

Progressive damage analysis of composite structures using higher-order layer-wise elements

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Article

A Two-Stage Sub-Threshold Voltage Reference Generator Using Body Bias Curvature Compensation for Improved Temperature Coefficient

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Abstract: Leakage diodes cause deviations in the thermal drift of ultra-low-power two-transistor (2T) reference circuits, resulting in either convex or concave output voltages against temperature, depending on the reference transistor types (n-type/p-type). This paper investigates the combined application of the convexity and concavity properties exhibited by the output voltage of complementary 2T references, one n-type and one p-type. By exploiting the body bias effect, this approach mitigates variations in the output reference voltage caused by temperature fluctuations. Software optimization is also used to obtain the required aspect ratios after formulating the required criteria for drain-induced barrier lowering (DIBL) elimination in the first stage. The performance of the proposed reference is evaluated by post-layout Monte Carlo simulations. In the range of 0 °C to 100 °C, the output reference voltage has an average temperature coefficient (TC) of 26.7 ppm/°C without any temperature trim. The output reference voltage is 195.5 mV with a standard deviation of 13.6 mV. The line sensitivity (LS) is 17.1 ppm/V in the supply voltage range of 0.5 V to 2.1 V at 25 °C. At 25 °C and 0.5 V, the power consumption is 28.8 pW, increasing to a maximum of 1.3 nW at 100 °C and 2.1 V.

Keywords: ultra-low-power (ULP); voltage reference; parasitic diodes; two-stage; leakage current; LS enhancement; second-order compensation



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1. Introduction

For proper operation, an accurate voltage or current reference [1] is needed in most electronic systems. In particular, it is a fundamental block of amplifiers [2], analog-to-digital converters (ADCs) [3], and regulators [4], among others. A voltage or current reference should be independent of temperature and supply voltage and should be robust against variations in the fabrication process. Moreover, since reference circuits are always on, their power consumption is particularly critical in the Internet of Things (IoT) sensor nodes, wearables, and medical implants. Ultra-low-power (ULP) references in mainstream CMOS technology have been actively investigated in recent years, lowering the power budget down to a few hundred femtowatts [5,6].

In ULP references, resistors are problematic because they occupy more silicon areas at low currents. Large resistors can be replaced by the transistor gate leakage current [7] or by MOSFET-only topologies. In such ULP CMOS voltage references (CVRs), however, the output is typically related to the transistors' threshold [8–12], which can be significantly affected by process variations. In order to enhance the robustness of CVRs to process variations, proportional to the faster-skewed process (PTFP) and complementary to the faster-skewed process (CTFP), circuits have been combined as part of the hybrid architecture presented in [13]. However, the minimum supply voltage and its TC are not very competitive. In [14], body biasing is exploited to design a reference less sensitive to the threshold voltage variations. However, it requires a minimum supply of 1.2 V and has a

TC ranging from 48 ppm/°C to 124 ppm/°C. Body biasing has also been used to adjust the output voltage at the expense of large power consumption and TC [15].

In this context, lowering the TC is one of the main challenges of ULP CVRs operating in the subthreshold region. In [16], it is shown that the pMOS diode's leakage current can be used to enhance the temperature behavior of the output reference voltage in ultra-low-power CVRs.

Adjusting the curvature of the reference voltage-to-temperature characteristic is a prevalent method employed in Bandgap Voltage References (BGRs) to enhance TC performance. For instance, in [17], the adjusted-temperature-curvature (ATC) compensation circuit is used to lower the TC down to 1.67 ppm/°C. However, the minimum supply voltage of 1.3 V and power consumption of 36.4 μ W are incompatible with the ULP design target.

Various techniques to improve the LS have been presented in the literature regarding the sensitivity to supply voltage changes. Using a quasi-cascode current mirror, the authors of [18] reduced the LS of [19] from 0.44%/V to 0.065%/V. This improvement was made possible at the cost of raising the supply voltage and power consumption from 0.45 V and 2.6 nW to 0.7 V and 25.9 nW, respectively.

The introduction of a two-stage circuit is another way to enhance LS [11]. In such references, the supply voltage primarily affects the reference voltage via the DIBL effect. To counteract the DIBL effect, a current proportional to the supply voltage is subtracted from the bias current of the output reference voltage branch [12]. This approach improves the LS from 1100 ppm/V to 190 ppm/V. By combining a two-stage structure with a DIBL compensator, the voltage reference circuit presented in [20] achieves an LS of 143.8 ppm/V. The LS and TC corrections are carried out in the structure's first and second stages, respectively. However, the curvature of the output voltage versus temperature characteristics in [20] cannot be altered because all transistors in the second stage are nMOS.

This paper presents a new TC correction circuit as the second stage in [20]. In detail, 2T voltage references of the p-type and the n-type are combined in this structure to reduce the temperature changes in the output reference voltage. In the output voltage-to-temperature characteristics of a 2T n-type voltage reference, a leakage current drawn by reverse-biased diodes at the output node produces a concave curve. In contrast, the leakage current sourced by reverse-biased diodes produces a convex characteristic in the 2T p-type voltage reference [16]. In the proposed reference, the two opposite behaviors of concavity and convexity of the n-type and p-type references are compensated by biasing the body of the load transistor in a 2T p-type reference with the output voltage of an n-type reference. Moreover, the LS is also improved by optimizing the DIBL effect removal in the first stage.

In the rest of this paper, the two-stage structure of [20] will be reviewed, and a more accurate expression for the DIBL compensation approach will be introduced in Section 2. Section 3 presents the proposed voltage reference, while the optimization of its TC by the new technique is given in Section 4. Section 5 reports the results from post-layout simulations of the proposed voltage reference circuit, and finally, some concluding results are drawn in Section 6.

2. Dibl Effect Compensation

This section begins with a summary of the DIBL effect compensation and LS improvement technique presented in [20], followed by a proposed approach for optimizing DIBL effect compensation. Figure 1 shows the two-stage structure with a DIBL effect compensator introduced in [20]. In the first stage, a DIBL effect compensator is used to reduce the LS, while for the second stage, a temperature compensator is used to correct the thermal drift of the output voltage. All transistors in the first stage are nMOS, and their bodies are connected to the ground. M_1 , M_3 , and M_4 are thick oxide transistors, while M_2 and M_5 are thin oxide transistors. The LS corrector increases the minimum supply voltage slightly (by approximately 150 mV) in exchange for a substantial reduction in the LS. The stable output voltage of the first stage makes the TC almost constant over the entire supply voltage range.

The circuit operates in the subthreshold region in which the drain current can be expressed as [21]:

$$I_D = \mu C_d \frac{W}{L} V_T^2 \exp\left(\frac{|V_{GS}| - |V_{TH}|}{nV_T}\right) \left(1 - \exp\left(\frac{-|V_{DS}|}{V_T}\right)\right) \quad (1)$$

where μ , C_d , W , and L are the mobility of electrons or holes (depending on the transistor type), depletion capacitor, width, and length of the transistor, respectively. V_{GS} , V_{DS} , V_{TH} , and V_T are the gate-source, drain-source, threshold, and thermal voltage, respectively. Increasing the drain-source voltage beyond 150 mV allows the last term to be ignored, although the drain-source voltage dependence remains through the DIBL effect, which influences the threshold voltage.

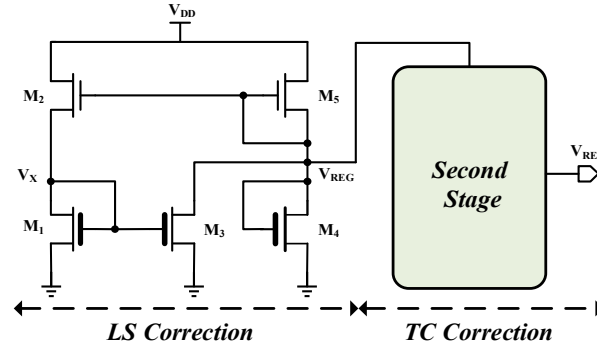


Figure 1. A two-stage circuit with DIBL effect compensation was proposed in [20].

