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Article

Viability of an Electrically Driven Pump-Fed Hybrid Rocket for Small Launcher Upper Stages

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Abstract: An electrically driven pump-fed cycle for a hybrid rocket engine is proposed and compared to a simpler gas-pressurized feed system. A liquid-oxygen/paraffin-based fuel hybrid rocket engine which powers the third stage of a Vega-like launcher is considered. Third-stage ignition conditions are assigned, and engine design and payload mass are defined by a proper set of parameters. Uncertainties in the classical regression rate correlation coefficients are taken into account and robust design optimization is carried out with an approach based on an epsilon-constrained evolutionary algorithm. A mission-specific objective function, which takes into account both the payload mass and the ability of the rocket to reach the required final orbit despite uncertainties, is determined by an indirect trajectory optimization approach. The target orbit is a 700 km altitude polar orbit. Results show that electrically driven pump-fed cycle is a viable option for the replacement of the conventional gas-pressurized feed system. Robustness in the design is granted and a remarkable payload gain is achieved, using both present and advanced technologies for electrical systems.

Keywords: hybrid rocket engines; multidisciplinary design optimization; robust optimization; electric feed system

1. Introduction

Hybrid rocket engine (HRE) performance is comparable to semi-cryo or storable liquid rocket engines (LREs) and solid rocket motors (SRMs). HREs have higher density-specific impulse I_p than typical bi-propellant LREs, whereas their mean specific impulse I_{sp} is higher than SRMs. HREs gather many favorable properties from SRMs such as safety, reliability, and low cost. On the other hand, HREs and LREs share shut-off/restart capabilities and can be throttled within a wide thrust range. Moreover, HREs are more environmentally friendly than both LREs and SRMs. Thus, many research programs worldwide are focusing on the development of HREs. Examples of applications are micro-gravity platforms, hypersonic accelerators, small satellites, upper stage for small launchers, launchers from Mars, Moon landers, debris removal, and commercial space flights [1–5].

In previous studies the authors analyzed the effect of the presence of uncertainties in the design parameters, such as in the regression rate, on rocket performance and mission goals [6,7]. Results showed that even small uncertainty in the determination of the regression rate may jeopardize vehicle performance and threaten seriously the mission. A proper robust design multidisciplinary approach [8] has been developed to couple propulsion system design and trajectory optimization, while reducing the sensitivity of the engine performance to uncertainties. The concept of “robustness” can be summarized as “the capability of the system to grant a fixed level of performance” (i.e., to match mission goals), “minimizing the effect of uncertainties in the design parameters without eliminating their causes” [9,10]. A Vega-like upper stage, powered by a gas-pressurized liquid-oxygen

(LOX)/paraffin-based fuel HRE, was considered as test case. Results showed that robustness in the design was achieved with a small payload reduction with respect to the optimal deterministic design. Gas-pressurized feed systems were adopted aiming to keep cost as low as possible. However, the high tank pressure, required to keep the thrust magnitude and regression rate sufficiently large during operation, results in relevant auxiliary and oxidizer tanks masses. Due to the relevant value of the total impulse of the upper stage, the liquid oxidizer tank is relatively large and the use of a turbopump feed system can reduce the engine dry mass. The tank weight reduction and the elimination of possible gas vessels overcome the turbopump system weight.

In a turbopump feed system, the pump is classically driven by a turbine, which is fed by gas or liquid working fluid. Electrical pump feed systems (EPFS), where a battery-powered electric motor replaces the turbine, have also been proposed for bi-propellant LREs. Different applications have been considered since the 1990s [11,12], and the advances in batteries and electric motor technologies have been making this feed system increasingly competitive [13–16]. In 2016 an EPFS bi-propellant engine was considered, alongside other classical propulsion systems, to power a Mars ascent vehicle (MAV) [17]. Results showed that EPFS, although lower in technology readiness level, was able to outperform a conventional gas-pressurized feed system. The application to small-sat launcher appears to be very appealing and feasible [18], as the use of the Rutherford engine proved (this LOX/RP1 (Rocket Propellant 1) engine, used to power the Rocket Lab's Electron launch vehicle in its recent successful second flight test, has an electrically driven pump feed system). Recently, Ref. [19] assessed the viability of an EPFS LOX/kerosene upper stage for the Korean Space Launch Vehicle-II, which is designed to insert 1500 kg into a 700 km Single Stage to Orbit (SSO) orbit.

In an HRE, the presence of just one liquid propellant makes the generation of a proper working fluid for the turbine more challenging. A gas-generator cycle cannot be adopted, unless auxiliary liquid fuel is embarked. Hydrogen peroxide could produce hot gases by means of a catalyzer, but this is not the case of LOX, here considered. LOX heating would not be so effective, while a tap-off cycle would introduce complexity, reduce reliability, and increase costs. Thus, the electric pump solution is even more appealing than in LREs. Nevertheless, no great attention has been devoted to EPFS in HRE. In a previous work [20], the authors proposed the EPFS for a HP (Hydrogen Peroxide)/PE (Polyethylene) upper stage, performing a deterministic optimization. In the present work, a robust-based design and optimization is performed considering EPFS with LOX/paraffin-based fuel. Only uncertainties in the classical regression rate correlation are taken into account. The authors use a combined procedure: an indirect method optimizes the trajectory for each combination of engine parameters [21,22] which, in turn, are selected by a particle swarm optimization algorithm [23]. The robust-based objective function is evaluated as a linear combination of an index that quantifies the effective reaching of the target orbit, based on the average performance under uncertainty, and the payload (that instead is not affected by uncertainties).

