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Stochastic Time-Domain Mapping for Comprehensive Uncertainty Assessment in Eye Diagrams

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Abstract—The eye diagram is one of the most common tools used for quality assessment in high-speed links. This paper proposes a method of predicting the shape of the inner-eye for a link subject to uncertainties. The approach relies on machine learning regression and is tested on the very challenging example of flexible link for smart-textiles. Several sources of uncertainties are taken into account related to both manufacturing tolerances and physical deformation. The resulting model is fast and accurate. It is also extremely versatile: rather than focusing on a specific metric derived from the eye-diagram, its aim is to fully reconstruct the inner eye and enable designers to use it as they see fit. The paper investigates the features and convergence of three alternative machine learning algorithms, including the single-output support vector machine regression, together with its least squares variant, and the vector-valued kernel ridge regression. The latter method is arguably the most promising, resulting in an accurate, fast and robust tool enabling a complete parametric stochastic map of the eye.

Index Terms—signal integrity, high-speed interconnects, smart textiles, wearable electronics, eye diagram, uncertainty quantification (UQ), kernel-machine regressions.

I. INTRODUCTION

Benefiting from constant interest from both industry and academia, stochastic analysis evolved significantly over the past years. Various techniques are currently available, allowing designers to evaluate the impact of system uncertainties for various circuit applications, packaging and interconnects. Historically, the most common approach to stochastic analysis was Monte Carlo (MC). Featuring several improved versions, the technique is straightforward. Data is collected via repeated simulation and allows various metrics to be computed, quantifying the performance and robustness of a system subject to uncertainties related either to the manufacturing process or environment parameters. [1], [2]. The main drawback of MC is its computational cost. This prompted researchers to look for alternative solutions to the computationally expensive brute-force MC sampling, allowing them to infer the statistical characteristics of a system from limited data. Many of the first successful approaches were based on polynomial chaos expansion (for an overview of this family of algorithms see [3]). These were followed by other machine learning inspired solutions falling mainly into the category of kernel machine

regression (e.g., [4]–[9]) and artificial neural networks (ANNs) (e.g. [10]–[14]).

This paper focuses on kernel-machine regression techniques, such as: the support vector machine (SVM) regression [15], the least-squares support vector machine (LS-SVM) [16] regression and the more recent vector-valued kernel ridge (KRR) [6], [7], [17] which have been proven particularly effective for various microelectronics and radio-frequency applications [4], [5], [8]. Indeed, kernel-machine regressions provide an interesting alternative to the otherwise more flexible ANNs, especially well suited for problems in which a “relatively small” set of training data is available [15], [16], [18]. Unlike ANNs, the linear model structure adopted by kernel regression (i.e., the model unknowns appear linearly) has the key advantage of heavily simplifying the training phase, which reduces to the solution of a standard convex optimization problem, thus leading to several advantages in terms of training time and accuracy w.r.t. the number of training samples [6], [10].

In this specific context, the present paper explores a new methodology for uncertainty quantification in the field of signal integrity. The inner boundaries of an eye-diagram are approximated by a polygon. Several kernel machine regression algorithms are then used to build a surrogate model capable of mimicking the impact of system uncertainties on this polygon, resulting in a “stochastic map”. A particularly challenging example was selected in order to demonstrate the technique: a flexible differential digital link for smart textiles. The implementation uses copper yarn and is subject to various sources of uncertainties, including high tolerances during manufacturing [19]. It is important to observe that unlike previous approaches, which predicted the impact of uncertainties on specific metrics derived from the eye diagram (e.g., vertical opening, eye SNR, etc), stochastic time-domain mapping fully models inner-eye geometry. Several metrics may thus be computed in post-processing, the use of masks is also possible. The aim is to allow a statistically meaningful design leading to more robust systems. The approach is particularly interesting for cases where high tolerances are an issue in the design flow. These include emerging technologies with non-standard manufacturing processes, or low-cost products for mass consumers where high tolerances are a result of financial considerations. Note, however, that the stochastic mapping approach is not application-oriented but general and very adaptable.

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The paper is organized as follows. An example related to wearable electronics, based on published data, is presented in Section II. A description of how the eye-diagram is processed follows in Section III. Section IV provides an in-depth description of the algorithms used to perform stochastic mapping. Numerical results relative to the selected example are collected in Section V and are followed by a brief Conclusion.

II. TEST CASE

In the past two decades significant progress has been made in the field of wearable electronics and wearable computing. Fabrics integrating sensors, processors, energy harvesters, lights and batteries, so called “smart textiles” or “e-textiles”, have attracted the interest of various private and public actors [19]–[25]. The defense industry has a particular interest for this field: providing the soldier on the modern battlefield with apparel integrating sensor hubs, processors and various interfaces has numerous advantages [21]. Civilian applications also exist and are either health-oriented or focus on various specialized garments designed for exploration, hazardous environments or extreme sports. In a more general context, e-textiles may also be used in non-wearable applications (e.g. smart bed-sheets) or even in applications which are not human-oriented (geo-textiles) [24].

