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### A Cellular Potts Model of single cell migration in

## presence of durotaxis

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Abstract\_ Cell migration is a fundamental biological phenomenon during which cells sense their surroundings and respond to different types of signals. In presence of durotaxis, cells preferentially crawl from soft to stiff substrates by reorganizing their cytoskeleton from an isotropic to an anisotropic distribution of actin filaments. In the present paper, we propose a Cellular Potts Model to simulate single cell migration over flat substrates with variable stiffness. We have tested five configurations: i) a substrate including a soft and a stiff region, ii) a soft substrate including two parallel stiff stripes, iii) a substrate made of successive stripes with increasing stiffness to create a gradient and iv) a stiff substrate with four embedded soft squares. For each simulation, we have evaluated the morphology of the cell, the distance covered, the spreading area and the migration speed. We have then compared the numerical results to specific experimental observations showing a consistent agreement.

Keywords\_ Cell migration, Durotaxis, Cell polarity, Anisotropy, CPM

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### 1. Introduction

Cell migration is a critical phenomenon occurring in several biological processes, such as morphogenesis [1], wound healing [2] and tumorogenesis [3]. It takes place in successive and cyclic steps [4] and it is triggered by specific interactions with the ExtraCellular Matrix (ECM). Actually, cell migration may occur in the absence of external signals thereby typically resulting in a random

walk. However, in most situations, cells are able to sense their surrounding environment and to respond for instance to chemical (i.e., chemotaxis) [5], electrical (i.e., electrotaxis) [6] or mechanical (i.e., mechanotaxis) [7] fields or yet to stiffness gradients (i.e., durotaxis) [8,9]. The latter mechanism consists of the cell preferential crawling from soft matrix substrates to stiffer ones, even in the absence of any additional directional cues [10,11]. By forming local protrusions (i.e., pseudopodia), the cells are in fact able to probe the mechanical properties of the surrounding environment and to more strongly adhere over stiff regions. Additionally, such behaviour results in a substantial reorganisation of the intracellular cytoskeleton. In fact, over soft substrates cells typically show an unstable and isotropic distribution of actin filaments, which are poorly extended and radially oriented, whereas over stiff substrates cell morphology is more stable and exhibits significant spreading and often anisotropic arrangements of actin filaments in the direction of migration (i.e., polarization) [12–16].

Although several computational models have been proposed in literature to investigate single cell migration, only few of them deal with durotaxis. Among others, it is worth to cite the work by Moreo et al. [17] who proposed a continuum approach based on an extension of the Hill's model for skeletal muscle behaviour to investigate cell response on two-dimensional (2D) substrates. They showed, in agreement with experimental observations, that cells seem to have the same behaviour when crawling on stiffer substrate and on pre-strained substrates. Harland et al. [18] instead represented a cell as a collection of stress fibres undergoing contraction and birth/death processes and showed that on stiff substrates cells exhibit durotaxis and stress fibres significantly elongate. Dokukina and Gracheva [19] developed a 2D discrete model of a viscoelastic

fibroblast cell using a Delaunay triangulation. At each node the balance of the forces was determined by the contributions i) of the frictions between the cell and the substrate, ii) of a passive viscoelastic force and iii) of an intrinsic active force. The authors then evaluated cell behaviour over a substrate with a rigidity step in good agreement with specific experimental observations. In fact, they found that the cell preferentially moves on the stiffer substrate and turns away from the soft substrate as reported by [8]. Stefanoni et al. [20] proposed a finite element approach able to account for the local mechanical properties of the underneath substrate and to analyze selected cell migratory determinants on two distinct configurations: an isotropic substrate and a biphasic substrate (which consists of two adjacent isotropic regions with different mechanical properties). Trichet et al. [14] employed instead the active gel theory to demonstrate that cells preferentially migrate over stiff substrates founding an optimal range of rigidity for a maximal efficiency of cell migration. Further, in [21] a vertex-based approach (i.e., the socalled Subcellular Element Model, SCE) was set to represent intracellular cytoskeletal elements as well as their mechanical properties. In particular, the dynamics of such subcellular domains were described by Langevin equations, which account for a weak stochastic component (i.e., that mimic cytoplasmic fluctuations) and elastic responses (i.e., modelled by generalized Morse potentials) to both intracellular and intercellular biomechanical forces. The same method was successfully applied in [22] for modelling substrate-driven bacteria locomotion. Finally, in Allena and Aubry [23] a 2D mechanical model was proposed to simulate cell migration over an heterogeneous substrate including slipping regions and to show that over softer regions the cell slows down and is less efficient.

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In the present work, we describe a Cellular Potts Model (CPM, developed in [24,25] and reviewed in [25–29]), which is a lattice-based stochastic approach employing an energy minimization philosophy, to reproduce single cell migration over flat substrates with different rigidity. In particular, we test four configurations: i) a substrate including a soft and a stiff region, ii) a soft substrate including two parallel stiff stripes, iii) a substrate made of successive stripes with increasing stiffness to create a gradient and iv) a stiff substrate with four embedded soft squares. For each scenario, we analyse cell behaviour in terms of morphology, distance covered, spreading/adhesive area and migration speed in order to capture the essential mechanisms of durotaxis. The computational outcomes are then compared with specific experimental observations taken from the existing literature.

The rest of this paper is organized as follows. In Section 2, we clarify the assumptions on which our approach is based and present the model components. The simulation results are then shown in Section 3. Finally, a justification of our model choices as well as a discussion on possible improvements is proposed in Section 4. Additionally, the article is equipped with an Appendix that deals with statistics and parameter estimates.

### 2. Mathematical model

The cell-substrate system is represented using a CPM environment [24,25]. The simulation domain is a three-dimensional (3D) regular lattice  $W \in \mathbb{R}^2$  constituted by identical closed grid sites, which are identified by their centre  $\mathbf{x} \mid \mathbb{R}^2$  and labelled by an integer number  $S(\mathbf{x}) \mid N$  (which can be interpreted as a degenerate spin) [30,31]. The boundary of a generic site  $\mathbf{x}$ , one of its neighbours

and its overall neighbourhood are defined as  $\P \mathbf{x}$ ,  $\mathbf{x}$  and  $W'_{\mathbf{x}}$ , respectively. Subdomains with identical label S form discrete objects  $S_{S}$  (with border  $\partial \Sigma_{\sigma}$ ), which have an associated type  $t(S_{S})$ . In the case of our interest, t = M stands for the medium, t = C for the cells and t = S for the i-th type of substrate. In this respect, we anticipate that each type of matrix region will differ for stiffness and therefore for adhesive affinity with moving individuals.

Cell dynamics result from an iterative and stochastic reduction of the energy of the overall system, given by a Hamiltonian H (units:  $Kg \cdot m^2/s^2$ ), whose expression will be clarified below. The employed algorithm is a modification of the Metropolis method for Monte Carlo-Boltzmann dynamics [24,32], which is particularly suitable to simulate the exploratory behaviour of biological individuals as cells. Procedurally, at each time step t of the algorithm, called Monte Carlo Step (MCS), a randomly chosen lattice site  $\mathbf{x}_{source}$  belonging to a cell tries to allocate its spin  $\sigma(\mathbf{x}_{source})$  to one of its unlike neighbours  $\mathbf{x}_{target} \in \mathbb{W}'_{x}$ , which is also randomly selected. Then, the net energy difference DH due to the proposed change of system configuration is calculated as

$$|DH|_{S(\mathbf{x}_{\text{source}}) \to S(\mathbf{x}_{\text{target}})} = H_{(\text{after spin copy})} - H_{(\text{before spin copy})}$$
(1)

The trial spin update is finally validated by a Boltzmann-like probability function defined as

$$P\left[S\left(\mathbf{x}_{\text{source}}\right) \to S\left(\mathbf{x}_{\text{target}}\right)\right]\left(t\right) = \min\left\{1, e^{-\frac{DH}{T_c}}\right\} \quad (2)$$

where t is the actual MCS and  $T_c \hat{l}$   $R_+$  is a Boltzmann temperature, that has been interpreted in several ways by CPM authors (see [33] for a comment on this

aspect). However, we here opt to give  $T_C$  the sense of a cell intrinsic motility (i.e., agitation rate), following the approach in [25]. Finally, it is useful to underline that the matrix substrates are considered fixed and immutable.

