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# Seismic Response of Viaducts and Bridges Isolated with FPS

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**Abstract.** This study deals with the evaluation of the seismic isolation of bridges equipped with single concave friction pendulum devices, by comparing the case in which the rigid abutment is present (i.e., multi-span continuous deck bridge) or not (i.e., single column bent viaduct). Two multi degree-of-freedom models are considered for the two cases, while the FPS behaviour is modelled including the velocity dependency. Furthermore, the comparison is carried out by varying the modelling parameters (i.e., pier and deck fundamental period, mass ratio and friction coefficient). The uncertainty in the seismic input is also included by subjecting the two systems to a set of different natural ground motions. The equation of motions are solved in non-dimensional form for both the models in order to obtain the maximum non-dimensional displacement of the substructure. This has led to the evaluation of the optimal sliding friction coefficient able to minimize the maximum non-dimensional pier displacement with the aim of studying the differences between the two numerical models.

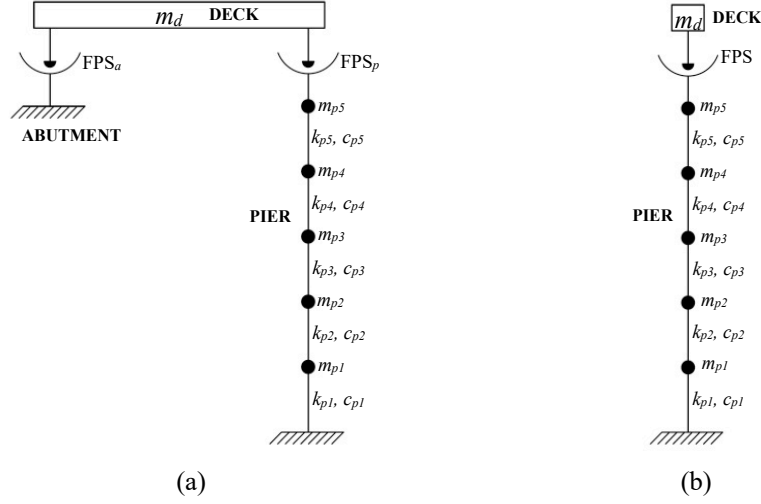
## INTRODUCTION

During the last decades, the safety assessment and maintenance management for infrastructures is becoming very relevant [1]-[3]. The goal of seismic isolation of bridges is to reduce the forces transmitted from the deck to the substructure, i.e., the piers, by increasing the period of the isolation system. During the past years, both the elastomeric and frictional isolators have demonstrated their effectiveness in enhancing seismic performance of structures and infrastructures [4]-[11]. In this context, an isolated three-span continuous deck bridge, equipped with elastomeric bearings, is studied in [12], with the goal to evaluate the bearings peak displacement placed at abutment locations. On the other hand, among the widely adopted isolators, the friction pendulum system (FPS) bearings have the advantage of making the properties of the device independent from the mass deck, which is important in the design phase of the isolator [13]-[15]. In particular, the introduction of the optimal friction coefficient, able to minimize the seismic response of the pier, was first introduced by Jangid in [16]-[17]. In this respect, the optimal friction coefficient is studied in [18] by varying many properties of the structure and the seismic input.

The goal of this work is to evaluate the pier-abutment-deck interaction when bridges are equipped with single concave friction pendulum isolators (FPS). In particular, two six-degree-of-freedom (dofs) models are compared: one representative of a single column bent viaduct (i.e., neglecting the presence of the rigid abutment) and the other for the case of multi-span continuous deck bridge (i.e., including the presence of the abutment). More precisely, for both cases, five dofs are adopted for the lumped masses of the elastic pier and one additional dof representative of the infinitely rigid deck. The equations of motion under a set of seismic inputs are solved for both the models, by performing a non-dimensional analysis. The FPS behaviour is represented by a widespread model that includes the dependency of the friction coefficient from the velocity. Many bridge properties are varied so as to perform a parametric analysis. Then, after having obtained the peak non-dimensional response at the pier level, the optimal sliding friction coefficient, able at minimizing this response, is investigated.