This new generation of electronics brings new challenges in terms of signal and power integrity. While the main design objective is always the transmitting electrical signals with as little distortion as possible, the specific context of e-textiles magnifies the impact of mechanical factors and forces designers to carefully consider aspects such as environment stability and service life [23]. Flexible data busses are characterized by much higher manufacturing imperfections than the ones in regular PCBs and suffer greater impact from environment parameters such as temperature and humidity. External mechanical action, both in terms of compression and stretching is also an issue.

The results obtained in this paper are based on the serial link shown in Fig. 1 which has been implemented and simulated in LTSPICE [26]. It consists of a differential data communication channel implemented by conductive copper wires weaved in a textile structure [27]. The flexible interconnect is described using the classic multiconductor transmission line theory and the per unit length parameters computed from the electrical and geometrical information of the structure [28], [29]. Note that conductive fibers remain, as of 2023, the most popular technological solution for interconnects in e-textiles [30]. The link features a differential driver at the near end and its paired receiver at the far end. In order to increase maximum data-rates, a passive equalizer is inserted between the driver and the line. It is assumed that the equalizer and buffers are implemented either using conventional electronics or semi-flexible substrates. They are affected by uncertainties, albeit to a lesser extent. The center section of the interconnect (identified by a transmission line segment with length L_2 in the scheme) accounts for a potentially altered geometry. This can either take the form of compression due to external mechanical action or to the very nature of the application (e.g. bending at

knees or elbows) or on the contrary stretching of the material. Either situation alters the distance between the conductors on a specific segment of the link. The circuit model accounts for the resulting discontinuity.

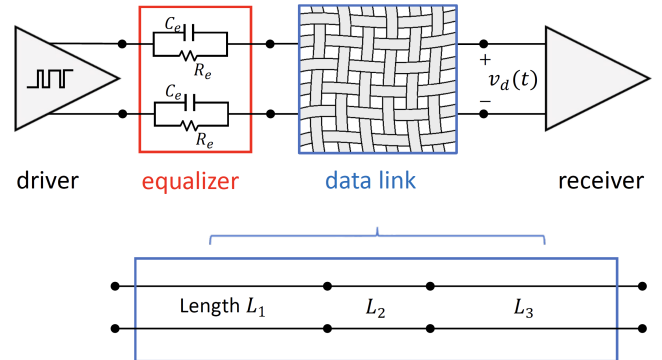


Fig. 1. System under test: digital link for wearable applications. The nominal values of the equalizer and of the line lengths are: $R_e = 70 \Omega$, $C_e = 3.2 \text{ pF}$ $L_1 + L_2 + L_3 = 33 \text{ cm}$,

NRZ encoding is used at a data rate of 2 Gbps. At this stage of the investigation, the driver and the receiver are modeled using compact, linear models, very similar to the ones implemented in IBIS-AMI simulations. Specifically, an equivalent Norton-based voltage controlled circuitual representation of the differential drivers and receivers is used, according to the method developed in [31]. This representation enables the accurate simulation of coupled channels including both differential- and common mode signals. The driver and the receiver currents are defined as a function of the pertinent output and input port voltages, respectively, via a constant conductance matrix. The dynamic behavior of the devices is represented by a dynamic linear time-invariant submodel. Time-varying current source terms are instead used to represent the switching activity of the driver in terms of a time varying analog waveform. Device parameters are representative of the application at hand and the involved data rate. For a detailed presentation of the buffer models see equation (2) and Fig. 2 in [31] and the explanations therein.

However, the methodology described in this paper can be used as is with non-linear buffer models. For applications where such models are required for increased accuracy, they may readily be used [31]–[33]. It is important to note that the geometrical specifications of the interconnect, including the fabrication tolerances, are based on the experimental work published in [19]. The selected structure is labelled as GSSG-1 (see Fig. 3 in the previously referenced paper) and consists in a differential pair between two ground conductors.

Without loss of generality, in our application, 11 uniformly distributed uncertain parameters are considered. The distance between the signal lines is $411 \mu\text{m} \pm 7.3 \%$. The distance between each signal line and the adjacent ground line is $481 \mu\text{m} \pm 6.7 \%$. Conductor diameter is $228 \mu\text{m} \pm 11.1 \%$. The total length of the link is $33 \text{ cm} \pm 1 \text{ cm}$ (mainly due to sizing). The section under mechanical stress varies in length from 2 to 5 cm and the compression [stretching] factor is 25 %

[10%]. Tolerances of 1% are assumed for the elements of the equalizer. Each eye diagram is computed for 4000 bits.

