 59.149 | 84.766 | 65.866 | 72.130 | 5 |
|  | $\sigma_{y z}^{\max }$ | 21.530 | 21.230 | 1.633 | 19.450 | 26.227 | 20.159 | 22.372 | 1 |
|  |  | 22.833 | 22.759 | 1.848 | 19.665 | 31.435 | 21.480 | 23.895 | 2 |
|  |  | 23.954 | 23.750 | 2.069 | 19.957 | 28.814 | 22.417 | 25.223 | 3 |
|  |  | 24.520 | 24.335 | 2.064 | 19.877 | 31.635 | 23.181 | 25.785 | 4 |
|  |  | 25.685 | 25.163 | 2.470 | 21.635 | 33.578 | 23.880 | 27.293 | 5 |
| $\epsilon_{y z}$ | $\sigma_{y y}^{\max }$ | 19.791 | 19.022 | 5.395 | 12.292 | 41.777 | 15.880 | 21.845 | 1 |
|  |  | 27.668 | 27.137 | 5.674 | 16.378 | 48.906 | 23.592 | 31.313 | 2 |
|  |  | 35.047 | 33.804 | 6.981 | 22.704 | 59.602 | 30.311 | 38.709 | 3 |
|  |  | 41.319 | 40.862 | 6.482 | 29.860 | 62.146 | 37.005 | 44.087 | 4 |
|  |  | 47.408 | 45.947 | 7.481 | 33.746 | 67.329 | 41.824 | 52.463 | 5 |
|  | $\sigma_{x y}^{\max }$ | 24.920 | 23.979 | 2.071 | 23.089 | 33.275 | 23.556 | 25.799 | 1 |
|  |  | 26.323 | 25.987 | 2.530 | 23.041 | 34.810 | 23.989 | 27.674 | 2 |
|  |  | 28.028 | 27.353 | 3.131 | 23.126 | 36.069 | 25.723 | 29.877 | 3 |
|  |  | 28.667 | 28.144 | 3.436 | 23.301 | 40.553 | 26.521 | 30.229 | 4 |
|  |  | 30.703 | 30.166 | 3.352 | 24.011 | 39.322 | 28.148 | 32.857 | 5 |
|  | $\sigma_{y z}^{\max }$ | 59.737 | 60.069 | 6.250 | 47.890 | 81.287 | 55.421 | 63.651 | 1 |
|  |  | 63.582 | 62.157 | 8.476 | 49.629 | 104.874 | 58.792 | 66.568 | 2 |
|  |  | 67.037 | 65.812 | 6.561 | 56.721 | 94.796 | 62.925 | 69.869 | 3 |
|  |  | 70.015 | 68.356 | 10.103 | 56.585 | 104.051 | 63.138 | 75.074 | 4 |
|  |  | 70.348 | 67.821 | 7.816 | 57.085 | 100.543 | 64.730 | 74.396 | 5 |

Table 11: Statistical parameters of stresses (MPa) for various void contents (\%) with applied $\epsilon_{x x}, \epsilon_{y y}, \epsilon_{z z}$, RVE-2 and VD-1


Table 12: Statistical parameters of stresses (MPa) for various void contents (\%) with applied $\epsilon_{x z}$, RVE-2 and VD-1

