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# Fractional viscoelastic modeling of anti-rutting response of bituminous binders

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## Abstract

A three-parameter fractional model, composed by a springpot in series with a dashpot, was employed to describe the rheological behaviour of a set of polymer modified bituminous binders obtained by combining a single base bitumen with different types of Styrene-Butadiene-Styrene copolymers at different concentrations. Due to their enhanced visco-elastic properties, polymer modified binders are widely used in asphalt pavements in order to prevent formation of ruts on road surfaces caused by accumulation of permanent deformation, especially at high in-service temperatures and under heavy traffic conditions.

The proposed fractional model was fitted to experimental data gathered from creep-recovery shear tests carried out by means of a Dynamic Shear Rheometer at various temperatures. The choice of adopting this type of test procedure was dictated by the fact that it has been proven to be effective in evaluating and ranking the anti-rutting response of bituminous binders.

Experimental strain-time curves were found to be in good agreement with model predictions. The fractional approach leads to a synthetic yet exhaustive description of the visco-elastic behavior of all materials. Variation of model parameters, each of which with a precise physical meaning, appears to be coherent with different binder compositions and testing conditions, reflecting the variations in terms of polymer concentration and temperature.

*Keywords:* asphalt pavements, fractional model, polymer modified binders, rutting, creep-recovery tests

## 1. Introduction

The term rutting is commonly used to indicate one of the main distress types affecting asphalt pavements, consisting in the accumulation of permanent deformation produced by repeated traffic

32 loading (Figure 1). Formation of ruts on pavement surfaces produces low levels of comfort and  
33 safety for vehicles and users, thus reducing overall pavement serviceability. This failure mode is  
34 promoted by the presence of severe traffic and environmental conditions, such as those  
35 characterized by high percentages of heavy slow-moving trucks and high in service temperatures.  
36 For these reasons, rutting resistance of pavements is greatly influenced by the rheological properties  
37 of bituminous binders used in the top bound layers, due to their time and temperature-dependent  
38 nature (Monismith et al. 1985, Sousa et al. 1991, Delgadillo and Bahia 2010).

39 Different experimental approaches have been proposed to evaluate the anti-rutting potential of  
40 bituminous binders. The one originally introduced in the framework of the SUPERPAVE grading  
41 system is based on visco-elastic parameter  $G^*/\sin\delta$  (Harrigan et al. 1994), but its limits have been  
42 widely demonstrated by several studies (Bahia et al. 2001, D'Angelo and Dongre 2002). Other  
43 protocols currently adopted in binder characterization for the same purpose refer either to the zero  
44 shear viscosity concept (Sybilski 1996) or to parameters derived from material response under  
45 repeated creep loading (D'Angelo et al. 2007). In both cases, however, experimental studies have  
46 highlighted the existence of significant drawbacks related to the fact that they seem not to be fully  
47 adequate to capture actual properties of specific types of binders, such as polymer modified ones  
48 (Morea et al. 2010, Zoorob et al 2012).

49 More recently, Santagata et al. (2013, 2015) introduced a method based on single creep-recovery  
50 shear tests carried out at predefined loading and recovery times. Experimental findings showed the  
51 effectiveness of the method when applied to binders modified with polymers and crumb rubber  
52 since the high levels of induced strain allow to differentiate reversible and non-reversible  
53 components of response. Moreover, effects caused by variations of additive type, composition,  
54 structure and dosage can be clearly highlighted.

55 While creep-recovery tests are relatively simple and quick to perform, modeling of the experimental  
56 data gathered from measurements appears not to be a trivial task. This is due to the fact that binders,  
57 as many viscoelastic materials, exhibit a creep-relaxation behavior of the power-law type (Mainardi  
58 1994, Hilfer 2000, Mainardi 2010), with the consequent need of introducing a great number of  
59 elements (and thus of parameters) in fitting operations when trying to describe such a response by  
60 means of classical exponential-type functions. Furthermore, since parameters are subjected to  
61 several restrictions, the employed numerical algorithm may revert to a complex constrained least  
62 squares problem (Sorvari and Malinen 2007).

63 Although power-law expressions for creep-recovery functions can be assumed *a priori*, without a  
64 physical sound derivation (Jäger et al. 2007, Füssl et al. 2014), they are implicitly generated by  
65 assuming a constitutive law of fractional type, i.e. involving time derivatives with non-integer order  
66 of strains and stresses (Carpinteri and Mainardi 1997). For this reason, approaches to visco-  
67 elasticity based on fractional calculus have attracted the attention of researchers for at least two  
68 decades, involving different materials and applications (Barpi and Valente 2003,2004 Atanckovic et  
69 al. 2013,2015, Deseri et al. 2014, Di Paola and Zingales 2012, Di Paola et al. 2013,2014, Paggi and  
70 Sapora 2015, Zopf et al. 2015).