In the following sections, we sum up the main features of grain geometry, ballistic model, feed systems, and indirect optimization procedure. Then we compare the performance of gas-pressurized and pump feed systems, making our conclusions.

2. Numerical Models

2.1. Grain Geometry and Ballistic Model

In the present work, the authors considered LOX/paraffin-based fuel as propellant combination for HREs design. Cryogenic LOX is stored in liquid phase in a tank and injected into the combustion chamber during operation. The combustion chamber stores the wax in solid phase as a cylindrical grain. Paraffin-based fuels, such as wax, present an unstable melt liquid layer that causes the entrainment of droplets into the gas stream [24]. The fuel mass transfer rate into the flame zone is strongly increased by the entrainment of droplets. Combustion takes place in the flame zone through diffusive mixing of oxidizer and fuel coming from the grain. For this reason, regression rate is relatively large, and a single

circular port can be adopted for the fuel grain, whereas classical fuels would require a multi-port grain design to avoid excessive length to diameter ratio (L/D) [25].

The grain outer radius R_g , the web thickness w , and the grain length L_b define the geometry of the circular-port grain as shown in Figure 1. The initial inner radius, i.e., the port radius before ignition, results to be $R_i = R_g - w$. The burning perimeter P and the port area A_p , for any given burning distance y ($0 \leq y \leq w$), can be computed as:

$$P = 2\pi (R_i + y) \quad (1)$$

$$A_p = \pi (R_i + y)^2 \quad (2)$$

An approximate relation, between chamber head-end pressure p_1 and chamber nozzle-stagnation pressure p_c , is used to take into account pressure losses inside the combustion chamber [26]:

$$p_1 = \left[1 + 0.2 \left(\frac{A_{th}}{A_p} \right)^2 \right] p_c \quad (3)$$

where A_{th} is the throat area. The authors assumed a uniform regression rate along the port axis while the combustion of the lateral end is neglected. Its value is determined by the oxidizer mass flow rate \dot{m}_O and grain geometry:

$$\dot{y} = a (\dot{m}_O / A_p)^n \quad (4)$$

In the present work a and n are assumed to be uncertain parameters. $a = 9.1 \times 10^{-5} \text{m}^{2n+1} \text{s}^{n-1} \text{kg}^{-n}$ and $n = 0.69$ are taken into consideration as reference nominal values when International System (SI) of units are used [24].

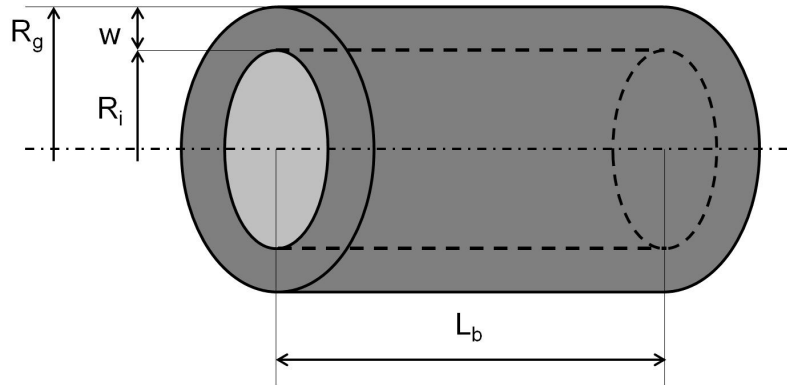


Figure 1. Schematic of the grain geometry.

The oxidizer flow rate is determined by the hydraulic resistance Z in the oxidizer flow path and the pressure provided by the feed system. Under the assumption of incompressible turbulent flow:

$$\dot{m}_O = \sqrt{(p_{fs} - p_1) / Z} \quad (5)$$

where p_{fs} is the feed system pressure. We assume a constant value of Z during the operation. Fuel mass flow \dot{m}_F can be obtained as:

$$\dot{m}_F = \rho_F \dot{y} A_b = \rho_F \dot{y} L_b P \quad (6)$$

where ρ_F is the fuel grain density, A_b is the burning area. One can compute the mixture ratio α as:

$$\alpha = \frac{\dot{m}_O}{\dot{m}_F} \propto \dot{m}_O^{1-n} A_p^n / A_b \quad (7)$$

An isentropic expansion in the nozzle is assumed, and the chamber nozzle-stagnation pressure p_c can be determined by:

$$p_c = \frac{(\dot{m}_O + \dot{m}_F)c^*}{A_{th}} \quad (8)$$

The authors used a 10-bar chamber pressure in performance evaluation of the propellant combination as a function of the mixture ratio α . Even though the actual pressure in the combustion chamber can span over a wide range during engine operations, the performance error, due to the constant chamber pressure assumption, is small for pressures and mixture ratios considered in this article. Frozen equilibrium expansion is assumed: exhaust gas composition is fixed throughout the nozzle and equal to combustion chamber one. We adopt the conservative assumption of frozen equilibrium expansion to account for the low combustion efficiency of HREs. Moreover, a 0.96 c^* -efficiency [27] is introduced. Third-degree polynomial curves, fitting the characteristic velocity and specific heat ratio, are embed in the code, to compute accurately and quickly the proper values as the mixture ratio changes during operation [28]. Thrust coefficient C_F can be evaluated as:

