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FAST DISCRIMINATIVE SPEAKER VERIFICATION IN THE I-VECTOR SPACE / Cumani, Sandro; Brummer, N.; Burget, L.; Laface, Pietro. - STAMPA. - (2011), pp. 4852-4855. (Intervento presentato al convegno 2011 IEEE International Conference on Acoustics, Speech, and Signal Processing ICASSP 2011 tenutosi a Prague (Czech Republic) nel May 22-27, 2011).

*Availability:*

This version is available at: 11583/2428783 since: 2017-11-21T14:14:35Z

*Publisher:*

IEEE

*Published*

DOI:

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# FAST DISCRIMINATIVE SPEAKER VERIFICATION IN THE I-VECTOR SPACE

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## ABSTRACT

This work presents a new approach to discriminative speaker verification. Rather than estimating speaker models, or a model that discriminates between a speaker class and the class of all the other speakers, we directly solve the problem of classifying pairs of utterances as belonging to the same speaker or not.

The paper illustrates the development of a suitable Support Vector Machine kernel from a state-of-the-art generative formulation, and proposes an efficient approach to train discriminative models based on Support Vector Machines.

The results of the experiments performed on the tel-tel extended core condition of NIST 2010 Speaker Recognition Evaluation are competitive or better, in terms of Decision Cost Function and Equal Error Rate, compared to the much more expensive generative models.

**Index Terms**— Discriminative Training, Two-covariance Kernel, Support Vector Machines, i-vectors

## 1. INTRODUCTION

Recent trends in speaker recognition have seen the development of fully Bayesian generative models. This has been made possible by advances in the representation of speech segments by means of low dimensional feature vectors referred to as i-vectors [1]. These techniques aim at modeling the i-vectors by decomposing them into a speaker and a channel component whose underlying distributions are then estimated through expectation-maximization. The most effective current flavors of these approaches are the Gaussian or Heavy-Tailed Probabilistic Linear Discriminant Analysis (HT PLDA) [2] and the Two-covariance model, a linear-Gaussian generative model introduced in [3]. The advantage of a Bayesian approach in speaker recognition is that, in principle, it produces likelihood ratios that do not need to be normalized [4]. In [2] this has been confirmed in the case of telephone speech, for heavy-tailed distributions, whereas normalization was needed for Gaussian distributions. A complete symmetry of the train and test segments is another interesting characteristic in these approaches.

In this work we illustrate a fast discriminative training procedure for a linear-Gaussian model. In this new approach, we do not model anymore speaker classes, but we build a binary classifier which simply classifies pair of utterances as either target (same speaker) or non-target (different speaker). Training is performed by means of Support Vector Machines (SVMs), using a suitable kernel derived from the two-covariance generative model. The advantage of this approach is that training is computationally inexpensive compared with the PLDA approach and test is extremely fast because scoring simply consists in matrix-vector multiplications.

The paper is organized as follows: Section 2 describes the SVM classifiers focusing on the properties that the training algorithm should have in order to make our task feasible. Section 3 briefly recalls the Two-covariance and the PLDA generative models. The steps necessary to derive a discriminative solution for the former model by means of an appropriate expansion of i-vector pairs are given in Section 4 together with the procedure to efficiently train the SVM. The experimental results comparing the performance of the discriminative and generative models are given in Section 5 and conclusion are drawn in Section 6.

## 2. SVM

A Support Vector Machine is a two-class classifier which looks for the hyperplane that best discriminates two given classes of patterns according to a maximum separation margin criterion.

The separation hyperplane is obtained by solving an unconstrained *regularized risk minimization* problem

$$\min_{\mathbf{w}} \frac{1}{2} \|\mathbf{w}\|^2 + C \cdot \sum_{i=1}^n \max(0, 1 - \zeta_i \mathbf{w}^T \mathbf{x}_i) \quad (1)$$

where vector  $\mathbf{w}$  is the vector representing the hyperplane and the second term is the (L1)-loss function

$$l_{L1}(\mathbf{w}, \mathbf{x}, \zeta) = \max(0, 1 - \zeta \mathbf{w}^T \mathbf{x}) \quad (2)$$

evaluated on training patterns  $\mathbf{x}_i \in \mathbb{R}^d$  with associated class label  $\zeta_i \in \{-1, +1\}$ .

Non-linear classification can be obtained by expanding the feature patterns into a high dimensionality space where linear classification is carried out. The kernel trick allows solving the SVM problem without explicitly constructing the expanded features, provided that the dot-products in the expanded space can be evaluated.

