

New Valid Inequalities for the Two-Echelon Capacitated Vehicle Routing Problem

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# Unveiling the Principal Modes of Human Upper Limb Movements through Functional Analysis

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The rich variety of human upper limb movements requires an extraordinary coordination of different joints according to specific spatio-temporal patterns. However, unveiling these motor schemes is a challenging task. Principal components have been often used for analogous purposes, but such an approach relies on hypothesis of temporal uncorrelation of upper limb poses in time. To overcome these limitations, in this work, we leverage on functional principal component analysis (fPCA). We carried out experiments with 7 subjects performing a set of most significant human actions, selected considering state-of-the-art grasp taxonomies and human kinematic workspace. fPCA results show that human upper limb trajectories can be reconstructed by a linear combination of few principal time-dependent functions, with a first component alone explaining around 60/70% of the observed behaviors. This allows to infer that in daily living activities humans reduce the complexity of movement by modulating their motions through a reduced set of few principal patterns. Finally, we discuss how this approach could be profitably applied in robotics and bioengineering, opening fascinating perspectives to advance the state of the art of artificial systems, as it was the case of hand synergies.

**Keywords:** upper limb kinematics, motor control, daily living activities, functional analysis, human-inspired robotics

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## 1. INTRODUCTION

Human hands represent an extraordinary tool to explore and interact with the external environment. Not surprisingly, a lot of studies have been devoted to model how the nervous system can cope with the complexity of hand sensory-motor architecture (Mason et al., 2001; Todorov and Ghahramani, 2004; Zatsiorsky and Latash, 2004; Thakur et al., 2008; Gabiccini et al., 2013; Santello, 2014). These studies have led to the definition of the so-called synergies, broadly intended as covariation patterns that can be represented at different levels (Santello et al., 2016). More specifically, at the level of motor units, neural activation shows a synergistic control in the time and/or frequency domain (Santello, 2014). At the muscle level, different works explored patterns of muscle activity whose timing and/or amplitude modulation enables the generation of different movements, see d'Avella and Lacquaniti (2013) for a review. Synergies have also been identified and defined as covariation patterns of joint angles, e.g., hand postural synergies (Santello et al., 1998, 2013; Mason et al., 2001), or covariation patterns among digit forces [for a review see Zatsiorsky and Latash (2004)]. However, to correctly understand human manipulation, in addition to hand analysis, the role of whole upper limb movements should be also taken into account. Indeed, the whole upper limb motions are devoted to guide and optimize position and orientation of the hand w.r.t. external targets.

For these reasons, in addition to many works devoted to analyze hand behavior, it is also possible to find studies modeling human upper limb motor workspace, either from a kinematic point of view, or from a muscular or neural point of view. In Heidari et al. (2016), the authors studied the kinematic movements of upper limb during selected tasks in order to compare stroke patients and normal subjects. In Butler et al. (2010), the authors developed a quantitative method to assess upper limb motor deficits in children with cerebral palsy using three-dimensional motion analysis during the reach and grasp cycle. Other papers studied muscular synergies in upper limb activities, as in d'Avella and Tresch (2002), where the authors introduced a model based on combinations of muscle time-varying synergies, and in d'Avella et al. (2006), where authors recorded electromyographic activity from shoulder and arm muscles during point-to-point movements. As for hand synergies, whose robotic applications are reviewed in Santello et al. (2016), synergies have also been applied to movement generation for virtual arms (Fu et al., 2013) as well as myocontrol of a multi-DoF planar robotic arm using muscle synergies (Lunardini et al., 2015). However, none of the previous studies considered the dynamic aspects of human upper limb motion, i.e., that different temporal evolutions and shapes of upper limb joints trajectories would result in different final hand poses.

Typical approaches based on principal component analysis are not suitable in this case because of the underlying hypothesis of temporal uncorrelation of upper limb poses in time. For this reason, to achieve this goal, we propose to use for the first time functional principal component analysis (fPCA) to study upper limb motions. fPCA is a statistical method for investigating dominant modes of variation of functional data in time and has been widely used in one-dimensional or multi-dimensional time series analysis in chemistry, weather phenomena, and medicine (Aguilera et al., 1999; Gokulakrishnan et al., 2006; Dai et al., 2013). The interested reader in functional data analysis could refer to Ramsay and Silverman (2002), Ramsay (2006), and Ramsay et al. (2009). In human movement studies, this method has been used to explore the presence of variations in repetitions of a specific task, e.g., in Ryan et al. (2006), an analysis of knee joint kinematics in the vertical jump was performed. In Coffey et al. (2011), fPCA was used to analyze a bio-mechanical dataset examining the mechanisms of chronic Achilles tendon injury and the functional effects of orthoses by comparing injured and healthy subjects. In Dai et al. (2013), fPCA was used in conjunction with PCA for the analysis of grasping motion. In this work, a new analysis of upper limb movements by fPCA is proposed to provide a description of the kinematic trajectories as combination of functional principal components (fPCs).

The choice to use fPCA as main data analysis tool is motivated by the fact that it allows to include some important features of the signal, such as shape and time dependence, which cannot be taken into account by other simpler data dimensionality reduction techniques (e.g., principal component analysis). To achieve this goal, we propose an experimental setup for studying upper limb movements, based on a Motion Capture (MoCap) system (*Phase Space*<sup>®</sup>). Using this tool, we carried out a series of experiments with human considering a comprehensive dataset of daily living activities (ADLs) and grasping/manipulation actions.

These actions were selected relying on the study of grasping taxonomies (Cutkosky, 1989; Feix et al., 2016), and considerations on human upper limb movement workspace (Lenarcic and Umek, 1994; Abdel-Malek et al., 2004; Perry et al., 2007). Our analysis has led to the reduction of complexity of upper limb trajectories by describing these as linear combinations of few principal functions (or modes). Implications for robotics are also discussed.