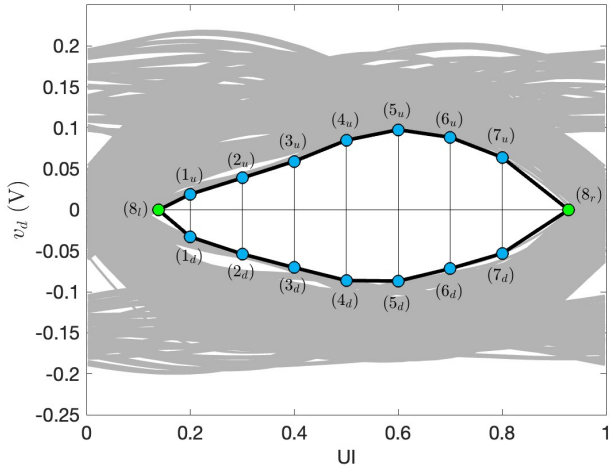


Fig. 2. Example eye diagram obtained for the data link of Fig. 1 for a given set of uncertain parameters. The plot also collects the information about the location of the polygonal edges associated to inner eye aperture, where the eye vertical apertures are labelled through the pairs from 1 to 7 and the eye width is indicated via the label pair number 8.

III. EYE APERTURE AND DATA LINK QUALITY

Throughout this paper, the performance of the communication via the data link is quantitatively assessed using the eye aperture on the receiver side, as obtained by observing the differential voltage response $v_d(t)$.

It is common practice to use the eye-diagram when designing high-speed interconnect systems. Associating eye-diagram analysis to uncertainty quantification and stochastic analysis has been investigated in recent years [34], [35]. In addition, thorough theoretical research has consolidated eye computation and processing, as well as jitter analysis making them highly reliable, standard tools [36], [37]. Machine learning techniques, such as the ones used in the paper, have also been used in the past in relation to eye-diagram analysis [5], [38], [39]. The novelty of the present work comes from the way in which machine learning is used, from the meta-modelling strategy itself. Instead of focusing on specific parameters derived from the eye-diagram and computed as scalar quantities (eye-height, horizontal opening etc), the clean inner eye is literally mapped by a polygonal representation. The meta-modelling process focuses on the vertices of the polygon. With this approach, most of the metrics commonly used in data-link design can be readily computed *a posteriori*, in a stochastic framework.

It should be noted that the methodology described in the present paper may be used regardless of the way in which the eye pattern is obtained. Post processing the image of the eye is one option, using sampled recorded responses is another. The former alternative usually relies on both in-house or commercial solutions enabling the fast simulation of a very large number of bits (on the order of millions) [31], [36]. The latter is usually preferred when the problem has a dominant

nonlinear nature, usually due to the buffers. In this case, a classic transient simulation is carried out by means of a circuit solver like SPICE where transceivers are replaced by physics-based transistor-level models or by faster behavioral nonlinear surrogates, yielding a sampled transient response of the pertinent variable of interest (e.g., $v_d(t)$) [33]. The inherent limitation in this case is the CPU time required to run SPICE and usually this is feasible when a relatively limited number of bits is considered, at most on the order of tens or hundreds of thousands.

A possible implementation of a compact routine allowing to compute the polygonal shape of the aperture and parameters such as the eye area is detailed in the appendix. This pseudo-code is made available in order to provide readers with a fully documented and self contained set of tools for both the computation of the inner eye, as described in this section and the surrogate modeling, as described in the next section.

Figure 2 shows an example eye diagram which can be obtained for the considered test case, together with its inscribed inner polygon (see the dark thick line) obtained with the proposed procedure. The diagram is generated from the data link response computed for a given sample of the uncertain parameters. The blue circles in the figure are the minimum and the maximum vertical positions of the clean inner eye area observed at a given set of points in the normalized unit interval. The green circles, instead, represent the jitter and can be used to define the horizontal eye aperture arising from the zero-crossing points, leading to the left and right vertices of the inner polygon.

It is important to point out that the optimal number of vertices of the inner polygon shown in Fig. 2 depends on the shape of the eye and thus is strongly related to the specific application at hand. In this paper, the points have been selected to guarantee a good accuracy of the approximated eye area. If needed, an automatic procedure can be devised, based on a heuristic step-by-step greedy algorithm. Basically the number of points along the abscissa, which represent the horizontal coordinates of the vertices, would gradually be increased in the range [0,1] of the unit interval until the variation of the resulting eye area becomes negligible. A relative threshold mechanism can be set. Also, one should avoid vertical probing in the area affected by time-domain jitter (e.g., the UI points 0.1 or 0.9 in the example eye). As already mentioned, horizontal probing is used to model this type of uncertainty.

IV. SURROGATE MODELS

A. Problem Statement

Let us consider the problem of approximating the variability of the vertices of a polygon approximating a generic eye diagram collected in the vector $\mathbf{y} = [y_1, \dots, y_D]^T \in \mathcal{Y}$ with $\mathcal{Y} \subseteq \mathbb{R}^D$ as a function of a set of parameters of the link collected in the vector $\mathbf{x} = [x_1, \dots, x_p]^T \in \mathcal{X}$ with $\mathcal{X} \subseteq \mathbb{R}^p$. For the example eye of Fig. 2, the entries of vector \mathbf{y} (i.e., D) correspond to positive and negative vertical positions of the blue circles calculated at 7 time points $[0.2, 0.3, \dots, 0.8]^T$ defined in a normalized unit interval, and

the horizontal position of the green circles associated to the jitter, respectively. The overall number of output components is $D = 16$, while the number of input parameters $p = 11$. Within the machine learning framework, the modeling problem stated above can be reformulated as the problem of building a generic vector-valued surrogate model $\mathcal{M} : \mathcal{X} \rightarrow \mathcal{Y}$, starting from the information available on the training set $\mathcal{D} = \{(\mathbf{x}_l, \mathbf{y}_l)\}_{l=1}^L$, where L represents the total number of training pairs, such that $\mathbf{x}_l \in \mathcal{X}$ corresponds to the l -th configuration of the input parameters and $\mathbf{y}_l = [y_l^{(1)}, \dots, y_l^{(D)}]^T \in \mathcal{Y}$ is the corresponding output vector.