$$C_F = 0.98 \left\{ \sqrt{\frac{2\gamma^2}{\gamma-1} \left(\frac{2}{\gamma+1} \right)^{\frac{\gamma+1}{\gamma-1}} \left[1 - \left(\frac{p_e}{p_c} \right)^{\frac{\gamma-1}{\gamma}} \right]} + E \frac{p_e}{p_c} \right\} - E \frac{p_0}{p_c} \quad (9)$$

where a 0.98 correction factor is introduced to modify the vacuum thrust coefficient of a 1-D isentropic expansion to the exit pressure p_e with constant heat ratio γ . Atmospheric pressure-related term $E \cdot p_0/p_c$ is always small since the third stage always flies at high altitude. One can determine mass flow rate at ignition (i.e., at $t = 0$) as:

$$(\dot{m}_p)_i = (1 + \alpha_i)(\dot{m}_F)_i = \frac{1 + \alpha_i}{\alpha_i}(\dot{m}_O)_i \quad (10)$$

Then initial throat area $(A_{th})_i$ and initial port area $(A_p)_i$ can be obtained:

$$(A_{th})_i = \frac{(\dot{m}_p)_i}{(p_c)_i c_i^*}; \quad (A_p)_i = \frac{(A_{th})_i}{J} \quad (11)$$

Nozzle throat erosion is here considered [29,30]. Bartz's method is used to model the dependence of the rate of throat erosion \dot{s} on throat radius R_{th} and chamber pressure p_c :

$$\dot{s} = \dot{s}_{ref} \left(\frac{p_c}{p_{c,ref}} \right)^{0.8} \left(\frac{R_{th,ref}}{R_{th}} \right)^{0.2} \quad (12)$$

R_{th} and E values are computed by integrating Equation (12). $\dot{s}_{ref} = 0.1$ mm/s, obtained from CFD analysis on the ablation of a carbon/carbon nozzle for LOX/wax HREs [31], is here adopted. Our model does not consider erosion along the nozzle, obtaining a greater reduction of E and a conservative solution. Eroded mass is not taken into account, either for thrust augmentation or for rocket mass reduction.

2.2. Feed Systems

In the present work, the authors compare the performance of two different feed systems: a gas-pressurized feed system (GPFS) and an EPFS. During engine operation of a gas-pressurized feed system, the oxidizer mass flow rate is determined by the pressure drop between tank and chamber head-end pressures. The tank pressure is maintained constant by a pressurizing gas, contained in a high-pressure auxiliary tank during an initial regulated phase, which is then followed by a blow-down phase. The pressure at the pump outlet is instead considered in an EPFS. EPFS requires additional

masses for batteries, electric motor, and pump while GPFS needs a heavier oxidizer tank, due to its higher pressure, and auxiliary gas and vessels. The performance of GPFS here considered, and put into comparison with EPFS, are taken from a previous optimization work by the authors [8]. Two sets of electrical properties for batteries and electric motor and pump are used in EPFS performance evaluation. Set A has already been employed by the authors, back in 2010, for the deterministic optimization of a HP/PE powered HRE [20]. Set B, instead, is taken from the most recent literature available [19].

2.2.1. GPFS

The GPFS has two operational modes. Initially, constant tank pressure is maintained by helium flowing from an auxiliary tank, thus p_{fs} is constant too. Later, a subsequent blow-down (BD) phase is performed and p_{fs} decreases during operation. The authors assume an initial ullage volume equal to 3% of the oxidizer volume to have a stable regulator response when the out flow starts [32]. The GPFS is characterized by two design parameters: the auxiliary gas tank volume V_a and the initial pressurizing gas pressure p_a . The exhausted oxidizer mass at the beginning of the BD phase $(m_O)_{BD}$ is conveniently used instead of V_a while the initial pressurizing gas pressure is kept constant at $p_a = 200$ bar. During the constant pressure mode, $p_{fs} = (p_t)_i = 25$ bar, whereas, during the BD phase, p_{fs} is calculated assuming an isentropic expansion of the pressurizing gas in the tank:

$$p_{fs} = (p_t)_i \left[\frac{(V_g)_{BD}}{V_g} \right]^{\gamma_g} \quad (13)$$

where the gas volume in the tank $V_g = (V_g)_i + m_O / \rho_O$ depends on the oxidizer mass m_O that has been exhausted, $(V_g)_{BD} = (V_g)_i + (m_O)_{BD} / \rho_O$ and γ_g is the specific heat ratio of the pressurizing gas.

2.2.2. EPFS

In the EPFS, an electric motor is used to drive the pump which feeds the oxidizer to the combustion chamber. A battery pack supplies the energy required by the electric motor during operation. Pump, electrical systems and batteries masses are evaluated by means of typical power density (power to mass ratio) values provided by existing literature. Thus, the electric motor and pump mass is evaluated as:

$$m_{ep} = \frac{P_{e,max}}{\delta_{ep}} \quad (14)$$

where $P_{e,max}$ is the maximum electrical power required. In the following, two values for the power density δ_{ep} has been assumed for the electric drive system plus pump: $(\delta_{ep})_A = 1.25$ kW/kg represents current technology [13,33] and $(\delta_{ep})_B = 3.92$ kW/kg for advances designs [19]. The electrical power required by the motor to drive the pump is:

$$P_e = \frac{\dot{m}_O(p_{fs} - p_t)}{\rho_O \eta_{ep}} \quad (15)$$

where p_{fs} is equal to the pump discharge pressure p_d and p_t is the oxidizer tank pressure. The tank pressure is assumed to be constant during operation and equal to 1 bar. The mass used to keep p_t constant during operation is small and then can be neglected. The conversion of electrical energy, stored in the batteries, into flow head rise is taken into account by the overall efficiency η_{ep} . In the present work, we assume two values for the overall efficiency, $(\eta_{ep})_A = 0.64$ and $(\eta_{ep})_B = 0.53$. One can notice that $(\eta_{ep})_B < (\eta_{ep})_A$, but $m_{ep} \propto (\delta_{ep} \cdot \eta_{ep})^{-1}$ which is actually smaller for the newer Set B quantities. Battery pack mass is constrained by the most stringent requirement between the maximum electrical power required $P_{e,max}$ and the total electrical energy $E_{e,tot}$ needed to drive the

pump during the whole burning time. In the present case, the discharge time is equal to the overall HRE burning time t_{burn} . Thus, the needed electrical energy is:

$$E_{e,tot} = \int_0^{t_{burn}} P_e dt \quad (16)$$

Batteries mass m_b can be evaluated by means of typical values of power density δ_{bp} and energy density δ_{be} (energy to mass ratio) that can be found in literature. A safety factor of 1.2 is assumed and therefore:

$$m_b = 1.2 \max \left(\frac{P_{e,max}}{\delta_{bp}}, \frac{E_{e,tot}}{\delta_{be}} \right) \quad (17)$$

Due to their small size and light weight compared to all other technologies, Lithium batteries, are considered for the present application. The authors considered two couples of densities to evaluate battery pack mass: $(\delta_{bp})_A = 3.0$ kW/kg and $(\delta_{be})_A = 90$ Wh/kg, based on Ragone plots [34], and $(\delta_{bp})_B = 6.95$ kW/kg and $(\delta_{be})_B = 198.5$ Wh/kg, based on state of the art Lithium-Polymer batteries [19]. These kinds of batteries are suitable for HRE applications because they require high power levels for a relatively short time, so that high rate capability is required. The pump is operated at constant power $P_e = P_{e,max}$. Thus, Equation (16) can be easily integrated and:

$$E_{e,tot} = P_{e,max} t_{burn} \quad (18)$$

The value of $(p_d)_i$ at the beginning of the HRE operation is an additional parameter, used in the direct optimization procedure. It fixes the value of $P_{e,max} = P_e = \text{constant}$, which is crucial for feed system and engine performance.

One can notice that power-constrained batteries mass can be evaluated before the actual trajectory is optimized, while energy-constrained mass must be computed “a posteriori”. The authors define a characteristic burn time $t_{burn}^* = \delta_{be}/\delta_{bp}$ that represents the simultaneous fulfillment of both constraints. If $t_{burn} \leq t_{burn}^*$, power-constrained mass is larger than energy-constrained one. Hence, battery pack mass does not depend on the actual ascent trajectory. On the other hand, if $t_{burn} \geq t_{burn}^*$, energy-constrained mass is larger than power-constrained one. In this case, batteries mass must be checked “a posteriori” to take into account the additional energy required by a longer mission. Electric properties values are summarized in Table 1 for the sake of clarity.

Table 1. Electric properties.

Design Set	δ_{bp} kW/kg	δ_{be} Wh/kg	δ_{ep} kW/kg	η_{ep} -	t_{burn}^* s
A	3.00	90.00	1.25	0.68	108
B	6.95	198.50	3.92	0.53	103

2.3. Trajectory Optimization

Once engine design parameters have been defined, an indirect procedure optimizes the orbit insertion trajectory [21]. A point mass rocket is considered for the trajectory optimization. State equations provide the derivative of position \mathbf{r} (radius, latitude and longitude), velocity \mathbf{v} (radial, eastward and northward components) and rocket mass M . In a vectorial form one has:

$$\frac{d\mathbf{r}}{dt} = \mathbf{v} \quad \frac{d\mathbf{v}}{dt} = \mathbf{g} + \frac{\mathbf{F} - \mathbf{D}}{M} \quad \frac{dM}{dt} = -\frac{|\mathbf{F}|}{c^* C_F} \quad (19)$$

An inverse-square gravity field is assumed:

$$\mathbf{g} = -\frac{GM_{\oplus}}{\|\mathbf{r}\|^3} \mathbf{r} \quad (20)$$

where G is the gravitational constant and M_{\oplus} is Earth mass. An interpolation of the standard atmosphere, as a function of the rocket altitude, provides density and pressure evaluation. Equations of motion are written in a non-dimensional form to improve the accuracy of the numerical integration. Indirect optimization procedure details are here only summarized and can be found in Ref. [35].

An adjoint variable is associated with each equation; the theory of optimal control provides Euler-Lagrange equations, algebraic equations that determine the control variables (i.e., the thrust direction), and the boundary conditions for optimality (which also implicitly define the engine switching times). A Newton's method-based procedure is used to solve the multi-point boundary value problem which arises. Further details about this procedure can be found in Ref. [36]. Tentative values are initially chosen for the problem unknowns and progressively modified to fulfill the boundary conditions. The unknown parameters are the time lengths of each phase and the initial values of five adjoint variables (the variable corresponding to longitude is null, the one corresponding to the mass is fixed at one, as the problem is homogeneous in the adjoint variables, which can therefore be arbitrarily scaled). Moreover, the overall oxidizer mass and the grain radius are additional unknowns. Dynamic pressure, heat flux and acceleration constraints are checked "a posteriori" and are not explicitly imposed during the trajectory optimization. However, the authors add a constraint that forces horizontal flight at the end of the first burn, to prevent the rocket from reentering the lower layers of the atmosphere (where the heat flux would become larger). Analogously, an additional unknown (the adjoint variable corresponding to the horizontal velocity component has a free discontinuity at the end of the first burn) is introduced in the trajectory optimization procedure.