As seen, the simulated system evolves to iteratively and stochastically reduce its free energy, which is defined by a Hamiltonian function H which, for any given time step t, reads

$$H(t) = H_{adhesion}(t) + H_{shape}(t)$$
 (3)

 $H_{adhesion}(t)$  is deduced from the Steinberg's Differential Adhesion Hypothesis (DAH) [24,34] and is due to the adhesion between cells and extracellular components (i.e., the medium or a given type of substrate). In particular, it reads

$$H_{\text{adhesion}}(t) = H_{\text{adhesion}}(t) = \mathop{\tilde{\text{A}}}_{\text{(1)xi } \text{ } \text{(1)S}_{\text{s}}\text{)}\text{C}(\text{(1)xi } \text{ } \text{(1)S}_{\text{st}}\text{)}} J_{t(S_{\text{s(x)}}), t(S_{\text{st}})}$$
(4)

with X and  $X^{\mathbb{C}}$  two neighbouring sites and  $S_s$  and  $S_{st}$  two neighbouring objects (with borders  $\P S_s$  and  $\P S_{st}$ , respectively).  $J_{t\left(S_{s\left(X\right)}\right),t\left(S_{s\left(X\right)}\right)}$   $\widehat{I}$  R are constant and homogeneous binding forces per unit area. They are symmetric with respect to their indices and can be specified as follows:

- $J_{C,M}$  is the adhesive strength between the cells and the collagenous medium which is constituted by a mixture of soluble adhesive ligands (i.e., carbohydrate polymers and non-proteoglycan polysaccharides) and water solvent;
- $J_{C,S_i}$  gives the adhesive strength between the cells and i-th type of substrate. Recalling the minimization theory of the CPM, we assume that the stiffer the substrate i, the lower the corresponding value  $J_{C,S_i}$  (i.e., the higher the adhesion between the cells and the i-th type of substrate). This is a pivotal hypothesis of our approach: it is consistent since it has been widely demonstrated in the

experimental literature that cells generate higher traction forces and generate more stable focal adhesion points when migrating over stiffer substrates [16,35–38].

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 $H_{shape}(t)$  defines the geometrical attributes of each cell  $S_s$ , which are written as elastic potentials as it follows:

$$\begin{split} H_{\text{shape}}\left(t\right) &= H_{\text{volume}}\left(t\right) + H_{\text{surface}}\left(t\right) \\ &= \mathop{\mathring{\text{el}}}_{\mathcal{S}_{\mathcal{S}}}^{\dot{\mathcal{E}}} k_{\mathcal{S}_{\mathcal{S}}} \left(v_{\mathcal{S}_{\mathcal{S}}}\left(t\right) - V_{\mathcal{C}}\right)^{2} + n_{\mathcal{S}_{\mathcal{S}}}\left(t\right) \left(\mathbf{S}_{\mathcal{S}_{\mathcal{S}}}\left(t\right) - \mathbf{S}_{\mathcal{C}}\right)^{2\dot{\mathbf{u}}\left(5\right)} \mathbf{b}^{\dot{\mathbf{u}}\left(5\right)} \end{split}$$

where  $V_{S_s}(t)$  and  $S_{S_s}(t)$  are the actual volume and surface of the cell  $S_s$  , whereas  $V_{\rm C}$  and  $S_{\rm C}$  the corresponding cell characteristic measures in the initial resting condition.  $K_{S_s}$  and  $n_{S_s}(t)$  are instead two mechanical moduli in units of energy. The former is linked to volume changes and, assuming that cells do not significantly grow during migration, is considered constant with a high value (i.e.,  $k_{S_s} = k_C >> 1$ ) for any individual  $S_s$ . The latter refers to the rigidity of a cell. As we will explain in details later on, for each cell  $S_s$ ,  $n_{S_s}$  is assumed to depend on the underneath type of substrate. In particular, each cell decreases its initially high (i.e., >> 1) rigidity, thereby being more able to deform, if it comes in contact with a stiff substrate. This assumption is consistent with experimental observations on the fact that cell contact with stiff matrix regions activate downstream intracellular pathways resulting in acto-myosin dynamics and therefore in cytoskeletal remodelling [8,39]. More specifically, it seems that certain cells have a binary sensor at their membrane junction sites that allows them to switch from a relaxed and rounded morphology, when the substrate is softer than the cell's elastic modulus [39–43], to a fan-shaped morphology with abundant stress fibres, when the substrate is stiffer or as stiff as the cell itself [39]. Further, it has been shown that cells tend to isotropically and poorly spread on soft substrates, whereas they form pseudopodia randomly distributed along the membrane on stiff substrates, resulting in a significant anisotropic spreading [16]. In this respect, according to several experimental observations [16,35–38,44], there exists a linear relationship between the adhesion forces exerted by the cell on the substrate and the spreading area of the cell. More specifically, the larger the contact area between the cell and the substrate, the higher the number of focal adhesion points that can be established. Nonetheless, the sequence of events is still unclear and two main processes may occur when a cell is seeded on a stiff substrate [45]:

- i) the cell adheres because of the stiffness of the substrate, then it significantly spreads;
- ii) the cell spreads because of the stiffness of the substrate, then it more strongly adheres.

Such uncertainty is the reason why in the present model both the adhesive parameters and the cell rigidity directly depend on the substrate stiffness, but are independent from each other.

The main components and the scales involved in the proposed model are summarized in the diagram in Fig. 1. Finally, all the parameters of the simulations are reported in Table 1, while the Appendix provides a careful explanation of how they have been estimated.

### 3. Numerical simulations

The characteristic size of each lattice site is 4  $\mu m$  and the geometrical domain W is a 70x70x30 regular grid (280  $\mu m$  x 280  $\mu m$  x 120  $\mu m$ ) with no-flux boundary conditions in all directions. This choice mimics the situation of a

delimited experimental device, where cells are not able to overcome the physical barriers. All our CPM cells are initially a hemisphere of a radius of 20 µm, whose initial position will be specified for each simulation setting. A MCS is set to correspond to 2 s of actual unit of time (see the Appendix for a comment on this aspect), which results in simulations covering time intervals between 16 min to 5.5 h. This choice enables cells to migrate over sufficiently long paths in order to compare numerical results and proper experimental observations. We have tested several cell-matrix settings, which are presented in the followings. The resulting simulations were performed on a modified version of the open source package CompuCell3D (downloadable at www.compucell3d.org). In particular, a Phyton script was specifically developed to account for substrate-dependent cell rigidity.