|  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\sigma_{x x}^{\max }$ | 32.767 | 32.319 | 3.446 | 26.510 | 44.510 | 30.611 | 34.751 | 1 |
|  | 36.017 | 35.512 | 3.425 | 29.454 | 48.059 | 33.690 | 38.151 | 2 |
|  | 39.285 | 38.334 | 4.576 | 30.620 | 56.095 | 35.895 | 41.802 | 3 |
|  | 42.610 | 41.396 | 4.990 | 34.802 | 56.516 | 38.725 | 45.264 | 4 |
|  | 44.116 | 42.772 | 5.809 | 33.754 | 66.041 | 39.720 | 47.688 | 5 |
| $\sigma_{y y}^{\max }$ | 23.626 | 23.185 | 2.302 | 20.092 | 31.829 | 22.337 | 24.424 | 1 |
|  | 26.079 | 26.024 | 2.512 | 21.805 | 35.437 | 24.336 | 27.393 | 2 |
|  | 28.590 | 28.122 | 3.216 | 23.405 | 43.579 | 26.226 | 30.115 | 3 |
|  | 30.838 | 30.872 | 3.278 | 25.150 | 39.111 | 27.985 | 33.019 | 4 |
|  | 32.180 | 31.488 | 3.944 | 25.201 | 46.000 | 29.641 | 34.641 | 5 |
| $\sigma_{z z}^{\max }$ | 29.516 | 28.611 | 3.092 | 25.473 | 42.860 | 27.759 | 30.228 | 1 |
|  | 32.688 | 32.010 | 3.532 | 26.525 | 41.951 | 29.982 | 35.574 | 2 |
|  | 35.315 | 34.712 | 4.251 | 28.611 | 54.328 | 32.231 | 37.741 | 3 |
|  | 37.839 | 37.318 | 4.015 | 30.645 | 48.793 | 35.024 | 39.910 | 4 |
|  | 39.838 | 39.881 | 4.213 | 30.862 | 56.272 | 36.787 | 42.442 | 5 |
| $\sigma_{x z}^{\max }$ | 23.951 | 23.738 | 1.447 | 22.199 | 29.425 | 22.781 | 24.715 | 1 |
|  | 26.216 | 25.583 | 2.520 | 22.534 | 36.084 | 24.593 | 27.471 | 2 |
|  | 27.619 | 27.162 | 2.810 | 22.868 | 39.971 | 25.700 | 29.040 | 3 |
|  | 28.650 | 28.126 | 2.617 | 24.548 | 41.136 | 26.927 | 29.869 | 4 |
|  | 30.031 | 29.514 | 3.651 | 25.055 | 42.677 | 27.142 | 32.170 | 5 |

- $\sigma_{x x}$ and $\sigma_{z z}$ is the stress component with the highest values in the matrix. In some cases, the increase of this component reached three times the value of the pristine RVE.

Further analyses can make use of the probability density function [39] as shown in Figs. 20 and 21. The aim is to show the major differences in the results stemming from the three modeling approaches, namely, RVE-1 and VD-1, RVE-2 and VD-1, and RVE-2 and VD-2. As stated above, there is an increase in both the mean and peak values as deeper RVE and clustering are considered. By moving from RVE-1/VD-1 to RVE-2/VD-2, the mean values increased by some $10 \%$.

## 5 Conclusions

The present work has investigated the influence of matrix voids on the prediction of the homogenized properties and stress fields in RVE for fiber-reinforced polymer composites. The assessments are numerical and based on a numerically efficient FE framework and refined 1D structural models from CUF. The RVE models have randomly distributed fibers and voids within the matrix. All three constituents are modeled via a component-wise approach via Lagrange polynomials defining the displacement field and the geometry. The use of 1D models avoids the aspect ratio constraints of 3D FE and leads to significantly

Table 13: Statistical parameters of stresses (MPa) for various void contents (\%) with applied $\epsilon_{y z}$ and $\epsilon_{x y}$, RVE-2 and VD-1