71 In the field of asphalt pavement engineering, few fractional approaches have been proposed for the  
72 study of the behavior of bituminous binders and mixtures (Oeser et al. 2008, Celauro et al. 2012,  
73 Fecarotti et al. 2012). In particular, a three-parameter model consisting in a dashpot in series with a  
74 springpot was recently introduced by Sapora et al. (in press) (see also Di Mino et al. in press), with  
75 the goal of reducing the number of fitting parameters (Oeser et al. 2008) and of increasing  
76 prediction accuracy (Celauro et al. 2012, Fecarotti et al. 2012). Such a model was successfully  
77 applied to creep-recovery test data obtained at various temperatures (ranging from 58 and 76°C) for  
78 two different modified binders (containing thermoplastic polymer and crumb rubber, respectively).

79 In the research work reported in this paper, the study of the anti-rutting response of modified  
80 bituminous binders by means of a fractional visco-elastic approach is extended to a wider array of  
81 materials, containing several polymers at different concentrations. Results are analyzed with the  
82 specific goal of highlighting the mechanical meaning of model parameters and of linking them to  
83 the characteristics of the considered binders.

84 Binders and testing procedures used in the experimental investigation are described in Section 2,  
85 whereas the implemented fractional approach is introduced in Section 3. Section 4 presents the  
86 comparison between test data and theoretical results, together with a thorough discussion of the  
87 mechanical meaning of model parameters; analogies and differences with the results presented in  
88 (Sapora et al. in press) are also addressed. Finally, Section 5 contains a synthesis of the main  
89 findings of the research work.

90 It is worth noting that the analysis presented herein lies in the framework of linear viscoelasticity of  
91 one-dimensional media, coherently with the experimental tests which were carried out: the solution  
92 is thus given in an analytical form, and the model parameters are obtained through a least-square  
93 fitting procedure. For the numerical handling of fractional viscoelastic material models through  
94 finite element analysis, see (Müller et al. (2013)).



96

97 Figure 1. Presence of ruts on pavement surface due to deformation in the top bound layers.

## 98 2. Materials and methods

99 Modification of bitumen by means of polymers has become very popular in the binder industry  
100 since it may provide a significant enhancement of performance-related properties (King et al. 1986,  
101 Collins et al. 1991, Wardlaw and Shuler 1991). For this reason, the use of polymer modified binders  
102 (PMBs) in road construction represents one of the preferred design options in the case of heavy duty  
103 pavements, subjected to intense traffic flow and severe environmental conditions.

104 Among the various types of polymers employed as chemical agents for the production of PMBs,  
105 Styrene-Butadiene-Styrene (SBS) synthetic rubbers are characterized by widespread diffusion: they  
106 are tri-block copolymers belonging to the category of the so-called thermoplastic elastomers that  
107 form, when adequately combined with base bitumen, a cross-linked network promoted by thermal  
108 and chemical bonding mechanisms. The elastomeric network consists of polystyrene domains  
109 connected by elastic butadiene threads which contribute to improve stiffness and elasticity of the  
110 material, especially at high temperatures. The ability of such polymers to form a completely cross-  
111 linked structure depends upon their concentration within the bituminous matrix and the  
112 thermodynamics of the combined system (Bahia et al. 2001).

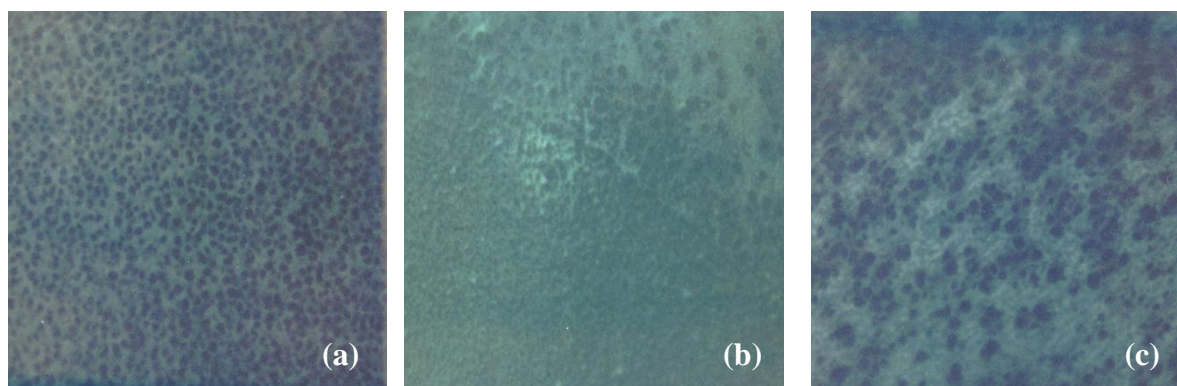
113 Materials used in the experimental investigation described in this paper include several PMBs  
114 obtained from the factorial combination of a single base bitumen (70/100 pen grade), three different

115 types of SBS and two concentrations. SBS polymers employed for modification were commercially  
 116 available products differing from each other in terms of chemical composition (low and high  
 117 styrene content) and molecular structure (linear and radial chains). Preparation of PMBs was carried  
 118 out in the laboratory by making use of a bath-oil mixer, operated at 180°C for 60 min with a mixing  
 119 speed of 800 rpm. Polymers were added to bitumen at two different dosages, equal to 3 and 6% by  
 120 weight of base bitumen.