### 3.1 Cells preferentially crawl over stiff substrates

We first consider a substrate split into a soft and a stiff region, i.e.,  $t = S_1$  and  $t = S_2$  (see Fig. 2a). A cell  $S_1$  is then seeded at the centre of the substrate and it is allowed to move for 500 MCS (approximately 16 minutes). The rigidity of  $S_1$ ,  $n_{S_1}$ , has initially a high value  $v_{\Sigma_1} = v_C = 25 \cdot 10^{-3} \text{ Kg/s}^2 \text{m}^2$ . However, it is allowed to decrease, of  $10^{-3} \text{ Kg/s}^2 \text{m}^2$  for MCS until a threshold value  $n_t$  equal to  $10^{-2} \text{ Kg/s}^2 \text{m}^2$ , while the cell is in contact with the stiff region  $S_2$ , thereby leading to a flattening of the initially rigid cellular hemisphere. In mathematical terms, we indeed have that

$$\nu_{\Sigma_{1}}(t) = \begin{cases} \max(\nu_{\Sigma_{1}}(t-1) - 10^{-3}; \nu_{t}) & \text{if } \exists (x, x' \in \Omega'_{x}) : x \in \Sigma_{1} \text{ and } x' \in S_{2}; \\ \nu_{\Sigma_{1}}(t-1) & \text{else,} \end{cases}$$
 (6)

for each MCS.

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We then study how cell behaviour is affected by variations in the ratio between the adhesive affinity of the cell with either the soft or the stiff substrate region. In particular, we keep fixed  $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$  while decreasing the value of  $J_{C,S_2}$  from 25 · 10<sup>-15</sup> Kg/s<sup>2</sup> to 1 · 10<sup>-15</sup> Kg/s<sup>2</sup> (which is equal to  $J_{stiff}$ , the lowest value consistent with the case of our interest, see the Appendix). As summarized in Fig. 3c, when  $J_{C,S_2}$  decreases, the cell is biased to crawl towards the stiff domain, as it is confirmed by the plot of the trajectories of its center of mass deriving from independent simulations. In fact, over a period of 500 MCS (≈ 16 minutes), the cell randomly moves around the substrate centre when  $\frac{J_{C,S_1}}{J_{C,S_2}} = 1$ (Fig. 3a) while, when  $\frac{J_{C,S_1}}{J_{C,S_2}} = 25$ , the cell trajectories dramatically shift over the stiff part of the substrate (Fig. 3b). Our numerical results are sustained and consistent with the experimental observations according to which cells (i.e., fibroblasts, smooth muscle cells, Mesenchymal Stem Cells (MSCs)) crawl from soft (1 to 5 kPa) to stiff (34 to 80 kPa) substrates (i.e., gels or polyacrylamide sheets) [9–11,46]. Notably during motion towards the stiff substrate, our CPM cell is also allowed to increase its remodeling ability, as its rigidity  $\nu_{\Sigma_1}$  progressively decreases upon contact with substrate  $S_2$  , according to Eq. (6). In this respect, a further set of simulations evaluates cell morphological differences due to the underneath type of substrate. Keeping the same domain as in Fig. 2a, two cells, i.e.,  $S_1$  and  $S_2$ , are initially seeded in the middle of the soft and the stiff regions, respectively. The rigidity of the two cells is then regulated by Eq. (6). As reproduced in Fig. 4 (in particular, panel (a) represents the final cell morphologies as resulted from a single representative simulation, whereas panel (b) gives the mean final cell morphologies, as the plain ellipsoids derive from an interpolation procedure of the cell adhesive areas coming from independent simulations, see the Appendix for further details), both individuals do not significantly move across the domain during a time lapse of 500 MCS (approximately 16 min). However, the adhesive area of the cell located over the soft region is almost 30% lower than the adhesive area of the cell that crawls over the stiff substrate (Fig. 4c). Such a cell behaviour is consistent with the experimental data by Lo and co-workers on 3T3 fibroblasts cultured on flexible polyacrylamide sheets coated with type I collagen, where a transition in rigidity was introduced by a discontinuity of the bis-acrylamide cross-linker, that resulted in two substrate regions with Young's modulus equal to either 14 kPa and 30 kPa [46]. In particular, on one hand, the value of the adhesive area of our CPM cell seeded on the soft substrate is not surprisingly similar to the corresponding data by Lo and co-workers [46], since we used such an experimental quantification for our parameter estimate (see the Appendix). On the other hand, the adhesive area of the CPM cell seeded on the stiff region is instead a completely independent and self-emerging model outcome: therefore its consistency with the measurements by Lo and colleagues [46] is relevant point of our work.

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### 3.2 Stiff vs soft substrate in the presence of an external cue

For the second series of simulations we consider again a domain split into a soft ( $t = S_1$  such as  $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ ) and a stiff ( $t = S_2$  such as  $J_{C,S_2} = J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$ ) region, but an additional external potential is introduced. This results in an imposed artificial bias in the spin flip rate that is able to affect the direction of cell migration. Entering more in details, the

expression of the Hamiltonian function presented in Eq. (3) is modified as it follows

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$$H(t) = H_{adhesion}(t) + H_{shape}(t) + H_{potential} (7)$$

where  $H_{potential} = -v_{ext} \left( \boldsymbol{x}_{target}^{c} - \boldsymbol{x}_{source} \right)$  and  $v_{ext}$  is a vector whose components determine the direction of the potential and whose modulus gives the relative importance in the overall system energy. For the sake of simplicity, we assume that the potential is constant in time and homogeneous throughout the entire domain. As we will see later, it is in fact an artificial term that simply helps cells to maintain a sustained directional movement. In this respect, what is relevant is only its modulus, i.e.,  $|\boldsymbol{v}_{ext}|$ . We then test two configurations:

- a) a cell  $S_1$  placed at the south-east corner and the external potential directed towards the north-west corner;
- b) the same cell  $\Sigma_1$  placed at the south-west corner of the substrate and the external potential directed towards the north-east corner.

In both cases, we set  $|v_{ext}| = 7 \cdot 10^{-21} \text{Kg} \cdot \text{m/s}^2$ , which results in plausible cell velocities (see later) and the simulations last 10000 MCS (approximately 5.5 h). Further, cell rigidity is again regulated by Eq. (6).

In system configuration a) (see Movie 1 and Fig. 5a), the external cue guides the cell towards the north-west corner of the domain. In particular, when a part of the cell comes into contact with the stiffer substrate, it becomes the leading edge. Further, the moving individual clearly accelerates as soon as it crosses the boundary between the two matrix regions (3.6  $\mu$ m/s versus 4.5  $\mu$ m/s, Fig. 5c), as experimentally observed in [8] for fibroblasts crawling over polyacrylamide

sheets. An increment of the adhesive area is observed as well when the cell shifts over the stiff region.

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In the case b), the external potential forces the cell to move towards the northeast corner of the domain (see Movie 2 and Fig. 5b). However, as soon as the individual approaches the soft region, it changes orientation, and starts moving and elongating parallel to the boundary between the two substrate regions. These outcomes may be compared to the experimental observations obtained by Lo et al. in [46], who cultured fibroblasts on the already described substrate system, i.e., characterized by two areas with different Young's modulus. In particular, Lo and colleagues seeded cells at low density to minimize the effects of intercellular interactions and to avoid that pulling or pushing forces from neighbours individuals may alter cell substrate probing processes (thereby impeding cells to freely move across the soft and the stiff regions). Then, cell migration was recorded over a time span of 10 h. Similarly to our numerical outcomes, the authors found that as cells move towards a stiffer substrate, new lamellipodia are formed in the direction of migration, thereby resulting in the dominant front end of the individuals. On the opposite, local retractions occur when cells approach a soft region, inducing therefore a change of direction. In a second series of experiments, Lo and co-workers showed that mechanical inputs triggered by substrate deformations might also control formation and retraction of lamellipodia. In particular, they externally pulled or pushed the substrate away or towards the cells centre to find that, due to the centripetal forces exerted by the 3T3 fibroblasts on the substrate [46], in the first case less motion is produced, since cells experience a softening of the substrate, whereas in the second case the overall motion is increased, since cells perceive the substrate as stiffer. In the

CPM model proposed here, the matrix substrates are not deformable, therefore the numerical simulations are unable to capture the experimental observations coming from this second set of assays.