The effect of temperature in the first stage on the output reference voltage is approximated as follows [20]:

$$\left(\frac{\partial V_{REF}}{\partial V_{REG}} \Big|_{T=constant} \times \frac{\partial V_{REG}}{\partial T}\right) / V_{REF} = LS_2 \times TC_1 \times V_{REG-avg} \approx 0 \quad (2)$$

where V_{REF} refers to the reference output voltage, while V_{REG} represents the output voltage of the first stage. T denotes the absolute temperature, and TC_1 and LS_2 are the temperature coefficient of the first stage and line sensitivity of the second stage, respectively. As a result, the first stage output voltage changes with temperature have a negligible impact on the total TC . In this design, the gate of M_2 is connected to the output node to produce a current proportional to the changes in V_O with respect to the supply voltage, to be sunk from the V_O node itself through M_1 and M_3 , aiming to reduce the supply sensitivity of V_{REG} .

This paper investigates the output voltage of the first stage in more detail and fewer simplifications than [20] to cancel DIBL's effect better. I_{D3} and I_{D5} can be obtained as described in [20]. Therefore, $I_{D4} = I_{D5} - I_{D3}$ can be expressed as follows:

$$V_{REG} = V_{TH4} + n_H V_T \ln\left(K_{R2} \exp\left(\frac{-V_{TH5}}{n_L V_T}\right) - K_{R1}^{N_{R1}} K_{R3} \exp\left(\frac{n_L V_{TH1} - n_H V_{TH2} - (n_H + n_L) V_{TH3} + n_H V_{REG}}{n_H (n_H + n_L) V_T}\right)\right) \quad (3)$$

where

$$\begin{aligned} K_{R1} &= (C_{d,L}(W/L)_2) / (C_{d,H}(W/L)_1) \\ K_{R2} &= (C_{d,L}(W/L)_5) / (C_{d,H}(W/L)_4) \\ K_{R3} &= (W/L)_3 / (W/L)_4 \end{aligned} \quad (4)$$

$N_{R1} = (1 + N_R)^{-1}$ and $N_R = n_H / n_L$. The subscript "H" denotes thick oxide transistors, whereas the subscript "L" represents thin oxide transistors. The DIBL effect's impact on the threshold voltage can be expressed as follows:

$$V_{TH} = V_{TH,0} - \lambda_D |V_{DS}| \quad (5)$$

where λ_D is the DIBL factor and $V_{TH,0}$ is the threshold voltage at $|V_{DS}| = 0$. Assuming the main supply voltage changes are applied to drain-source voltages of M_2 and M_5 , the following expression can be derived by substituting (5) in (3):

$$V_{REG} = V_{TH4} + n_H V_T \ln \left(K_{R2} \left(\exp \left(\frac{-V_{TH5,0}}{n_L V_T} \right) \exp \left(\frac{\lambda_{D5} V_{DS5}}{n_L V_T} \right) - K_{R1}^{N_{R1}} K_{R3} \exp \left(\frac{\lambda_{D2} V_{DS2}}{(n_H + n_L) V_T} \right) \times \exp \left(\frac{n_L V_{TH1} - n_H V_{TH2,0} - (n_H + n_L) V_{TH3} + n_H V_{REG}}{n_H (n_H + n_L) V_T} \right) \right) \right) \quad (6)$$

To compensate for DIBL’s effect, the expression in the logarithm argument should be independent of the drain-source voltages of M_2 and M_5 . In the circuit design, transistor dimensions are chosen so that $V_{DS2} \approx V_{DS5} \approx V_{DS}$. Also, V_{REG} is assumed to be constant. In Figure 2, the simulation results show that the V_{REG} and V_X mean values are 348.7 mV and 349.3 mV, respectively. With these criteria, the following expression is obtained by differentiating the argument of the logarithm in (6) with respect to V_{DS} and setting it equal to zero.

$$AK_{R2} \frac{\lambda_{D5}}{n_L V_T} \exp \left(\frac{\lambda_{D5} V_{DS}}{n_L V_T} \right) = BK_{R1}^{N_{R1}} K_{R3} \frac{\lambda_{D2}}{(n_L + n_H) V_T} \exp \left(\frac{n_L \lambda_{D2} V_{DS}}{(n_H + n_L) V_T} \right) \quad (7)$$

where $A = \exp(-V_{TH5,0}/n_L V_T)$ and $B = \exp \left(\frac{n_L V_{TH1} - n_H V_{TH2,0} - (n_H + n_L) V_{TH3} + n_H V_{REG}}{n_H (n_H + n_L) V_T} \right)$. Thus, to perform DIBL compensation, the following conditions should be met:

$$\lambda_{D5} = N_{R1} \lambda_{D2} \quad (8)$$

$$BN_{R1} K_{R1}^{N_{R1}} K_{R3} \lambda_{D2} = AK_{R2} \lambda_{D5} \quad (9)$$

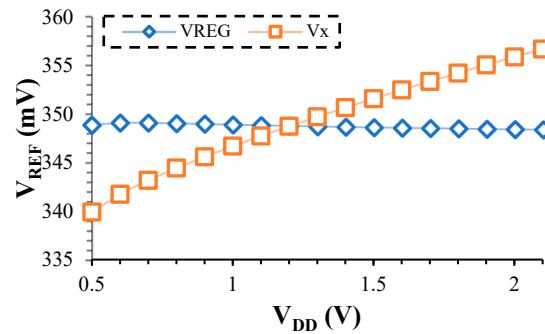


Figure 2. Simulation results of V_{REG} and V_X versus supply voltage.

The appropriate length of transistors M_2 and M_5 (which affect λ_{D2} and λ_{D5}) have to be chosen to satisfy Equation (8) in order to mitigate the DIBL effect. Then, (9) can be satisfied by K_{R1} , K_{R2} , and K_{R3} . The minimum length for M_2 is chosen to obtain the minimum suitable length of M_5 . Figure 3 shows the dependence of L_S on L_5 and W_3 for $L_2 = 0.18 \mu\text{m}$. The average of 100 Monte Carlo runs is used for each point. The shown dot has the lowest L_S values in this figure. Based on the analysis, the values of $L_5 = 0.45 \mu\text{m}$ and $W_3 = 3.7 \mu\text{m}$ are chosen for the design.

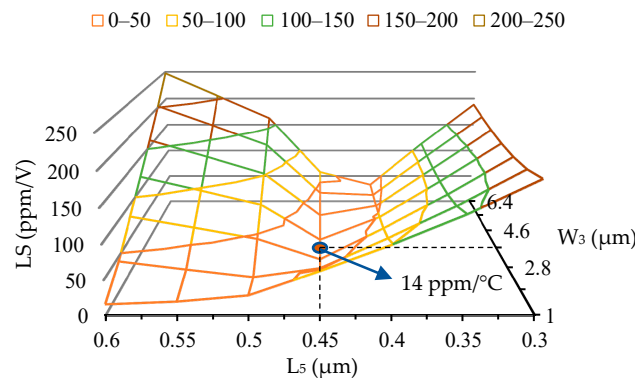


Figure 3. Adjusting L_5 and W_3 to satisfy Equations (8) and (9) using Monte Carlo analysis at each point on the graph.

3. Proposed Voltage Reference Generator

The proposed voltage reference generator aims to enhance the overall thermal drift of parasitic diode leakage currents. It achieves this by combining the opposite voltage versus temperature of 2T n-type and p-type voltage reference generators presented in Section 3.1. In Section 3.2, a comprehensive explanation of the methodology employed to integrate the temperature behaviors of the aforementioned structures, along with their corresponding mathematical expressions, is provided.