|  |  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\epsilon_{y z}$ | $\sigma_{y y}^{\max }$ | 20.020 | 19.301 | 4.532 | 11.050 | 35.085 | 16.953 | 22.898 | 1 |
|  |  | 27.768 | 26.507 | 6.810 | 17.752 | 53.593 | 22.986 | 29.985 | 2 |
|  |  | 32.251 | 30.610 | 5.944 | 22.022 | 48.272 | 27.419 | 35.547 | 3 |
|  |  | 38.163 | 36.618 | 8.120 | 23.685 | 58.861 | 31.776 | 43.498 | 4 |
|  |  | 41.886 | 40.531 | 7.193 | 29.472 | 60.791 | 35.895 | 47.705 | 5 |
|  | $\sigma_{x y}^{\max }$ | 25.900 | 25.516 | 2.101 | 23.338 | 33.271 | 23.953 | 27.415 | 1 |
|  |  | 27.200 | 27.059 | 2.433 | 23.652 | 35.062 | 25.201 | 28.757 | 2 |
|  |  | 29.144 | 28.554 | 2.968 | 23.558 | 39.388 | 27.234 | 31.167 | 3 |
|  |  | 30.633 | 29.866 | 3.777 | 24.850 | 42.728 | 27.808 | 32.637 | 4 |
|  |  | 31.346 | 30.510 | 3.869 | 25.140 | 45.029 | 28.566 | 33.845 | 5 |
|  | $\sigma_{y z}^{\max }$ | 60.572 | 60.762 | 4.968 | 48.284 | 77.659 | 56.989 | 63.214 | 1 |
|  |  | 66.553 | 64.988 | 7.414 | 54.657 | 101.766 | 61.653 | 69.257 | 2 |
|  |  | 70.233 | 68.658 | 7.139 | 57.289 | 96.886 | 65.634 | 73.226 | 3 |
|  |  | 73.706 | 71.556 | 9.671 | 59.329 | 117.436 | 66.662 | 76.852 |  |
|  |  | 73.963 | 71.153 | 8.176 | 62.108 | 97.577 | 68.744 | 78.685 | 5 |
| $\epsilon_{x y}$ | $\sigma_{y y}^{\max }$ | 22.565 | 22.174 | 5.419 | 12.646 | 46.350 | 18.364 | 25.469 | 1 |
|  |  | 30.965 | 29.366 | 7.871 | 15.009 | 66.575 | 26.259 | 33.711 | 2 |
|  |  | 33.777 | 31.783 | 7.372 | 21.799 | 56.058 | 28.692 | 36.546 | 3 |
|  |  | 39.585 | 38.555 | 8.006 | 25.038 | 65.015 | 33.669 | 43.868 | 4 |
|  |  | 44.343 | 42.294 | 9.157 | 29.837 | 74.184 | 37.520 | 49.710 | 5 |
|  | $\sigma_{x y}^{\max }$ | 65.118 | 64.859 | 3.490 | 60.580 | 74.632 | 62.103 | 67.171 | 1 |
|  |  | 67.810 | 67.368 | 4.508 | 60.467 | 78.017 | 64.616 | 71.403 | 2 |
|  |  | 69.975 | 69.362 | 4.958 | 60.876 | 85.716 | 65.998 | 73.325 | 3 |
|  |  | 72.375 | 71.477 | 5.551 | 63.173 | 95.013 | 68.403 | 76.123 | 4 |
|  |  | 73.706 | 73.696 | 5.093 | 63.207 | 85.359 | 69.924 | 77.209 | 5 |
|  | $\sigma_{y z}^{\max }$ | 22.067 | 21.734 | 1.468 | 19.713 | 25.920 | 20.996 | 22.934 | 1 |
|  |  | 23.150 | 22.732 | 1.681 | 19.762 | 27.572 | 21.943 | 24.216 | 2 |
|  |  | 24.595 | 24.502 | 1.937 | 21.794 | 34.707 | 23.237 | 25.341 | 3 |
|  |  | 25.302 | 25.016 | 1.844 | 21.704 | 31.895 | 23.959 | 26.641 | 4 |
|  |  | 26.028 | 25.592 | 2.163 | 22.031 | 33.482 | 24.404 | 27.289 | 5 |




$\vdash---\checkmark \square------\mid++$
(a)

(b)

$$
\vdash---\square
$$

(c)

Figure 20: Fitting of the probability density function of $\sigma_{z z}^{\max }$ with applied $\epsilon_{z z}$ (a) RVE-1 and VD-1, (b) RVE-2 and VD-1, (b) RVE-2 and VD-2, void content 5\%