B. Scalar-Output SVM and LS-SVM Regressions

The above vector-valued learning scenario can be reinterpreted as the problem of learning D independent scalar regressions (i.e., one for each output component), each of them considering the training set $\mathcal{D}^{(i)} = \{(\mathbf{x}_l, y_l^{(i)})\}_{l=1}^L$, such that $\mathcal{D} = \cup_{i=1}^D \mathcal{D}^{(i)}$, in which $y_l^{(i)}$ is i -th component of the output vector associated to the l -th input configuration \mathbf{x}_l . This allows to reformulate the overall vector-valued learning problem in terms of D independent scalar-output regressions, which can be suitably tackled with standard kernel machine approaches, such as the SVM and LS-SVM regressions [4].

Specifically, each training set $\mathcal{D}^{(i)} = \{(\mathbf{x}_l, y_l^{(i)})\}_{l=1}^L$ can be used together with the SVM and LS-SVM regression to train the corresponding surrogate model [15], [16], such that:

$$\mathcal{M}_{SVM/LS-SVM}^{(i)}(\mathbf{x}) = \sum_{l=1}^L \beta_l^{(i)} k^{(i)}(\mathbf{x}_l, \mathbf{x}) + b^{(i)}, \quad (1)$$

where $\beta_l^{(i)}$ and $b^{(i)}$ are the regression coefficients and bias term estimated during the model training and $k^{(i)}(\cdot, \cdot) : \mathbb{R}^{p \times p} \rightarrow \mathbb{R}$ is a scalar kernel function associated to the i -th output component.

Several kernel functions $k(\cdot, \cdot)$ have been proposed in the literature. Hereafter in this paper, we will adopt the Gaussian radial basis function (RBF) kernel, which writes [15]:

$$k(\mathbf{x}_i, \mathbf{x}) = \exp\left(-\frac{\|\mathbf{x}_i - \mathbf{x}\|^2}{2\sigma^2}\right) \quad (2)$$

where σ^2 is the kernel hyper-parameter.

The SVM and the LS-SVM regression share the same dual space representation in (1). However, for the SVM regression the coefficients $\beta_l^{(i)}$ and the bias terms $b^{(i)}$ are estimated by minimizing the ε -insensitive loss function computed between the model predictions and training outputs, while for the LS-SVM regression the above unknowns are estimated as the ones minimizing a squared loss function [15], [16]. A Tikhonov regularizer and its corresponding hyperparameter are used by both methods to suppress over fitting and to improve their generalization on the test set, by minimizing the model variance and thus its sensitivity to the training set [40].

Concerning the training algorithms, the SVM regression is built by numerically solving a quadratic optimization problem [15], and thanks to the ε -insensitive norm, it can lead to a sparse solution in which some of the coefficients $\beta_l^{(i)} = 0$.

On the other hand, the training of the LS-SVM regression can be done in a closed-form as the solution of a linear system of equations. Concerning the model hyperparameters, the SVM regression with Gaussian RBF kernel requires the tuning of 3 hyperparameters: the shape factor σ in (2), the width of the ε -insensitive zone and the regularizer hyperparameters. On the other hand, the LS-SVM regression with Gaussian RBF kernel requires the tuning of 2 hyperparameters: the shape factor σ in (2) and the regularizer hyperparameters. For each regression the above hyperparameters are tuned via cross-validation [40]. The Statistics and Machine Learning Toolbox and the LS-SVMLab Toolbox version 1.8 [41] have been used for the SVM and the LS-SVM regression, respectively.

It is important to remark that this type of modeling scheme for vector-valued problem, based on single-output regressions, requires the training and tuning of the hyperparameters of D regression models, thus compromising its efficiency in regression problems with a large number of output components [42].