## 2. EXPERIMENTAL PROTOCOL AND SETUP

### 2.1. A Set of Daily Living Tasks

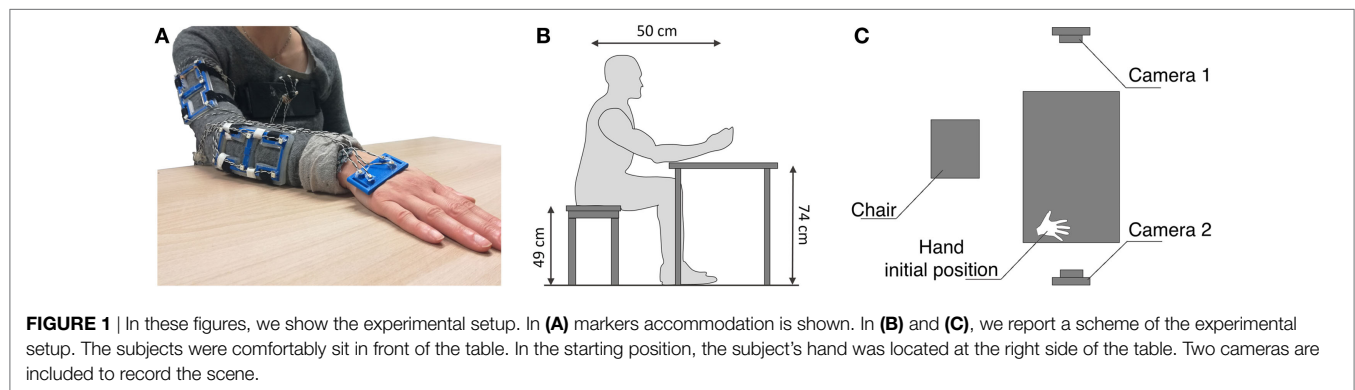
In order to develop a comprehensive study of human upper limb movements, one of the key features for the generation of a valid dataset is the definition of a set of meaningful actions (Santello et al., 1998; Mason et al., 2001; Todorov and Ghahramani, 2004; Vinjamuri et al., 2010). For this reason, we selected a set of movements driven by the study of grasping taxonomies (Cutkosky, 1989; Feix et al., 2016), and the analysis of human upper limb movement workspace (Lenarcic and Umek, 1994; Abdel-Malek et al., 2004; Perry et al., 2007). The output of this selection resulted in a set of 30 different actions, divided into intransitive, transitive, and tool-mediated actions to avoid bias due to the affordances of the objects used for the grasp investigation. Indeed, as Cubelli et al. (2000) suggested starting from apraxia investigation and Handjaras et al. (2015) confirmed with cortical imaging, different movements are generated by different cortical activations, because require different motor schema, based on the type of interaction with the environment. These movements can be classified into three classes, according to the presence or absence of an object and, if the object is present, on the approach with it: intransitive class, which collects actions that does not need the use of an object; transitive class, which collects actions that introduces the use of an object; and tool-mediated class, which collects actions where an object is used to interact with another one. Tasks are meant to be executed three times with dominant hand, the subject seating on a chair, with the objects placed on a frontal table at a fixed distance. At the end of the task, the subject returned to the starting point. The complete list of actions is reported in **Table 1**.

### 2.2. An Experimental Setup for Data Acquisition

We focused on kinematic recordings, which were achieved using a commercial system for 3D motion tracking with active markers (*Phase Space*<sup>®</sup>). Ten stereo-cameras working at 480 Hz tracked 3D position of markers, which were fastened to supports rigidly attached to upper limb links. In this manner, 20 markers were accommodated on the upper limb so that the distance between elements of each support was fixed. Supports were suitably designed for these experiments and printed in ABS (see **Figure 1A**). The acquisition was implemented through a custom application developed in C++, employing Boost libraries (Schäling, 2011) to enable the synchronization between Phase Space data and other sensing modalities, such as force/torque sensors and EEG, and the Phase Space OWL library to get the optical tracking system data.

**TABLE 1** | Protocol actions.

#	#Cutkosky	Class	Description
1		Intransitive	Ok gesture (lifting hand from the table)
2		Intransitive	Thumb down (lifting hand from the table)
3		Intransitive	Exultation (extending the arm up in the air and keeping it in with closed fist)
4		Intransitive	Hitchhiking (extending the arm along the frontal plane, laterally, parallel to the floor, with extended elbow, closed fist, extended thumb)
5		Intransitive	Block out sun from own face (with open hand, touching the face with the palm and covering the eyes)
6		Intransitive	Greet (with open hand, moving wrist) (three times)
7		Intransitive	Military salute (with lifted elbow)
8		Intransitive	Stop gesture (extending the arm along the sagittal plane, parallel to the floor, with extended elbow, open palm)
9		Intransitive	Pointing (with index finger) of something straight ahead (with outstretched arm)
10		Intransitive	Silence gesture (bringing the index finger, with the remainder of the hand closed, on the lips)
11	2	Transitive	Reach and grasp a small suitcase (placed along own frontal plane) from the handle, lift it and place it on the floor (close to own chair, along own sagittal plane)
12	3	Transitive	Reach and grasp a glass, drink for 3 s (stop signal by the examiner) and place it in the initial position
13	4	Transitive	Reach and grasp a phone receiver (placed along own sagittal plane), carry it to own ear for 3 s (stop signal by the examiner) and place it in the initial position
14	6	Transitive	Reach and grasp a book (placed overhead on a shelf), put in on the table and open it (from right side to left side)
15	8	Transitive	Reach and grasp a small cup from the handle (2 fingers + thumb), drink for 3 s (stop signal by the examiner) and place it in the initial position
16	11	Transitive	Reach and grasp an apple, mimic biting, and put it in the initial position
17	12 13	Transitive	Reach and grasp a hat (placed on the right side of the table) from its top and place it on own head
18	12	Transitive	Reach and grasp a cup from its top, lift it and put it on the left side of the table
19	15	Transitive	Receive a tray from someone (straight ahead, with open hand) and put it in the middle of the table
20	16	Transitive	Reach and grasp a key in a lock (vertical axis), extract it from the lock and put it on the left side of the table
21	1	Tool mediated	Reach and grasp a bottle, pour water into a glass, and put the bottle in the initial position
22	2 3 4	Tool mediated	Reach and grasp a tennis racket (placed along own frontal plane), and play a forehand (the subject is still seated)
23	5	Tool mediated	Reach and grasp a toothbrush, brush teeth (horizontal axis, one time on left side one time on right side), and put the toothbrush inside a cylindrical holder (placed on the right side of the table)
24	6	Tool mediated	Reach and grasp a laptop and open the laptop (without changing its position) (4 fingers + thumb)
25	7 8 9	Tool mediated	Reach and grasp a pen (placed on the right side of the table) and draw a vertical line on the table (from the top to the bottom)
26	7	Tool mediated	Reach and grasp a pencil (placed along own frontal plane) (3 fingers + thumb) and put it inside a squared pencil holder (placed on the left side of the table)
27	9	Tool mediated	Reach and grasp a tea bag in a cup (1 finger + thumb), remove it from the cup, and place it on the table on the right side of the table
28	10	Tool mediated	Reach and grasp a doorknob (disk shape), turn it clockwise, and counterclockwise and open the door
29	13	Tool mediated	Reach and grasp a tennis ball (with fingertips) and place it in a basket placed on the floor (close to own chair)
30	14	Tool mediated	Reach and grasp a cap (2 fingers + thumb) of a bottle (held by left hand), unscrew it, and place it overhead on a shelf



Seven adult right-handed subjects (5 males and 2 females, aged between 20 and 30) performed the experiment. Each task was repeated three times in order to increase the robustness of collected data. The experimenter gave the starting signal to subjects. In the instructions, the experimenter emphasized that the whole movement should be performed in a natural fashion. The object order was randomized for every subject. Each subject performed

the whole experiment in a single day. No subject knew the purpose of the study, and had no history of neuromuscular disorders. Each participant signed an informed consent to participate in the experiment, and the experimental protocol was approved by the Institutional Review Board of University of Pisa, in accordance with the declaration of Helsinki. The complete experimental setup is reported in **Figures 1B,C**. Moreover, we used two

cameras (Logitech hd 1080p) to record the scene of the experiments in order to visually compare the real and the reconstructed movement.