Many algorithms exist that solve problem 1, providing both primal and dual solutions [5]. The nature of the classification problem we address in this paper does not allow for an explicit construction of the kernel matrix, which would have a size  $O(n^4)$ ,  $n$  being the number of i-vectors in the training set. However, we will show that, by using an appropriate feature expansion, the loss function and its gradient with respect to the hyperplane parameters in the (expanded) space of the i-vectors pairs can be evaluated without explicitly expanding the i-vector pairs. Deriving a formulation for the dot-product in the expanded space we can efficiently train our models by using a primal SVM solver such as the one proposed in [6].

### 3. GENERATIVE MODELS

I-vectors are a recently proposed compact representation of speaker segments which boosted the study of fully Bayesian generative models [1, 3]. The procedure for extracting i-vectors has been described and effectively used in [7, 8].

#### 3.1. Two-covariance model

We need to briefly recall in this subsection the two-covariance modeling of [3] because we derive our expression for the SVM dot-product from its formulation. The i-vectors are assumed to be features produced by a linear-Gaussian generative model  $\mathcal{M}$ . In particular, an i-vector  $\phi$  can be decomposed into a speaker  $y$  and a Gaussian distributed channel component  $z$ :

$$\phi = y + z \quad (3)$$

$$P(\phi|y, \mathcal{M}) = \mathcal{N}(\phi|y, W^{-1}) \quad (4)$$

where  $W^{-1}$  is the within-speaker covariance matrix. If we assume the prior for  $y$  is Gaussian distributed

$$P(y|\mathcal{M}) = \mathcal{N}(y|\mu, B^{-1}) \quad (5)$$

then also the posterior given a set  $S$  of  $n$  i-vectors associated to speaker identity  $y$  is normal, being

$$P(y|S, \mathcal{M}) = \mathcal{N}(y|L^{-1}\gamma, L^{-1}) \quad (6)$$

$$\gamma = B\mu + W \sum_{\phi \in S} \phi \quad L = B + nW \quad (7)$$

Since our problem is to decide if two spoken segments belong to the same or to a different speaker, we have three sets,  $S_1$ ,  $S_2$  if the two i-vectors are in different sets, otherwise both belong to set  $S_{1,2}$ .

The resulting formulation for the speaker detection log-likelihood has been given in [3]

$$\begin{aligned} \log l = & \frac{1}{2}(\log |B| - \mu^T B \mu + \log |\tilde{\Lambda}| + \gamma_{1,2}^T \tilde{\Lambda} \gamma_{1,2}) \\ & - \frac{1}{2}(2 \log |B| - 2\mu^T B \mu + 2 \log |\tilde{\Gamma}| + \gamma_1^T \tilde{\Gamma} \gamma_1 \\ & + \gamma_2^T \tilde{\Gamma} \gamma_2) \end{aligned} \quad (8)$$

where

$$\begin{aligned} \tilde{\Lambda} &= (B + 2W)^{-1} & \tilde{\Gamma} &= (B + W)^{-1} \\ \gamma_{1,2} &= B\mu + W(\phi_1 + \phi_2) & \gamma_i &= B\mu + W\phi_i \end{aligned}$$

#### 3.2. PLDA model

The two covariance model can be seen as a particular case of the more general framework of Probabilistic Linear Discriminant Analysis [4, 2], where an i-vector is represented as

$$\phi = U_1 y + U_2 x + z \quad (9)$$

where  $x$  represents ‘‘channel factors’’ and  $z$  is the residual error. The matrices  $U_1$  and  $U_2$  are used to constrain the speaker and channel spaces to be of lower dimension than the i-vector space.

### 4. DISCRIMINATIVE MODEL

We are not interested in exactly evaluating (8) to perform discriminative training, we derive instead a formally equivalent expression which can be transformed into a valid dot-product. By dropping the  $\frac{1}{2}$  factor and collecting in a constant  $k$  all the i-vector independent terms in the sum, (8) can be rewritten as:

$$\log l = k + \gamma_{1,2}^T \tilde{\Lambda} \gamma_{1,2} - \gamma_1^T \tilde{\Gamma} \gamma_1 - \gamma_2^T \tilde{\Gamma} \gamma_2 \quad (10)$$