3.1. Effects of Parasitic Diodes Leakage Current in 2T n-Type and p-Type Voltage Reference Generators

Figure 4a,b illustrate the 2T n-type and p-type reference circuits, respectively. In the 2T n-type reference circuit, the output node contains two parasitic diodes, the reversed biased drain-body of M_6 , and the source-body of M_7 . Both diodes draw current from the output node and are shown in red. The reverse saturation currents drawn from the output node result in a concave reference voltage versus temperature curve for the 2T n-type reference (with the substrate connected to the ground) [16]. This behavior is illustrated in Figure 4a, which shows the simulated temperature dependence of the output voltage for different widths of the current source transistor. The length of both transistors is $2\ \mu\text{m}$, and the load transistor's width is $20\ \mu\text{m}$.

In the 2T p-type reference, the presence of a reverse-biased junction diode between the drain-body of M_9 results in the injection of a leakage current to the output node. The body terminal of M_8 is biased with a 200 mV DC voltage, which resembles the approximate voltage that is to be provided by a preceding stage in the proposed design. Since the applied body potential is higher than the output voltage of this stage, the source-body diode of M_8 will also inject a leakage current into the output node. The effect of the M_8 n-well diode is considered as a parasitic load on the preceding stage (the preceding stage is explained in the proposed design of the following subsection), which supplies the body bias of M_8 . The n-well parasitic diode of M_9 is located between V_{REG} and GND and has a negligible impact on the output voltage temperature-dependent behavior; however, the leakage current of this diode will affect the power dissipation. The pull-up parasitic diodes that inject the leakage current into the output node are highlighted in blue. These parasitic diodes inject reverse saturation currents to the output node, resulting in a convex output voltage versus temperature characteristic [16], as shown in Figure 4b for different M_9 transistor widths. Other dimensions are considered similar to the 2T n-type voltage reference.

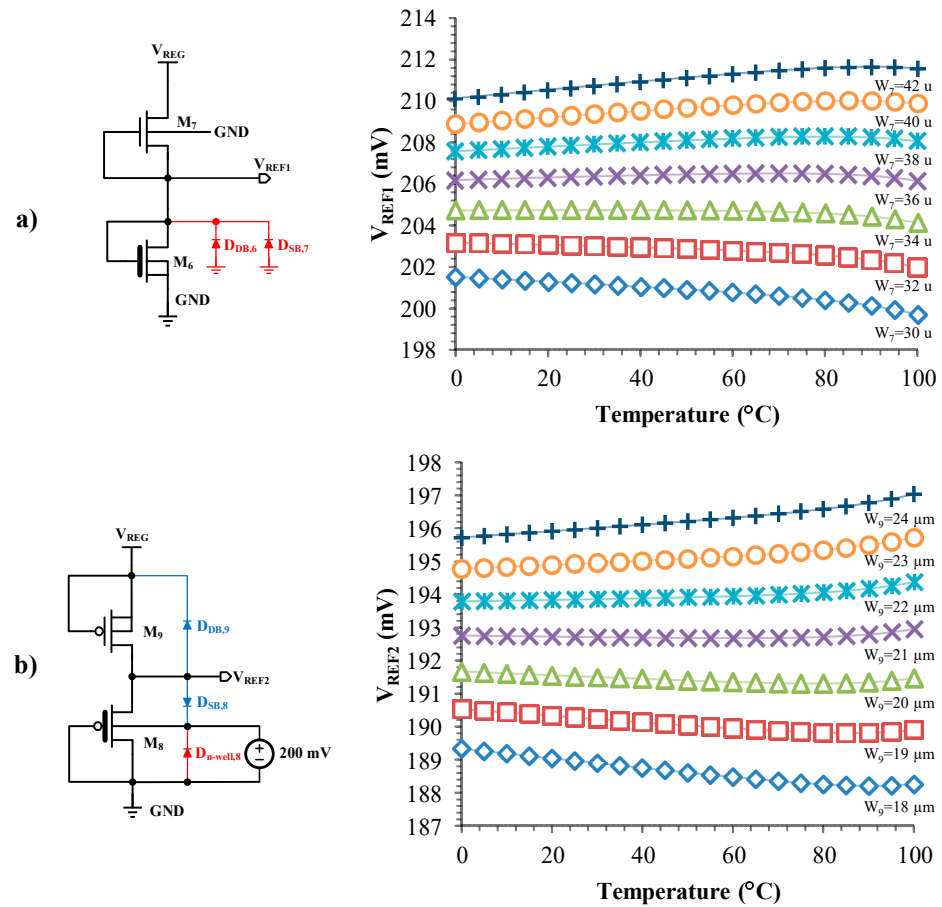


Figure 4. Simulation results of (a) 2T n-type reference output voltage versus temperature for different widths of M_7 ; (b) 2T p-type reference output voltage versus temperature for different widths of M_9 .

3.2. Proposed Circuit

The proposed voltage reference takes advantage of the opposite concavity in the voltage versus temperature behavior of 2T n-type and p-type CVRs to achieve curvature compensation. For this purpose, the output voltage of a 2T n-type reference is used to modulate the bulk voltage of the main 2T p-type reference, as demanded, to correct the curvature of its thermal drift.

In detail, considering the dependence of the threshold voltage of a pMOS transistor on its body voltage, the following is presented:

$$|V_{TH}| = |V_{TH,0}| + \gamma \left(\sqrt{|2\Phi_F| + V_{BS}} - \sqrt{|2\Phi_F|} \right) \quad (10)$$

in which Φ_F is the Fermi potential, V_{BS} is the bulk-source voltage, and $V_{TH,0}$ refers to the threshold voltage without body effect. For simplicity, $\sqrt{|2\Phi_F| + V_{BS}}$ in (10) is linearized according to (11) as follows:

$$\sqrt{|2\Phi_F| + V_{BS}} = C_1 V_{BS} + C_2 \quad (11)$$

$|V_{BS}|$ in this design is considered around 0 to 200 mV and $2\Phi_F \approx 0.8$ V. According to Figure 5, the C_1 and C_2 coefficients are approximately 0.53 and 0.9, respectively. By placing (11) into (10), $C_3 = \gamma C_1 = 0.35$ and $\gamma \left(C_2 - \sqrt{|2\Phi_F|} \right) \approx 0$. With these coefficients, the threshold voltage is expressed by the following equation.

$$|V_{TH}| = |V_{TH,0}| + C_3 V_{BS} \quad (12)$$

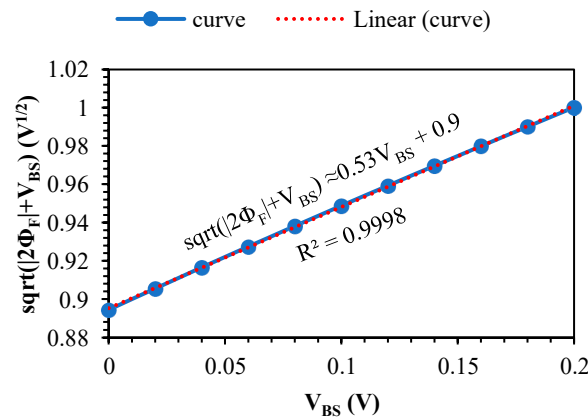


Figure 5. Linearization of $\sqrt{2\Phi_F + V_{BS}}$ for V_{BS} from 0 to 200 mV.

Equation (12) reveals that the body voltage scaled by the C_3 coefficient is added to the threshold voltage. Figure 6 illustrates the variation in V_{TH8} versus V_{BS8} . The slope of the variation is approximately near the predicted value of C_3 . Since the body of M_8 is biased by a 2T n-type circuit in the proposed reference, a concave-in-temperature contribution is added to its threshold voltage. Figure 7 illustrates the difference in the threshold voltage of M_8 between the zero-body-bias state and the state biased with the output voltage of the 2T n-type reference.