In the present work, an HRE suitable for the replacement of third (solid) and fourth (liquid) stage of the Vega launcher is considered [37]. The performance of the first stage, second stage, and the exhausted masses are given. The conditions at the ignition of the third stage, consistent with a launch from Kourou, are assigned: altitude $h = 86.88$ km, latitude $\phi = 9.11^\circ$, velocity components in the radial, eastward and northward directions $u_r = 0.142$ km/s, $v_e = 0.230$ km/s, $w_n = 4.146$ km/s, respectively, and mass $m_i = 14,522$ kg [25]. Altitude, eccentricity and inclination (700 km, zero and 90 deg, respectively) define target final orbit. The longitude of the ascending node is left free.

2.4. Robust Design Model

Robust optimization problem can be formally cast as [10]:

$$\begin{aligned} &\text{find} && \mathbf{b} \in \mathbb{R}^n \\ &\text{to maximize} && \Phi_{avg}(\mathbf{b}, \mathbf{p}) \\ &\text{subject to} && g_j(\mathbf{b}, \mathbf{p} + \mathbf{z}^p) \leq 0, j = 1, \dots, r \\ &\text{and to} && \mathbf{b}_L \leq \mathbf{b} \leq \mathbf{b}_U \end{aligned} \quad (21)$$

where \mathbf{b} is the design variables vector, \mathbf{p} is the uncertain variables vector, \mathbf{z}^p is the noise vector of \mathbf{p} , g_j is the j -th inequality constraint, \mathbf{b}_L and \mathbf{b}_U are the lower and upper boundary of the design variables, respectively.

Here the initial mass of the upper stage is given at ignition and the hydraulic resistance Z is evaluated to have $p_t/p_c = 2.5$ at ignition in nominal condition. Six parameters are required to define the propulsion system: the grain outer radius R_g , the web thickness w , the fuel grain length L_b , the final exhausted oxidizer mass $(m_O)_f$ and the initial nozzle area ratio E_i . The sixth parameter is the exhausted oxidizer mass at the beginning of the BD phase $(m_O)_{BD}$, when GPFS is used, while the pump discharge pressure p_d is needed when EPFS is considered. Therefore $\mathbf{b}_{GPFS} = [R_g, w, L_b, (m_O)_f, (m_O)_{BD}, E_i]$ and $\mathbf{b}_{EPFS} = [R_g, w, L_b, (m_O)_f, p_d, E_i]$. Upper and lower boundary of the design variables for GPFS and EPFS are shown in Tables 2 and 3 respectively.

Table 2. Design parameters ranges: GPFS.

Boundary	R_g m	w m	L_b m	$(m_O)_f$ kg	$(m_O)_{BD}$ kg	E_i -
b_L	0.55	0.25	4.3	6971	3195	15
b_U	0.60	0.35	4.5	7697	3631	20

Table 3. Design parameters ranges: EPFS.

Boundary	R_g m	w m	L_b m	$(m_O)_f$ kg	p_d bar	E_i -
b_L	0.55	0.25	4.3	6971	10	15
b_U	0.60	0.35	4.5	7697	50	20

Uncertain parameters are the regression rate coefficients a and n , i.e., $\mathbf{p} = [a, n]$. Uncertainties are taken into account assigning three different levels for each uncertain variables: $a_i \times 10^5 = 9, 9.1, 9.2 \text{ m}^{2n+1} \text{ s}^{n-1} \text{ kg}^{-n}$ for $i = 1, 2, 3$, respectively, and $n_j = 0.68, 0.69, 0.7$ for $j = 1, 2, 3$, respectively. The altitude of the attained orbit h_{ij} is evaluated for each of the nine possible couples a_i, n_j . Since two objectives are relevant (i.e., payload μ and altitude h), an ϵ -constraint approach is adopted [38] to find the Pareto front of robust solutions. Here only the average performance is analyzed. The average constraint violation $\Delta_{avg} = \sum_{ij} p_i p_j \max_{ij}(0, h^* - h_{ij})$ is considered. We assume a binomial distribution giving $p_1 = p_3 = 0.25$ and $p_2 = 0.5$. The average altitude is then $h_{avg} = h^* - \Delta_{avg}$ and the objective function can be computed as:

$$\Phi_{avg} = \mu - k \max(0, \epsilon - h_{avg}) \quad (22)$$

$k = 20 \text{ kg/km}$ is selected to force the average altitude at ϵ . Only the case $\epsilon = h^* = 700 \text{ km}$ (that is the most demanding in terms of robustness) is here considered.

The selection of the optimal robust design is performed by means of a particle swarm optimization (PSO) algorithm. PSO is an optimization procedure belonging to the class of evolutionary algorithms (EAs) that search for an optimal solution in a prescribed search space. It is inspired by the social behavior showed by flock of birds and school of fishes [39,40]. Solutions, here called particles, fly through the problem space by following the optimum particle (i.e., the alpha-member of the flock or school). Cognitive and social acceleration drive the motion of each particle and their position and speed are updated at each iteration. Basic steps of PSO are shown in Figure 2 and PSO settings are presented in Table 4. Additional details about PSO implementation and tuning can be found in Refs. [23,41].