## NON DIMENSIONAL ANALYSIS

To model the seismic response of bridges, both including or neglecting the presence of the rigid abutment, a six-degree-of-freedom (dofs) model is adopted, where 5 dofs are used for the lumped masses of the reinforced concrete (RC) elastic pier, as suggested in [18]-[19], and 1 additional dof is for the infinitely rigid RC deck.



**FIGURE 1.** Six degree-of-freedom models: (a) considering the presence of the rigid abutment; (b) neglecting the presence of the rigid abutment.

Focusing on the case of multi-span continuous deck bridge, where the rigid RC abutment is modelled (Figure 1), subjected to a seismic input along the longitudinal direction, the equation of motion are:

$$\begin{bmatrix} m_d & m_d & m_d & m_d & m_d & m_d \\ 0 & m_{p5} & m_{p5} & m_{p5} & m_{p5} & m_{p5} \\ 0 & 0 & m_{p4} & m_{p4} & m_{p4} & m_{p4} \\ 0 & 0 & 0 & m_{p3} & m_{p3} & m_{p3} \\ 0 & 0 & 0 & 0 & m_{p2} & m_{p2} \\ 0 & 0 & 0 & 0 & 0 & m_{p1} \end{bmatrix} \begin{bmatrix} \ddot{u}_d(t) \\ \ddot{u}_{p5}(t) \\ \ddot{u}_{p4}(t) \\ \ddot{u}_{p3}(t) \\ \ddot{u}_{p2}(t) \\ \ddot{u}_{p1}(t) \end{bmatrix} + \begin{bmatrix} c_d & 0 & 0 & 0 & 0 & 0 \\ -c_d & c_{p5} & 0 & 0 & 0 & 0 \\ 0 & -c_{p5} & c_{p4} & 0 & 0 & 0 \\ 0 & 0 & -c_{p4} & c_{p3} & 0 & 0 \\ 0 & 0 & 0 & -c_{p3} & c_{p2} & 0 \\ 0 & 0 & 0 & 0 & -c_{p2} & c_{p1} \end{bmatrix} \begin{bmatrix} \dot{u}_d(t) \\ \dot{u}_{p5}(t) \\ \dot{u}_{p4}(t) \\ \dot{u}_{p3}(t) \\ \dot{u}_{p2}(t) \\ \dot{u}_{p1}(t) \end{bmatrix} + \begin{bmatrix} \frac{m_d}{2} g / R_p + \frac{m_d}{2} g / R_a & \frac{m_d}{2} g / R_a & \frac{m_d}{2} g / R_a & \frac{m_d}{2} g / R_a & \frac{m_d}{2} g / R_a & \frac{m_d}{2} g / R_a \\ -\frac{m_d}{2} g / R_p & k_{p5} & 0 & 0 & 0 & 0 \\ 0 & -k_{p5} & k_{p4} & 0 & 0 & 0 \\ 0 & 0 & -k_{p4} & k_{p3} & 0 & 0 \\ 0 & 0 & 0 & -k_{p3} & k_{p2} & 0 \\ 0 & 0 & 0 & 0 & -k_{p2} & k_{p1} \end{bmatrix} \begin{bmatrix} u_d \\ u_{p5} \\ u_{p4} \\ u_{p3} \\ u_{p2} \\ u_{p1} \end{bmatrix} + \begin{bmatrix} \frac{m_d}{2} g \mu_p (\dot{u}_d(t)) Z(t) + \frac{m_d}{2} g \mu_a \left( \dot{u}_d(t) + \sum_{i=1}^5 \dot{u}_{pi}(t) \right) Z(t) \\ -\frac{m_d}{2} g \mu_p (\dot{u}_d(t)) Z(t) \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = +\ddot{u}_g(t) \cdot \begin{bmatrix} -m_d \\ -m_{p5} \\ -m_{p4} \\ -m_{p3} \\ -m_{p2} \\ -m_{p1} \end{bmatrix} \quad (1)$$