121 Description of the complete set of modified binders is given in Table 1. All of them were tested in  
 122 short-term aged conditions simulated by means of the Rolling Thin Film Oven Test (RTFOT),  
 123 according to the AASHTO procedure (2009). Examples of Scanning Electron Microscope (SEM)  
 124 images illustrating the microstructure of PMBs with higher SBS concentration are reported in  
 125 Figure 2.

PMB code	Description	
	Type of modifier	Dosage (%)
A-3	A - radial SBS with low Styrene content	3
A-6		6
B-3	B - radial SBS with high Styrene content	3
B-6		6
C-3	C - linear SBS with high Styrene content	3
C-6		6

126 Table 1. Description of modified bituminous binders used in the experimental investigation.



127  
 128 Figure 2. SEM images corresponding to binders A-6 (a), B-6 (b) and C-6 (c).

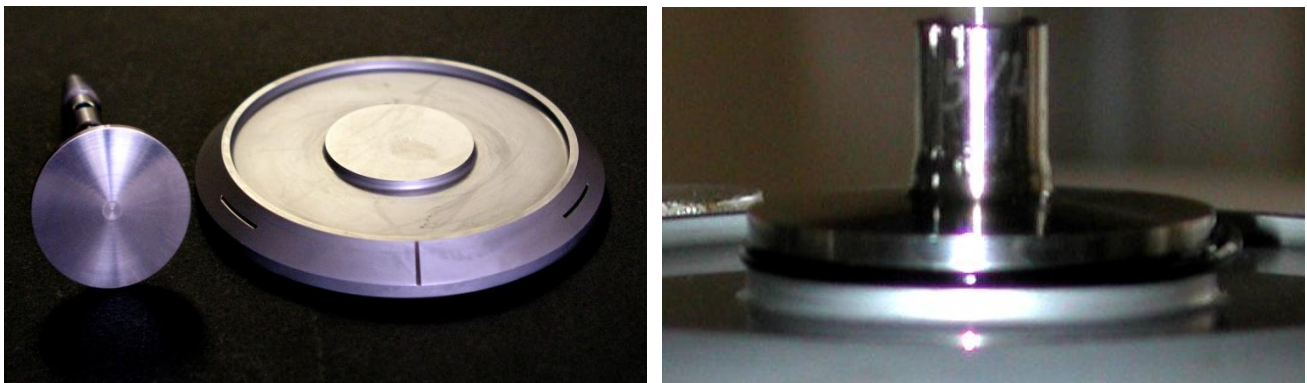
129 The protocol adopted for binder testing consists in a creep phase, during which a shear stress of 100  
 130 Pa is applied for a loading time of 900 s, followed by a recovery phase, in which load is removed  
 131 and strain evolution is monitored for additional 900 s. Creep-recovery tests were carried out at  
 132 different temperatures, selected depending upon the type of binder in order to emphasize its actual  
 133 visco-elastic response. In particular, 40 and 60°C were adopted for PMBs containing 3% polymer

134 (A-3, B-3, C-3), whereas 60 and 80°C were used for those characterized by 6% concentration (A-6,  
135 B-6, C-6).

136 The testing device employed to carry out creep-recovery tests was a Dynamic Shear Rheometer  
137 (DSR), Physica MCR 301 DSR from Anton Paar Inc., an air bearing stress-controlled device  
138 equipped with a permanent magnet synchronous drive (minimum torque = 0.1  $\mu\text{Nm}$ , torque  
139 resolution < 0.1  $\mu\text{Nm}$ ) and an optical incremental encoder for the measurement of angular rotation  
140 (resolution < 1  $\mu\text{rad}$ ). A cone-plate sensor system with 35 mm diameter and 4° cone angle was used  
141 for measurements.

142 Test specimens were prepared by pouring the binder (preheated at 150°C for the time needed to  
143 achieve a sufficient fluidity) on the lower plate of the sensor system and by thereafter sandwiching  
144 it between the plate and the upper cone. The amount of material placed on the plate was slightly  
145 overdosed, in order to allow the formation of a proper bulge at the periphery of the sample after  
146 reaching final measurement position. With the aim of preventing temperature gradients throughout  
147 the binder volume, specimens were conditioned at test temperature for 15 minutes before actual  
148 measurements.

149 The employed sensor system and the final test configuration reached after specimen preparation are  
150 displayed in Figure 3.



151  
152 Figure 3. Sensor system and test configuration.

### 153 **3. Implemented fractional model and parameter calibration**

154 The fractional model implemented in the present study (Figure 4) includes a springpot connected in  
155 series with a dashpot (Sapora et al. in press). While the dashpot simply accounts for time-dependent  
156 viscous response under loading, the springpot is a structural element with a fractional order  $\alpha$   
157 governing the transition from elastic to viscous behavior.

158 The strain- stress ( $\varepsilon$ - $\sigma$ ) constitutive law of the model is the following:

159 
$$\frac{d\varepsilon(t)}{dt} = \frac{1}{b_1} \frac{d^{1-\alpha}\sigma(t)}{dt^{1-\alpha}} + \frac{1}{b_2} \sigma(t) \quad (1)$$

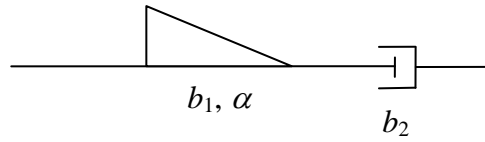
160 where  $b_1$  and  $\alpha \in (0,1)$  are the springpot parameters, and  $b_2$  is the dynamic viscosity related to the  
 161 dashpot.