C. Vector-Valued KRR

An alternative modeling approach consists of applying a vector-valued formulation of the kernel ridge regression (KRR) which allows to directly account for the vector-valued nature of the regression problem at hand [6], [7], [17]. Specifically, the vector-valued KRR can be directly adopted to train a single vector-valued surrogate model $\mathcal{M}_{KRR} : \mathcal{X} \rightarrow \mathcal{Y}$, which according to the represented theorem for vector-valued regression problems presented in [44], writes:

$$\mathcal{M}_{KRR}(\mathbf{x}) = \sum_{l=1}^L \mathbf{K}(\mathbf{x}, \mathbf{x}_l) \mathbf{c}_l, \quad (3)$$

where $\mathcal{M}_{KRR}(\mathbf{x}) = [\mathcal{M}_{KRR}^{(1)}(\mathbf{x}), \dots, \mathcal{M}_{KRR}^{(D)}(\mathbf{x})]^T$ is a vector collecting the model prediction for any $\mathbf{x} \in \mathcal{X}$, $\mathbf{K}(\cdot, \cdot) : \mathbb{R}^{p \times p} \rightarrow \mathbb{R}^{D \times D}$ is a multi-output kernel matrix and $\mathbf{c}_l = [c_{1,l}, \dots, c_{D,l}]^T \in \mathbb{R}^D$ are column vectors collecting the regression unknowns.

A separable structure consisting of the product of scalar kernel function is considered for the matrix kernel function $\mathbf{K}(\mathbf{x}, \mathbf{x}')$ [17], such that:

$$[\mathbf{K}(\mathbf{x}, \mathbf{x}')]_{[d,d']} = k_{\mathbf{x}}(\mathbf{x}, \mathbf{x}') k_o(d, d'), \quad (4)$$

where $k_{\mathbf{x}}$ and k_o are scalar kernels acting independently on the input space (i.e., $k_{\mathbf{x}} : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$) and on the output dimensions (i.e., $k_o : \{1, \dots, D\} \times \{1, \dots, D\} \rightarrow \mathbb{R}$). Without loss of generality, the Gaussian RBF kernel in (2) will be used hereafter for the kernel $k_{\mathbf{x}}$ and k_o , respectively.

For the considered model structure, the regression coefficients collected in the vectors \mathbf{c}_l can be estimated in a closed-form via the solution of a discrete-time Sylvester equation (additional mathematical details are provided in [6]), which writes:

$$\mathbf{K}_{\mathbf{x}} \mathbf{C} \mathbf{B} + \lambda \mathbf{C} = \mathbf{Y}, \quad (5)$$

where λ is the hyperparameter associated to the Tikhonov regularizer, \mathbf{K}_x is a $L \times L$ Gram matrix computed from the input samples $\{\mathbf{x}_l\}_{l=1}^L$ (i.e., $[\mathbf{K}_x]_{ij} = k_x(\mathbf{x}_i, \mathbf{x}_j)$), \mathbf{B} is a $D \times D$ Gram matrix computed on the output dimensions $\{1, \dots, D\}$ (i.e., $[\mathbf{B}]_{ij} = k_o(d_i, d_j)$), $\mathbf{C} = [\mathbf{c}_1, \dots, \mathbf{c}_L]^T \in \mathbb{R}^{L \times D}$ is a matrix collecting the model unknowns and $\mathbf{Y} = [\mathbf{y}_1, \dots, \mathbf{y}_L]^T$ is a $L \times D$ matrix associated to the training output.

Thanks to the properties of the Kronecker product, the above matrix equation can be vectorized and reformulated in terms of a standard linear system with (LD) equations in (LD) unknowns [43] with a computational cost proportional to $\mathcal{O}(L^3 D^3)$ for a plain inversion or to $\mathcal{O}(KL^2 D^2)$, where K is the number of iteration, for a conjugate gradient descent algorithm [6]. On the other hand, this paper will use a more efficient implementation based on a diagonalization procedure, inspired by [45], for which the computational cost for the model training reduces from $\mathcal{O}(L^3 D^3)$ to $\mathcal{O}(L^3 + D^3 + L^2 D + LD^2)$, thus leading to beneficial effect on the training time when the product (LD) is large (additional details can be found in [46]).

Different from modeling strategies based on scalar-output regressions in Sec. IV-B, the training of the proposed implementation of the vector-valued KRR requires the tuning of 3 hyperparameters only. Such tuning is done via a 3-fold cross validation. Moreover, the vector-valued formulation allows to learn possible correlations in both the input and output dimensions, thus improving the model reliability and robustness to noise.

V. NUMERICAL RESULTS

The simulation setup described in Sec. III was used to generate the training and test sets used to construct and assess the accuracy of a surrogate models constructed via the SVM, LS-SVM and vector-valued KRR regressions presented in Sec. IV. These training and test sets were generated by randomly varying the considered 11 parameters defining the link, according to the range of variation discussed in Sec. II, via a latin hypercube sampling (LHS) scheme [47]. For each set of parameters, the received differential voltage $v_d(t)$ was recorded and the eye aperture was computed according to the procedure in Sec. III. All performance figures in the present section were computed using 5000 test samples, i.e. 5000 different responses of the received voltage v_d along with its corresponding eye plot and inner polygon. Also in this case, the input configurations of the test were generated by randomly varying the considered 11 parameters of the link according to the range of variation discussed in Sec. II via a LHS scheme.