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### 3.3 Two stiff stripes embedded in a soft substrate

The third configuration that has been tested includes a soft substrate (again  $t = S_1$  with  $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ ) with two embedded stiff stripes (again  $t = S_2 \text{ with } J_{C,S_2} = J_{stiff} = 1.10^{-15} \text{ Kg/s}^2$ ), which are both 28 µm-wide (Fig. 2b). A cell  $S_1$  is initially seeded at the south-west corner, whose rigidity is allowed to decrease following the constitutive law (Eq. (6)). An external potential is then introduced towards the north-east corner of the domain: its intensity  $|v_{ext}|$  is allowed to vary from a minimal value of  $7 \cdot 10^{-21}$  Kg·m/s<sup>2</sup> to a maximal value of 28·10<sup>-21</sup> Kg·m/s<sup>2</sup>. All simulations last 10000 MCS, which correspond to nearly 5.5 h. In the case of a low  $|v_{ext}| = 7 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$  (see Fig. 6a and Movie 3), the cell typically migrates towards the first stiff substrate stripe: then it remains stuck over it and goes on migrating along such a matrix region. Furthermore, its morphology, due to the dependency of its elasticity on the underneath type of substrate, changes as the crawling individual acquires an elongated shape. Such a behaviour is due to the fact that the external potential is too low to overcome the adhesive interactions between the cell and the stiffest substrate: in particular, the individual has not energetic benefits (deriving from the external bias) to move further in the domain, i.e., to pass the first stiff stipe. The outcomes of our CPM are consistent to that observed for cells (i.e., endothelial cells or fibrosarcoma cells) seeded on

2D substrates (i.e., maleic acid copolymer surfaces) structured with fibronectin stripes which orient their actin fibres along the stripe direction [47–49].

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On the other hand, if the modulus of the external potential increases, we have a higher percentage of cells that are able to cross the entire domain (Fig. 6b). In particular, when  $|v_{ext}|$  is maximal (i.e.,  $28\cdot10^{-21}$  Kg·m/s<sup>2</sup>, Fig. 6c and Movie 4), the cells constantly migrate at the north-east corner of the domain passing also the second stiff stripe. In this case, the cell average velocity increases over the stiff stripes (about 4.4 µm/s) whereas it varies between 3.6 µm/s and 3.9 µm/s over the soft regions (Fig. 6d). With the maximal external potential, cell morphology does not significantly vary, as the moving individuals typically maintain an almost hemispheric shape, without substantial elongation or increments in the adhesive area during the entire motion. They in fact behave as translating rigid bodies, subjected to an external high force. This interesting behaviour is the consequence of the fact that the cells do not need to reorganize (nor have enough time to do it) to be able to crawl, as their motion is mainly due to the external bias: the specific substrate regions are only able to further accelerate (or partially slow down) cell movement, as previously commented. The numerical outcomes in the case of low or intermediate values of  $|\boldsymbol{v}_{ext}|$  can be compared to those experimentally tested by Choi et al. [50] and Vincent et al. [51], where different cell phenotypes were seeded on micropatterned hydrogels with stiffness gradient. Although no external bias was introduced in such experimental configurations, a similar behaviour may be observed. In the former work [50], the authors proposed two mechanicallypatterned hydrogels: one constituted by 100 µm stiff (10 kPa) and 500 µm soft (1 kPa) stripes and one containing 500 μm stiff (10 kPa) and 100 μm soft (1 kPa). First, Adipose-derived Stem Cells (ASCs) and C2C12 myoblasts were allowed to adhere and both were able to sense the stiffness gradient and to migrate towards the stiffer stripes (i.e., durotaxis) [46]. Such behaviour was also observed when cells were far away from the stripe interface (around 250 µm). Nevertheless, since cells only detect stiffness differences over short distances (around some microns) [52], in this case the authors implied that the phenomenon was mostly due to random walk towards the interface rather than to durotaxis itself. Regarding the morphology of the cells, both ASCS and C2C12 myoblasts aligned in the direction of the long axis of the stripe as we observe in our numerical simulations (Fig. 5a and Movie 3) in the case of low intensity of the external potential. Second, less contractile cells such as neurons were seeded on the hydrogels, which did not show any preferential adhesion confirming previous experimental observations according to which they prefer a softer niche [53].

In the latter work [51], the authors developed three types of polyacrylamide (PA) hydrogel systems of stiffness gradients: physiological (1 Pa/ $\mu$ m), pathological (10 Pa/ $\mu$ m) and step (100 Pa/ $\mu$ m). The step stiffness gradient, which is the configuration of interest for the simulations presented above in this section, was constituted by 500  $\mu$ m wide regions of soft PA alternated with ~100  $\mu$ m wide stripes of stiff hydrogel producing a stripped stiffness profile. MSCs were plated and they spread and attached independently of the gradient strength or the stiffness within hours after the seeding, whereas after 3 days they started to migrate towards stiffer regions. Additionally, cells crawled at 18  $\pm$  0.7  $\mu$ m/hr, which is approximately 6-fold faster than on the other gradient configurations discussed in the same paper (i.e. physiological and pathological) and confirms that durotaxis velocity is influenced by gradient strength [11].

# 396 3.4 Stiffness gradient

In this section, we present the results for a simulation involving a substrate made of six successive stripes (i.e.,  $t = S_i$ where i = I,...,6, each 46 µm-wide) which are organized to obtain a soft-to-stiff gradient from the left to the right side of the domain (from the red to the yellow subdomains). Such substrate regions are characterized by different cell adhesive affinity, i.e.,  $J_{C,S_i}$ , which vary from  $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$  to  $J_{C,S_6} = J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$ , respectively (see Fig. 2c and the corresponding caption for the specific details). A cell  $S_i$  is initially seeded at the south-west corner and an external potential is introduced towards the north-east corner of the domain, whose magnitude  $|v_{ext}|$  is varied again from a minimal value of  $7 \cdot 10^{-21} \text{ Kg·m/s}^2$  (Movie 5) to a maximal value of  $28 \cdot 10^{-21} \text{ Kg·m/s}^2$  (Movie 6). The rigidity  $n_{S_i}$  of  $S_i$  is allowed to decrease (from the usual initial high value of  $v_C = 25 \cdot 10^{-3} \text{ Kg/s}^2\text{m}^2$ ) with a law analogous with Eq. (6), but which takes into account of the presence of different types of substrates, i.e.,

$$\nu_{\Sigma_1}(t) = \begin{cases} \max(\nu_{\Sigma_1}(t-1) - \nu_i; \nu_t) & \text{if } \exists (x, x' \in \Omega_x') : x \in \Sigma_1 \text{ and } x' \in S_i; \\ \nu_{\Sigma_1}(t-1) & \text{else,} \end{cases}$$
(8)

where t is the actual MCS,  $n_t$  is the usual threshold value (equal to  $10^{-2}$  Kg/s<sup>2</sup>m<sup>2</sup>) and i = 2,...,6. In this respect,  $v_i = 0.05 \cdot 10^{-3}$ ,  $0.06 \cdot 10^{-3}$ ,  $0.1 \cdot 10^{-3}$ ,  $0.2 \cdot 10^{-3}$ ,  $1 \cdot 10^{-3}$  Kg/s<sup>2</sup>m<sup>2</sup> while the cell is in contact with substrate  $S_2$ ,  $S_3$ ,  $S_4$ ,  $S_5$ ,  $S_6$ , respectively.  $n_{S_1}$  remains indeed constant and equal to  $v_C$  if the cell is located over the softest substrate  $S_1$ . All the resulting simulations last 10000 MCS (5.5 h). As reproduced in Fig. 7a, the percentage of cells able to reach the north-east corner increases

concomitantly with increments of  $|v_{ext}|$ . Moreover, by fixing  $|v_{ext}| = 28 \cdot 10^{-21}$  Kg·m/s<sup>2</sup>, it is possible to observe that the cell average velocity increases from 3.6  $\mu$ m/s to 4.4  $\mu$ m/s as they move from softer to stiffer substrates (Fig. 7b). This result is coherent with the model outcomes of the previous set of simulations (i.e., see Fig. 6c and d), where we have observed that in the case of very high external potential cells accelerate while crossing on stiffer matrix regions, even if they do not significantly undergo morphological transitions.