Table 14: Statistical parameters of the axial stresses (MPa) for various void contents (\%) with applied $\epsilon_{x x}, \epsilon_{y y}, \epsilon_{z z}$, RVE-2 and VD-2

|  |  | , | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\epsilon_{x x}$ | $\sigma_{x x}^{\max }$ | 61.184 | 60.513 | 5.420 | 51.224 | 80.075 | 57.401 | 63.775 | 1 |
|  |  | 68.120 | 67.009 | 6.479 | 57.352 | 84.459 | 63.328 | 71.757 | 2 |
|  |  | 73.616 | 73.292 | 7.045 | 60.621 | 95.766 | 68.139 | 76.427 | 3 |
|  |  | 81.647 | 80.292 | 8.969 | 67.006 | 112.855 | 74.983 | 86.571 |  |
|  |  | 88.384 | 86.704 | 10.851 | 71.621 | 122.568 | 80.835 | 94.156 | 5 |
|  | $\sigma_{y y}^{\max }$ | 40.114 | 39.585 | 3.715 | 33.903 | 52.691 | 37.195 | 42.301 | 1 |
|  |  | 44.505 | 43.602 | 4.582 | 36.722 | 55.507 | 40.712 | 47.476 | 2 |
|  |  | 48.049 | 46.903 | 4.703 | 39.253 | 60.303 | 44.565 | 50.210 | 3 |
|  |  | 53.014 | 52.126 | 5.967 | 44.620 | 75.771 | 48.688 | 56.000 | 4 |
|  |  | 57.265 | 56.281 | 7.259 | 45.180 | 82.883 | 52.087 | 61.074 | 5 |
|  | $\sigma_{z z}^{\max }$ | 39.811 | 38.870 | 3.900 | 33.616 | 52.128 | 36.866 | 42.412 | 1 |
|  |  | 44.218 | 43.421 | 4.736 | 35.187 | 55.609 | 40.608 | 46.922 | 2 |
|  |  | 47.793 | 47.275 | 4.681 | 39.196 | 59.951 | 44.829 | 50.088 | 3 |
|  |  | 52.135 | 50.979 | 6.274 | 42.419 | 79.755 | 47.546 | 55.520 | 4 |
|  |  | 56.144 | 54.872 | 7.290 | 41.707 | 85.881 | 51.257 | 59.882 | 5 |
| $\epsilon_{y y}$ | $\sigma_{x x}^{\max }$ | 22.866 | 22.151 | 2.369 | 19.637 | 31.509 | 21.278 | 24.125 |  |
|  |  | 26.168 | 25.364 | 2.567 | 22.763 | 34.504 | 24.079 | 27.980 | 2 |
|  |  | 28.521 | 28.007 | 2.817 | 23.172 | 40.033 | 26.839 | 29.830 | 3 |
|  |  | 31.286 | 30.456 | 3.531 | 26.334 | 45.258 | 28.994 | 32.568 | 4 |
|  |  | 33.911 | 33.667 | 4.004 | 27.330 | 46.940 | 30.669 | 36.192 | 5 |
|  | $\sigma_{y y}^{\max }$ | 457.284 | 457.156 | 0.552 | 456.355 | 458.813 | 456.880 | 457.644 | 1 |