Replacing (7) in (10) we obtain

$$\begin{aligned} \log l = & (B\mu + W(\phi_1 + \phi_2))^T \tilde{\Lambda} (B\mu + W(\phi_1 + \phi_2)) \\ & - (B\mu + W\phi_1)^T \tilde{\Gamma} (B\mu + W\phi_1) \\ & - (B\mu + W\phi_2)^T \tilde{\Gamma} (B\mu + W\phi_2) + \tilde{k} \end{aligned} \quad (11)$$

which we rewrite as

$$\begin{aligned} \log l = & \phi_1^T \Lambda \phi_2 + \phi_2^T \Lambda \phi_1 + \phi_1^T \Gamma \phi_1 + \phi_2^T \Gamma \phi_2 \\ & + (\phi_1 + \phi_2)^T c + k \end{aligned} \quad (12)$$

with

$$\begin{aligned} \Lambda &= W^T \tilde{\Lambda} W & \Gamma &= W^T (\tilde{\Lambda} - \tilde{\Gamma}) W \\ c &= 2W^T (\tilde{\Lambda} - \tilde{\Gamma}) B\mu & k &= \tilde{k} + (B\mu)^T (\tilde{\Lambda} - 2\tilde{\Gamma}) B\mu \end{aligned} \quad (13)$$

To demonstrate that (12) is a dot-product in some i-vector pairs expanded space, we recall that the computation of a quadratic form  $x^T A y$  can be expressed in terms of the Frobenius inner product as  $x^T A y = \langle A, x y^T \rangle =$

$\text{vec}(A)^T \text{vec}(xy^T)$ , where the operator  $\text{vec}(A)$  is the operator that stacks the columns of  $A$  into a column vector. Hence, the expression for the speaker detection log-likelihood can be rewritten as

$$\log l = \langle \Lambda, \phi_1 \phi_2^T + \phi_2 \phi_1^T \rangle + \langle \Gamma, \phi_1 \phi_1^T + \phi_2 \phi_2^T \rangle + c^T (\phi_1 + \phi_2) + k \quad (14)$$

Thus, if we stack the parameters as

$$w = \begin{bmatrix} \text{vec}(\Lambda) \\ \text{vec}(\Gamma) \\ c \\ k \end{bmatrix} = \begin{bmatrix} w_\Lambda \\ w_\Gamma \\ w_c \\ w_k \end{bmatrix} \quad (15)$$

and we expand the i-vectors pairs as

$$\varphi(\phi_1, \phi_2) = \begin{bmatrix} \text{vec}(\phi_1 \phi_2^T + \phi_2 \phi_1^T) \\ \text{vec}(\phi_1 \phi_1^T + \phi_2 \phi_2^T) \\ \phi_1 + \phi_2 \\ 1 \end{bmatrix} = \begin{bmatrix} \varphi_\Lambda(\phi_1, \phi_2) \\ \varphi_\Gamma(\phi_1, \phi_2) \\ \varphi_c(\phi_1, \phi_2) \\ \varphi_k(\phi_1, \phi_2) \end{bmatrix} \quad (16)$$

the scoring given by (12) can be expressed as a dot-product as

$$\begin{aligned} S(\phi_1, \phi_2) &= \log l \\ &= S_\Lambda(\phi_1, \phi_2) + S_\Gamma(\phi_1, \phi_2) \\ &\quad + S_c(\phi_1, \phi_2) + S_k(\phi_1, \phi_2) \\ &= w_\Lambda^T \varphi_\Lambda(\phi_1, \phi_2) + w_\Gamma^T \varphi_\Gamma(\phi_1, \phi_2) \\ &\quad + w_c^T \varphi_c(\phi_1, \phi_2) + w_k^T \varphi_k(\phi_1, \phi_2) \\ &= w^T \varphi(\phi_1, \phi_2) \end{aligned} \quad (17)$$

The terms  $S_\Lambda, S_\Gamma, S_c, S_k$  represent the contributions of the different terms of  $w$  to the final score.

#### 4.1. Fast scoring

Since the number of i-vectors pairs is of the order of hundred of millions in our experiments, the evaluation of a kernel matrix (the kernel being the one induced by the dot-product in (17)) would be clearly unfeasible. However, if we use a primal SVM solver, we need only to evaluate the SVM loss function and its gradient with respect to the hyperplane. Both evaluation requires, in principle, a sum over all the i-vectors pair, but in the next two subsections we show that given the dot-product in (17) the loss function and the gradient evaluations can be done without an explicit expansion of all the i-vectors pairs.