### 3. MOTION IDENTIFICATION

#### 3.1. Modeling of Upper Limb Kinematics

An accurate description of human upper limb is challenging due to the high complexity of the kinematic structure, e.g., for axis location and direction, which are usually time varying. In order to explore the system complexity, the interested reader can refer to Maurel and Thalmann (2000) and Holzbaur et al. (2005). In this work, we used a trade-off between complexity and accuracy taking inspiration from Benati et al. (1980). This allows to get an acceptable computational time, still maintaining a good level of explanation of physical behavior. Taking inspiration from Gabiccini et al. (2013), we adopted a model with 7 degrees of freedom (DoFs) and 3 invariable shape links. Joints angles are defined as  $q_1, \dots, q_7$ :  $q_1$  is associated with the shoulder abduction–adduction;  $q_2$  is associated with the shoulder flexion–extension;  $q_3$  is associated with the shoulder external–internal rotation;  $q_4$  is associated with the elbow flexion–extension;  $q_5$  is associated with the elbow pronation–supination;  $q_6$  is associated with the wrist abduction–adduction;  $q_7$  is associated with the wrist flexion–extension. In **Figure 2A**, a scheme of the model is reported.

#### 3.2. Model Parameters

In order to describe the forward kinematics of the arm, 5 different reference systems was defined:  $S_{ref}$ , centered in  $O_{ref}$ , fixed to the

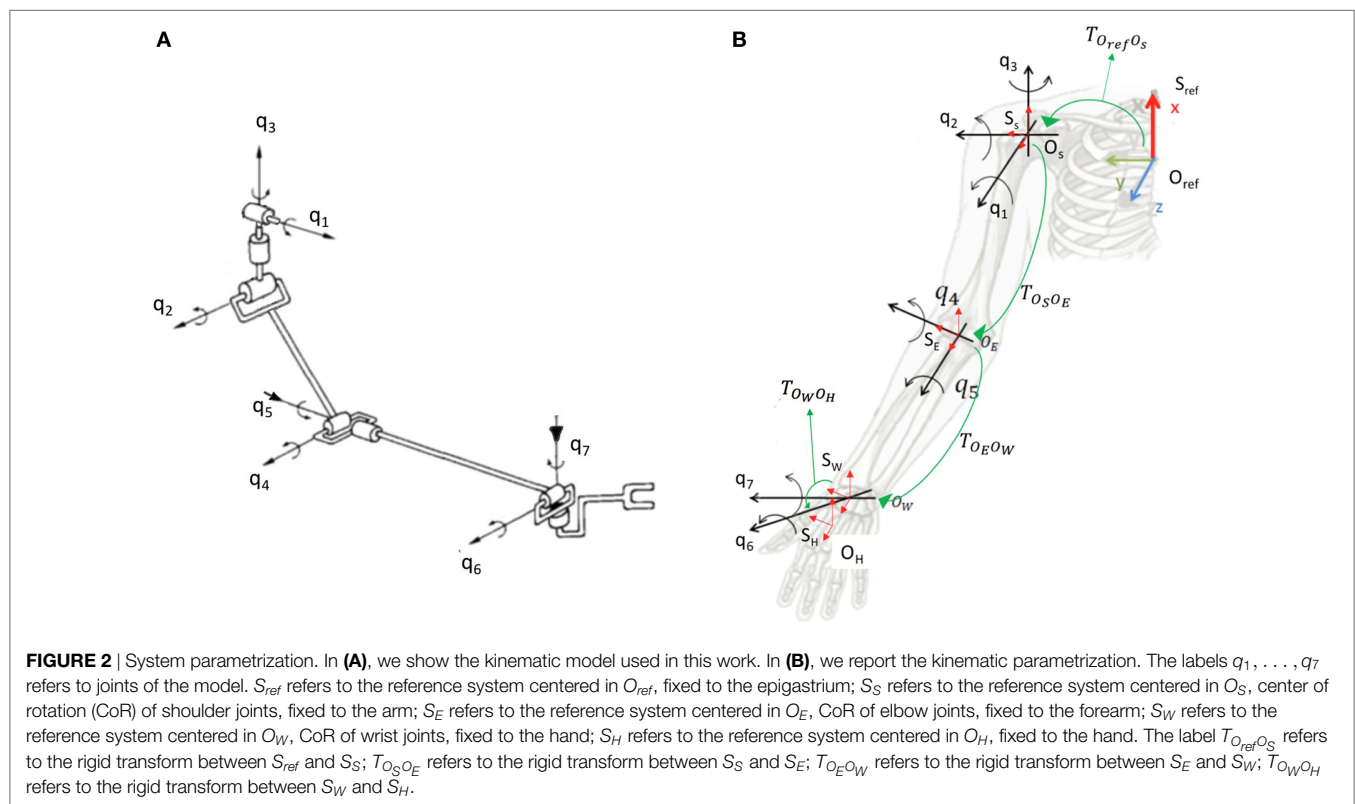
epigastrium;  $S_S$ , centered in  $O_S$ , Center of Rotation (CoR) of shoulder joints, fixed to the arm;  $S_E$ , centered in  $O_E$ , CoR of elbow joints, fixed to the forearm;  $S_W$ , centered in  $O_W$ , CoR of wrist joints, fixed to the hand;  $S_H$ , centered in  $O_H$ , fixed to the hand. The rigid transform between  $S_{ref}$  and  $S_S$  is  $T_{O_{ref}O_S}$ ; the rigid transform between  $S_S$  and  $S_E$  is  $T_{O_S O_E}$ ; the rigid transform between  $S_E$  and  $S_W$  is  $T_{O_E O_W}$ ; the rigid transform between  $S_W$  and  $S_H$  is  $T_{O_W O_H}$ . The defined reference systems are shown in red in **Figure 2B**. Green arrows indicate rigid transforms from a reference system and the next one in the kinematic chain. To parameterize the  $i$ -th segment, we use the *product of exponentials* (POE) formula (Brockett, 1984):

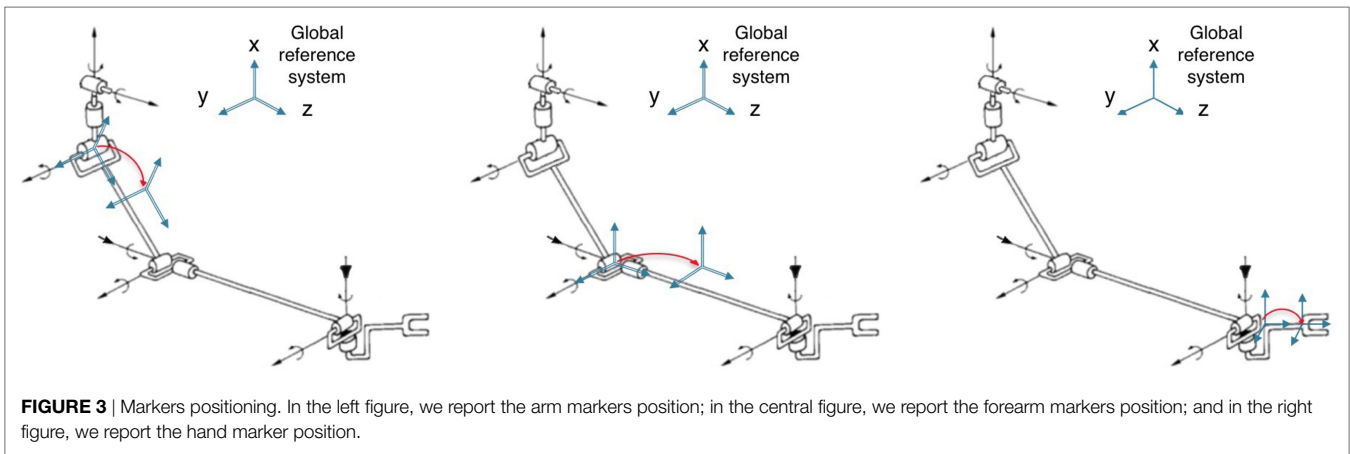
$$g_{O_{ref}O_j}(\theta) = \left[ \prod_{k=1}^j e^{\hat{\xi}_k \theta_k} \right] g_{O_{ref}O_j}(0)$$