|  |  | 458.239 | 458.170 | 0.819 | 457.000 | 461.811 | 457.595 | 458.680 | 2 |
|  |  | 458.946 | 458.838 | 0.793 | 457.575 | 461.419 | 458.336 | 459.458 | 3 |
|  |  | 459.707 | 459.490 | 0.976 | 458.037 | 462.620 | 458.936 | 460.405 | 4 |
|  |  | 459.983 | 459.844 | 0.866 | 458.020 | 462.887 | 459.389 | 460.556 | 5 |
|  | $\sigma_{z z}^{\max }$ | 23.566 | 22.745 | 2.524 | 19.554 | 31.632 | 21.862 | 24.934 | 1 |
|  |  | 26.963 | 26.282 | 3.284 | 21.994 | 38.557 | 24.740 | 28.313 | 2 |
|  |  | 30.692 | 29.707 | 4.496 | 24.935 | 53.239 | 27.897 | 32.357 | 3 |
|  |  | 32.340 | 31.371 | 4.368 | 26.345 | 55.498 | 29.557 | 34.407 | 4 |
|  |  | 35.936 | 34.555 | 4.906 | 28.757 | 52.841 | 32.105 | 38.669 | 5 |
| $\epsilon_{z z}$ | $\sigma_{x x}^{\max }$ | 40.884 | 39.986 | 4.289 | 33.392 | 57.787 | 37.971 | 43.399 | 1 |
|  |  | 46.842 | 45.322 | 6.268 | 35.751 | 69.818 | 42.370 | 49.646 | 2 |
|  |  | 52.476 | 51.505 | 8.343 | 40.776 | 89.037 | 46.746 | 55.205 | 3 |
|  |  | 55.604 | 53.630 | 7.955 | 44.153 | 88.789 | 49.953 | 58.041 | 4 |
|  |  | 60.714 | 58.703 | 9.607 | 48.107 | 103.831 | 54.355 | 65.274 | 5 |
|  | $\sigma_{y y}^{\max }$ | 41.576 | 40.548 | 4.476 | 34.441 | 57.409 | 38.447 | 44.151 | 1 |
|  |  | 47.688 | 46.730 | 6.036 | 37.894 | 69.273 | 43.320 | 50.476 | 2 |
|  |  | 53.528 | 52.091 | 8.501 | 41.823 | 89.030 | 47.383 | 56.144 | 3 |
|  |  | 56.632 | 54.894 | 7.921 | 44.355 | 89.260 | 51.292 | 59.340 | 4 |
|  |  | 62.257 | 59.939 | 9.384 | 47.014 | 101.843 | 56.464 | 66.879 | 5 |
|  | $\sigma_{z z}^{\max }$ | 63.501 | 62.090 | 7.024 | 53.176 | 88.684 | 58.399 | 67.208 | 1 |
|  |  | 73.075 | 71.401 | 8.955 | 57.582 | 103.572 | 66.655 | 77.292 | 2 |
|  |  | 82.106 | 80.633 | 12.928 | 64.174 | 133.630 | 74.139 | 87.171 | 3 |
|  |  | 87.218 | 84.795 | 11.703 | 69.644 | 134.656 | 79.457 | 92.648 | 4 |
|  |  | 96.180 | 92.460 | 14.073 | 72.974 | 151.082 | 85.732 | 102.695 | 5 |