A similar configuration was experimentally proposed by Cheung et al. [10] who, using a microfluidics-based lithography technique, fabricated a micropatterned cell-adhesive substrate made of a series of PEG-fibrinogen hydrogels with uniform stiffness ranging from 0.7 to 50 kPa. Human Foreskin Fibroblasts (HFFs) were then plated and their migratory trajectories were analysed over 22 h. The authors found that the cells that were initially seeded on a stiffness frontier tended to migrate towards the stiffer region, while cells plated on uniform stiffness spread in both directions.

### 3.5 Role of the characteristic dimension of the gradient stiffness

The external potential introduced in most of the previous sets of simulations, is an artificial term that is included in the Hamiltonial to bias and sustain cell movement across the entire matrix substrate. In experimental assays, the directional component in cell motion is typically established by geometrical cues, such as microtracks and microchannels [54,55], or gradients of soluble or insoluble chemical substances (chemotaxis and haptotaxis, respectively) or, in the case of our interest, gradients of substrate stiffness [10,51]. However, we have observed from our simulations that the sequence of different types of substrate

stripes employed in the previous section does not suffice to determine a persistent cell movement across the entire matrix, since a high enough external potential has to be included to allow cells reach the north-east corner of the domain (see the plot in Fig. 7a). The reason of this discrepancy between computational and experimental outcomes relies in the fact that "real cells", once established a direction of movement, are able to dramatically orient their cytoskeleton (via the polarization of actin filaments) and, eventually, start a persistent shape-dependent locomotion. This way, real individuals are able to cross also large portions of substrates without slowing down or changing direction. Such a cell behaviour can not be captured in our approach since we do not include a proper model component reproducing selected intracellular cytoskeletal dynamics (in this respect, the interested reader may refer to [56,57], where polarization processes and the subsequent cell persistent movements are simulated in CPMs either by introducing an asymmetric correction to the Boltzman probability law or by adding a further inertial term in the Hamiltonian). The CPM cells of our model are only able to isotropically spread (due to decrements in their rigidity upon contact with stiff substrates) or elongate following the geometry of the underlying matrix region in order to maximize their adhesive interactions with the stiffer areas of the domain (but only when the external potential is substantially low, see Fig. 6a and c). However, the model presented in this paper can be used to predict if a sustained cell motion can be achieved by only varying the geometrical characteristics of the matrix substrate. With this purpose in mind, we employ the same type of domain as in Section 3.4, but we progressively decrease the width of the substrate stripes. We then evaluate the minimal magnitude of the external potential needed by cells to reach the border of the domain opposite to their initial

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position (again the south-west corner). Cell rigidity follows the law in Eq. [8] and the simulations last 10000 MCS (5.5 h). As summarized in panel (a) of Fig. 8, we can observe a tri-phasic behaviour. For sufficiently wide stripes (i.e., > 45 µm), a cell sustained movement results only with very high external potentials (i.e.,  $>25 \cdot 10^{-21} \text{ Kg·m/s}^2$ ). Then, for lower stripe widths (i.e., in the range of 35-45 µm) the critical value of the external potential modulus decreases almost linearly. Finally, for low enough stripe widths (i.e.,  $< 35 \mu m$ ), the potential necessary to have a sustained cell movement significantly drops, until becoming negligible for stripe widths lower than 35 µm (Movie 7). Summing up, we can state that the characteristic dimension of the stiffness gradient (here determined by the width of the matrix stripes), which allows a persistent cell movement without the artificial help of an external bias, is lower than the mean cell diameter (i.e., that in our simulations is around 40-45 µm). From a computational viewpoint, the rationale of this behaviour is that when a CPM cell is located on a given substrate stripe it is however able to wandering its close proximity (due to the stochastic Metropolis algorithm) which, if the stripe width is low enough, includes the neighbouring matrix region. In this respect, the CPM cell simultaneously experiences the adhesive affinity with a couple of neighbouring substrate stripes and then it moves towards the stiffer one, thereby advancing across the domain. Such a process is reiterated for all pairs of substrate stripes, thereby resulting in a sustained directional movement. These results can be interpreted from an experimental viewpoint as a prediction on the fact that cells may exhibit a persistent motion also without an intracellular polarization, i.e., by only maintain an amoeboid movement, if the substrate stiffness gradient is sufficiently fine-grained.

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We finally conclude this section by analysing how cell velocity is affected by the wide of the substrate stripes, in the range of values sufficiently low to have a sustained cell crawling in the absence of an external potential (i.e.,  $< 35 \mu m$ ). As it is possible to see in panel (b) of Fig. 8, lower widths of the substrate regions (which means, as previously seen, more fine-grained stiffness gradients) results in increments in cell average velocity. From the computational viewpoint, this is due to the fact that the more the different stripes of the matrix are small, the more the previously described cell probing mechanism is facilitated and accelerated, thereby resulting in higher cell average velocities.

### 3.6 Soft squares embedded in a stiff substrate

As a final simulation, we test the substrate configuration in Fig. 2d, where four soft squares ( $t = S_1$  with  $J_{C,S_1} = J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ ) are embedded in a stiff substrate ( $t = S_2$  with  $J_{C,S_2} = J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$ ) at its three corners (northwest, north-east and south-east) and at the centre. A cell  $S_1$  is initially seeded at the south-west corner and an external potential is introduced towards the northeast corner of the domain, whose magnitude  $|v_{ext}|$  has been set equal to an intermediate  $14 \cdot 10^{-21} \text{ Kg·m/s}^2$ . As usual, cell rigidity is allowed to decrease according to Eq. (6) and the observation time is 10000 MCS (i.e., nearly 5.5. h). The cell starts moving in the direction determined by the potential with a trajectory of approximately  $45^\circ$  but, as soon as it encounters the central soft square, the cell avoids and circumvents it. As the original path is recovered, the cell needs to squeeze between the north-east square and the substrate frontier in order to achieve the target corner of the domain (Movie 8 and Fig. 9). The choice

of the migration track may depend on the initial position of the cell. In the present simulation, the cell is seeded along the substrate diagonal, thus the probability of circumventing the central soft square counter clockwise (as it happens here) or clockwise are the same. However, if the cell is seeded slightly downward and/or right, it will most certainly employ a counter clockwise trajectory, whereas if it is plated upward, it will probably follow a clockwise path. It is useful to notice that with a significantly higher modulus of the external potential the cell would have been able to pass across the soft regions, without deforming to avoid them, coherently with the simulations proposed in Fig. 6c.

This configuration is similar to that proposed in [23] where the cell must avoids two slipping regions in order to reach the external cue placed at 45°. Although the employed numerical approaches are substantially different, taken together the outcomes confirm the tendency of the cell to migrate over stiffer substrates where the higher adhesion forces may be developed.

### 4. Conclusions

In this paper we have proposed a three-dimensional CPM approach to simulate single cell migration over matrix domains in which soft and stiff regions are combined.