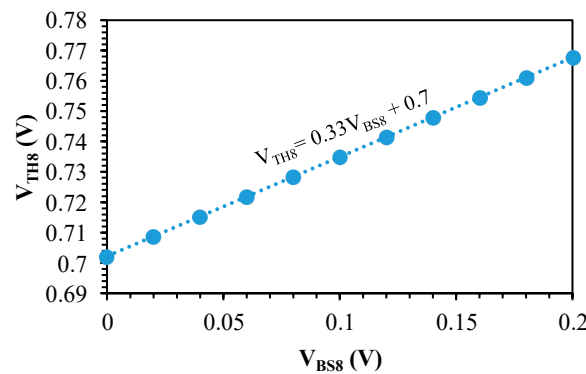


Figure 6. Simulation of the threshold voltage of M_8 with respect to V_{BS8} .

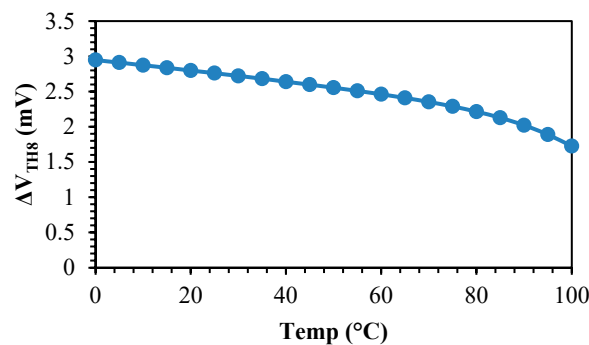


Figure 7. ΔV_{TH8} between two bias modes: with body bias through output voltage of a 2T n-type reference and with zero body bias.

Imposing the equality of the drain currents of M_8 and M_9 and based on Equation (1), the reference voltage can be expressed as

$$V_{REF} = |V_{TH8}| - N_R|V_{TH9}| + n_H V_T \left(\ln(A_1) + \ln\left(\frac{(W/L)_9}{(W/L)_8}\right) \right) \quad (13)$$

where $A_1 = \frac{\mu_{p9}C_{d9}}{\mu_{p8}C_{d8}}$. Considering the dependence of the body terminal of M_8 , $V_{BS8} = V_{B8} - V_{REF}$ and also using (12) in (13), (14) is obtained.

$$V_{REF} = \frac{n_H V_T \left(\ln(A_1) + \ln\left(\frac{(W/L)_9}{(W/L)_8}\right) \right)}{1 + C_3} + \frac{|V_{TH8,0}| - N_R |V_{TH9,0}| + C_3 V_{B8}}{1 + C_3} \quad (14)$$

The value of C_3 shows that V_{B8} will add up to the reference voltage by a factor of 0.26. By using the output voltage of 2T n-type as V_{B8} , convexity and concavity can be adjusted to cancel each other, thus reducing the reference voltage changes. Therefore, the proposed circuit for reducing the temperature curve of the 2T p-type is shown in Figure 8.

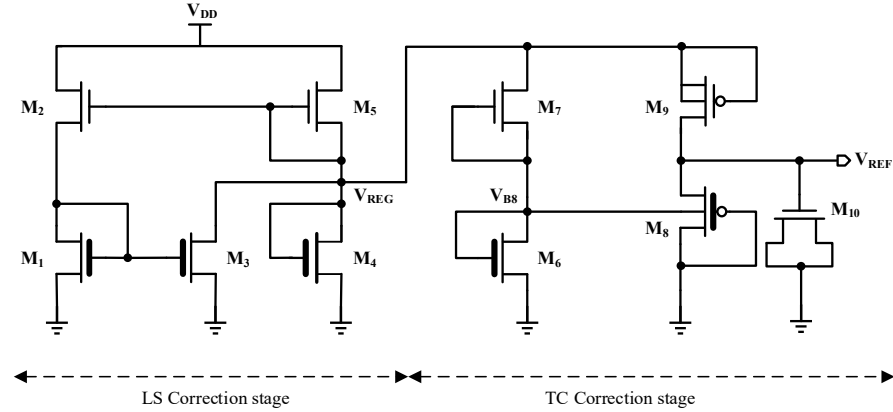


Figure 8. The complete architecture of the proposed voltage reference circuit.

It is possible to simplify (14) to (15).

$$V_{REF} = \frac{V_{REF,2T_P} + C_3 V_{REF,2T_N}}{1 + C_3} \quad (15)$$

$V_{REF,2T_P}$ and $V_{REF,2T_N}$ are 2T p-type and n-type reference voltages, respectively. The output reference voltage changes for $V_{REF,2T_P}$ and $V_{REF,2T_N}$ in temperature compensated form, the reference voltage obtained in (15) (through substituting $V_{REF,2T_N}$ and $V_{REF,2T_P}$ into (15)), and the reference voltage versus temperature changes are simulated in Figure 9. The mean values of V_{REF} obtained from (15), $V_{REF,2T_P}$, $V_{REF,2T_N}$, and output V_{REF} are 192.5 mV, 188.8 mV, 207.1 mV, and 195.3 mV, respectively. Assuming $I_{D6} = I_{D7}$ and similarly to (13), V_{B8} is obtained as follows:

$$V_{B8} = V_{TH6} - N_R V_{TH7} + n_H V_T \left(\ln(A_2) + \ln\left(\frac{(W/L)_7}{(W/L)_6}\right) \right) \quad (16)$$

where $A_2 = \frac{\mu_{n7}C_{d7}}{\mu_{n6}C_{d6}}$. Since the substrate is grounded, M_7 is affected by the body effect. By substituting (12) into (16), V_{B8} can be expressed as follows:

$$V_{B8} = V_{TH6,0} - N_R (V_{TH7,0} + C_3 V_{SB7}) + n_H V_T \left(\ln(A_2) + \ln\left(\frac{(W/L)_7}{(W/L)_6}\right) \right) \quad (17)$$

According to Figure 8 and connecting the substrate to the ground, $V_{SB7} = V_{B8}$. Therefore, (17) can be simplified to (18).

$$V_{B8} = \frac{n_H V_T \left(\ln(A_2) + \ln\left(\frac{(W/L)_7}{(W/L)_6}\right) \right) + V_{TH6,0} - N_R V_{TH7,0}}{1 + N_R C_3} \quad (18)$$

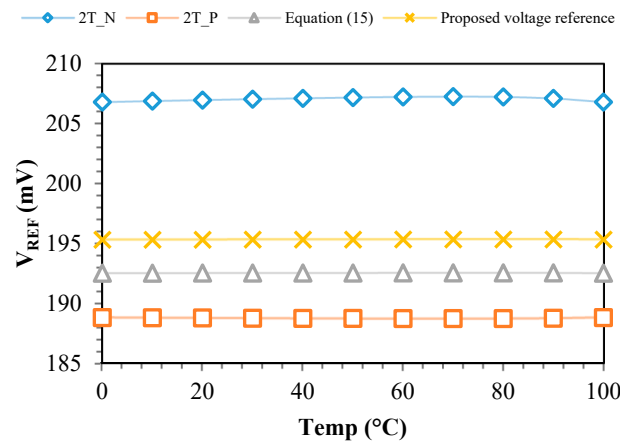


Figure 9. The compensated output reference voltage of 2T n-type and p-type, the predicted value through the sum of the output voltages of 2T n-type and p-type according to Equation (15), and the output reference voltage.

