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## Research Article

# The link between $s$ and $d$ components of electron boson coupling constants in one band $d$ wave Eliashberg theory for high $T_c$ superconductors

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## Abstract

The phenomenology of overdoped high  $T_c$  superconductors can be described by a one band  $d$  wave Eliashberg theory where the mechanism of superconducting coupling is mediated by antiferromagnetic spin fluctuations and whose characteristic energy  $\Omega_0$  scales with  $T_c$  according to the empirical law  $\Omega_0 = 5.8 k_B T_c$ . This model presents universal characteristics that are independent of the critical temperature such as the link between the  $s$  and  $d$  components of electron boson coupling constants and the invariance of the ratio  $2\Delta/k_B T_c$ . This situation arises from the particular structure of Eliashberg's equations which, despite being non-linear equations, present solutions with these simple properties.

## Introduction

Eliashberg's theory [1] was born as a generalization of the BCS theory to explain some anomalies in the experimental data concerning lead. Subsequently, it was seen that the theory can be successfully applied to explain the experimental data of practically almost all superconducting materials [2,3], first of all low  $T_c$  phononic superconductors [4], then magnesium diboride [5,6], graphite intercalated compound  $CaC_6$  [7], iron-based superconductors [8-12]. This theory can be applied to describe particular systems such as proximized systems [13] and field effect junctions [14-16]. For what concerns the high  $T_c$  superconductors [17-21], their properties strongly depend on their oxygen content. It is possible to identify three different regimes: under, optimal and overdoping. While the discussion is still open as regards the underdoping regime, it is almost certain that the fundamental mechanism in the optimal and over regime is due to antiferromagnetic spin fluctuations,

and especially in the over regime, the experimental data can be described satisfactorily by one band  $d$  - wave Eliashberg's theory [22,23]. Detailed studies are present in the literature on cuprates and precisely on tunneling spectra that can be reproduced by using the framework of  $d$  - wave Eliashberg's theory [24-26]. In this paper, we provide an extensive investigation of the consequences of a different symmetry of coupling in the two components of self-energy: the renormalization function  $Z(i\omega_n)$  ( $s$ -wave symmetry) and the gap function  $\Delta(i\omega_n)$  ( $d$ -wave symmetry) and if some link exists between them. We focus here on physical quantities which can be evaluated in the imaginary axis formalism. Furthermore, it has been experimentally determined that, in cuprates, a link [27] exists between magnetic resonance energy  $\Omega_0$  and critical temperature. So we will study the properties of one band  $d$ -wave Eliashberg's theory where a fundamental role will be played by the assumption that the representative energy  $\Omega_0$  of these systems is related to the critical temperature by



a universal relationship [27]  $\Omega_0 = 5.8 k_B T_c$ . This assumption represents a very strong constraint in correlating the values of the two-electron boson coupling constants  $\lambda_d$  and  $\lambda_s$ . For each value,  $\lambda_s$  we will look for the value  $\lambda_d$  which exactly reproduces the  $T_c$  superconductor and we will study which relation exists between the  $d$  and  $s$  components of the electron boson coupling constant. Finally, we will see that this model has the particular property that the relationship between the gap and the critical temperature ( $\frac{2\Delta_d}{k_B T_c}$ ) is independent of the particular value of the critical temperature.

### Model

The one-band  $d$ -wave Eliashberg equations [23,30-35] are two coupled equations: one for the gap  $\Delta(i\omega_n, \phi)$  and one for the renormalization functions  $Z(i\omega_n, \phi)$ . These equations, in the imaginary axis representation (here  $\omega_n$  denote the Matsubara frequencies), when the Migdal theorem holds [29], are:

$$\omega_n Z(\omega_n, \phi) = \omega_n + \pi T \sum_m \int_0^{2\pi} \frac{d\phi'}{2\pi} \Lambda(\omega_n, \omega_m, \phi, \phi') N_Z(\omega_m, \phi') \quad (1)$$