#### 4.2. Loss function evaluation

Let us denote  $D$  the matrix of all stacked i-vectors  $\phi_i$

$$D = [\phi_1 \phi_2 \dots \phi_n]$$

$\Theta \in \{\Lambda, \Gamma, c, k\}$  a component of the hyperplane, and let  $S_\Theta$ , the score matrix of training patterns due to component  $\Theta$ , be

defined as:  $S_{\Theta_{i,j}} = S_\Theta(\phi_i, \phi_j)$ . From (17) and (12) the score matrices can be evaluated as

$$S_\Lambda(\phi_1, \phi_2) = \phi_1^T \Lambda \phi_2 + \phi_2^T \Lambda \phi_1 \Rightarrow S_\Lambda = 2D^T \Lambda D \quad (18)$$

$$S_\Gamma(\phi_1, \phi_2) = \phi_1^T \Gamma \phi_1 + \phi_2^T \Gamma \phi_2 \Rightarrow S_\Gamma = \tilde{S}_\Gamma + \tilde{S}_\Gamma^T \quad (19)$$

$$S_c(\phi_1, \phi_2) = c^T (\phi_1 + \phi_2) \Rightarrow S_c = \tilde{S}_c + \tilde{S}_c^T \quad (20)$$

$$S_k(\phi_1, \phi_2) k \Rightarrow S_k = k \cdot \mathbf{1} \quad (21)$$

where

$$\begin{aligned} \tilde{S}_\Gamma &= \underbrace{[d_\Gamma \dots d_\Gamma]}_n, & d_\Gamma &= \mathbf{diag}(D^T \Gamma D), \\ \tilde{S}_c &= \underbrace{[d_c \dots d_c]}_n, & d_c &= D^T c \end{aligned}$$

**diag** is the operator that returns the diagonal of a matrix as a column vector,  $\mathbf{1}$  is an  $n \times n$  matrix of ones.

Denoting by  $S$  the sum of these partial score matrices, the SVM loss function can be summarized as:

$$\begin{aligned} L(D, Z) &= C \sum_{i,j} \max(0, 1 - \zeta_{i,j} w^T \varphi(\phi_i, \phi_j)) \\ &= C \langle \mathbf{1}, \max(\mathbf{0}, \mathbf{1} - (Z \circ S)) \rangle \end{aligned} \quad (22)$$

where  $\mathbf{0}$  is an  $n \times n$  matrix of all zeros,  $Z$  is the  $n \times n$  matrix of labels for trials  $(\phi_i, \phi_j)$ ,  $Z_{i,j} = \zeta_{i,j} \in \{-1, +1\}$ , and  $\circ$  is the element-wise matrix multiplication operator.

#### 4.3. Gradient Evaluation

The gradient of the loss function can be evaluated from its derivative with respect to the  $m$ -th dimension of  $w$  as

$$\begin{aligned} \frac{\partial L}{\partial w_m} &= \sum_{i,j} \frac{\partial l_{L1}(w, (\phi_i, \phi_j), \zeta_{i,j})}{\partial (w^T \varphi(\phi_j, \phi_j))} \frac{\partial w^T \varphi(\phi_j, \phi_j)}{\partial w_m} \\ &= \sum_{i,j} g_{i,j} \frac{\partial S_{i,j}}{\partial w_m} = \sum_{i,j} g_{i,j} \varphi(\phi_i, \phi_j)_m \end{aligned} \quad (23)$$

where  $g_{i,j}$  is the derivative of the loss function with respect to the dot product

$$g_{i,j} = \begin{cases} 0 & \text{if } S_{i,j} \zeta_{i,j} \geq 1 \\ -\zeta_{i,j} & \text{otherwise} \end{cases}$$

Let  $G$  be the matrix  $G_{i,j} = g_{i,j}$ , then

$$\begin{aligned} \nabla L &= \begin{bmatrix} \nabla_\Lambda L \\ \nabla_\Gamma L \\ \nabla_c L \\ \nabla_k L \end{bmatrix} = \begin{bmatrix} \text{vec} \left( \sum_{i,j} g_{i,j} (\phi_i \phi_j^T + \phi_j \phi_i^T) \right) \\ \text{vec} \left( \sum_{i,j} g_{i,j} (\phi_i \phi_i^T + \phi_j \phi_j^T) \right) \\ \sum_{i,j} g_{i,j} (\phi_i + \phi_j) \\ \sum_{i,j} g_{i,j} \end{bmatrix} \\ &= \begin{bmatrix} 2 \cdot \text{vec}(DGD^T) \\ 2 \cdot \text{vec}([D \circ (\mathbf{1}_A G)] D^T) \\ 2 [D \circ (\mathbf{1}_A G)] \mathbf{1}_B \\ \mathbf{1}_B^T G \mathbf{1}_B \end{bmatrix} \end{aligned} \quad (24)$$

where  $\mathbf{1}_A$  is a  $d \times n$  matrix of ones.