Table 4. PSO settings.

Parameter	Value
Number of generations, N_G	100
Number of particles, N_I	20
Dimension of particles	6
Ranges of particles	$b_U - b_L$
PSO method	1-trelea type 1
Cognitive acceleration, $C1$	2.0
Social acceleration, $C2$	2.0
Check population method	Saturation
End velocity weight	0.4
Linear varying factor	0.2
Maximum velocity, v_{max}	$0.25(b_U - b_L)$
Mass mutation parameter	98%

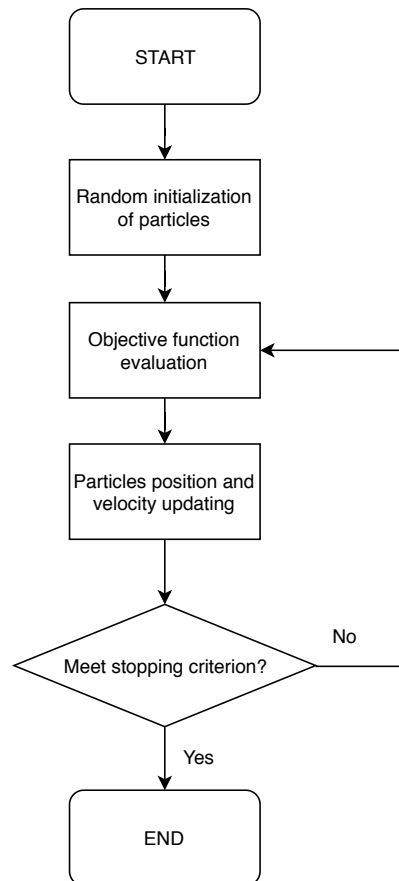


Figure 2. PSO: flow chart.

3. Numerical Results

As described in the previous sections, a two-layer optimization is employed for trajectory and engine design: the indirect trajectory optimization maximizes the final mass given engine geometry, which, in turn, is optimized by means of a robust-based design approach. The average height violation Δ_{avg} is forced to zero, due to the large value for k in Equation (22), and Φ coincides with the payload for all the robust designs summarized in Table 5. Please note that the final burn of the HRE has a very short duration and a limited influence on the rocket performance. Hence subsequent figures show only the first burn for the sake of simplicity.

Table 5. Design parameters and performance.

Case	R_g m	w m	L_b m	$(m_O)_f$ kg	E_i -	$(m_O)_{BD}$ kg	p_d bar	μ kg	Δ_{avg} km	Φ_{avg} kg	t_{burn} s	I_{SP} s
GPFS	0.591	0.294	4.360	7403	17.32	3195	-	2069.8	0.0	2069.8	177	296
EPFS _A	0.579	0.303	4.438	7408	17.44	-	27.7	2321.7	0.0	2321.7	157	296
EPFS _B	0.563	0.334	4.368	7381	18.14	-	39.8	2467.7	0.0	2467.7	158	296

When pump feed system is adopted, mixture ratio and regression rate tend to be larger at the end of the engine burn with respect to GPFS values, as shown in Figures 3 and 4 respectively. Figures 5 and 6 display that pump discharge pressure and oxidizer mass flow variations are actually limited (less than 5%), due to pump constant power operation during the engine burn. Hence efficiency and electrical density assumption for the electric motor and pump system are valid. Thrust history and longitudinal acceleration exhibit different behavior for GPFS and EPFS as reported in Figures 7 and 8 respectively.

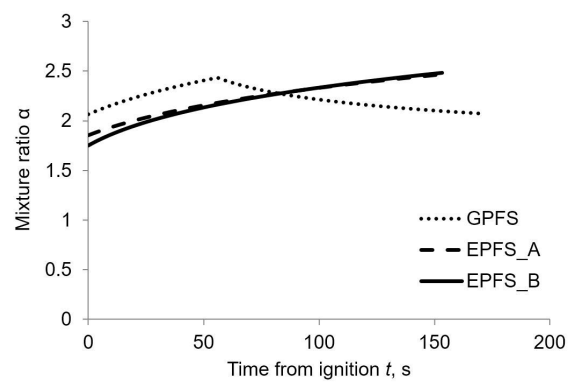


Figure 3. Mixture ratio history.

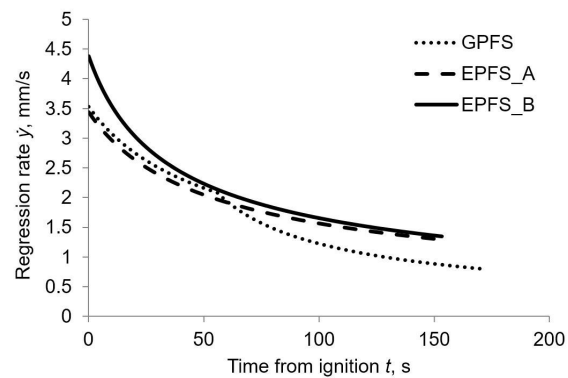


Figure 4. Regression rate history.