The CPM method is becoming an increasingly common technique for the mathematical modelling of a wide range of biological phenomena, including avascular and vascular tumor growth [58–61], gastrulation [62], skin pigmentation [63], yeast colony growth [64], stem cell differentiation [65], fruiting body formation of Dictyostelium discoideum [66], epidermal formation [67], hydra regeneration [66], retinal patterning [68], wound healing [69,70], biofilms [71],

chick limb-bud growth [72-74], cellular differentiation and growth of tissues, blood flow and thrombus development [75–77], angiogenesis [70,78–81], dynamics of vascular cells [82–85], cell scattering [86], cell migration on and within matrix environments [56,57,87]. Notably, in [88] the authors introduced a compartmentalized approach to subdivide a Myxococcus Xanthus into strings of subcellular domains with different rigidity, this in order to give the bacterium a particular geometry and to control its overall length. Further, in [89] a keratocyte has been represented with a set of undifferentiated hexagonal subunits, which has allowed to reproduce its polarization during motion. In this respect, it is useful to underline that, as commented in [25], although these approaches are correct, the fact that the proposed subcellular compartments do not have an immediate or direct correspondence with real subcellular elements, has limited the practicality and the usefulness of the relative models. The most accurate way of realistically reproducing different and extremely complex cell morphologies is to compartmentalize them according to the compartmentalization "suggested in nature", and thus to explicitly represent for instance the plasmamembrane (PM), the cytosolic region, the nucleus, and other intracellular organelles (e.g., mitochondria, ribosomes, Golgi apparatus, and secretory granules). This way is in fact possible, for example, to localize within the proper cell compartment selected biochemical pathways and/or to study the role play by the nucleus in cell movement, given its higher rigidity with respect to the surrounding cytoplasm [56,57,87].

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Key benefits of the CPM energetic formalism are its simplicity and extensibility: almost any biological mechanism can in fact be included in the model, simply by adding an appropriate generalized potential term in the

Hamiltonian functional. For instance, it is possible to easily comprehend the importance of each mechanism involved in the simulated phenomenon by only altering the relative Potts parameter, so that the other terms in the Hamiltonian scale accordingly. In particular, by equating all the other terms to zero, it is possible to understand whether a mechanism is individually capable of producing the phenomenon of interest or whether it requires cooperative processes. Further critical features of the CPM (compared to alternative cell-based modelling approaches that represent biological individuals as point particles, such as Interacting Particle Systems or purely discrete models, or fixed-sized spheres or ellipsoids, such as Cellular Automata) is that i) it differentiates between bound and unbound regions of cell membranes and ii) morphological changes can be easily and realistically reproduced. These characteristics have been fundamental in our choice of using a CPM to describe the phenomenon of our interest since they are particularly suitable to implement our two main model assumptions, drawn according to the experimental observations reported in the literature: i) the adhesiveness of cells changes according to the substrate stiffness, that models the fact that higher traction forces and more stable focal points are generated over a stiffer substrate [16,35–38] and ii) each cell adapts its morphology as a function of the substrate stiffness so that over a soft region it maintains a rounded shape, whereas over a stiffer domain a significant spreading occurs [39-43]. The considerations above are in remarkable agreement with the scholarly dissertation proposed by Voss-Böhme in the conclusive section of her article [33]. She in fact argued that the application of CPMs is reasonable when the biological problem of interest involves "considerable variability in cell sizes and shapes", which is the case of the cell morphological transitions due to contact with soft/stiff substrates.

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On the opposite, when "essentially isotropic, non-polarized cells of uniform size are considered", it would be preferable the use of more coarse-grained modelling approaches, like the already cited Cellular Automata or Interacting Particle Systems, which are better analysed both mechanistically and analytically.

Further, we have opted for a 3D setting since the adhesive interactions between cells and matrix substrates occur *under* the cell body (i.e., they are localized over the contact area between the cells themselves and the underneath substrate). In bidimensional CPMs cell-matrix interactions instead occur only "laterally", as the cells do not move *on* substrates but *within* the same plane as the matrix. Indeed, a three-dimensional domain is more appropriate to reproduce an adhesive-driven cell migration.

We have then used our CPM-based approach to test cell behaviour in different domain configurations, where soft and stiff substrates coexisted. In particular, the numerical outcomes have been consistently compared to specific experimental data, in terms of cell morphology, distance covered, spreading/adhesive area and migration speed. In this respect, following the dichotomy proposed in the already cited work by Voss-Böhme [33], we have interpreted our CPM as a phenomenological method. In particular, the resulting remarkable agreement (not only qualitative but also quantitative) between in vitro and in silico data has allowed us to conclude that our approach, although strongly simplified, was able to capture the main mechanisms underlying cell migration in presence of durotaxis. We have finally turned to use our model in a predictive manner, with the aim to analyse how the external potential and the critical dimensions of a substrate stiffness gradient (here represented by the width of the different types of matrix stripes) affect cell movement. In this respect, we have found that cells are

able to achieve a sustained cell migration in the absence of an external bias (and in the absence of intracellular polarization mechanisms) where the underneath matrix is characterized by a sufficient fine-grained gradient of rigidity.

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However, our approach is not free of some serious shortcomings. First, it does not reproduce the active and continuous reorganization of the cytoskeleton, which provides the support for cells and mediates their coordinated and directed movements, mainly in response to mechanical tensions and stresses exchanged with the underneath substrate. In this respect, selected geometrical and mechanical properties of the cells, such their elongation and elasticity, should evolve according to a model of actin filament dynamics, which are powered, for example, by ATP (adenosine triphosphate) hydrolysis and controlled by inside-out signalling mechanisms transmitted from and by the extracellular matrix via focal adhesion points. Further, in our model, the substrates are not deformable and therefore it has not been possible to account how the matrix reacts to the probing processes exerted by crawling cells. Finally, it is useful to underline that our specific CPM application does not suffer of the limitation that Voss-Böhme proved to characterize most CPMs (see again [33]), i.e., cells die out in the longrun due to modifications in the original Metropolis algorithm. We have in fact focused on relatively short observation times: our model has indeed worked in a well-behaved parameter regime where the temporal evolution of the simulated system has been still directed towards the minimization of the Hamiltonian functional and the non-controlled, voter-like part of the lattice updates has been negligible.

### **Appendix**

### A.1 Morphological and migratory determinants

The *position* of a cell was established by the coordinate of its center of mass (CM). In particular, a cell was assumed to be located on a given type of substrate if its center of mass was located on that matrix region. In this respect, the migratory *trajectory* of a cell was generated by tracking the position of its center of mass at each time step (i.e., at each MCS).

The *adhesive area* of a cell was defined as the extension of its surface in contact with the substrate of interest at the final observation time.

The *average velocity* of an individual on a given type of substrate was measured as the ratio between the width of the substrate region itself (which is clarified for each simulation setting) and the time needed by the cell to cross it. In this respect, to obtain the amount of time spent by a cell to pass a given matrix region it is sufficient to multiply the corresponding average velocity for the width of the substrate of interest.

### A.2 Statistics

In the plots, we represented cell trajectories coming from 10 independent and randomly chosen simulations. A number of 10 was chosen since we observed that it was sufficient to have a correct interpretation of the simulation outcomes but it was also low enough to have an acceptable graphical quality, as too many cell paths overlapped one to each other, thereby resulting undistinguishable.

Cell average velocity and adhesive area were instead given in the corresponding graphs as mean  $\pm$  sd over 100 independent simulations.