where  $\hat{\xi}_k$  are the twists of the joints defining the kinematic chain,  $\theta = [\theta_1, \dots, \theta_k, \dots, \theta_j]^T$  are the exponential coordinates of the second kind for a local representation of SE(3) (Special Euclidean group,  $4 \times 4$  rototranslation matrices) for the  $j$ -th link, and  $g_{O_{ref}O_j}(0)$  is the initial configuration. For further details, the interested reader can refer to Gabiccini et al. (2013).

#### 3.3. Markers Modeling

Links movements were tracked by fastening optical active markers to upper limb links. Markers positioning is inspired by Biryukova et al. (2000). In order to improve tracking performance, a redundant configuration of marker was used, in particular 4 markers fixed to the chest, 6 markers fixed to the lateral arm, 6 markers





fixed to the dorsal forearm, and 4 markers fixed to the hand dorsum. A picture showing marker distribution is reported in **Figure 1A**. The position of each marker can be calculated as rigid transform w.r.t. the center of the corresponding support. The supports kinematic can be described as a rigid transform from the link reference system to the support reference system, as depicted in **Figure 3**.

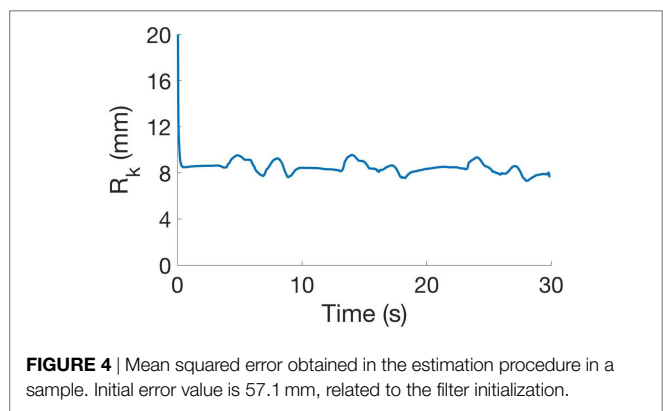
The model is completely parameterized using 14 parameters (different for each subject) collected in a vector  $p_G$ : bones length (arm and forearm, 2 parameters); rigid transform from epigastrium to the shoulder CoR (3 parameters); rigid transform from shoulder CoR to the center of arm marker support (3 parameters); rigid transform from elbow CoR to the center of forearm marker support (3 parameters); and rigid transform from wrist CoR to the center of hand marker support (3 parameters). The parameter vector  $p_G$  was calibrated for each subject. Given  $p_G$ , the upper limb pose is described by 7 joints angles  $[q_1, \dots, q_7]^T$  collected in a vector  $x$ .

### 3.4. Model Calibration and Angles Estimation

As previously mentioned, the parameters of the kinematic model must be adapted for the specific subject that performs the experiments. The optimal parameters were obtained by solving a constrained least-squares minimization problem:

$$(x^*, p_G^*) = \arg \min_{x_k \in D_x, p_G \in D_p} \frac{1}{2} \sum_{k=1}^{N_p} r_k^T r_k.$$

The residual function  $r_k$  is calculated as  $r_k(x_k, p_G) = y_k - f(x_k, p_G)$ , where:  $y_k$  is the marker position vector measured with Phase Space;  $x_k$  is the vector of estimated joint angles;  $p_G$  is the vector of model kinematic parameters;  $D_x$  is the upper limb joints range of motion;  $D_p$  is the variation around a preliminary estimation of parameters performed with manual measurements; and  $f(x_k, p_G)$  is the estimated positions vector of markers using the forward kinematics. The vector of measures  $y_k$  and the vectors of estimations  $f(x_k, p_G)$  can be obtained by concatenating the measures of marker positions and estimations at different time frames. To obtain an effective calibration output, the selected frames for the



calibration procedure must consider different poses of the kinematic chain. For the experiments reported in this work, we had  $r_k$  normalized w.r.t. the dimension of  $y_k$  equal to  $15.30 \pm 16.25$  mm; as an example we show in **Figure 4** the values of  $r_k$  in a sample task. Taking inspiration from Gabiccini et al. (2013), the calibrated model was then used to identify the joints angles using an Extended Kalman Filter (EKF). Indeed, the model can be considered as an uncertain noisy process where at time frame  $k$  the joints angle vector  $x_k$  is the state of the process,  $y_k$  is the markers position vector,  $w_k$  and  $v_k$  are process and observation zero mean Gaussian noises, with covariance  $Q_k$  and  $R_k$ , respectively, and  $f(x_k)$  is the forward kinematics. The system can be described using the following equations:

$$\begin{cases} x_k = x_{k-1} + w_k \\ y_k = f(x_k) + v_k \end{cases} \quad (1)$$

Given the state at time frame  $k-1$ , the state at time  $k$  was obtained using a 2-steps procedure: *prediction* of the future state  $\hat{x}_{k|k-1} = \hat{x}_{k-1}$ ; *update* of the state estimated in the first step by calculating  $\hat{x}_{k|k} = \hat{x}_{k|k-1} + K_k \tilde{r}_k$ . The correction amount of the state prediction is the product between the residual values vector  $\tilde{r}_k = y_k - f(\hat{x}_{k|k-1})$  and the Kalman Gain  $K_k$ . This gain is calculated as product between the covariance matrix estimation of the predicted state  $P_{k|k-1}$ , the jacobian matrix, i.e.,  $H_k = \frac{\partial f(x)}{\partial x}$ , and the inverse matrix of the residual covariance.

### 3.5. Experimental Results

The performance of the estimation tool for time frame  $k$  can be evaluated by calculating the mean squared error (MSE)  $R_k$  as

$$R_k = \frac{1}{N_{\text{markers}}} \|(y_k - f(\hat{x}_{k|k}))\|$$

where  $N_{\text{markers}}$  is the number of markers,  $y_k$  is the marker positions vector, and  $f(\hat{x}_{k|k})$  is the vector of markers estimated positions using the joint angles calculated with the EKF. Typical values of  $R_k$  are  $\approx 1$  cm, with a mean error for hand and forearm markers of  $\approx 0.5$  cm and a mean error for arm markers of  $\approx 1.8$  cm. Identified angles was used to reconstruct the movements, which were represented using a virtual model of upper limb suitably implemented in MatLab for these reconstructions. The reconstructions were used for a visual check w.r.t. the real movement recorded with cameras. This allows to verify the human-likeness of the reconstructed movement.