162 Definition of the fractional derivative of order  $\alpha$  related to a generic function  $f$  can be expressed in  
 163 the form (Samko et al. 1993):

164 
$$\frac{d^\alpha f(x)}{dx^\alpha} = \frac{1}{\Gamma(1-\alpha)} \int_0^x \frac{f'(y)}{(x-y)^\alpha} dy \quad \alpha \in (0,1) \quad (2)$$

165 where  $\Gamma$  is the Euler-Gamma function.

166 According to (2), the  $\alpha$ -derivative of a function reverts to the function itself for  $\alpha = 0$ , and to the  
 167 first order classical derivative for  $\alpha = 1$ . It should also be noted that as  $\alpha$  varies, the mechanical  
 168 meaning of  $b_1$  in (1) obviously changes, passing from a stiffness ( $Force \times Length^{-2}$ ) for  $\alpha = 0$ , to a  
 169 viscosity ( $Time \times Force \times Length^{-2}$ ) for  $\alpha = 1$ .



170  
 171 Figure 4. Fractional model implemented in the analysis.

172  
 173 The creep function  $D(t)$  related to the constitutive law (1) can be derived as:

174 
$$D(t) = \frac{t^\alpha}{b_1 \Gamma(1+\alpha)} + \frac{t}{b_2} = \frac{t}{b_2} \left( 1 + \frac{b_2}{b_1 \Gamma(1+\alpha)} t^{\alpha-1} \right) \quad (3)$$

175 whereas the creep-recovery constitutive relationship can be written as:

176 
$$\varepsilon(t) = \left\{ \left[ \frac{t^\alpha}{b_1 \Gamma(1+\alpha)} + \frac{t}{b_2} \right] U(t) - \left[ \frac{(t-t^*)^\alpha}{b_1 \Gamma(1+\alpha)} + \frac{(t-t^*)}{b_2} \right] U(t-t^*) \right\} \sigma_0 \quad (4)$$

177 being  $U(t)$  the unit-step (or Heaviside) function,  $t^*$  the time at which unloading starts and  $\sigma_0$  constant  
 178 applied stress.



179 It is important to point out what are the limit cases of the considered fractional model. Elastic  
 180 response is maximized for  $\alpha = 0$ , in which case the springpot reverts to a spring and  $b_1$  plays the  
 181 role of a stiffness: in this case the model coincides with the well-know Maxwell model consisting in  
 182 a spring in series with a dashpot. On the other hand, viscous behaviour is amplified the most for  
 183  $\alpha = 1$ : the model then reverts to two dashpots in series, each with the same viscosity ( $b_1 = b_2$ ).

184 In order to fit the model to experimental data obtained from creep-recovery tests described in  
 185 Section 2, the three model parameters  $\alpha$ ,  $b_1$  and  $b_2$  were determined by means of a numerical  
 186 algorithm which evaluates the coefficients of a nonlinear regression function through a least squares  
 187 estimate. Due to possible settlement phenomena observed in the initial phase of creep, data recorded  
 188 in the first 1% of the loading history were neglected (Sapora et al. in press).

189 Values of  $\alpha$ ,  $b_1$  and  $b_2$  obtained from fitting, together with the corresponding absolute mean  
 190 percentage error  $\bar{\delta}$ , are reported in Tables 1 and 2 for PMBs containing 3 and 6% polymer,  
 191 respectively.

T [°C]	A-3				B-3				C-3			
	$\alpha$	$b_1$	$b_2$	$\bar{\delta}$	$\alpha$	$b_1$	$b_2$	$\bar{\delta}$	$\alpha$	$b_1$	$b_2$	$\bar{\delta}$
40	0.570	0.966	2.14	1.44	0.567	0.596	3.12	1.37	0.731	0.0133	0.000	3.77
60	1.000	0.173	0.173	4.06	1.000	0.188	0.188	3.88	1.000	0.464	0.464	10.3

192 Table 2. Fitted parameters  $\alpha$ ,  $b_1$  [ $\text{Ns}^\alpha/\text{m}^2$ ],  $b_2$  [ $\text{Ns}/\text{m}^2$ ] and mean percentage error  $\bar{\delta}$  corresponding to  
 193 PMBs containing 3% SBS tested at 40 and 60°C.

T [°C]	A-6				B-6				C-6			
	$\alpha$	$b_1$	$b_2$	$\bar{\delta}$	$\alpha$	$b_1$	$b_2$	$\bar{\delta}$	$\alpha$	$b_1$	$b_2$	$\bar{\delta}$
60	0.259	0.044	6.41	1.75	0.104	0.063	61.4	0.69	0.156	0.0738	39.9	1.46
80	1.000	0.091	0.091	1.66	0.245	0.109	2.88	3.87	0.334	0.427	0.402	10.3

194 Table 3. Fitted parameters  $\alpha$ ,  $b_1$  [ $\text{Ns}^\alpha/\text{m}^2$ ],  $b_2$  [ $\text{Ns}/\text{m}^2$ ] and mean percentage error  $\bar{\delta}$  corresponding to  
 195 PMBs containing 6% SBS tested at 60 and 80°C.