Table 15: Statistical parameters of the stresses (MPa) for various void contents (\%) with applied $\epsilon_{x z}$, RVE-2 and VD-2

|  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\sigma_{x x}^{\max }$ | 32.989 | 32.163 | 4.044 | 25.498 | 52.723 | 30.281 | 35.119 | 1 |
|  | 37.825 | 37.247 | 4.337 | 31.297 | 53.423 | 34.628 | 39.197 | 2 |
|  | 40.695 | 39.884 | 4.293 | 32.023 | 54.350 | 37.516 | 43.715 | 3 |
|  | 44.599 | 43.274 | 5.376 | 36.180 | 57.803 | 40.217 | 47.929 | 4 |
|  | 47.680 | 46.473 | 7.485 | 36.011 | 87.341 | 42.779 | 50.664 | 5 |
| $\sigma_{y y}^{\max }$ | 23.970 | 23.514 | 2.522 | 20.285 | 35.145 | 22.029 | 25.709 | 1 |
|  | 27.385 | 26.824 | 2.984 | 22.268 | 38.468 | 25.163 | 29.026 | 2 |
|  | 29.982 | 29.079 | 3.444 | 22.793 | 41.750 | 27.830 | 31.888 | 3 |
|  | 32.563 | 31.732 | 3.941 | 26.255 | 45.894 | 29.673 | 35.459 | 4 |
|  | 35.136 | 34.596 | 5.267 | 26.979 | 59.975 | 31.538 | 37.009 | 5 |
| $\sigma_{z z}^{\max }$ | 29.750 | 28.976 | 2.766 | 26.211 | 38.862 | 27.658 | 31.333 | 1 |
|  | 33.682 | 33.081 | 3.497 | 27.400 | 43.096 | 31.294 | 35.923 | 2 |
|  | 37.313 | 36.264 | 4.594 | 29.645 | 55.192 | 34.171 | 39.632 | 3 |
|  | 40.226 | 39.670 | 4.597 | 29.768 | 58.403 | 37.550 | 42.241 | 4 |
|  | 44.324 | 43.313 | 6.283 | 33.381 | 66.927 | 40.089 | 46.637 | 5 |
| $\sigma_{x z}^{\max }$ | 24.560 | 24.170 | 1.895 | 22.350 | 34.621 | 23.125 | 25.373 | 1 |
|  | 26.646 | 26.128 | 2.818 | 22.206 | 35.983 | 24.560 | 28.000 | 2 |
|  | 27.902 | 27.354 | 2.887 | 23.337 | 41.013 | 25.770 | 29.446 | 3 |
|  | 29.453 | 29.013 | 3.479 | 24.420 | 43.170 | 26.818 | 31.159 | 4 |
|  | 30.902 | 30.032 | 3.095 | 26.062 | 42.359 | 28.670 | 32.773 | 5 |



Figure 21: Fitting of the probability density function of $\sigma_{y z}^{\max }$ with applied $\epsilon_{y z}$ (a) RVE-1 and VD-1, (b) RVE-2 and VD-1, (b) RVE-2 and VD-2, void content 4\%

Table 16: Statistical parameters of the stresses (MPa) for various void contents (\%) with applied $\epsilon_{y z}$ and $\epsilon_{x y}$, RVE-2 and VD-2