Table I provides a quantitative picture of the accuracy of the considered three surrogate modeling approaches for an increasing number of training samples L from 60 to 300 (see first column). Both the eye apertures in mV , computed at the different location pairs labeled from one to seven in Fig. 2, and the eye width in ps corresponding to the eighth pair in the same figure are considered (second column). The remaining columns collect the average absolute errors computed as the mean absolute deviation of the eye apertures in mV and eye width in ps predicted by the considered surrogate

TABLE I
ABSOLUTE AVERAGE ERROR COMPUTED FROM THE PREDICTIONS OF THE SURROGATE MODELS BUILT VIA THE REGRESSION TECHNIQUES PRESENTED IN SEC. IV FOR AN INCREASING NUMBER TRAINING SAMPLE (I.E., $L = 60, 150,$ AND 300) ON A TEST SET WITH 5000 EYE REALIZATIONS.

	Methods	SVM	LS-SVM	Vector-Valued KRR
L	pairs	Ave Error	Ave Error	Ave Error
60	1 _u -1 _d (mV)	6.21	6.18	5.97
	2 _u -2 _d (mV)	7.49	7.25	6.73
	3 _u -3 _d (mV)	6.65	6.68	6.91
	4 _u -4 _d (mV)	7.49	7.17	7.29
	5 _u -5 _d (mV)	10.13	6.80	6.68
	6 _u -6 _d (mV)	4.03	3.83	3.79
	7 _u -7 _d (mV)	4.25	4.07	4.03
	8 _r - 8 _l (ps)	3.62	3.22	3.34
150	1 _u -1 _d (mV)	4.73	4.61	4.52
	2 _u -2 _d (mV)	4.16	4.27	4.20
	3 _u -3 _d (mV)	4.93	4.92	4.99
	4 _u -4 _d (mV)	9.99	4.86	4.75
	5 _u -5 _d (mV)	4.22	3.78	3.79
	6 _u -6 _d (mV)	3.06	2.72	2.73
	7 _u -7 _d (mV)	2.72	2.66	2.65
	8 _r - 8 _l (ps)	2.67	2.63	2.67
300	1 _u -1 _d (mV)	3.50	3.44	3.51
	2 _u -2 _d (mV)	3.25	3.19	3.13
	3 _u -3 _d (mV)	3.75	3.71	3.72
	4 _u -4 _d (mV)	4.05	3.96	4.03
	5 _u -5 _d (mV)	3.08	2.96	2.99
	6 _u -6 _d (mV)	2.38	2.40	2.33
	7 _u -7 _d (mV)	2.32	2.31	2.20
	8 _r - 8 _l (ps)	2.23	2.15	2.12

models, and the corresponding ones obtained from the 5000 reference eye realizations in the test set. Bold text is used to highlight the lowest errors among the different modeling methods. This comparison clearly highlights the capability of all the considered surrogate models to learn the actual information provided by the training set. Among them, in most of the considered modeling scenarios, the vector-valued KRR shows an improved accuracy compared to the SVM and LS-SVM regression, thanks to its capability of learning possible correlation among the output components.

Moreover, as shown in Fig. 3, the vector-valued KRR approach also offers a faster training time with respect to the other plain scalar-output kernel regressions, since its training CPU time seems to be less affected by the number of training samples (i.e., L). It is important to remark that the CPU times reported in Fig. 3 refer to the training time only, and do not

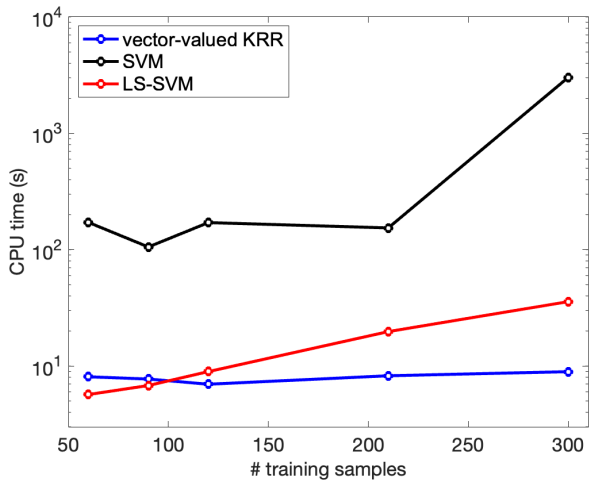


Fig. 3. Comparison of the training time of the proposed regression techniques for an increasing number of training samples. The CPU times do not include the computational cost for the generation of the training set.

include the computational cost relative to the generation of the training set.

The generation of 300 training samples required approximately 11 hours. This expensive data-collection phase must be carried out once. After the model training, its evaluation on the 5000 test samples required few seconds, while the corresponding SPICE simulations required 4 days.

Figure 4 shows all the possible eye apertures computed for the test samples (see gray cloud) superimposed by the best, median and worst profiles of the inner area computed using the reference responses (top panel, black lines) and, respectively, the proposed vector-valued KRR surrogate model (bottom panel, blue lines). The median curve corresponds to the 50% threshold between all the larger and the smaller eye apertures. This additional and less conventional performance figure stresses the flexibility of the proposed approach in possibly providing the information of the probability (e.g., in terms of a quantiles) associated to a given eye aperture.