where  $u_d$  is the deck displacement with respect to the pier top,  $u_{pi}$  is the displacement of the  $i$ th lumped mass of the pier with respect to the lower one,  $m_d$  is the mass of the deck,  $m_{pi}$  is the mass of the  $i$ th lumped mass of the pier,  $k_{pi}$  is the corresponding stiffness,  $c_d$  and  $c_{pi}$  are, respectively, the viscous damping coefficient for the device and for the pier masses,  $Z(t)$  indicate the sign function of the velocity, with  $t$  the instant of time and the dots indicate differentiation. The resisting forces of the FPS bearings located on top of the abutment and on the pier are, respectively,  $F_a(t)$  and  $F_p(t)$ , expressed as the sum of an elastic component and a viscous component, as follows [15]:

$$\begin{aligned} F_a(t) &= \frac{m_d g}{2} \left[ \frac{1}{R_a} \left( u_d(t) + \sum_{i=1}^5 u_{pi} \right) + \mu_a \left( \dot{u}_d + \sum_{i=1}^5 \dot{u}_{pi} \right) \operatorname{sgn} \left( \dot{u}_d + \sum_{i=1}^5 \dot{u}_{pi} \right) \right] \\ F_p(t) &= \frac{m_d g}{2} \left[ \frac{1}{R_p} u_d(t) + \mu_p (\dot{u}_d) \operatorname{sgn}(\dot{u}_d) \right] \end{aligned} \quad (2)$$

where the stiffness of the deck is equal to  $k_d = W / R = m_d g / R$ , half for the bearing on the abutment and half for the pier, the radii of curvature of the FPS bearings are  $R_a$  and  $R_p$ , placed, respectively, on the abutment and on the pier and assumed equal,  $g$  is the gravity constant,  $\mu$  is the sliding friction coefficient of the bearings. As anticipated, the fundamental period of the deck only depends on the geometrical properties of the isolator, since it is expressed as  $T_d = 2\pi\sqrt{m_d/k_d} = 2\pi\sqrt{R/g}$  [15]. It noteworthy that the two expressions in (2) differ only in terms of displacements, since  $F_a(t)$  depends on the relative displacement of the deck with respect to the ground while  $F_p(t)$  is function of the deck displacement with respect to the pier top. Regarding the sliding friction coefficient, its dependency on the velocity is such that [20]-[23]:

$$\mu(\dot{u}_d) = f_{\max} - (f_{\max} - f_{\min}) \cdot \exp(-\alpha |\dot{u}_d|) \quad (3)$$

where  $f_{\max}$  and  $f_{\min}$  are the sliding friction parameters at maximum and zero velocity,  $\alpha$  is a parameter that controls the transition from low to large velocities. In this work, it is assumed  $\alpha$  equal to 30 and  $f_{\max} = 3f_{\min}$  [23].

The equation of motions expressed in (1) are then elaborated so as to obtain their nondimensional form, according to the Buckingham's  $\Pi$ -theorem [24]. In particular, a time scale is introduced and assumed equal to  $1/\omega_d$ , with  $\omega_d = \sqrt{k_d/m_d}$  indicating the circular frequency of the isolation system. Thus, passing from the time  $t$  to  $\tau = t\omega_d$ , the ground motion input of equation (1) becomes  $\ddot{u}_g(t) = a_0 l(t) = a_0 l(\tau)$ , where  $l(t)$  is a nondimensional function of the seismic input time-history over time  $t$ , while  $l(\tau)$  contains the same information in the new time  $\tau$ . In addition, a length scale is introduced equal to  $a_0/\omega_d^2$ , where  $a_0$  is an intensity measure for the seismic input. In the end, dividing the equations in (1) for the deck mass  $m_d$  and introducing the time and length scales, the nondimensional equations become:

$$\begin{aligned}
& \begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & \lambda_{p5} & \lambda_{p5} & \lambda_{p5} & \lambda_{p5} & \lambda_{p5} \\ 0 & 0 & \lambda_{p4} & \lambda_{p4} & \lambda_{p4} & \lambda_{p4} \\ 0 & 0 & 0 & \lambda_{p3} & \lambda_{p3} & \lambda_{p3} \\ 0 & 0 & 0 & 0 & \lambda_{p2} & \lambda_{p2} \\ 0 & 0 & 0 & 0 & 0 & \lambda_{p1} \end{bmatrix} \begin{bmatrix} \ddot{\psi}_d(\tau) \\ \ddot{\psi}_{p5}(\tau) \\ \ddot{\psi}_{p4}(\tau) \\ \ddot{\psi}_{p3}(\tau) \\ \ddot{\psi}_{p2}(\tau) \\ \ddot{\psi}_{p1}(\tau) \end{bmatrix} + \\
& + \begin{bmatrix} 2\xi_d & 0 & 0 & 0 & 0 & 0 \\ -2\xi_d & 2\xi_{p5} \frac{\omega_{p5}}{\omega_d} \lambda_{p5} & 0 & 0 & 0 & 0 \\ 0 & -2\xi_{p5} \frac{\omega_{p5}}{\omega_d} \lambda_{p5} & 2\xi_{p4} \frac{\omega_{p4}}{\omega_d} \lambda_{p4} & 0 & 0 & 0 \\ 0 & 0 & -2\xi_{p4} \frac{\omega_{p4}}{\omega_d} \lambda_{p4} & 2\xi_{p3} \frac{\omega_{p3}}{\omega_d} \lambda_{p3} & 0 & 0 \\ 0 & 0 & 0 & -2\xi_{p3} \frac{\omega_{p3}}{\omega_d} \lambda_{p3} & 2\xi_{p2} \frac{\omega_{p2}}{\omega_d} \lambda_{p2} & 0 \\ 0 & 0 & 0 & 0 & -2\xi_{p2} \frac{\omega_{p2}}{\omega_d} \lambda_{p2} & 2\xi_{p1} \frac{\omega_{p1}}{\omega_d} \lambda_{p1} \end{bmatrix} \begin{bmatrix} \dot{\psi}_d(\tau) \\ \dot{\psi}_{p5}(\tau) \\ \dot{\psi}_{p4}(\tau) \\ \dot{\psi}_{p3}(\tau) \\ \dot{\psi}_{p2}(\tau) \\ \dot{\psi}_{p1}(\tau) \end{bmatrix} + \\
& + \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ -1 & \lambda_{p5} \frac{\omega_{p5}^2}{\omega_d^2} & 0 & 0 & 0 & 0 \\ 0 & -\lambda_{p5} \frac{\omega_{p5}^2}{\omega_d^2} & \lambda_{p4} \frac{\omega_{p4}^2}{\omega_d^2} & 0 & 0 & 0 \\ 0 & 0 & -\lambda_{p4} \frac{\omega_{p4}^2}{\omega_d^2} & \lambda_{p3} \frac{\omega_{p3}^2}{\omega_d^2} & 0 & 0 \\ 0 & 0 & 0 & -\lambda_{p3} \frac{\omega_{p3}^2}{\omega_d^2} & \lambda_{p2} \frac{\omega_{p2}^2}{\omega_d^2} & 0 \\ 0 & 0 & 0 & 0 & -\lambda_{p2} \frac{\omega_{p2}^2}{\omega_d^2} & \lambda_{p1} \frac{\omega_{p1}^2}{\omega_d^2} \end{bmatrix} \begin{bmatrix} \psi_d(\tau) \\ \psi_{p5}(\tau) \\ \psi_{p4}(\tau) \\ \psi_{p3}(\tau) \\ \psi_{p2}(\tau) \\ \psi_{p1}(\tau) \end{bmatrix} + \begin{bmatrix} \frac{g\mu(\dot{\psi}_d(\tau)) \operatorname{sgn}(\dot{\psi}_d(\tau))}{a_0} \\ -\frac{g\mu(\dot{\psi}_d(\tau)) \operatorname{sgn}(\dot{\psi}_d(\tau))}{a_0} \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = +I(\tau) \cdot \begin{bmatrix} -1 \\ -\lambda_{p5} \\ -\lambda_{p4} \\ -\lambda_{p3} \\ -\lambda_{p2} \\ -\lambda_{p1} \end{bmatrix} \quad (4)
\end{aligned}$$

where  $\psi_d = u_d \omega_d^2 / a_0$  and  $\psi_{pi} = u_{pi} \omega_d^2 / a_0$  are the nondimensional displacements,  $\omega_d = \sqrt{k_d / m_d}$  and  $\omega_{pi} = \sqrt{k_{pi} / m_{pi}}$  are the circular vibration frequencies,  $\xi_d = c_d / 2m_d \omega_d$  and  $\xi_{pi} = c_{pi} / 2m_{pi} \omega_{pi}$  are the damping factors (respectively for the deck and for the  $i$ -th lumped masses of the pier) and  $\lambda_p = \lambda_{pi} = m_{pi} / m_d$  is the mass ratio of the  $i$ -th lumped mass (all the lumped masses are assumed equal). Hence, the nondimensional parameters  $\Pi$  of the problem are:

$$\Pi_{\omega_p} = \frac{\omega_p}{\omega_d}, \quad \Pi_{\omega_g} = \frac{\omega_d}{\omega_g}, \quad \Pi_{\lambda} = \lambda_p, \quad \Pi_{\xi_d} = \xi_d, \quad \Pi_{\xi_p} = \xi_{pi}, \quad \Pi_{\mu} = \frac{\mu(\dot{\psi}_d) g}{a_0} \quad (5)$$

In the end, to discard the dependency of the nondimensional parameter  $\Pi_{\mu}$  from the velocity, its value is substituted by  $\Pi_{\mu}^* = f_{\max} g / a_0$ .

Regarding the equations of motion for the case of a single-column bent viaduct (Figure 2), where the abutment is not considered, the nondimensional equation of motion are equal to the ones in (1) and (4), with the only difference that the term relative to  $F_a(t)$  is not present.

## PROBLEM'S PARAMETERS

In this section, the main properties of the problem are discussed. These assumptions are valid both for the case of considering or neglecting the presence of the pier-deck-abutment interaction.

First of all, concerning the seismic input, a set of 30 seismic ground motions is considered, selected from 19 different earthquakes [25]-[27]. The magnitude varies in the range 6.3 to 7.5, the source-to-site distance goes from 13 km to 98 km and the peak ground acceleration is in the range 0.13 - 0.82 g. The intensity measure (IM) [28]-[32], as also previously indicated as the seismic intensity  $a_0$ , is herein chosen as the spectral pseudo-acceleration  $S_A(T_d, \xi_d)$ . Assuming the damping ratio  $\xi_d$  equal to zero [33], the spectral pseudo-acceleration becomes only function of the deck fundamental period, meaning that  $a_0 = S_A(T_d)$ .

Regarding the structural properties, the damping ratios are set equal to  $\Pi_{\xi_d} = \xi_d = 0\%$  and  $\Pi_{\xi_p} = \xi_p = 5\%$ , the pier period varies from 0.10s to 0.20s, the deck period is in the range 2s-4s, the mass ratio assumes the value 0.1, 0.15, 0.2 and, finally, the normalized friction coefficient is in between 0 and 2.

The equation of motions expressed in (4) are solved for each of the two models by varying the previously mentioned parameters and by considering each of the 30 ground motions, using the Runge-Kutta-Fehlberg integration algorithm available in Matlab-Simulink [34]. For each simulation, the peak normalised response in terms of pier top displacement is numerically calculated and expressed as:

$$\psi_{u_p} = \frac{u_{p, \max} \omega_d^2}{a_0} = \frac{\left( \sum_{i=1}^5 u_{p_i} \right)_{\max} \omega_d^2}{a_0} \quad (6)$$

Then, the response parameters are probabilistically treated and assumed as lognormally distributed [33],[35]-[37], with geometric mean  $GM(\psi_{u_p})$  and standard deviation  $\beta(\psi_{u_p})$  as follows [38]-[47]:

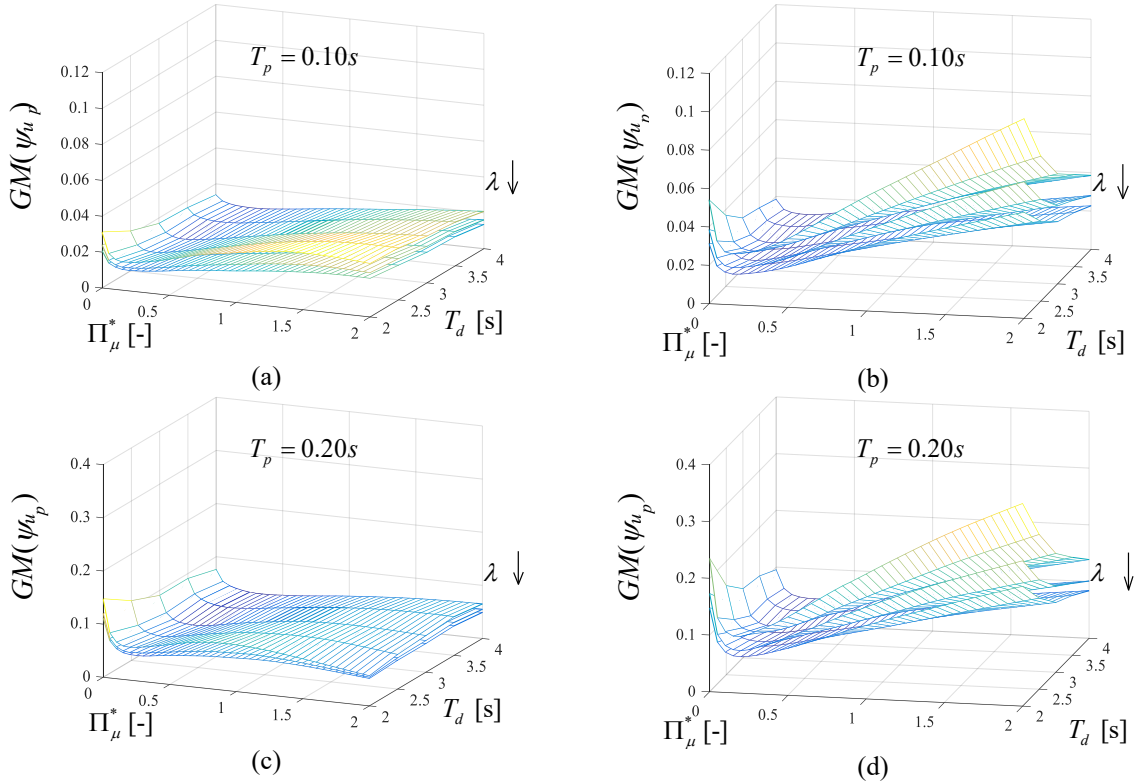
$$GM(\psi_{u_p}) = \sqrt[N]{\psi_{u_p 1} \cdot \dots \cdot \psi_{u_p N}} \quad (7)$$

$$\beta(\psi_{u_p}) = \sqrt{\frac{\left( \ln \psi_{u_p 1} - \ln [GM(\psi_{u_p})] \right)^2 + \dots + \left( \ln \psi_{u_p N} - \ln [GM(\psi_{u_p})] \right)^2}{N-1}} \quad (8)$$

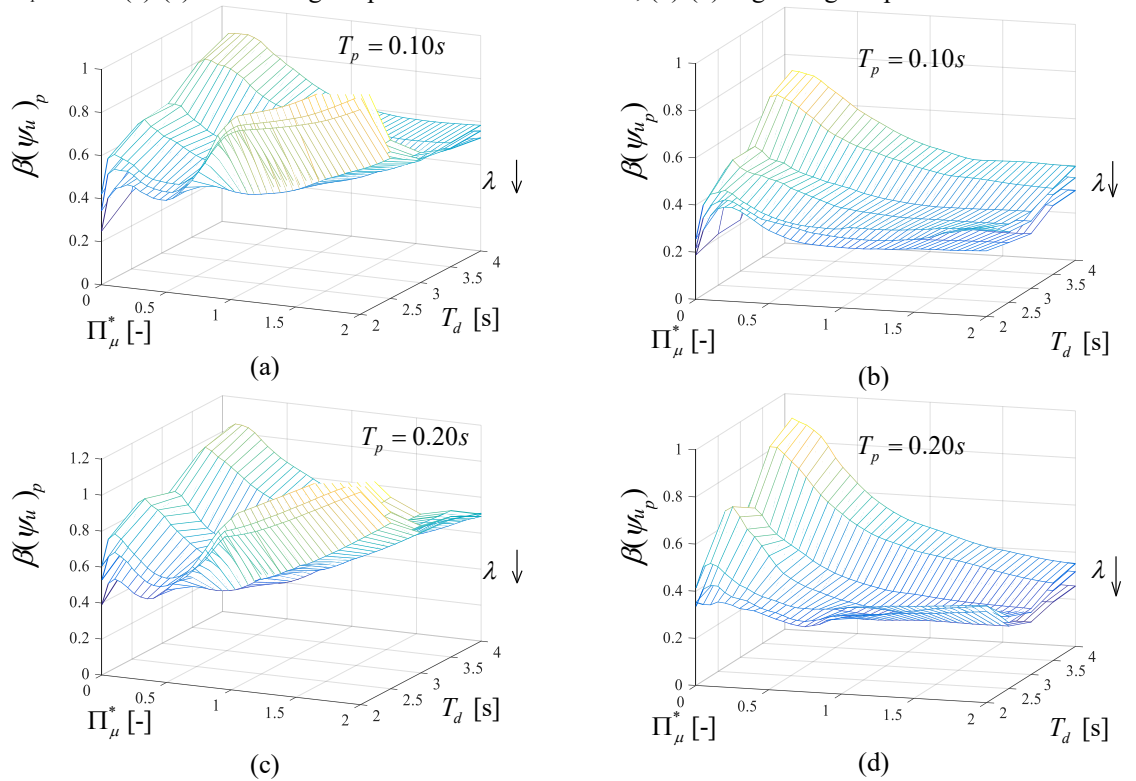
where  $\psi_{u_p j}$  is the j-th realization of the response parameter and  $j=1, \dots, N$  with  $N=30$  the total number of seismic inputs.