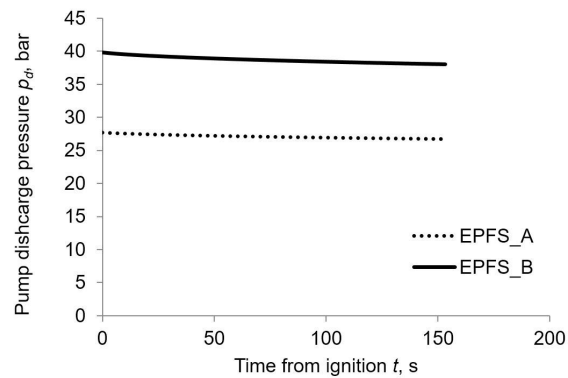


Figure 5. Discharge pressure history.

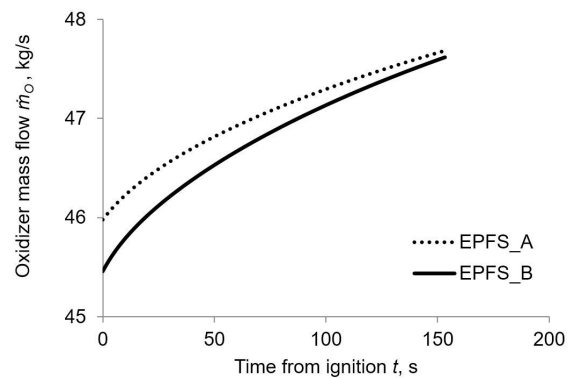


Figure 6. Oxidizer mass flow history.

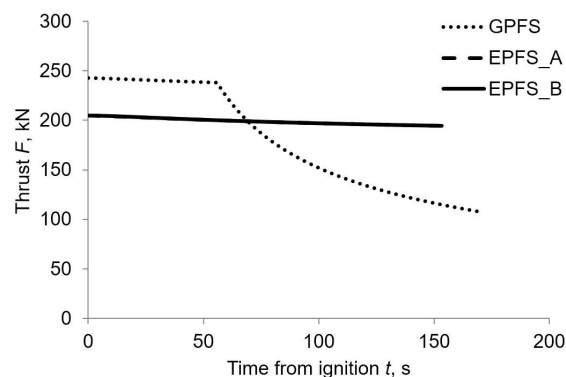


Figure 7. Thrust history.

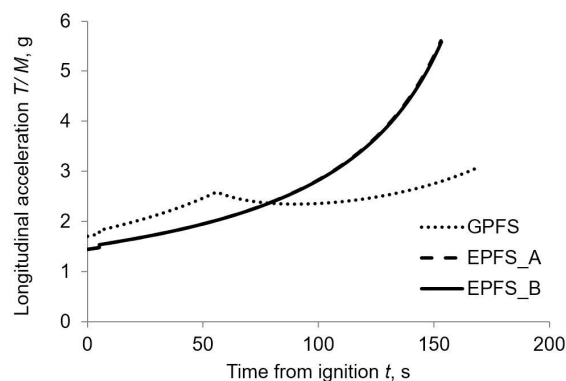


Figure 8. Longitudinal acceleration history.

The thrust in the first half of the burn is larger for the GPFS, with respect to EPFS one, to maintain an acceptable thrust level during the subsequent BD phase. On the other hand, EPFS can maintain an almost constant thrust for all the burn duration and thus its initial thrust level can be lower than GPFS one.

One can notice that EPFS_A and EPFS_B have almost the same thrust history. Nevertheless, the thrust level is obtained in two different ways: EPFS_A optimal design is characterized by lower discharge pressure (i.e., low chamber pressure) and a larger nozzle (i.e., large throat area) than EPFS_B ones. This behavior is forced by the low electric motor and pump power density $(\delta_{ep})_A$ that penalizes high-pressure designs. On the other hand, EPFS_B optimal design favors a higher discharge, and thus chamber, pressures alongside a smaller and lighter nozzle (i.e., small throat area) than EPFS_A ones. The latter optimization strategy is allowed by the advanced electrical properties considered in set B and grants a remarkable nozzle mass saving without thrust reduction.

Mass budgets for robust solutions are reported in Table 6 whereas normalized mass ratios are summarized in Table 7. The current Vega configuration payload for the mission considered in the present work is equal to 1500 kg [37]. The main sources of performance improvement, for both GPFS and EPFS designs, are a remarkable saving in the dry masses of the upper stages and reduced Δv losses. Furthermore, one can notice that EPFS_A saves roughly 350 kg due to lighter tank (pumps allow for unpressurized oxidizer tank), smaller nozzle, and far lower pressurizing gas mass than GPFS one. Moreover, EPFS does not require the auxiliary tank. Thus, the total mass saving is close to 500 kg with respect to GPFS. On the other hand, EPFS requires electric motor and batteries masses that are equal to roughly 230 kg for EPFS_A and 150 kg for EPFS_B. Hence, the payload gain when EPFS is considered, with respect to GPFS, is equal to 252 kg and 398 kg when current or advanced technologies are considered in electric motor and pump masses evaluation. EPFS_B motor, pump and batteries masses are smaller than EPFS_A ones due to better electrical properties despite an actually larger electric power consumption (i.e., higher initial discharge pressure) and electric energy requirement.

Table 6. Mass budget comparison.