Using (18) in (14) results in the following equation:

$$V_{REF} = \frac{n_H V_T (\ln(A_1 A_2^{C_4})) + n_H V_T \ln\left(\frac{(W/L)_9}{(W/L)_8} \cdot \left(\frac{(W/L)_7}{(W/L)_6}\right)^{C_4}\right)}{1 + C_3} + \frac{|V_{TH8,0}| + C_4 V_{TH6,0} - N_R (|V_{TH9,0}| + C_4 V_{TH7,0})}{1 + C_3} \tag{19}$$

where $C_4 = C_3 / (1 + N_R C_3) \approx 0.196$. In the first-order approximation, parameters V_{TH} , V_T , and μ are considered dependent on temperature. The threshold voltage is a complex function of temperature, which can be expressed by [22]

$$V_{TH} = V_{TH}(T_0) + \alpha(T - T_0) + \beta(T - T_0)^2 + \gamma(T - T_0)^3 + \dots \tag{20}$$

The parameters α , β , and γ represent the first-, second-, and third-order coefficients, respectively, that describe the temperature dependence of the threshold voltage. Although this relationship is nonlinear, it can be approximated with a linear function. Additionally, using concave and convex curves for the output voltages of 2T n-type and p-type devices can help mitigate the effects of second-order nonlinearities. T_0 is the reference temperature. The temperature dependence of mobility can be expressed by (21) as follows [23]:

$$\mu(T) = \mu(T_0) \left(\frac{T}{T_0}\right)^{-M} \tag{21}$$

M is the temperature exponent of carrier mobility, which is usually 1.5. Since a ratio of the same type of mobilities is used, the thermal drift of the mobility in (19) is canceled. By substituting $V_T = k_B T / q$ and using a linear function of (20) in (19), the appropriate aspect ratio is obtained to compensate for temperature dependences as follows:

$$\frac{(W/L)_9}{(W/L)_8} \cdot \left(\frac{(W/L)_7}{(W/L)_6}\right)^{C_4} = \frac{1}{A_1 A_2^{C_4}} \exp\left(\frac{q}{n_H k_B} (\alpha_8 + C_4 \alpha_6 - N_R (\alpha_9 + C_4 \alpha_7))\right) \tag{22}$$

By choosing suitable transistor dimensions to achieve complete temperature compensation of voltage reference and by inserting (22) into (19), a temperature-compensated expression for the output reference voltage can be obtained as follows:

$$V_{REF} = \frac{\Delta V_{TH} + \Delta \alpha \cdot T_0}{1 + C_3} \tag{23}$$

where

$$\Delta V_{TH} = |V_{TH8,0}(T_0)| + C_4 V_{TH6,0}(T_0) - N_R(|V_{TH9,0}(T_0)| + C_4 V_{TH7,0}(T_0)) \quad (24)$$

$$\Delta\alpha = N_R(\alpha_9 + C_4\alpha_7) - (\alpha_8 + C_4\alpha_6)$$

4. TC Optimization

In Equation (22), the aspect ratio for temperature compensation is evaluated. The aspect ratio on the left side of the equation becomes 1.26 using the typical corner technology parameters in (22). This aspect ratio is shifted with the change in the technology parameters in various corners. Therefore, Monte Carlo analysis optimization would be more appropriate than just one corner optimization to reduce the average TC [16].

Flicker noise and short channel effects are reduced as transistor length increases [24]. To make a compromise between the occupied chip area and second-order effects, the second-stage transistor lengths are chosen at 2 μm. Figure 10 shows the Monte Carlo analysis used on the schematic to find an optimal aspect ratio for temperature compensation.

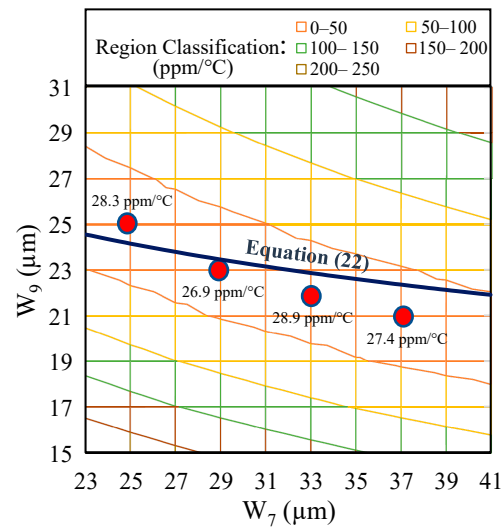


Figure 10. TC Monte Carlo analysis with 100 runs for two parameters of W_7 and W_9 and temperature compensation prediction of (22).

For temperature compensation, transistor widths of M_6 – M_9 are important since the second stage is responsible for temperature correction of the output voltage. For this purpose, by selecting $W_6 = W_8 = 20$ μm, W_7 and W_9 are swept to find the suitable design solution. The dots represent the values of TC, as determined by post-layout Monte Carlo analysis, in the range with the lowest TC. It is noteworthy that Equation (22) reasonably estimates the optimal dimension ratio, validating the derived equations. Because of the different parameters in different corners and simplified equations, there is a slight difference between optimal dimensions based on Monte Carlo and (22). As can be seen, the optimal TC lies in $W_7 = 29$ μm and $W_9 = 23$ μm, which results in a TC of 26.9 ppm/°C. The dimensions of all the proposed voltage reference transistors are reported in Table 1.

Table 1. Summary of post-layout Monte Carlo analysis (1000 runs).

Transistor	Type	Size
M_1	Thick oxide	1 μm/1 μm
M_2	Thin oxide	20 μm/0.18 μm
M_3	Thick oxide	3.7 μm/1 μm
M_4	Thick oxide	0.22 μm/20 μm

Table 1. Cont.

Transistor	Type	Size
M ₅	Thin oxide	(101.1 μm/0.45 μm) × 4
M ₆	Thick oxide	20 μm/2 μm
M ₇	Thin oxide	29 μm/2 μm
M ₈	Thick oxide	20 μm/2 μm
M ₉	Thin oxide	23 μm/2 μm
M ₁₀	Thin oxide	9 μm/15 μm

5. Simulation Results

The proposed two-stage voltage reference has been tested in 0.18 μm CMOS technology. Figure 11 depicts the proposed design layout, which occupies an area of 2358.8 μm². This section presents the performance of the proposed reference obtained from post-layout simulations.

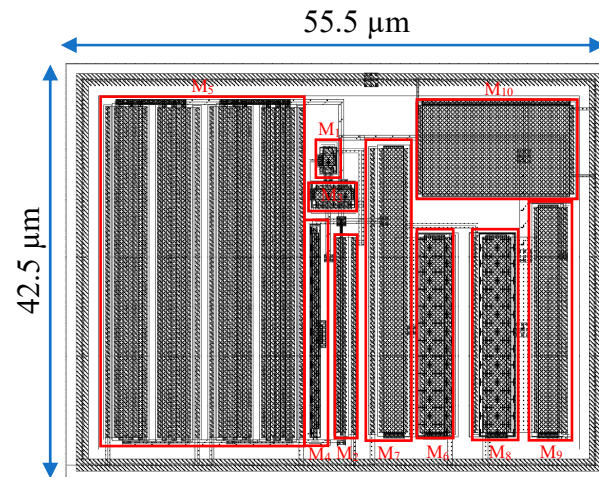


Figure 11. Proposed voltage reference layout.

Figure 12 shows the variations in the output reference voltage against the temperature and supply voltage in the typical corner. The LS in the 0.5 V to 2.1 V supply voltage range at 25 °C is equal to 13.6 ppm/V, and the TC in the 0 °C to 100 °C temperature range at 0.5 V supply voltage is equal to 6.8 ppm/°C. In Figure 13, the TC changes with respect to the supply voltage are shown. The TC changes only 0.35 ppm/°C, with a variation in the supply voltage from 0.5 V to 2.1 V.

Monte Carlo analysis is used to investigate the effect of process and mismatch variations on TC, LS, power consumption, and the output reference voltage, as shown in Figure 14. In Figure 14a–d, the TC is reported in the temperature range from 0 °C to 100 °C at 0.5 V supply voltage, and the LS is simulated in the 0.5 V to 2.1 V supply voltage range at 25 °C. Power consumption and V_{REF} are also shown at 0.5 V and 25 °C.

In Figure 14e–h, the maximum supply voltage and temperature scenarios are investigated. The results of the Monte Carlo analysis are summarized in Table 2. The bias current of the circuit branches and the resulting power consumption have been reduced to 28.8 pW at room temperature through the connection of the gate to the source of the transistors that act as current sources, namely transistors M₅, M₇, and M₉. In addition to low power consumption, the proposed voltage reference has both low LS and TC of 17.1 ppm/V and 26.7 ppm/°C, respectively. As the supply voltage rises, the TC maintains a near-constant value, and there is a slight change in the LS as the temperature increases. When either the supply voltage or operating temperature increases, the power consumption will rise due to the temperature- and voltage-dependent bias current.