$$Z(\omega_n, \phi) \Delta(\omega_n, \phi) = \pi T \sum_m \int_0^{2\pi} \frac{d\phi'}{2\pi} [\Lambda(\omega_n, \omega_m, \phi, \phi') - \mu^*(\phi, \phi')] \times \Theta(\omega_c - |\omega_m|) N_\Delta(\omega_m, \phi') \quad (2)$$

where  $\Theta(\omega_c - \omega_m)$  is the Heaviside function,  $\omega_c$  is cut-off energy and

$$\Lambda(\omega_n, \omega_m, \phi, \phi') = 2 \int_0^{+\infty} \Omega d\Omega \alpha^2 F(\Omega, \phi, \phi') / [(\omega_n - \omega_m)^2 + \Omega^2] \quad (3)$$

$$N_Z(\omega_m, \phi) = \frac{\omega_m}{\sqrt{\omega_m^2 + \Delta(\omega_m, \phi)^2}} \quad (4)$$

$$N_\Delta(\omega_m, \phi) = \frac{\Delta(\omega_m, \phi)}{\sqrt{\omega_m^2 + \Delta(\omega_m, \phi)^2}} \quad (5)$$

We assume [2,23,30-35] that the electron boson spectral function  $\alpha^2(\Omega)F(\Omega, \phi, \phi')$  and the Coulomb pseudopotential  $\mu^*(\phi, \phi')$  at the lowest order contain separated  $s$  and  $d$ -wave contributions,

$$\alpha^2 F(\Omega, \phi, \phi') = \lambda_s \alpha^2 F_s(\Omega) + \lambda_d \alpha^2 F_d(\Omega) \sqrt{2} \cos(2\phi) \sqrt{2} \cos(2\phi') \quad (6)$$

$$\mu^*(\phi, \phi') = \mu_s^* + \mu_d^* \sqrt{2} \cos(2\phi) \sqrt{2} \cos(2\phi') \quad (7)$$

as well as the self-energy functions:

$$Z(\omega_n, \phi) = Z_s(\omega_n) + Z_d(\omega_n) \cos(2\phi) \quad (8)$$

$$\Delta(\omega_n, \phi) = \Delta_s(\omega_n) + \Delta_d(\omega_n) \cos(2\phi) \quad (9)$$

We put the factor  $\sqrt{2}$  inside the definition  $\Delta_d(\omega_n)$  because, experimentally, the peak of the density of the state is, usually, identified  $\Delta_d(\omega_{n=0})$  while, as we will see,  $Z_d(\omega_n)$  is always zero. The spectral functions  $\alpha^2 F_{s,d}(\Omega)$  are normalized in the way that  $2 \int_0^{+\infty} \frac{\alpha^2 F_{s,d}(\Omega)}{\Omega} d\Omega = 1$  and of course, in this model the renormalization function is pure  $s$ -wave ( $Z(\omega_n, \phi) = Z_s(\omega_n)$ ) while the gap function is pure  $d$ -wave ( $\Delta(\omega_n, \phi) = \Delta_d(\omega_n) \cos(2\phi)$ ). We consider just solutions of the Eliashberg equations in pure

$d$ -waveform because this is the indication of the experimental data. This means that the  $s$  component of the gap function is zero and this situation happens because, usually [36],  $\mu_s^* \gg \mu_d^*$ ). In the more general case, in principle, the gap function has  $d$  and  $s$  components. The renormalization function  $Z(\omega, \phi) = Z_s(\omega)$  has just the  $s$  component because the equation  $Z_d(\omega_n)$  is a homogeneous integral equation with just the solution  $Z_s(\omega_n) = 0$  [37]. For simplicity, we also assume that  $\alpha^2 F_s(\Omega) = \alpha^2 F_d(\Omega)$  the spectral functions are the difference between two Lorentzian, i.e.  $\alpha^2 F_{s,d}(\Omega) = C[L(\Omega + \Omega_0, \gamma) - L(\Omega - \Omega_0, \gamma)]$  where  $L(\Omega \pm \Omega_0, \gamma) = [(\Omega \pm \Omega_0)^2 + (\gamma)^2]^{-1}$ ,  $C$  is the normalization constant necessary to obtain  $2 \int_0^{+\infty} \frac{\alpha^2 F_{s,d}(\Omega)}{\Omega} d\Omega = 1$ ,  $\Omega_0$  and  $\gamma$  are