In the plots representing the cell final distribution on the different types of substrate, the relative frequency was given by the number of individuals that, over 100 independent simulations, were located over each matrix region at the end of the observation time. Indeed, the sum of the relative frequencies is, in all cases, equal to 100.

Finally, dashed and plain ellipsoids representing, respectively, initial and final cell morphologies in a given simulation setting were established by interpolating the cell adhesive areas coming from 10 independent simulations (typically the ones used to track the cell trajectories for the same simulation setting). Obviously, the initial cell position was the constant for each simulation setting, whereas the initial cell shape was the same for all cases (i.e., an hemisphere of 20  $\mu$ m of radius).

#### A.3 Parameter estimates

Given the energetic nature of the CPM, a direct one-to-one correspondence between model parameters and experimental quantities is not straightforward (as commented also in [27] and in [90]). In particular, as explained in details in [33], the CPM parameters can be subdivided in i) directly interpretable and measurable quantities, such as cell geometrical dimensions ii) effective parameters that subsume various cellular and subcellular properties, such as the adhesive strength and the elastic moduli determining cell geometrical attributes iii) "merely technical coefficients", such as the Boltzmann temperature, that has been interpreted in different ways by CPM authors (in this work, we opted to link the value of  $T_C$  to an intrinsic cell motility, i.e., the amplitude of cell boundary fluctuations: consistently, we therefore added the subscript "C" to the coefficient

 $T_c$ ). However, a plausible parameter setting was inferred by a proper comparison with experimental findings, taking also advantage of selected sensitivity analysis performed in other CPM-based works. First, the initial/target dimensions of our virtual cells were consistent with the measures of NIH 3T3 mouse fibroblasts used by Lo and colleagues [8] for their assays on durotaxis. Since, as previously seen, we did not include in our model any nutrients and therefore cells were not allowed to grow during migration, we set a high  $\kappa_{\rm C} = 25 \cdot 10^{-9} \ {\rm Kg/(s^2m^4)}$  to keep cell volume fluctuations within a few per cent. Such a specific value was taken from other CPMs dealing both with single cell dynamics [82] and with multicellular phenomena [91], where it was estimated after some trials. Further, observing from the data by Lo et al. [46] that 3T3 cells seeded on soft enough substrates did not significantly spread or undergo morphological transitions, we set a high value  $\nu_C = 25 \cdot 10^{-3} \text{ Kg/(s}^2 \text{m}^2)$  also for the intrinsic cell rigidity which, as previously seen, can decreases (in our work) only upon cell contact with stiffer substrates. This choice is consistent with other CPM-based approaches [57,70,82,91] that employed similar values (i.e.,  $\geq$  15) to model an initially low cell deformability.

We then turned to estimate both the Boltzmann temperature  $T_C$  and the cell-substrate adhesiveness, denoted as  $J_{soft}$  thoughout the paper, in the case of the softest matrix regions considered in this paper (i.e., the ones pseudo-coloured in red in the simulations, typically identified by  $\tau = S_1$ ). In particular, we looked for the couple of coefficients  $(T_C, J_{soft})$  that simultaneously best fitted the *in vitro* results by Lo and co-workers in the corresponding experimental setting (i.e., collagen-coated polyacrylamide substrate properly manipulated to obtain a low Young's modulus of 14 kPa) in terms of cell adhesive area (which was called by Lo and colleagues "projected area" [46]). As it is possible to observe in Fig. 10,

there is a quite large range of values that matched experimental and computational data (i.e., the yellow area of the graph): however, we opted for the intermediate couple of coefficients  $T_C = 50 \cdot 10^{-27} \text{ Kgm}^2/\text{s}^2$  and  $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ . Decrements in cell-substrate adhesive strength and in cell rigidity, allowed in our model as a consequence of cell contact with stiffer matrix regions, were then performed until selected threshold values, i.e.,  $v_t = 10^{-2}~{\rm Kg/s^2m^2}$  and  $J_{stiff} = 1$  $10^{-15}~{
m Kg/s^2}$ , respectively. In particular,  $v_t$  was the lowest value of cell rigidity that permitted to avoid unrealistic (often disconnected) cell shapes.  $J_{stiff}$ , i. e., the adhesive force between cells and the stiffest substrates (the ones pseudo-coloured in yellow in the simulation snapshots, typically labelled by  $\tau = S_2$ , except from the case of the simulations dealing with the stiffness gradient) was instead the lowest value for which cells did not start to slow down during migration. In fact, as studied in details in [87], a too high cell-substrate adhesiveness partially inhibits cell movement, as CPM cells are not able to detach from the matrix component if the corresponding J-parameter is too low. Finally, the cell-medium contact strength was set equal to  $J_{soft}$  (i.e., =  $25 \cdot 10^{-15}$  Kg/s<sup>2</sup>). The rationale of this choice relied in the fact that for lower values of  $J_{C,M}$  cells detached from the substrate and fluctuate in the middle of the medium, which was obviously an unrealistic situation. On the opposite, too high values of  $J_{C,M}$  (i.e.,  $> 30 \cdot 10^{-15}$ Kg/s<sup>2</sup>) forced cells to completely lay down on the matrix, in order to minimize their contact surface with the medium, but also this situation was not plausible. Finally, the correspondence between 1 MCS and 2 seconds of actual time was taken from another CPM reproducing three-dimensional cell migration in matrix environments [87]. Further, we observed that this setting resulted in a remarkable accordance, in terms of cell velocity, between computational and experimental

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737		results: our CPM cells in fact move at speeds in a range of (3, 5) $\mu m/s$ , which is
738		consistent with the values measured by Vincent and colleagues [51] in the case of
739		MSCs plated on polyacrylamide (PA) hydrogels with selected stiffness.
740		Acknowledgements
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1097	Figures, Movies and Tables		
1098	Fig. 1 Cell behaviour is determined by a modified Metropolis algorithm, which	is based on a	
1099	iterative and stochastic minimization of the cell-matrix system energy, defined by		
1100	functional H. In particular, it includes energetic contributions for cell geometrical		
1101	cell-substrate adhesive affinity. A Boltzmann-like law finally controls the likeli	hood of the	

acceptance of domain configuration updates, which is further biased by the intrinsic cell motility, established by parameter  $T_C$ .

Fig. 2 Snapshots of the tested substrate configurations: (a) soft (red:  $t_{s_i}$  with  $J_{C,S_1}=25\cdot 10^{-15}$  Kg/s²) and stiff (yellow:  $t_{s_i}$  with  $J_{C,S_2}=1\cdot 10^{-15}$  Kg/s²) substrates, (b) soft (red:  $t_{s_i}$  with  $J_{C,S_1}=25\cdot 10^{-15}$  Kg/s²) substrate with two stiff (yellow:  $t_{s_i}$  with  $J_{C,S_2}=1\cdot 10^{-15}$  Kg/s²) stripes, (c) sequence of stripes with different stiffness (red:  $t_{s_i}$  with Kg/s  $J_{C,S_1}=25\cdot 10^{-15}$  Kg/s²) stripes, with  $J_{C,S_2}=20\cdot 10^{-15}$  Kg/s², orange:  $t_{s_i}$  with  $J_{C,S_3}=15\cdot 10^{-15}$  Kg/s², light orange:  $t_{s_i}$  with  $J_{C,S_4}=10\cdot 10^{-15}$  Kg/s², dark yellow:  $t_{s_i}$  with  $J_{C,S_5}=5\cdot 10^{-15}$  Kg/s², yellow:  $t_{s_i}$  with  $J_{C,S_6}=1\cdot 10^{-15}$  Kg/s²), (d) stiff (yellow:  $t_{s_i}$  with  $J_{C,S_2}=1\cdot 10^{-15}$  Kg/s²) substrate with embedded soft (red:  $t_{s_i}$  with  $J_{C,S_1}=2510^{-15}$  Kg/s²) squares.