The use of a trimming network can significantly reduce the variations in the reference voltage by modifying the aspect ratio of M_8 . In [10], a suitable scenario for trimming the TC is proposed by removing the extra switches and eliminating variable parasitic diodes. When trimming transistors need to be in the off-state, using a sufficient negative voltage for source-gate transistors minimizes the effects on the output voltage behavior.

To examine the effect of a 3-bit TC trim circuit from [10] in reducing TC, a simple scenario is shown in Figure 15.

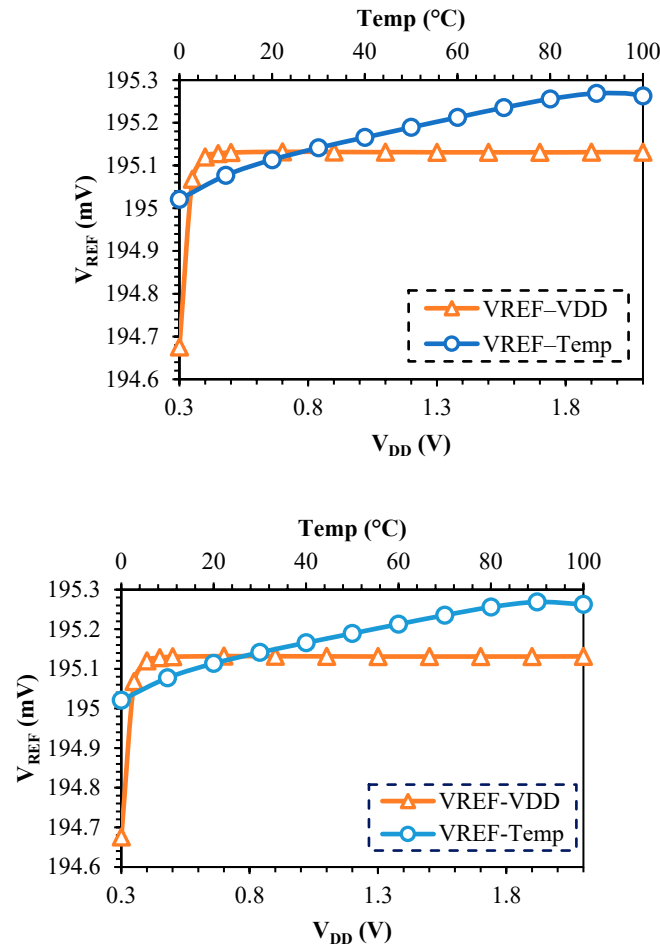


Figure 12. Variations in reference voltage against supply voltage from 0.3 V to 2.1 V and against temperature from 0 °C to 100 °C.

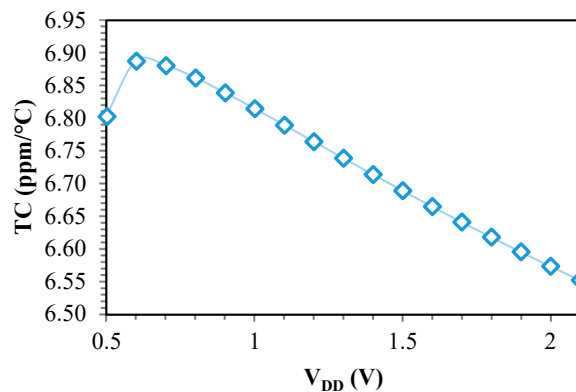


Figure 13. TC changes versus supply voltage.

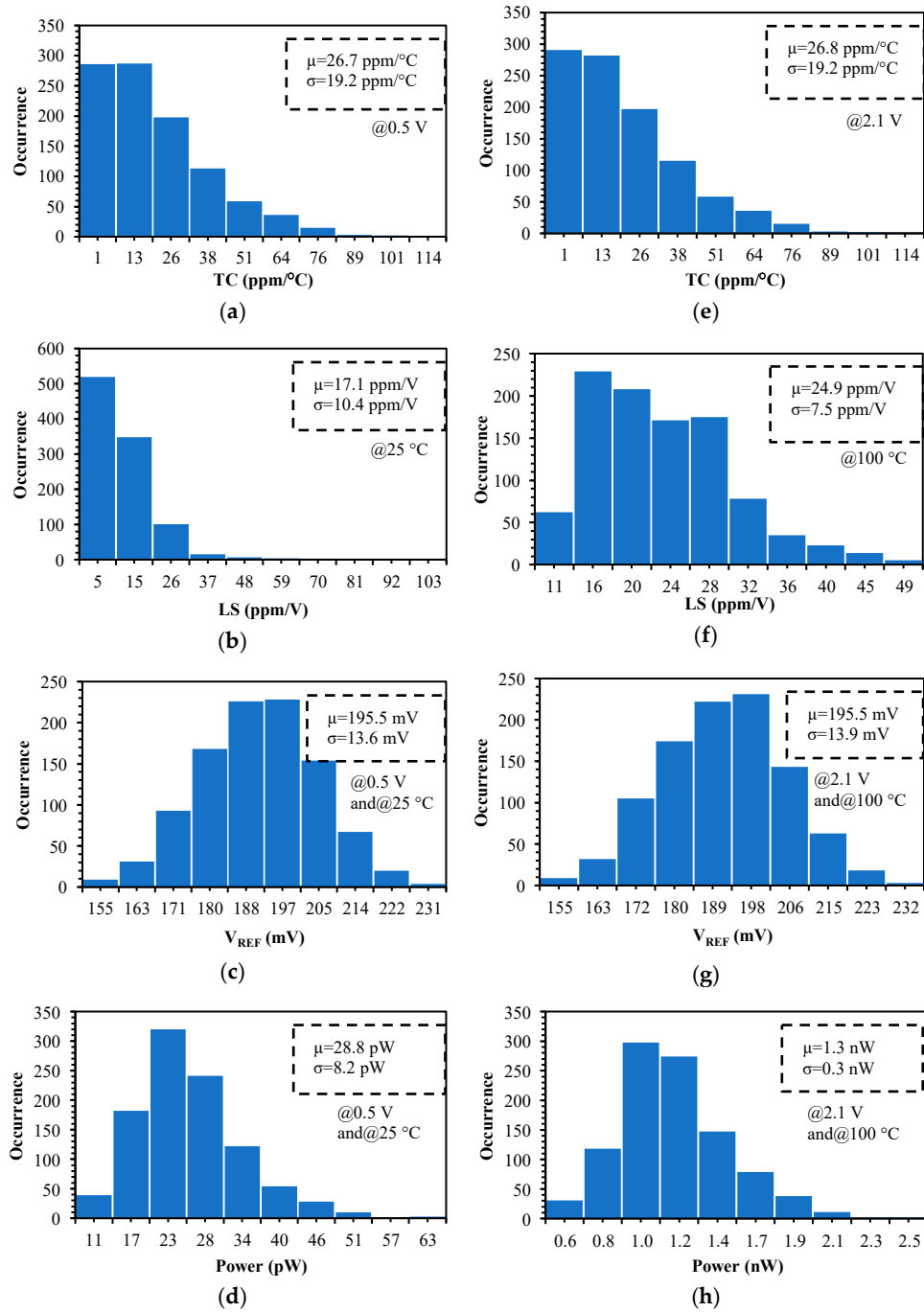


Figure 14. Monte Carlo analysis with 1000 runs on process and mismatch of post-layout.

Table 2. Summary of post-layout Monte Carlo analysis (1000 runs).