## SEISMIC RESPONSE AND OPTIMAL FRICTION COEFFICIENT

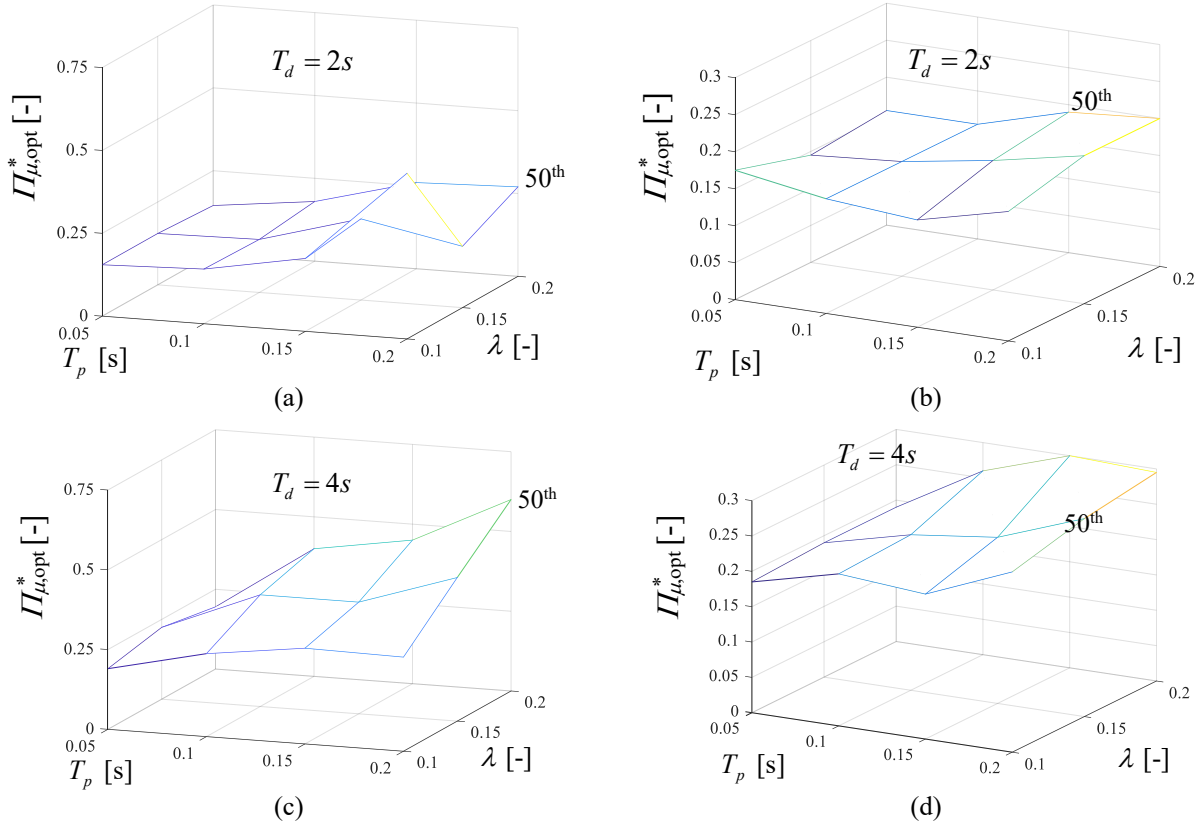
In this section, the response of the pier and the optimal friction coefficient results are illustrated. Figure 3 shows, for both the structural systems, the mean value of the maximum normalized pier displacement  $GM(\psi_{u_p})$  as function of  $T_d$  and  $\Pi_{\mu}^*$ , for fixed values of  $T_p$  and  $\lambda$ . In general, the mean value decreases for larger values of  $T_d$  and of  $\lambda$ . On the opposite, the response is lower for lower values of pier period. Regarding the dependency on the normalized friction coefficient  $\Pi_{\mu}^*$ , it is possible to observe the existence of an optimal value where the response is minimized. Figure 4 presents the same results but in terms of dispersion  $\beta(\psi_{u_p})$ . The dispersion tends to be larger if the pier-abutment-deck interaction is modelled and in general tends to be larger when the optimal value of  $\Pi_{\mu}^*$  is reached and to not be influenced by the other parameters.