Again, no explicit expansion of i-vectors is necessary for this evaluation.

Male Set				
System	EER	oldDCF	minDCF	actDCF
G-PLDA	3.82%	0.165	0.401	0.442
G-PLDA+AT-norm	2.11%	0.106	0.309	0.374
HT-PLDA	1.55%	0.082	0.313	0.364
2C-SVM	1.50%	0.074	0.308	0.355

Female Set				
System	EER	oldDCF	minDCF	actDCF
G-PLDA	4.08%	0.179	0.448	0.531
G-PLDA+AT-norm	2.54%	0.122	0.438	0.454
HT-PLDA	2.29%	0.118	0.412	0.415
2C-SVM	2.35%	0.108	0.394	0.398

All				
System	EER	oldDCF	minDCF	actDCF
G-PLDA	4.21%	0.183	0.470	0.498
G-PLDA+AT-norm	2.39%	0.118	0.420	0.422
HT-PLDA	1.98%	0.102	0.379	0.393
2C-SVM	1.94%	0.095	0.373	0.378

**Table 1.** EER, SRE08 DCF (oldDCF), SRE10 minimum DCF (minDCF) and actual DCF (actDCF) for the extended tel-tel core condition (condition 5) of NIST SRE10

## 5. EXPERIMENTS

Three systems have been trained on the NIST SRE10 standard training lists and tested on the extended tel-tel core condition (condition 5) of SRE10 [9], a Gaussian PLDA (G-PLDA), an Heavy-Tailed PLDA (HT-PLDA) and the discriminative Two-covariance SVM system (2C-SVM). The 2C-SVM is compared with G-PLDA because PLDA is a more general framework than two-covariance model, from which the discriminative approach has been derived, and both rely on Gaussian distribution of i-vectors and noise. Moreover, we compare 2C-SVM with HT-PLDA, which assumes heavy-tailed distributions for the priors, and has shown impressive performance improvement with respect to G-PLDA [2].

Even if the expression given in (12) can be directly used to train an SVM, the lack of normalizations of the i-vector dimensions results in poor classification performances, due to the presence of the SVM regularizer term. Thus, the SVM is trained by centering the i-vectors and scaling the i-vector space to whiten the within-speaker covariance matrix. Class balancing is then performed as to optimize for a point in between the EER and the DCF (see section 5 operating points).

The results are given in terms of EER and normalized minimum and actual Decision Cost Functions as defined by NIST for SRE08 and SRE10 [9]. The scores have been calibrated on the SRE08 data [10]. Both PLDA systems has been trained with 400 speaker factors and 400 channel factors. 400 dimension i-vectors have been extracted via a 60-dimensional features full-covariance 2048 Gaussians UBM [8].

Table 1 summarizes the obtained results for the female and male speaker separately, and pooled together.

As pointed out in [2], Gaussian PLDA requires score normalization, which has been performed in our experiments by

means of Adaptive T-norm [11], whereas no normalization is required for heavy-tailed PLDA and for the 2C-SVM systems.

Discriminative training not only performs better than generative modeling under the assumption of Gaussian distributed i-vectors, but its performance is even slightly better than the Heavy-Tailed PLDA.

As far as training complexity is concerned, less than 3 hours were needed to train the male system (16969 utterances, approximately 290 millions of trials) and about the same time has been spent for the female one (21663 utterances – more than 450 million trials) on a HP DS160G5 server equipped with two Xeon X5472 3 GHz quad-core processors and 32 GB of DDR2-800 RAM. Testing *all* test segments against *all the other test segments* is done in less than 2 seconds.

## 6. CONCLUSIONS

A fast discriminative training approach for speaker verification based on i-vectors has been presented. On NIST telephone evaluation data, the resulting models perform better, without the need of normalization techniques, than the generative ones, even compared with heavy-tailed models.

## 7. ACKNOWLEDGMENTS

We would like to thank Ondřej Glembek, Pavel Matějka and Oldřich Plchot from Brno University of Technology, for providing us with the BUT i-vectors, and Fabio Castlato from Loquendo SpA for giving us the PLDA results we used as baseline.

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