Parameters	μ	σ	σ/μ
TC (ppm/°C) @0.5 V	26.7	19.2	71.9%
@2.1 V	26.8	19.2	71.6%
LS (ppm/V) @25 °C	17.1	10.4	60.8%
@100 °C	24.9	7.5	30.1%
V _{REF} (mV) @0.5 V and 25 °C	195.5	13.6	7%
@2.1 V and 100 °C	195.5	13.9	7.1%
Power (pW) @0.5 V and 25 °C	28.8	8.2	28.5%
@2.1 V and 100 °C	1308	305	23.3%

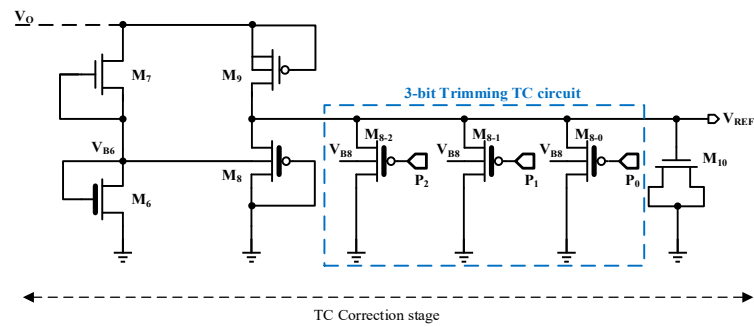


Figure 15. TC correction stage using a 3-bit trimming TC circuit.

As the trim transistors apply a constant parasitic diode load to the output node independent of their state, this constant load can be compensated with the other parasitic diodes at the output. Given that the output voltage is approximately 0.2 V, the minimum source-gate voltage of the trim transistors while in the off-state is approximately -0.3 V. The currents I_8 , I_{8-0} , I_{8-1} , and I_{8-2} in the TT corner are illustrated in Figure 16 when M_{8-0} and M_{8-1} are in the off-state.

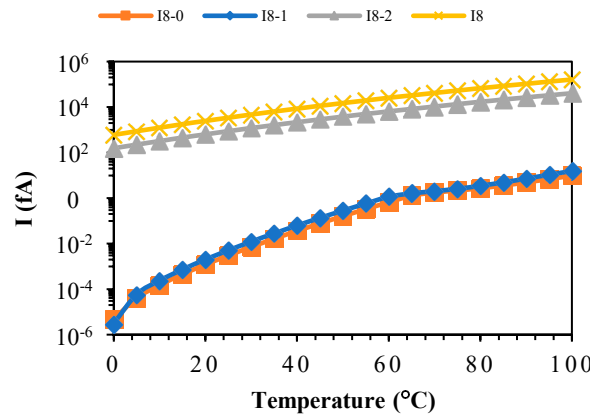
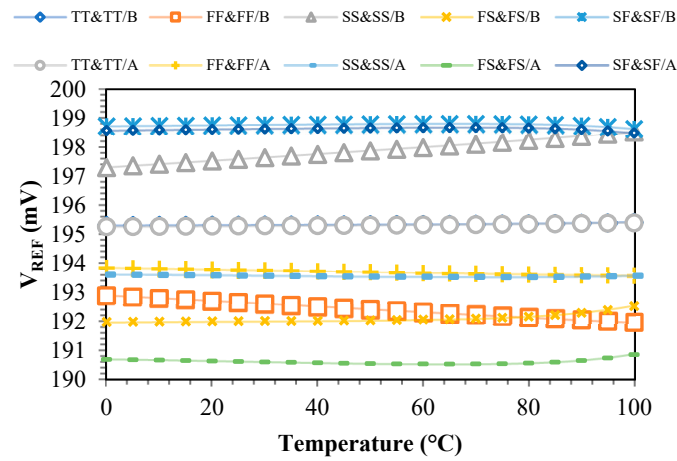


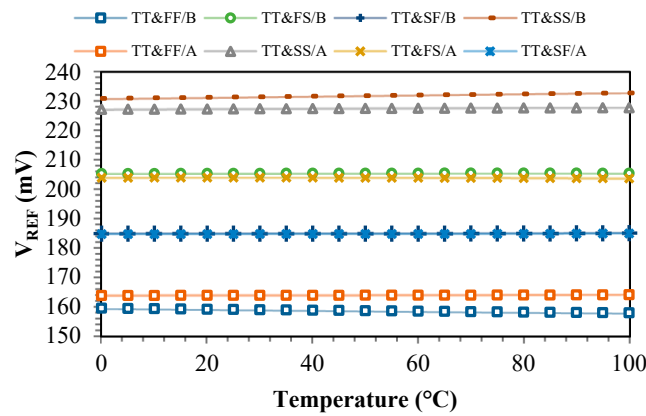
Figure 16. Comparison of the current of the trim transistors in the off-state with the on-state and the current of the M_8 transistor when the supply voltage is 0.5 V.

Notably, the currents flowing through the switched-off transistors are significantly lower than that of the voltage reference generator transistors. Consequently, the impact of these switched-off transistors on the output voltage can be neglected.

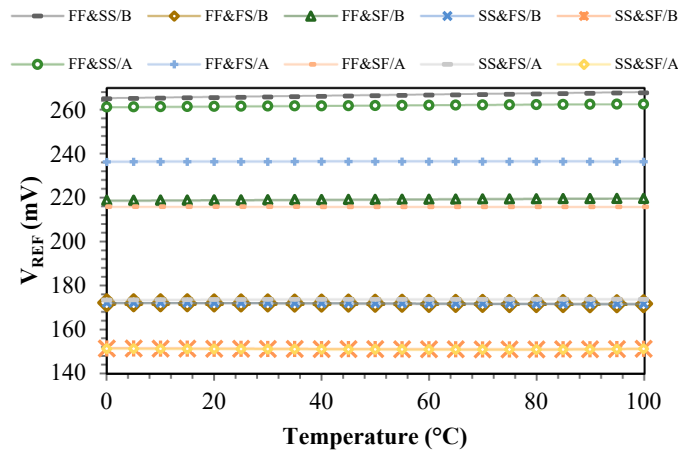
The TCs in the different corners are examined before and after the trim in Figure 17. Before trimming, the TC for TT&TT (first corners for thin oxide and second for thick oxide transistors), FF&FF, SS&SS, FS&FS, and SF&SF is 5.48 ppm/°C, 47.28 ppm/°C, 62.25 ppm/°C, 28.28 ppm/°C, and 8.82 ppm/°C, respectively. After trimming, they become 6.78 ppm/°C, 13.68 ppm/°C, 4.2 ppm/°C, 17.16 ppm/°C, and 9.43 ppm/°C, respectively. The average TC in these five corners before the trim is 30.42 ppm/°C, while after the trim, it becomes 10.25 ppm/°C. Furthermore, in other corners, such as FF&SF, as well as TT&SS, the trim circuit reduces the TC from 39.5 ppm/°C and 80.5 ppm/°C to 4.5 ppm/°C and 22.8 ppm/°C, respectively. Increasing the number of trim bits can further improve the TC of the circuit, but this comes at the cost of increasing the complexity and occupied area.



(a)



(b)



(c)

Figure 17. Variations in reference output voltage versus temperature in different corners before and after trim. The figure legend lists the transistor corners with thin oxide first, followed by those with thick oxide, using keywords A for after trim and B for before trim. (a) Main corners, (b) TT for thin oxide with some other corners for thick oxides, and (c) FF and SS for thin oxide with some other corners for thick oxides.

The startup times exhibiting the worst performance across various corners with 0.5 V supply voltage and at 0 °C are illustrated in Figure 18. The power supply is turned on at 100 ms. The startup time associated with SS has the highest value, at 341.4 ms.