the peak energy and half-width, respectively. The half-width is  $=\Omega_0/2$ . This choice of the shape of the spectral function and the fact that  $\alpha^2 F_s(\Omega) = \alpha^2 F_d(\Omega)$ , is a good approximation of the true spectral function [38] connected with antiferromagnetic spin fluctuations. The same thing also happens in the case of iron pnictides [39]. In any case, even making different choices for  $\gamma$  the link between  $\lambda_d$  and  $\lambda_s$  remains the same but changes (very little) the coefficients of the linear fit. The cut-off energy is  $\omega_c = 1000$  meV and the maximum quasiparticle energy is  $\omega_{max} = 1100$  meV. In the first approximation, we put  $\mu_d^* = 0$  (if the  $s$  component of the gap is zero the value of  $\mu_s^*$  is irrelevant). Now we fix the critical temperature and for any value,  $\lambda_s$  we seek the value  $\lambda_d$  that exactly reproduces the initial fixed critical temperature. After, via Padè approximants [40], we calculate the low-temperature value ( $T = T_c/10$  K) of the gap because, in presence of a strong coupling interaction, the value  $\Delta_d(\omega_{n=0})$  obtained by solving the imaginary-axis Eliashberg equations can be very different from the value  $\Delta_d$  obtained from the real-axis Eliashberg equations [31].

### Results and discussions

We fix three different critical temperatures (70 K, 90 K and 110 K) and for any particular critical temperature, we choose different values  $\lambda_s$  and determine which value  $\lambda_d$  exactly reproduces the chosen critical temperature by numerical solution of Eliashberg equations. In Figure 1 we can see that

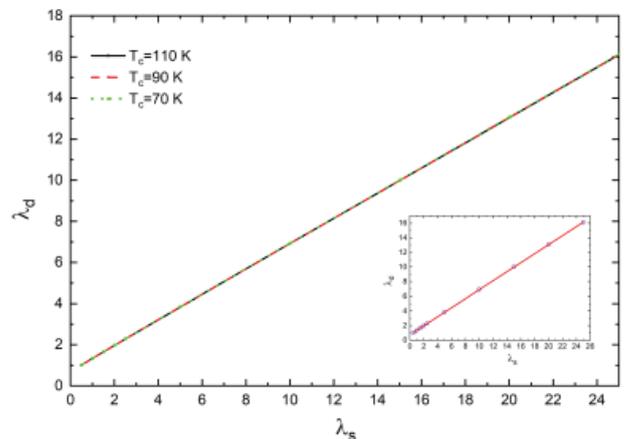


Figure 1: (Color online)  $\lambda_d$  versus  $\lambda_s$  for three different critical temperatures:  $T_c = 70$  K (green point line),  $T_c = 90$  K (red dash line) and  $T_c = 110$  K (black solid line). In the inset the linear fit (solid line) of the  $T_c = 70$  K (open dark blue circles) case is shown.

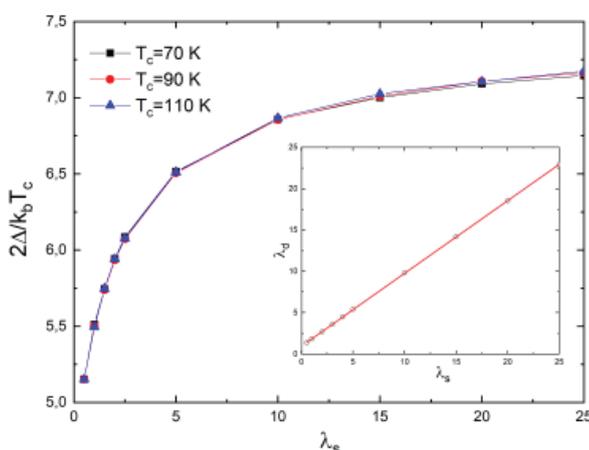
the three curves  $\lambda_d$  versus  $\lambda_s$  are coincident. The inset of Figure 1 it is shown the linear fit of these results. We obtain a linear link between  $\lambda_d$  and  $\lambda_s$