#### 196 4. Discussion of results

197 Shear strain test data obtained for PMBs characterized by the lower SBS content (A-3, B-3, C-3)  
 198 and theoretical results provided by Eq.(4) with fitted parameters reported in Table 2 are  
 199 diagrammed as a function of time in Figs. 5-7. For each material and test condition, experimental  
 200 and theoretical curves appear to be very close to each other, indicating that a good agreement was  
 201 generally found. This is coherent with  $\bar{\delta}$  values that are abundantly lower than 5%. The only  
 202 exception is represented by binder C-3 tested at 60°C, for which the creep experimental curve

203 deviates from the theoretical one, showing a trend characterized by the increase of strain rate with  
204 loading time; the corresponding mean percentage error is non negligible, reaching a value of the  
205 order of 10%.

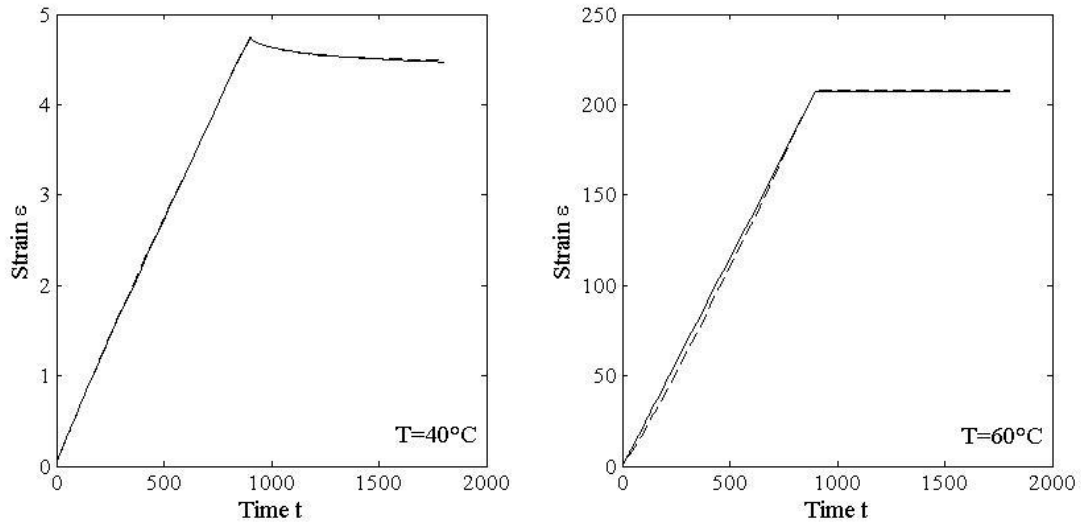
206 In all cases, materials tested at 40°C exhibit a certain amount of delayed elastic strain which is  
207 partially recovered during the unloading phase. On the contrary, at 60°C the accumulated strain at  
208 the end of the loading phase is fully irreversible. This evidence can be explained by considering that  
209 the raise in temperature produces the breakdown of physical crosslinks within polymer styrene  
210 domains; in such conditions the SBS added to the bituminous matrix acts as a simple filler which  
211 contributes to increase viscosity of the binder without improving its elasticity.

212 Such a transition from visco-elastic to viscous behaviour is reflected in the variation of fitted  
213 fractional parameters. In particular, values of  $\alpha$  determined at 40°C range, approximately, between  
214 0.55 and 0.75 whereas at 60°C they become equal to 1 with the fractional model being reduced to  
215 two dashpots in series ( $b_1 = b_2$ ). Anyhow, it must be pointed out that values of  $\alpha$  equal to 0.55 or  
216 higher indicate the predominance of viscous components in material's response even at 40°C (i.e.  
217 the springpot is more similar to a dashpot than to a spring) suggesting the added amount of  
218 elastomer (3%) not to be sufficient to create a continuous polymeric network in accordance with  
219 results published elsewhere (Lu and Isacsson 1997). Moreover, the increase of the fractional  
220 exponent when passing from 40 to 60°C appears to be in contrast with findings of other studies  
221 (Di Mino et al. in press), in which  $\alpha$  is showed to decrease with temperature (together with  $b_1$  and  
222  $b_2$ ). Both trends can be considered acceptable from a practical point of view since the global  
223 response is described by the combined effects of  $\alpha$ ,  $b_1$  and  $b_2$  variations; however, the first one  
224 seems to be more logical from a theoretical point of view, matching the extreme cases described in  
225 Section 3. Similar considerations are valid for values reported in Table 3.