## 4. DATA ANALYSIS

The goal of this work is the study of functional motor synergies of upper limb. This is accomplished using functional PCA, a statistical method that allows to study the differences in shapes between functions. In order to avoid the inclusion in this analysis of undesired features due to misalignments in time or in velocity of the samples, we performed the following pre-processing techniques: segmentation, to divide the repetition of each task, time warping, to synchronize in time all the elements of the dataset.

### 4.1. Segmentation

For each task, the three repetitions have been segmented using the following procedure (see **Figure 5**):

1. select the data elements of the third DoF ( $q_3$ );
2. find the first two peaks  $p_1, p_2$  of the signal;

3. evaluate the mean slope  $s_1, s_2$  of the signal in a section close to each peak;
4. calculate the segmentation point as  $t_1 = \frac{p_1 s_1 + p_2 s_2}{s_1 + s_2}$ ;
5. repeat points 2–4 using the second and the third peaks and obtain  $t_2$ .

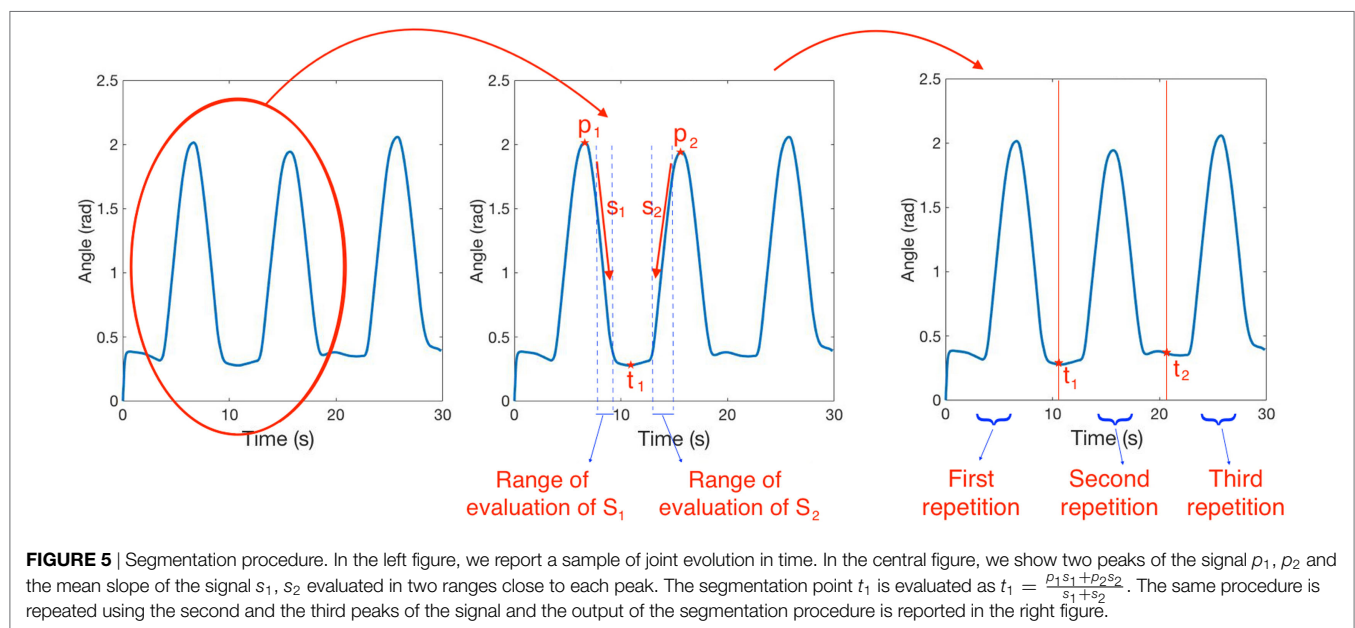
$q_3$  data (i.e., shoulder flexion–extension) was used for segmentation because it almost always contains three distinct peaks. If the peaks were not detectable, another DoF with detectable peaks was used instead. Note that the segmentation is performed using the same couple of segmentation points for all the 7 DoFs.

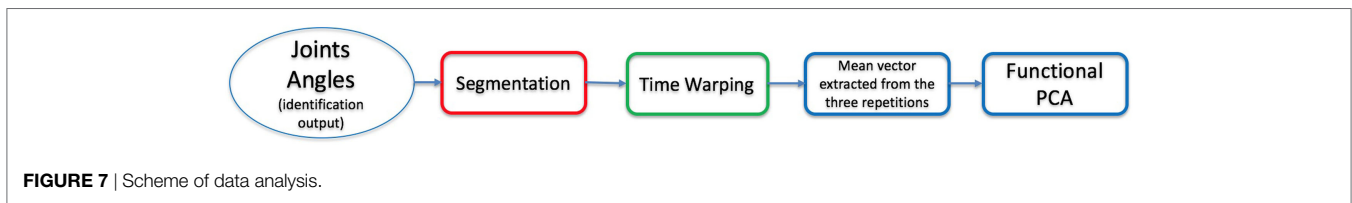
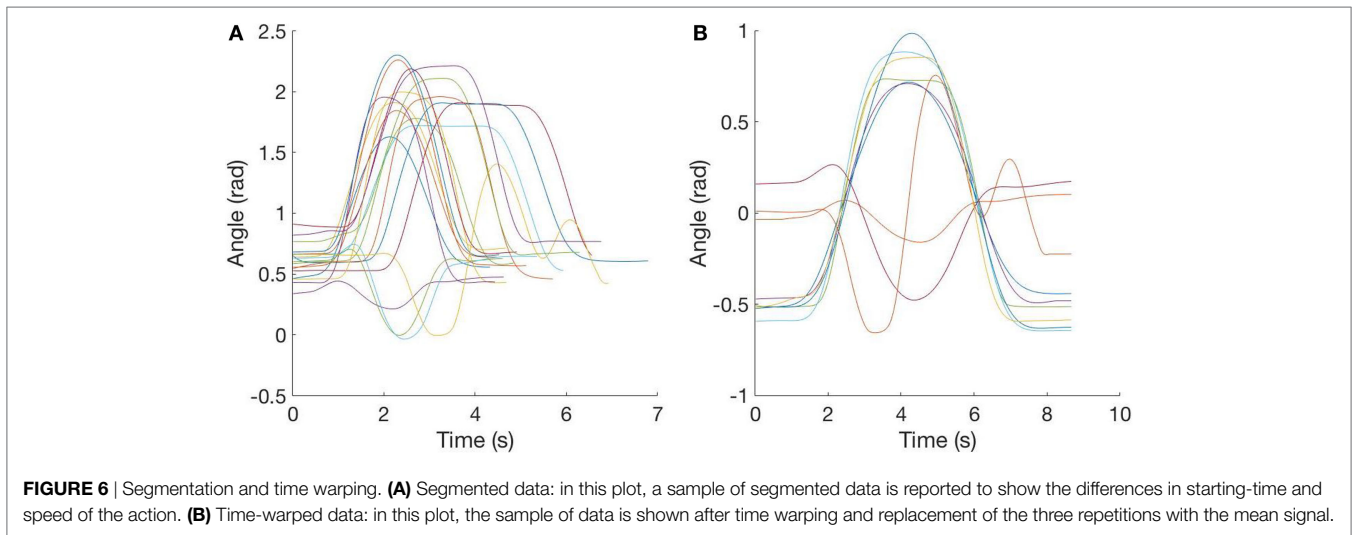
Considering different subjects and tasks, differences between shapes are evident (see **Figure 6A**). The three repetitions of each task should be replaced by the corresponding mean vector to increase robustness. This replacement can be performed only after signal synchronization, achieved using a time-warping procedure.