**FIGURE 2.** Median value of the maximum normalized pier displacement as function of  $T_d$  and  $\Pi^*_\mu$ , for fixed values of  $T_p$  and  $\lambda$  : (a)-(c) considering the presence of the abutment; (b)-(d) neglecting the presence of the abutment



**FIGURE 3.** Dispersion of the maximum normalized pier displacement as function of  $T_d$  and  $\Pi^*_\mu$ , for fixed values of  $T_p$  and  $\lambda$  : (a)-(c) considering the presence of the abutment; (b)-(d) neglecting the presence of the abutment



**FIGURE 4.** Optimal friction coefficient as function of  $T_p$  and  $\lambda$ , for fixed values of  $T_d$ : (a)-(c) considering the presence of the abutment; (b)-(d) neglecting the presence of the abutment

From the previous results, it is possible to observe the existence of an optimal value where the response is minimized. In Figure 4 it is illustrated the optimum of  $\Pi_{\mu}^*$ , which is not only function of the parameters involved in the problem (i.e.,  $T_d$ ,  $T_p$ ,  $\lambda$ ), but it also depends on the structural system (i.e., if considering or not the presence of the abutment). In particular, the sagging zones of the response as function of  $\Pi_{\mu}^*$  are more pronounced when the interaction with the abutment is not considered, since the bearing on top of the abutment slides faster than the device placed on the pier. Furthermore, when all the structural parameters  $\lambda$ ,  $T_p$ ,  $T_d$  are considered with their maximum values, larger values of the optimum friction coefficient are required to increase the energy dissipation.

Finally, it is important to highlight that any numerical model is always characterized by uncertainties that influence the numerical simulations and so the safety assessment, as discussed in [48]-[58].

## CONCLUSION

This work analyses the seismic performance of bridges isolated with single concave friction pendulum bearings, focusing on the pier-abutment-deck interaction. In particular, two six-degree-of-freedom structural systems are modelled: one including the presence of the abutment (i.e., multi-span continuous deck bridge) and another neglecting its presence (i.e., single-column bent viaduct). Different values for the main problem parameters are considered within a parametric analysis and the uncertainty in the seismic input is included by considering a set of 30 natural ground motions. The equations of motions are numerically solved in a non-dimensional form so as to evaluate the maximum normalized response of the pier. This response tends to first decrease and then increase as function of the normalized friction coefficient of the bearing. When the presence of the abutment is considered (i.e., multi-span continuous deck bridge), this minimum value is less pronounced, since the bearing on top of the abutment tends to slide faster than the one on the pier. The existence of a minimum value for the pier response has

suggested to evaluate an optimal value for the normalized friction coefficient, as function of the other parameters involved. In the case multi-span continuous deck bridge, higher optimal values are observed.

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