226 By comparing the materials to each other, it is clearly noticed that binder C-3 exhibits the most  
227 elastic response at  $T = 40^\circ\text{C}$ , its behaviour being described by a single springpot. On the other hand,  
228 A-3 and B-3 present nearly the same value for  $\alpha$  but different values of  $b_1$  and  $b_2$ : the springpot  
229 contribution to overall deformation appears to be more significant for A-3, which presents a lower  
230  $b_2/b_1$  ratio (Eq. (3)), even though B-3 is less deformable in absolute terms. At 60°C, C-3 shows the  
231 highest value of  $b_2$  that, as specified before, assumes the meaning of a dynamic viscosity, thus  
232 indicating the highest resistance to flow for such a material, followed, in order, by B-3 and A-3.  
233 This is coherent with the characteristics of the various SBSs used for modification and more  
234 specifically with the presence, in type C and type B, of a higher styrene content that contributes to

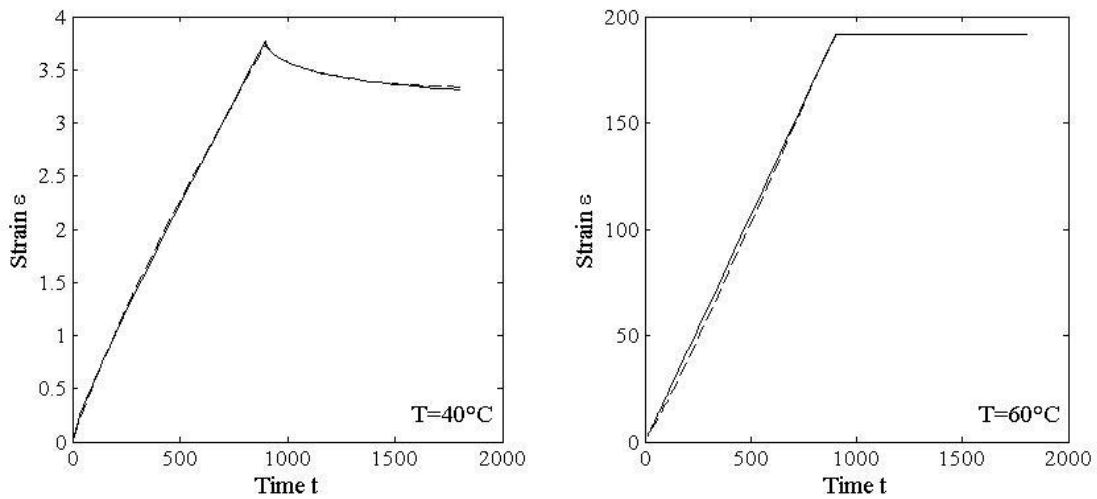
235 increase the hardness of the polymers and, consequently, of the corresponding polymer-bitumen  
236 blends.

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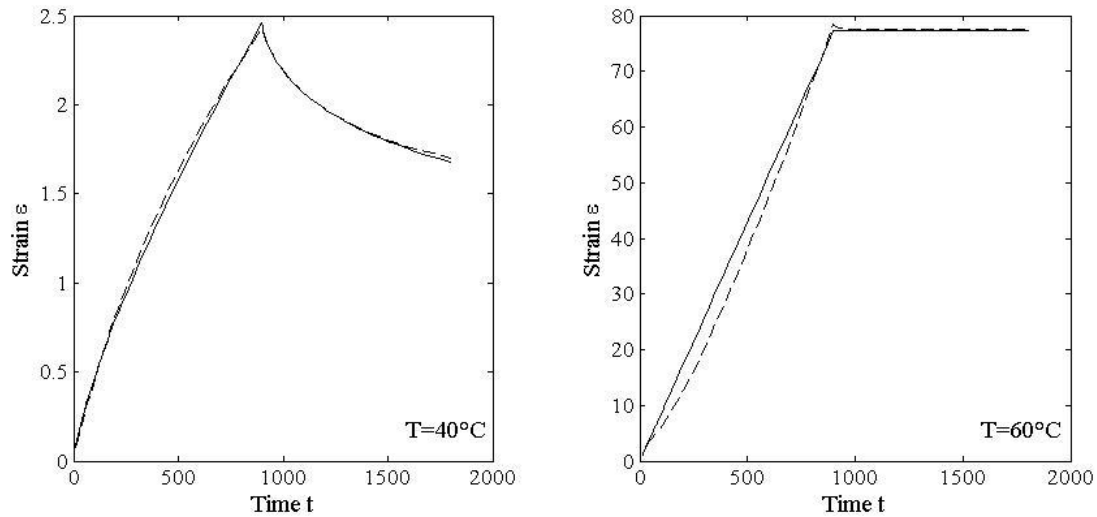
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239 Figure 5. Creep-recovery curves of binder A-3 tested at  $40^{\circ}\text{C}$  (a) and  $60^{\circ}\text{C}$  (b):  
240 experimental data (dotted line) and theoretical results (solid line).



241

242 Figure 6. Creep-recovery curves of binder B-3 tested at  $40^{\circ}\text{C}$  (a) and  $60^{\circ}\text{C}$  (b):  
243 experimental data (dotted line) and theoretical results (solid line).



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Figure 7. Creep-recovery curves of binder C-3 tested at 40°C (a) and 60°C (b):  
experimental data (dotted line) and theoretical results (solid line).