### 4.2. Time Warping

The synchronization between two signals allows to increase the affinity by conforming starting-time and speed of the action. This can be achieved by finding the optimal time-shift and time-stretch of one signal w.r.t. the other one. This problem is known in literature as *dynamic time warping* (DTW) and widely explored in sound engineering and pattern recognition (Rabiner et al., 1978; Berndt and Clifford, 1994; Müller, 2007; Salvador and Chan, 2007). In this work, DTW is needed to allow the mediation of the three repetitions, to avoid misalignment, and to compare different tasks and subjects' data. For the problem explored in this work, the following assumptions were done: monotonicity, to preserve data integrity, and linear distortion of time. Given two time series,  $v_1$  and  $v_2$ , the affinity between the two signals is increased by the solution of the following least-squares minimization problem:

$$(S, T) = \arg \min_{S>0, T} (\|v_1(t) - v_2(St - T)\|)$$





where  $S$  is a scaling factor for the velocity of signal  $v_2$  and  $T$  is the amount of shifting in time applied to  $v_2$ . The dataset elements were time-warped w.r.t. a reference time series, selected in the set as the element whose length is the mean value w.r.t. the length of all dataset elements. For each element,  $S$  and  $T$  are calculated by performing DTW on DoFs used for segmentation, then all the components are time-warped using the optimum set of parameters. The time-warped vectors have the same number of frames (number of elements). Once the time warping was performed on all the dataset elements, the three repetitions for each task can be replaced by the corresponding mean vector. A sample output of this procedure is reported in **Figure 6B**. In **Figure 7**, a scheme of the data analysis procedure is reported.

### 4.3. Principal Component Analysis

To explain fPCA, it is useful to start from classic principal component analysis (PCA). Principal component analysis (PCA) is a statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables called principal components. This transformation is defined in such a way that the first principal component (PC) has the largest possible variance (that is, it accounts for the largest part of the variability in the data). The other components explain an amount of variance in decreasing order, with the constraint that each principal component is orthogonal to the previous ones. Hence, the resulting vectors represent an orthogonal basis set. Principal components are calculated as eigenvectors of the covariance matrix of data. The variance explained by each PC is calculated as normalization of the corresponding eigenvalue. Given the first eigenvector  $\xi_1$ , the

principal component score  $f_{i1} = \xi_1' x_i$  maximizes  $\sum_i f_{i1}^2$  subject to  $\|\xi_1\| = 1$ ; the second eigenvector  $\xi_2$  maximizes  $\sum_i f_{i2}^2$  subject to  $\|\xi_2\| = 1$  and  $\xi_2' \xi_1 = 0$ , and so on.

### 4.4. Functional Principal Component Analysis

Functional PCA can be described as a functional extension of PCA. The first functional principal component  $\xi_1(t)$  is the function for which the principal component score  $f_{i1} = \int \xi_1(t) x_i(t) dt$  maximizes  $\sum_i f_{i1}^2$  subject to  $\int \xi_1^2(t) dt = \|\xi_1\| = 1$ ; the second functional principal component  $\xi_2(t)$  maximizes  $\sum_i f_{i2}^2$  subject to  $\|\xi_2\| = 1$  and  $\int \xi_2(t) \xi_1(t) dt = 0$ , and so on. In practice, this is done implementing the following steps:

1. Consider a dataset of functions  $x_i$  and extract the mean signal  $\bar{x}$  as  $\bar{x}_j = \frac{1}{N} \sum_{i=1}^N x_{ij}$ ;
2. Remove the mean calculated in step 1 from each data element by  $\tilde{x}_i = x_i - \bar{x}$ ;
3. Define a basis function. The basis must contain a number of functions large enough to consider all possible modes of variations of data. Usually basis elements are exponential functions, splines, Fourier basis (Ramsay and Silverman, 2002; Ramsay, 2006; Ramsay et al., 2009);
4. Given the basis functions  $b_1, \dots, b_N$ , each data element can be described as combination of basis elements  $\tilde{x}_i = \sum_{k=1}^N \theta_k b_k$ ;
5. Then each function is described by a vector of coefficients  $\Theta = (\theta_1, \dots, \theta_N)'$ ;
6. PCA is now performed on these vectors. This leads to define the PCs, which are vectors of coefficients;

7. Each PC is, then, transformed into the corresponding function principal components (fPCs) using basis elements as  $x_{rec} = \bar{x} + c_1\xi_1 + c_2\xi_2 + c_3\xi_3 + \dots$ ;
8. Each fPC explains a certain percentage of variance. The variance explained by an fPC is quantified normalizing (w.r.t. the sum of the eigenvalues) the corresponding eigenvalue of the covariation matrix.

#### 4.5. Movement Reconstruction and Performance Analysis

We used fPCA on this dataset after the post-processing phase reported in previous sections. 15 fifth order spline basis elements were used, taking inspiration for the polynomial description in Flash and Hogan (1985). Each basis function is defined by piecewise polynomial functions. The places where the pieces of the spline intersect are known as knots. Each piece has the following form

$$s_k(t) = \sum_{i=1}^5 a_{ik}(t - t_k)^i$$

where  $t_k$  is the  $k^{th}$  knot. The fPCs can be used to reconstruct the data sample by adding  $M$  fPCs weighted by coefficients  $c_i$ , i.e.,  $x_{rec} = \bar{x} + c_1\xi_1 + \dots + c_i\xi_i + \dots + c_M\xi_M$  with  $M \leq N$ .