|  |  | $\bar{x}$ | $q_{2}$ | $s$ | min | max | $q_{1}$ | $q_{3}$ | Voids |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\epsilon_{y z}$ | $\sigma_{y y}^{\max }$ | 20.290 | 19.264 | 5.407 | 13.098 | 52.881 | 16.789 | 22.535 | 1 |
|  |  | 31.790 | 31.594 | 6.446 | 21.305 | 56.715 | 26.491 | 34.959 | 2 |
|  |  | 40.235 | 37.751 | 8.673 | 27.987 | 77.049 | 34.250 | 42.887 | 3 |
|  |  | 46.519 | 45.106 | 7.191 | 35.307 | 70.625 | 41.917 | 51.084 | 4 |
|  |  | 57.071 | 56.090 | 9.011 | 40.612 | 82.125 | 50.009 | 61.905 | 5 |
|  | $\sigma_{x y}^{\max }$ | 25.724 | 25.044 | 2.482 | 23.377 | 38.514 | 24.045 | 26.752 | 1 |
|  |  | 28.199 | 27.628 | 2.987 | 23.464 | 38.133 | 26.143 | 29.557 | 2 |
|  |  | 29.629 | 29.094 | 3.231 | 24.094 | 40.065 | 27.266 | 31.219 | 3 |
|  |  | 31.108 | 30.273 | 4.038 | 24.273 | 46.375 | 28.401 | 33.198 | 4 |
|  |  | 32.239 | 31.666 | 4.052 | 25.462 | 45.885 | 29.247 | 34.163 | 5 |
|  | $\sigma_{y z}^{\max }$ | 61.989 | 62.027 | 4.920 | 51.904 | 82.254 | 58.386 | 64.902 | 1 |
|  |  | 67.716 | 66.712 | 7.379 | 54.425 | 98.255 | 63.042 | 70.546 | 2 |
|  |  | 70.507 | 68.962 | 7.909 | 57.407 | 96.102 | 64.842 | 74.168 | 3 |
|  |  | 73.761 | 72.232 | 8.135 | 58.936 | 104.704 | 68.343 | 77.213 | 4 |
|  |  | 77.246 | 75.763 | 8.513 | 63.038 | 107.611 | 71.231 | 82.170 | 5 |
| $\epsilon_{x y}$ | $\sigma_{y y}^{\max }$ | 23.606 | 22.164 | 6.074 | 14.351 | 47.181 | 19.767 | 26.322 | 1 |
|  |  | 33.531 | 32.056 | 8.677 | 20.891 | 74.465 | 27.439 | 36.996 | 2 |
|  |  | 42.219 | 39.942 | 8.821 | 26.222 | 66.975 | 36.359 | 46.840 | 3 |
|  |  | 48.904 | 47.841 | 7.635 | 33.686 | 71.438 | 43.108 | 54.139 | 4 |
|  |  | 58.139 | 55.929 | 9.302 | 41.535 | 92.147 | 51.706 | 63.112 | 5 |
|  | $\sigma_{x y}^{\max }$ | 65.690 | 65.300 | 3.661 | 60.662 | 75.835 | 62.713 | 67.627 | 1 |
|  |  | 69.364 | 68.307 | 4.653 | 62.345 | 85.661 | 65.422 | 73.146 | 2 |
|  |  | 71.130 | 71.107 | 5.694 | 60.118 | 84.438 | 66.109 | 75.247 | 3 |
|  |  | 72.958 | 72.508 | 5.534 | 62.908 | 92.724 | 69.058 | 76.192 | 4 |
|  |  | 75.239 | 74.535 | 5.912 | 61.754 | 98.422 | 71.969 | 78.361 | 5 |
|  | $\sigma_{y z}^{\max }$ | 22.257 | 21.935 | 1.702 | 19.992 | 27.488 | 20.958 | 22.779 | 1 |
|  |  | 23.764 | 23.419 | 2.172 | 20.403 | 33.136 | 22.158 | 24.645 | 2 |
|  |  | 24.815 | 24.466 | 2.189 | 21.597 | 33.206 | 23.023 | 26.072 | 3 |
|  |  | 26.086 | 25.630 | 2.174 | 21.772 | 32.160 | 24.626 | 27.107 | 4 |
|  |  | 27.191 | 26.770 | 2.646 | 22.004 | 39.498 | 25.503 | 28.379 | 5 |

lower computational costs. The present framework can deal with various sets of void distributions to investigate the influence of void content and morphology. Such analyses considered multiple scenarios and statistical metrics. The RVE is 3D, and the influence of its depth is another assessed parameter. The most significant findings are the following:

- As well-known, the influence of void distributions and RVE dimensions on the homogenized properties is low. The void content is the fundamental parameter to consider, independently of the void arrangement.
- The void arrangement influences the stress fields. The clustering of voids leads to higher stress mean values and peaks, and broader ranges of stress.
- Likewise, deeper RVE leads to higher stress values. The combined effect - deeper RVE and clustering - may lead to some $10 \%$ increments in the mean values of stress.
- All six stress components are affected with particularly significant variations in cross-sectional axial components.

The future extensions should consider the nonlinear analysis to investigate the influence of voids on failure. Furthermore, the modeling of more complex RVE architectures and the multiscale analysis are of interest.

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[^0]:    *Professor of Aerospace Structures and Aeroelasticity, erasmo.carrera@polito.it
    ${ }^{\dagger}$ Associate Professor, marco.petrolo@polito.it
    ${ }^{\ddagger}$ Ph.D. Student, manish.nagaraj@polito.it
    ${ }^{\text {§ Research Assistant, michele.delicata@polito.it }}$