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Diagrams reporting the results obtained for highly modified binders (A-6, B-6, C-6) are shown in Figs. 8-10. Also in this case a good fitting is observed ( $\bar{\delta} < 5\%$ ) with the only exception, once again, given by binder containing type C SBS tested at the higher temperature. In fact, the creep curve at 80°C shows a trend similar to that displayed in Figure 7-b, which appears to be not well described by the proposed model (the mean absolute error exceeds 10%). This type of shear thinning behaviour can be therefore considered peculiar of the linear SBS used in this investigation when subjected to high levels of shear deformations (Stastna et al. 2003).

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In contrast with data illustrated before,  $\alpha$  values are generally very low (except in the case of A-6 tested 80°C that will be commented later) with springpot elements approaching a condition corresponding to the spring case. This can be evidently attributed to the presence of a high amount of polymer that results in the formation of a diffused cross-linked structure with a pronounced rubber-like behaviour.

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However, a distinction can be made between binder A-6 and the other two binders B-6 and C-6.

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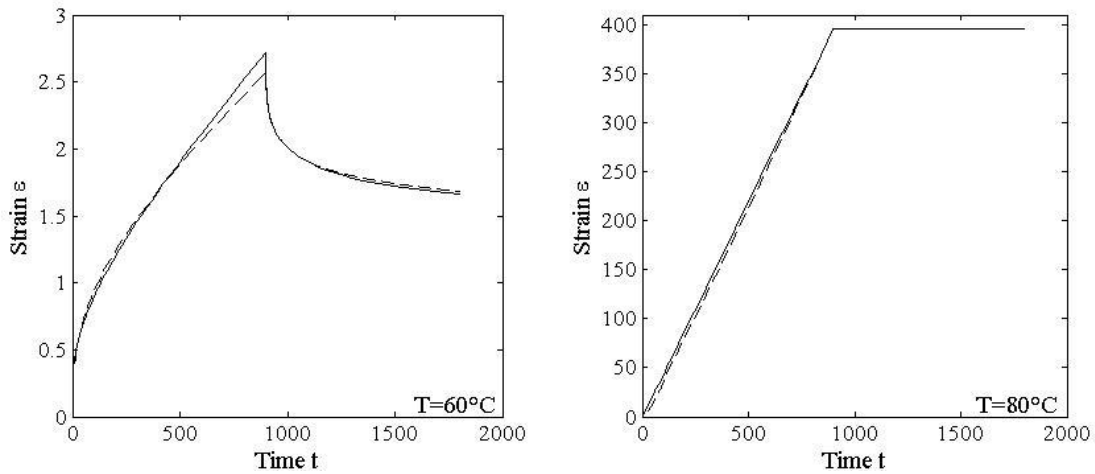
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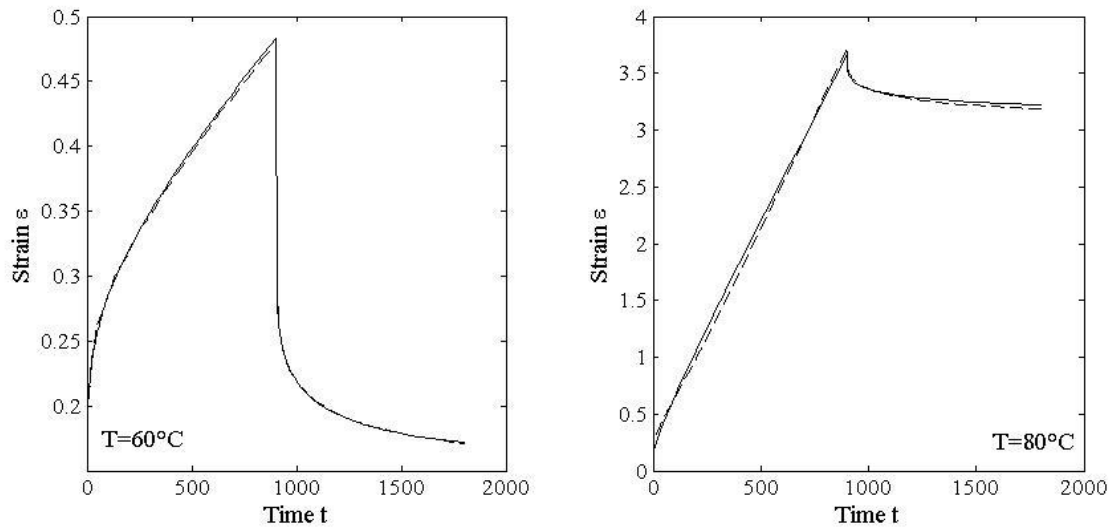
In fact, at 60°C the latter ones behave like viscoelastic solids which are able to recover most of the deformation experienced during the loading phase. This can be evidently attributed to the presence of a high styrene content which promotes the formation of rigid polystyrene domains within the bituminous matrix. If compared to each other, B-6 prevails on C-6 in terms of stiffness and degree of elasticity, probably due to its radial/branched molecular structure. At 80°, as obvious, both materials become less stiff (lower values of  $(b_2/b_1)$ ) and less elastic (higher values of  $\alpha$ ) even though they maintain a certain aptitude to recover deformation.