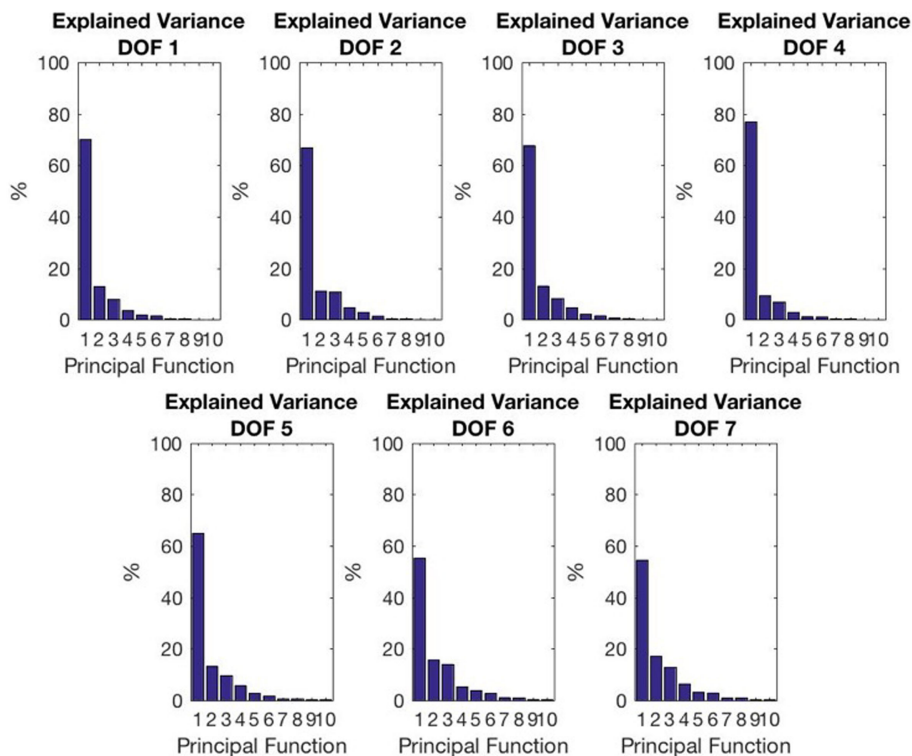
This analysis allows to infer that the first fPC by itself account for 60–70% of the variation w.r.t. the mean function, as reported in **Figure 8**, with a mean value between the DoFs of 65.2%, a minimum value of 54.4% and a maximum of 76.9%. What is noticeable is that reconstruction with the first fPCs provides good results, in fact the explained variance of the first three fPCs is

higher than 84% for all DoFs. In **Figure 9**, we show how the main principal functions can shape the reconstruction of the joints trajectories. Individual basis function does not need to represent meaningful movements. What is needed is that a combination of basis elements (plus an offset) could reproduce any original trajectory of the joints of the dataset. The reconstruction performance is showed in **Figure 10A**, in which a reconstruction using 1, 2, and 3 fPCs is reported. In order to quantify the reconstruction performance, an index of reconstruction error can be evaluated as

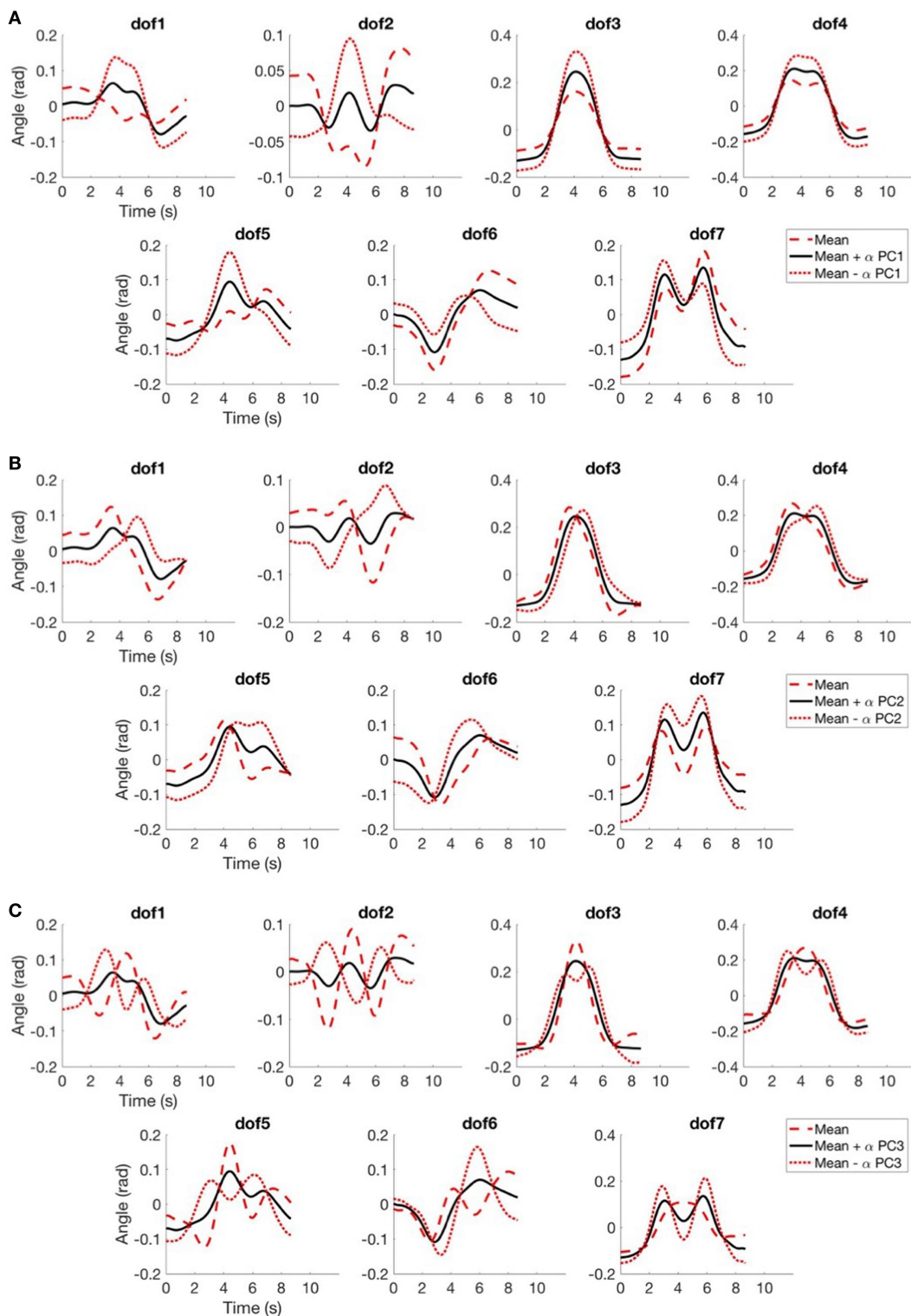
$$E_{RMS} = \sqrt{\frac{1}{N_{DoF}} \sum_{i=1}^{N_{DoF}} \left( \sqrt{\frac{1}{N_{frames}} \sum_{j=1}^{N_{frames}} (x - x_{rec})^2} \right)^2}$$

where  $x$  is the real function and  $x_{rec}$  is the reconstructed function.