Similarly, Fig. 5 plots three possible eye apertures defined by their corresponding polygons associated to three sets of uncertain parameters. The figure compares the prediction obtained using the proposed vector-valued KRR model trained with 300 training samples with the reference profiles, thus highlighting the very good accuracy of the proposed surrogate modeling approach.

As an additional and final validation, the eye quality is assessed by a single scalar quantity such as the eye aperture computed from the proposed polygonal approximation of the inner eye area. For the same test case, Fig. 6 compares the probability density functions (PDFs) computed from the same 5000-sample test set, used as reference, with the corresponding ones obtained from the surrogate model built via the LS-SVM regression, the SVM regression and the proposed vector-valued KRR by using $L = 300$ samples. The three panels show the PDFs associated to the eye area (left panel), eye height computed in the region of the fourth polygonal edge pairs of Fig. 2, i.e., $(4_u) - (4_d)$ (central panel) and eye width,

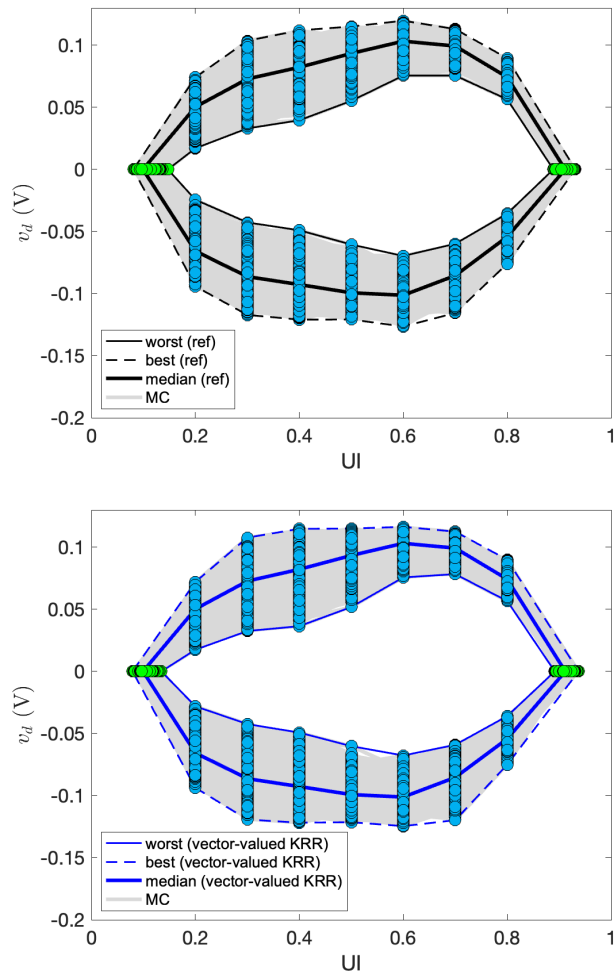


Fig. 4. Data link analysis carried out by computing the best, the worst (dashed and solid thin lines) and the median (thick) inner eye aperture. The above eye apertures are superimposed to the complete set of eye diagrams obtained for the test set (light gray cloud). The blue and the green clouds of circles play the same role of the corresponding colored circles in Fig. 2. Top panel: reference; bottom panel: vector-valued KRR.

again defined between pairs $(8_r) - (8_l)$ (right panel). The eye area is computed as briefly outlined in the fourth item of the procedure described in the appendix. The above comparison highlights a good agreement among the PDFs predicted by the proposed surrogate models and the ones computed from 5000 test samples, especially on the tails of the distributions.

VI. CONCLUSIONS

The main novelty of the present paper is the stochastic time-domain mapping approach. For a given eye pattern, the inner eye is mapped using a suitable polygonal approximation. After an initial training stage, a parametric surrogate model is built, predicting the effect of system uncertainties on the shape of this polygon. This allows designers to effectively compute the metric of their choice or use eye-masks in a stochastic context. The procedure was demonstrated in the case of a flexible data link for wearable applications, with uncertain electrical and geometrical parameters, using machine learning regression to build the surrogate model. Data was collected

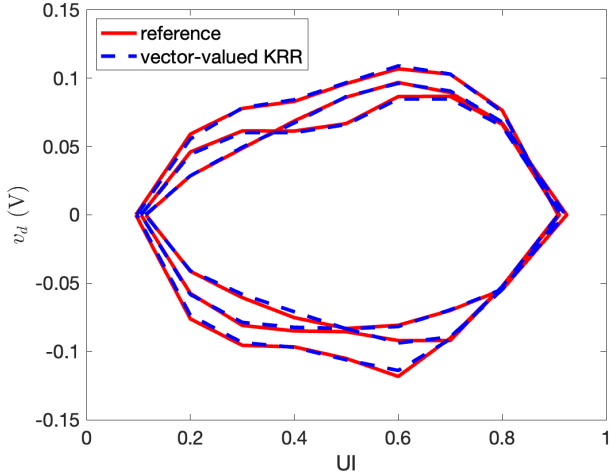


Fig. 5. Eye aperture computed for three sets of uncertain data link parameters. The eye opening polygons obtained by the proposed vector-valued KRR model are compared to the reference ones.

by simulating the link in a differential configuration operating at 2 Gbps. Three types of regressions were used, showing that for the problem at hand, a vector formulation of the so-called kernel ridge regression is the preferable choice. A nice additional feature is that the latter naturally embeds the possible correlation which exists among the vertices of the eye polygon. This also has a beneficial effect in terms of training time, model reliability and robustness.