$$\lambda_d = 0.616\lambda_s + 0.732 \quad (10)$$

These results are general and do not depend on the particular shape of the electron-boson spectral function. If we change the shape of the electron-boson spectral function and we choose, for example,  $\alpha^2 F_{s,d}(\Omega) = 0.5\Omega_0 \delta(\Omega - \Omega_0)$  we find that the linear link between  $\lambda_d$  and  $\lambda_s$  changes very little and becomes  $\lambda_d = 0.575\lambda_s + 0.655$ . Even the introduction of a Coulomb potential different from zero, as we have verified, does not involve a substantial modification of our results. In principle, it is possible to obtain this result (the linear link between  $\lambda_s$  and  $\lambda_d$ ) in a more simple but less general way. In fact, a similar conclusion relative to the linear connection between  $\lambda_s$  and  $\lambda_d$  may also be derived from the analysis of the approximate MacMillan formula for  $T_c$  [41] generalized to  $d$ -wave case [42]:

$$k_B T_c = \Omega_0 \exp\left(-\frac{1 + \lambda_s}{2\lambda_d}\right) \quad (11)$$

The problem is that the MacMillan equation works just in a weak coupling regime. Now we solve, for each couple of  $\lambda_d$  and  $\lambda_s$  values, the Eliashberg equations at  $T = T_c/10$  and after, via Pade we calculate the value of superconductive gap (the energy of the density of states peak). In Figure 2 the rates  $\frac{2\Delta_d}{k_B T_c}$  are shown for three systems with different critical temperatures (70 K, 90 K and 110 K). The curves are exactly coincidental. We have also studied what happens when the ratio  $\frac{\Omega_0}{k_B T_c}$  is equal to two as in the case of the heavy fermion [43]  $UPd_2Al_3$  with  $T_c = 2$  K which could represent an extreme situation. In this case, the link remains linear and becomes  $\lambda_d = 0.880\lambda_s + 0.966$  as it is possible to see in the inset of Figure 2. Finally, in the case of extremely strong coupling ( $\frac{\Omega_0}{k_B T_c} \ll 1$ ) it is possible to



**Figure 2:** (Color online)  $|\Delta_d|/k_B T_c$  for  $T_c = 70$  K (green up filled triangles circles),  $T_c = 90$  K (red filled circles) and  $T_c = 110$  K (black filled squares) versus  $\lambda_s$ . The lines are guides for eyes. In the inset  $|\lambda_d|$  versus  $|\lambda_s|$  when  $T_c = 2$  K and  $\Omega_0 = 2k_B T_c$  is shown (black open circles) with the linear fit (solid red line).

demonstrate in an analytical way, following the calculus of ref 26, when  $\frac{\lambda_s}{2\lambda_d} > 1$ , that  $\lambda_d \approx \lambda_s$  i.e. the link remains linear.

## Conclusion

In this article, it has been shown that one band  $d$ -wave Eliashbeg's theory presents universal aspects as the linear link between  $\lambda_d$  and  $\lambda_s$  or the values  $2\Delta_d/k_B T_c$  that are independent of the particular critical temperature. These universal aspects are related to the assumption that the typical bosonic energy is correlated to the critical temperature as shown by experimental data ( $\Omega_0 = 5.8 k_B T_c$ ). We here proved that in a fully numerical solution of the Eliashberg equation, such linear links hold with great accuracy. A generalization and development of our results can be obtained by explicitly considering the momentum dependence of the self-energy without average on the Fermi surface as was done by Kamila A. Szewczyk, et al. [44]. Obviously, we would include in the calculations, unlike them, as we have done now, the link, observed experimentally, between the critical temperature and the representative energy of the bosonic spectrum.

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