267 Binder A-6 at 60 °C shows a typical visco-elastic behaviour characterized by a lower stiffness and  
268 degree of elasticity with respect to that of abovementioned binders B-6 and C-6 (lower values of  
269  $(b_2/b_1)$ , higher value of  $\alpha$ ) and, as previously highlighted, at 80°C reaches viscous flow conditions ( $\alpha$   
270  $= 1$  with  $b_1 = b_2$ ). Such an evidence can be linked with the low styrene content of the SBS used for  
271 the preparation of this type of PMB, that results in weak bonding between styrene blocks at very  
272 high temperatures thus overcoming polymer networking effects.



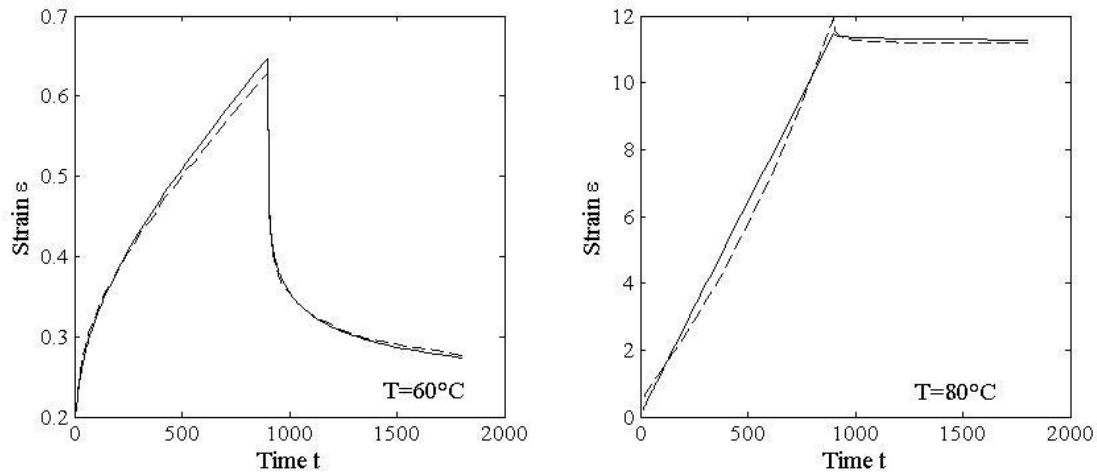
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274 Figure 8. Creep-recovery curves of binder A-6 tested at 60°C (a) and 80°C (b):  
275 experimental data (dotted line) and theoretical results (solid line).



276

277 Figure 9. Creep-recovery curves of binder B-6 tested at 60°C (a) and 80°C (b):  
278 experimental data (dotted line) and theoretical results (solid line).



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Figure 10. Creep-recovery curves of binder C-6 tested at  $60^{\circ}\text{C}$  (a) and  $80^{\circ}\text{C}$  (b):  
experimental data (dotted line) and theoretical results (solid line).

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## 5. Conclusions

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The three-parameter ( $\alpha$ ,  $b_1$ ,  $b_2$ ) fractional visco-elastic model consisting in a springpot in series with a dashpot was employed in the research study reported in this paper to model the creep-recovery experimental behaviour of several modified bituminous binders, differing in polymer type and concentration. The results were analyzed with the specific purpose of verifying the capability of the model of capturing peculiarities of material response and to link model parameter to variations in materials' composition and testing conditions.

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From the findings of the study, the following main conclusions can be drawn.

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Experimental strain-time curves obtained from testing were found in good agreement with model predictions, as indicated by absolute mean percentage error values always lower than 5%. The only exceptions are represented by binders containing the linear SBS polymer that showed a typical shear thinning behaviour when subjected to high levels of deformations. This confirms the effectiveness of the fractional approach that leads to a synthetic but exhaustive description of the visco-elastic behavior of materials with a precise physical meaning of model parameters: whereas  $b_1$  and  $b_2$  describe the stiffness and dynamic viscosity of the binder,  $\alpha$  governs the global elastic-viscous transition.

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Variation of abovementioned parameters appears to be coherent with the composition of different materials and testing conditions, reflecting the variations in terms of polymer concentrations and temperatures.

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In particular, materials characterized by low polymer content exhibited high values of springpot parameter  $\alpha$ , indicating materials' response to be significantly governed by viscous components.

303 These become even more predominant as temperature increases, with the concurrent decrease of  
304  $b_2/b_1$  ratio values.

305 In the case of highly modified materials,  $\alpha$  values drop dramatically showing the evolution from a  
306 viscous to a pronounced visco-elastic behavior. This is especially true for binders containing SBS  
307 (both linear and radial) characterized by a high styrene content, the response of which can be  
308 assimilated to that of a visco-elastic solid.

309 Such results suggests SBS to be able to form a continuous cross-linked network only if added to the  
310 base bituminous matrix in a sufficiently high amount. In such conditions, binder containing radial  
311 SBS with high styrene content was found to prevail at both considered temperatures, as  
312 demonstrated by higher values of  $\alpha$  and  $b_2/b_1$  ratio.

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