Stochastic mapping takes variability analysis one step further. It is of particular interest for applications where either the level of uncertainties or their impact is particularly high. These include flexible or structural electronics, ultra-low power systems, systems designed to operate in various hostile environments, but also very-low cost applications where high tolerances are a consequence of financial considerations.

APPENDIX

The proposed algorithm for the computation of the eye aperture through a polynomial approximation is described below. The procedure is outlined, including the essential steps using a metalanguage description and a MATLAB-like code. It is assumed that the sampled response of $v_d(t)$ is stored in the vector \mathbf{v}_d . It collects the values of the received differential voltage at the time samples stored in vector \mathbf{t} . Also, due to the differential communication scheme, a zero-threshold ($\text{threshold}=0$ in the code) is assumed for computing the state (i.e., bit) transitions.

The main steps of the algorithm are:

- 1) the estimated crossing times are stored in vector \mathbf{t}_z and are determined via linear interpolation:

```
>> vd = vd-threshold;
>> iz = find(diff(sign(vd)));
>> a = (vd(iz)-vd(iz-1))./(t(iz)-t(iz-1));
>> tz = (-vd(iz)+a.*t(iz))./a;
```

- 2) the time axis and the crossing times are wrapped into the unit interval defined by the bit time (TBIT); also, the jitter width (JITW) is computed by considering

the largest and the smallest wrapped (i.e., normalized) transition times:

```
>> tzoffset = mod(tz(1),TBIT);
>> tzw = mod(tz-tzoffset,TBIT);
>> JLEFT = TBIT-min(tzw(tzw>TBIT/2));
>> JRIGHT = max(tzw(tzw<TBIT/2));
>> JITW = JLEFT+JRIGHT;
```

- 3) within the unit interval, a number of sampling points is set (e.g., POINTS=[0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8]) and the minimum and the maximum values of the received signal observed at these sampling points are computed, $v_d(t = (\text{POINTS}(kk) + (n-1)) * \text{TBIT})$. In the above notation, the index kk varies from one to the max number of items in vector POINTS, and n ranges from one to the maximum number of bits composing the bitstream. The procedure in this step is suitably modified to avoid probing the differential signal in the jitter region. It is important to point out that the above mentioned max and min values define, for a given point in the unit interval, the position of the vertical eye height (e.g., see the blue circles in Fig. 2). Also, the green circles in on the left and on the right side of the eye correspond, in the x -axis, to $\text{JRIGHT}/\text{TBIT}$ and $1-\text{JLEFT}/\text{TBIT}$, respectively;
- 4) based on the inner polygonal shape built in the previous steps, different eye parameters (such as the eye width, height and area) can be readily computed. Among the previous parameters, the area can be computed via embedded functions such as `polyarea` in MATLAB or via the superposition of the 2D basic shapes (i.e., triangles or trapezoids) defined by the different vertices of the inner eye polygon like the one shown in Fig. 2.

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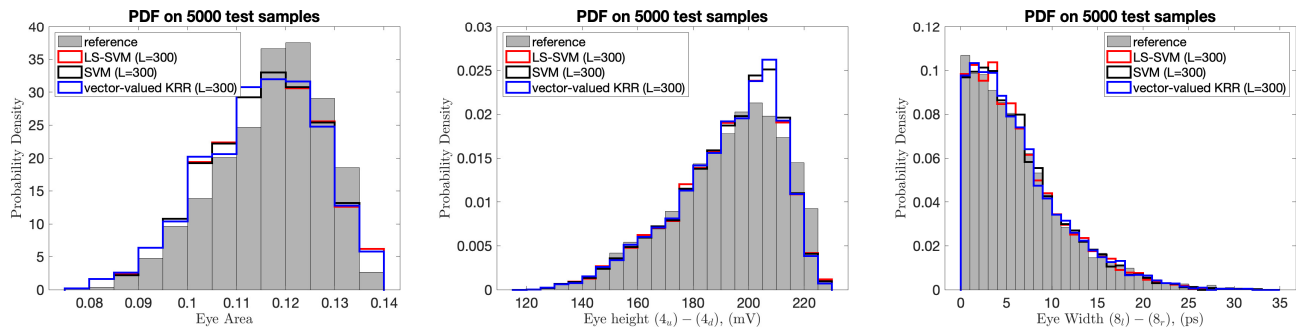


Fig. 6. Comparison between the PDFs of the eye area, height and width computed from the predictions of a surrogate model built via the LS-SVM regression, the LS-SVM regression and the vector-valued KRR with $L = 300$ training samples and the corresponding ones calculated on 5000 test samples.

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