Case	μ kg	m_O kg	m_F kg	m_{sl} kg	m_{cc} kg	m_t kg	m_{nz} kg	m_{case} kg	m_g kg	m_a kg	m_b kg	m_{ep} kg
GPFS	2069.8	7403.5	3364.0	0.00	160.2	299.4	351.1	165.6	23.6	149.8	-	-
EPFS _A	2321.7	7407.7	3392.4	0.00	147.4	12.0	309.7	163.7	0.0315	-	98.0	134.4
EPFS _B	2467.7	7380.5	3414.6	0.00	162.3	12.0	239.7	158.4	0.0314	-	77.3	74.4

Table 7. Mass budget comparison: normalized ratios.

Case	$\frac{\mu}{m_i}$	$\frac{m_p}{m_i}$	$\frac{m_p}{m_p + m_{dry}}$
	-	-	-
GPFS	0.143	0.741	0.904
EPFS _A	0.160	0.744	0.926
EPFS _B	0.170	0.743	0.937

4. Conclusions

An indirect trajectory optimization procedure coupled with an evolutionary algorithm has been used to assess the performance viability of an electrically driven pump-fed HRE. The performance of EPFS have been compared to GPFS ones. The optimization of an upper stage of a Vega-like launcher has been considered. The optimization is performed for a given insertion orbit and lift-off weight. The authors take into account uncertainties in the regression rate to grant robustness of the optimal solution. A linear combination of average altitude and payload has been used as mission-specific performance index. The solution is forced to nullify the spread of the orbit altitude by the chosen index formulation, thus assuring the required robustness.

Results show that electric pumps are a viable option for the replacement of a GPFS for the present application. Present technology in batteries and electric motor allows for a payload improvement of approximately 250 kg with respect to GPFS, granting the same level of robustness. A further payload gain is achieved when advanced batteries are considered. Pump power control law can be taken into consideration in future works to improve engine performance and reduce electrical systems masses and maximum longitudinal acceleration.

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Abbreviations

The following abbreviations are used in this manuscript:

BD	Blow-Down
CFD	Computational Fluid Dynamics
EA(s)	Evolutionary Algorithm(s)
EPFS	Electric Pump Feed System
GPFS	Gas-Pressurized Feed System
HP	Hydrogen Peroxide
HRE(s)	Hybrid Rocket Engine(s)
LOX	Liquid-Oxygen

LRE(s)	Liquid Rocket Engine(s)
MAV	Mars Ascent Vehicle
PE	Polyethylene
PSO	Particle Swarm Optimization
RP1	Rocket Propellant 1
SI	International System of units
SRM(s)	Solid Rocket Motor(s)
SSO	Single Stage to Orbit

Nomenclature

A_b	burning surface area, m^2
A_p	port area, m^2
A_{th}	nozzle throat area, m^2
a	regression constant, $m^{1+2n} kg^{-n} s^{n-1}$
\mathbf{b}	design variables vector
\mathbf{b}_L	lower bound vector
\mathbf{b}_U	upper bound vector
C_F	thrust coefficient
c^*	characteristic velocity, m/s
\mathbf{D}	drag vector, N
D	rocket outer diameter, m
E	nozzle area ratio
E_e	electric energy, Wh
\mathbf{F}	thrust vector, N
F	thrust, N
G	gravitational constant, Nm^2/kg^2
\mathbf{g}	gravity acceleration, m/s^2
$g_j(\mathbf{b})$	j-th inequality constraint
h	altitude, km
h^*	target altitude, km
I_{SP}	mean specific impulse, s
I_p	density-specific impulse, $kg s/m^3$
J	throat area to initial port area ratio
k	linear combination constant, kg/km
L	overall engine length, m
L_b	fuel grain length, m
M	rocket mass, kg
M_\oplus	Earth mass, kg
m	mass, kg
N	number
n	mass-flux exponent
P	burning perimeter, m
P_e	electric power, kW
\mathbf{p}	uncertain variables vector
p	pressure, bar
R_g	grain outer radius, m
R_i	grain initial inner radius, m
R_{th}	throat radius, m
\mathbf{r}	position vector, m
s	eroded distance, mm
t	time, s
u_r	velocity component in the radial direction, km/s
V	volume, m^3
v_e	velocity component in the eastward direction, km/s
\mathbf{v}	velocity vector, m/s
\mathbf{v}_{max}	maximum particle velocity vector in PSO
w	web thickness, m

w_n	velocity component in the northward direction, km/s
y	burning distance, m
Z	hydraulic resistance, 1/(kg m)
\mathbf{z}^p	noise vector of \mathbf{p}
α	mixture ratio
γ	specific heat ratio
δ_{ep}	electric motor and pump power density, kW/kg
δ_{be}	batteries energy density, Wh/kg
δ_{bp}	batteries power density, kW/kg
Δ	altitude violation, m
ϵ	multi-objective constraint, km
η_{ep}	electric motor and pump efficiency
μ	payload, kg
ρ	density, kg/m ³
Φ	objective function, kg
ϕ	latitude, deg

Superscripts

\cdot	time derivative
$*$	characteristic

Subscripts

0	ambient
1	combustion chamber at head-end
A	set A electric properties
a	auxiliary gas
avg	average
B	set B electric properties
BD	beginning of blow-down phase
b	batteries
burn	engine burn
c	combustion chamber at nozzle entrance
cc	combustion chamber
d	discharge
dry	dry
e	nozzle exit
ep	electric motor and pump
F	fuel
f	final
fs	feed system
G	generations
g	pressurizing gas
I	individuals
i	initial value
max	maximum
nz	nozzle
O	oxidizer
p	overall propellant (oxidizer + fuel)
ref	reference
sl	sliver
t	oxidizer propellant tank
th	throat
tot	total

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