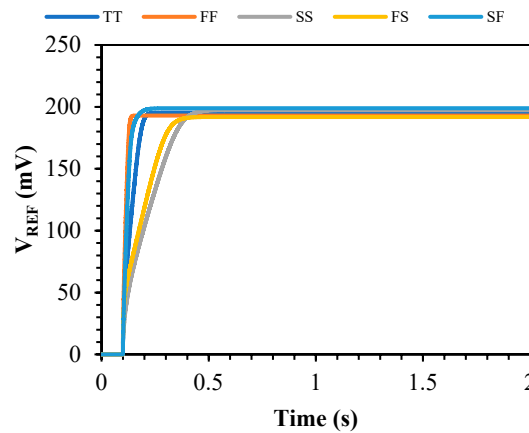


Figure 18. The startup time of the reference voltage at 0 °C and different corners when the minimum supply voltage ($V_{DD} = 0.5$ V) is turned on at 0.1 s.

Voltage references are used in analog and digital hybrid systems, so it is necessary to determine their sensitivity to fluctuations in the supply voltage. The M_{10} transistor is used as a 262 fF capacitor at the output node. At minimum supply voltage and room temperature (25 °C), the PSR from 0.1 Hz to 10 MHz is shown in Figure 19 without an external decoupling capacitor, double the output node capacitance (using an external 262 fF capacitor), and triple the output node capacitance (using an external 524 fF capacitor). The PSR near-DC frequencies are very low due to the efficient LS compensation. The minimum PSR is -89.3 dB at 0.1 Hz in all cases, and at high frequencies, it increases due to the leakage capacitors of the transistors and, finally, without external decoupling, remains constant at about -33.3 dB capacitor and, by using the external 262 fF and 524 fF decoupling capacitor, it becomes -38.4 dB and -41.6 dB, respectively.

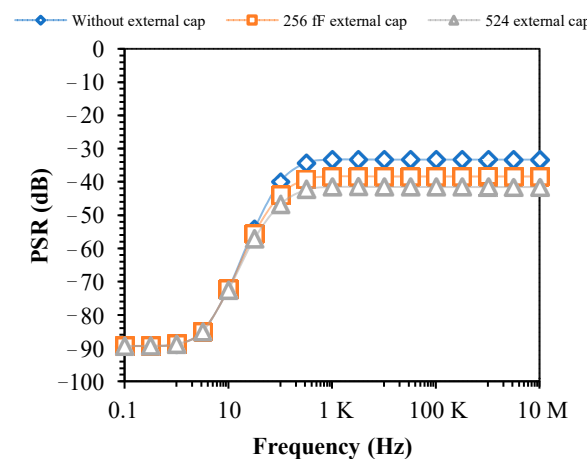


Figure 19. PSR of the proposed design at 0.5 V supply voltage, 25 °C, and for frequencies from 0.1 Hz to 10 MHz.

Figure 20 depicts the output noise within the frequency range of 0.1 Hz to 100 Hz, maintaining identical conditions to the PSR. The integrated noise from 0.1 Hz to 10 Hz without additional load capacitors, using the 262 fF external decoupling capacitor and 524 fF, respectively, generates 16.3 μ V, 16.2 μ V, and 16 μ V. In the 0.1 Hz to 100 Hz range, it becomes 41.8 μ V, 34.8 μ V, and 30.3 μ V, respectively. The output noise and PSR can decrease more if the load capacitor increases.

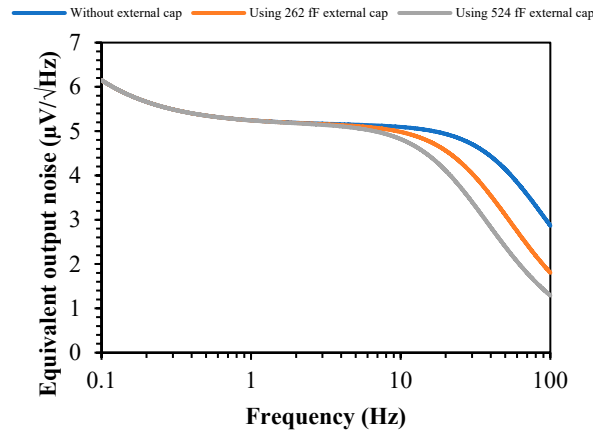


Figure 20. Output noise from 0.1 Hz to 100 Hz.

A comparison of the proposed voltage reference with all-MOSFET ultra-low-power designs is provided in Table 3. The proposed circuit has the best LS compared to the other voltage references. The LS of [20] is improved in the proposed voltage reference by a more accurate optimization to compensate for the DIBL effect. The proposed structure provides a TC of 26.7 ppm/°C without a TC trim circuit. After trimming, which needs more manufacturing and testing costs as well as more silicon area, [9,10,12] provide a more suitable TC. For [10] to operate correctly, a supply voltage of 0.8 V must be provided, and the power consumption associated with [9,12] exceeds that of the proposed design. The following FoM is used in Table 3 [10] to compare the voltage references with a number.

$$FoM = \frac{(T_{max} - T_{min})^2}{TC \times LS \times Power} \times 10^{-23} \frac{^{\circ}C \cdot V}{W} \tag{25}$$

Table 3. Comparison of the proposed voltage reference with similar ones.

Design	This Work *	[6] *	[12]	[20] *	[16]	[8]	[25]	[9]	[10] *
Tech (µm)	0.18	0.18	0.18	0.18	0.18	0.13	0.18	0.18	0.18
Min supply (V)	0.5	0.12	0.6	0.4	0.25	0.5	0.25	0.6	0.8
LS (ppm/V)									
µ	17.1	2200 [†]	190	143.8	3000	330	1600	1100	51.7
σ	10.4	-	60	17.3	-	360 ^T	500	-	51.5 ^T
Power (pW)	28.8	0.25	48	19.1	113	2.2	5.4	664	25.9
Temp range (°C)	0–100	−40–120	0–100	0–80	−40–140	−20–80	0–120	0–120	−20–80
TC (ppm/°C)									
µ	26.7	89.81	52	39.2	73.5	62	265	495	34.3
σ	19.2	11.7	10.1 ^T	-	11.7	29 ^T	45	11.6 ^T	4.4 ^T
σ			19	28		41		-	26.5
σ			1.5 ^T	-		11		1.4 ^T	7 ^T
PSR (dB)									
@10 Hz	−72 ^C	−78 ^C	−62.7 ^C	−90.9	-	−50.5 ^C	−70	−45 ^C	−41.2
@10 KHz	−33.3 ^C	−96 ^C	−50.2 ^C	−78	-	−58.5 ^C	−83.5	−55 ^C	−25.6
V _{REF} (mV)	195.5	65.7	147.9 ^T	119.2	118.1	176	91.4	457.1 ^T	206 ^T
Area (µm ²)	2358.8	70	33,200	2183	924	9300	2200	1700	10,208
FoM (°C·V/W)									
Before trim	7.61	5.18	0.22	0.59	0.01	2.22	0.06	0.001	2.18
After trim	-	-	1.08	-	-	0.32	-	0.02	16.97

[†] TT corner; ^T After trim; ^C using decoupling capacitor; * Monte Carlo simulation.

It is evident from Table 3 that in trimless designs, the proposed technique shows the highest figure of merit (FoM), whereas when the trim is employed, the optimal FoM corresponds to that of reference [10]. The proposed structure improves both LS and TC while consuming just 28.8 pW.

6. Conclusions

This paper presents an all-MOSFET voltage reference in 0.18 μm CMOS. Combining 2T n-type and p-type voltage references alleviates the curvature changes in the output reference voltage versus temperature, and an optimized design has been adopted to compensate the DIBL effect in the first stage. The circuit performance is estimated by post-layout Monte Carlo simulations over 1000 runs. The average TC is 26.7 ppm/ $^{\circ}\text{C}$ from 0 $^{\circ}\text{C}$ to 100 $^{\circ}\text{C}$. On average, the LS is decreased to 17.1 ppm/V for supply voltages from 0.5 V to 2.1 V, confirming optimized DIBL effect compensation. Last but not least, the mean power consumption is 28.8 pW, which makes it suitable for ultra-low-power applications in energy-autonomous IoT sensor nodes, wearable devices, and medical implants.

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