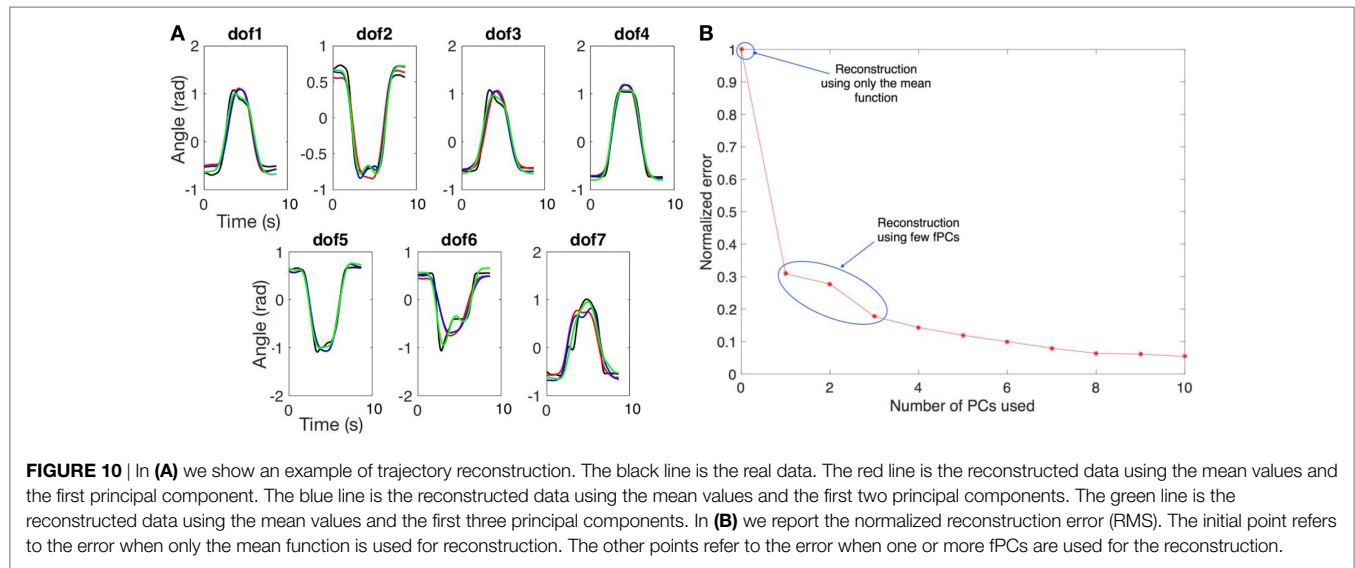
**Figure 10B** reports a plot of the normalized error, calculated as  $E_{RMS}/\max(E_{RMS})$ , for different number of fPCs used. Initial point refers to the case where only mean function is used for reconstruction and the value of  $E_{RMS}$  is 0.6 rad. The reconstruction using one fPC has an  $E_{RMS}$  value lower than 0.2 rad, adding other fPCs, the reconstruction error decay, i.e., using three fPCs the  $E_{RMS}$  value is around 0.1 rad. Furthermore, the whole reconstructed movement for the upper limb (considering all DoFs) was displayed using a visualization tool developed in MatLab, showing a high level of anthropomorphism and realism. We can conclude that the kinematic complexity of upper limb trajectories can be simplified and easily described using the mean function and few principal functional modes.



**FIGURE 8** | Explained variance for different DoFs and for each fPC.



**FIGURE 9** | In **(A)**, we report the mean function (in black) and the same mean function with the contribution of the first principal function, weighted with a coefficient  $\alpha$  equal to one (with positive sign in red dashed line, with negative sign in red dotted line); in **(B)**, we report the mean function (in black) and the same mean function with the contribution of the second principal function with a coefficient  $\alpha$  equal to one (same legend of **(A)**); in **(C)**, we report the mean function (in black) and the same mean function with the contribution of the third principal function with a coefficient  $\alpha$  equal to one (same legend of **(A)**).



## 5. CONCLUSION AND IMPLICATIONS FOR ROBOTICS AND BIOENGINEERING

In this work, we have shown that the complexity of upper limb movements in activities of daily living can be described using a reduced number of functional principal components. To achieve this goal, we developed an experimental setup, which is based on kinematic recordings but also allows to include additional sensing modalities. Kinematic data are based on a 7 DoFs model and are quantified through a calibration-identification procedure. Collected data were used to characterize upper limb movements through functional analysis. The findings of this work can be used to pave the path toward a more accurate characterization of human upper limb principal modes, opening fascinating scenarios in rehabilitation, e.g., for automatic recognition of physiological and pathological movements (e.g., stroke affected subjects) through machine learning.

At the same time, the here reported results and future investigations could also offer a valuable inspiration for the design and control of robotic manipulators. First, recognizing that few principal modes describe most of kinematic variability could provide insights for a more effective planning and control of robotic manipulators. For the planning phase, using input trajectories as combinations of the main functional components, which explain most of the kinematic variability, could represent a successful initial guess to control the movement of the robot—eventually combined with a feedback correction. This combination of feedforward and feedback components could be successfully employed also with soft robotic manipulators, i.e., robots designed to embody safe and natural behaviors relying on compliant physical structures purposefully used to achieve desirable and sometimes variable impedance characteristics. In these cases, standard methods of robotic control can effectively fight against or even completely cancel the physical dynamics of the system, replacing them with a desired model—which defeats the purpose of introducing physical compliance. To overcome this limitation in Della Santina et al. (2017), an anticipative model of human motor control was proposed, which used a feedforward

action combined with low-gain feedback, with the goal of obtaining human-like behavior through iterative learning. Results presented in this work could be used to define the feedforward component for the control of soft robots. Second, using human-like primitives for controlling robotic systems could improve the effectiveness and safety of human–robot interaction (HRI). Indeed, several studies identified anthropomorphism as one of the key enabling factor for successful, acceptable, predictable, and safe HRI in many fields, such as human robot co-working and rehabilitative/assistive robotics (Duffy, 2003; Bartneck et al., 2009; Riek et al., 2009; Dragan and Srinivasa, 2014). Furthermore, the here reported experimental and analytical framework could be used to identify principal actuation schemes for under-actuated robotic devices. As an example, in Casini et al. (2017), we used the identification procedure and the kinematic model reported in this work to estimate the contribution of wrist joints in the most common poses for grasping. We performed PCA on the estimated joints of the wrist pre-grasp poses and we found that the flexo-extension DoF plays a dominant role. We used these results to calibrate an under-actuated wrist system, which is also adaptable and allows to implement different under-actuation schemes, demonstrating its effectiveness to accomplish grasping and manipulation tasks. Future works will aim at using functional data to allow a dynamic implementation of principal kinematic modes of human upper limb in robotic systems. Finally, the integration of other sensing modalities, such as electro-encephalographic recordings, could be used to study neural correlates of human upper limb motions, thus possibly inspiring the development of effective brain–machine interfaces for assistive robotics.

## ETHICS STATEMENT

This study was carried out in accordance with the recommendations of Regione Toscana, D.G.R. no. 158 23/02/2004, “Direttive regionali in materia di autorizzazione e procedure di valutazione degli studi osservazionali,” with written informed consent from all subjects in accordance with the Declaration of Helsinki, and in observation of the “Guideline for good clinical practice E6(R1),

International Council for Harmonization of Technical Requirements for Pharmaceuticals for Human Use (ICH).” The protocol was approved by the local Ethical Committee, i.e., “Comitato Etico di Area Vasta Nord-Ovest (CEAVNO).”

## AUTHOR CONTRIBUTIONS

GA, CS, MB, and AB designed the study. GA, FF, and MB designed the protocol. GA, EB, and FF designed and developed

the experimental setup. GA and FF performed the experiments. GA, CS, and MB performed data analysis. All authors contributed to writing the manuscript.

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**Conflict of Interest Statement:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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