Fig. 3 Simulation for a substrate with soft (red) and stiff (yellow) regions. As the ratio  $\frac{J_{C,S,1}}{J_{C,S,2}}$ , increases, the cells are typically biased to migrate towards the stiff region (c). This is also confirmed by the trajectories of the cell centre of mass, which are relatively close to the centre of the substrate when  $\frac{J_{C,S,1}}{J_{C,S,2}} = 1$  (a), whereas they are substantially shifted on the stiff region when  $\frac{J_{C,S,1}}{J_{C,S,2}} = 25$  (b).

Fig. 4 Two cells are initially seeded on a soft (red) and a stiff (yellow) substrate, respectively. (a) Simulation snapshot of the final positions (i.e., at MCS = 500 corresponding to nearly 16 minutes) of the two cells. (b) Initial (dashed) and final (plain) contour shapes give an idea of the position and the morphology of the two cells. (c) Cell adhesive area as a function of the type of substrate. The area is about 30% higher in the case of the cell seeded over the stiff substrate, due to the

specific constitutive law given to cell rigidity (i.e., Eq. (6)).

Fig. 5 Simulation for a substrate with soft (red) and stiff (yellow) subdomains. The trajectories of the cell centre of mass as well as the initial (dashed) and the final (plain) cell contours are traced

1128	respectively for (a) a cell initially seeded at the south-east corner and an external potential
1129	introduced towards the north-west corner and (b) a cell initially seeded at the south-west corner
1130	and an external potential directed towards the north-east corner. (c) Cell average velocity over
1131	either the stiff and soft substrate.
1132	
1133	Fig. 6 Configuration with a soft (red) substrate with two embedded stiff stripes (yellow). (a) and
1134	(c) Simulations with $ \boldsymbol{v}_{ext}  = 7 \cdot 10^{-21} \text{ Kg·m/s}^2 \text{ and }  \boldsymbol{v}_{ext}  = 28 \cdot 10^{-21} \text{ Kg·m/s}^2 \text{ respectively.}$
1135	Representative cell trajectories are plotted together with the initial (dashed) and the final (plain)
1136	cell contours. (b) Relative cell frequency as function of $ v_{ext} $ . (d) Cell average velocity over the
1137	different substrate regions in the case of $ \boldsymbol{v}_{ext}  = 28 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ .
1138	
1139	Fig. 7 Results for the simulation with a soft to stiff gradient (Sec. 3.4). (a) Relative cell frequency
1140	as $ v_{ext} $ increases. (b) Average cell velocity over the different substrate regions in case of $ v_{ext} $ =
1141	$28 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ .
1142	
1143	Fig. 8 Results for the simulations with a soft to stiff gradient (Sec. 3.5). (a) $ v_{ext} $ necessary to
1144	allow cells reach the opposite border of the domain vs width of substrate stripes. (b) Average cell
1145	velocity over the different substrate regions for different widths of the matrix stripes in case of a
1146	stiffness gradient sufficient fine-grained to have a cell persistent movement even in the absence of
1147	an external potential.
1148	
1149	Fig. 9 Snapshots from a representative simulation dealing with a domain with four soft squares (red) embedded
1150	in a stiff substrate (yellow). The cell is initially seeded at the south-west corner and migrates in the direction of
1151	an external potential ( $ v_{ext}  = 14 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ ), i.e., towards the north-east corner. Snapshots are taken at 2
1152	min (a), 30 min (b), 1.5 h (c), 2 h (d), 2.5 h (e), 3.5 h (f), 4.5 h (g) and 5.5 h (g).
1153	
1154	Fig. 10 Cell adhesive area at 5.5 h, obtained from CPM simulations for different values both of the Boltzmann
1155	temperature $T_C$ and of the adhesiveness between the cell and the softest substrate, i.e., $J_{soft}$ . Values are given as
1156	the mean over 100 simulations. The experimental value measured by Lo and co-workers in corresponding

1157 conditions is  $1.74 \cdot 10^3 \mu m^2$ . From this plot, it was indeed possible to observe that the parameter region pseudo-1158 colored in yellow gave the best fitting couples of coefficients. In particular, we opted for  $T_C = 50$ .  $10^{-27} \text{ Kgm}^2/\text{s}^2$  and  $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ . 1159 1160 1161 Movie 1 Simulation of cell migration over a stiff-soft substrate (yellow = stiff region, red = soft 1162 region) in presence of an external potential directed towards the north-west corner (Sec. 3.2). The 1163 cell is initially seeded at the south-east corner. 1164 1165 Movie 2. Simulation of cell migration over a stiff-soft substrate (yellow = stiff region, red = soft 1166 region) in presence of an external potential directed towards the north-east corner (Sec. 3.2). The 1167 cell is initially seeded at the south-west corner. 1168 1169 Movie 3. Simulation of cell migration over a soft substrate (red) including two parallel stiff stripes 1170 (yellow) in presence of an external potential ( $|v_{ext}| = 7.10^{-21} \text{ Kg·m/s}^2$ ) directed towards the north-1171 east corner (Sec. 3.3). The cell is initially seeded at the south-west corner. 1172 1173 Movie 4. Simulation of cell migration over a soft substrate (red) including two parallel stiff stripes (yellow) in presence of an external potential ( $|v_{ext}| = 28 \cdot 10^{-21} \text{ Kg·m/s}^2$ ) directed towards the 1174 1175 north-east corner (Sec. 3.3). The cell is initially seeded at the south-west corner. 1176 1177 Movie 5. Simulation of cell migration over a substrate with a soft-to-stiff gradient from the left to 1178 the right part of the domain (the cell-substrate adhesive affinities vary from  $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ to  $J_{stiff} = 1.10^{-15} \text{ Kg/s}^2$ ) (Sec. 3.4). A low external potential ( $|\boldsymbol{v}_{ext}| = 7.10^{-21} \text{ Kg} \cdot \text{m/s}^2$ ) is directed 1179 1180 towards the north-east corner of the substrate, whereas the cell is seeded at the south-west corner. 1181 1182 Movie 6. Simulation of cell migration over a substrate with a soft-to-stiff gradient from the left to 1183 the right part of the domain (the cell-substrate adhesive affinities vary from  $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ 

to  $J_{stiff}=1\cdot10^{-15}~{\rm Kg/s^2})$  (Sec. 3.4). A high external potential ( $|\boldsymbol{v}_{ext}|=28\cdot10^{-21}~{\rm Kg\cdot m/s^2})$  is

1185	directed towards the north-east corner of the substrate, whereas the cell is seeded at the south-west
1186	corner.
1187	
1188	Movie 7. Simulation of cell migration over a substrate with a soft-to-stiff gradient from the left to the right part
1189	of the domain (the cell-substrate adhesive affinities vary from $J_{soft} = 25 \cdot 10^{-15} \text{ Kg/s}^2$ to $J_{stiff} = 1 \cdot 10^{-15} \text{ Kg/s}^2$ ).
1190	Here, the width of the stripes has been highly reduced (i.e., $=28 \ \mu m$ ) and no external potential is introduced
1191	(Sec. 3.5).
1192	
1193	Movie 8. Simulation of cell migration over a stiff substrate (yellow) with four embedded soft
1194	squares (red) (Sec. 3.6). The cell is initially seeded at the south-west corner and an external
1195	potential ( $ v_{ext}  = 14 \cdot 10^{-21} \text{ Kg} \cdot \text{m/s}^2$ ) is directed towards the north-east corner of the domain.
1196	
1197	Table 1 Main parameters of the model.