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# **Analysis of the mechanical expansion process of thin-walled tubes for air heat-exchanger production**

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# **Analysis of the mechanical expansion process of thin-walled tubes for air heat-exchanger production**

## **Abstract**

Finned tube air heat-exchangers are built by joining the tubes to the fins by various techniques. A technique mostly used for large heat-exchangers consists of fitting the tubes into the holes of the fins by expanding the tubes using a mechanical process. The expansion is achieved by inserting an ogive of a larger diameter into the tube. The intimate contact of tubes and fins due to the press fitting ensures the proper thermal connection. This work tries to describe an experimental-numerical procedure useful to study and predict the mechanical process and the process parameters. The procedure, based on material properties obtained from tensile tests and the use of the inverse method to identify the material parameters, is based on bi-dimensional finite element (FE) models used to simulate the expansion process. The FE model is then used for process optimisation regarding such parameters as the ogive shape and ogive sizes, friction coefficient and speed of insertion of the ogive into the tube. Indeed, size and shape uncertainties strongly influence the process parameters and the process quality, as well as the heat-exchanger efficiency. The use of numerical models was proven highly

effective in predicting and optimizing the process by quickly analysing the influencing factors and optimising the production.

**Keywords:** air heat-exchanger manufacturing; tubes mechanical expansion; process simulation; plasticity; FEM simulation.

## **1. Introduction**

In the type of air heat-exchangers made with fins, the tubes can be made of copper, nickel or other metal alloys. The fins have a regular pattern of holes in which tubes are fitted and assembled into packs. The optimal thermal connectivity between the tubes and the fins, which gives the maximum exchange of heat between the fluid (circulating in the tubes) and the air (passing over the fins), is obtained when the contact area between them is maximised, and this can be achieved either by using some intermediate highly conducting materials, that is some soldering metal, or by press fitting, when a radial homogeneous pressure is exchanged in the contact area. This press fitting assembly can be obtained by plastically expanding the tubes, and the expansion can be hydraulic or mechanical. As discussed by MacGregor et al. [1], in the hydraulic expansion, a fluid is introduced in the tube and pressurised at a required level. As discussed by A Valle et al. [2], in the mechanical expansion process, the external diameter of the tube is made larger than the diameter of the holes in the fins through the insertion of a tool. The diameter of the tool is larger than the internal diameter of the tube. The tool can be a sphere or an ogive, in any case with an axisymmetric section. Usually, the sphere is pushed through the tube by a fluid with a suitable pressure applied from one end of the tube itself. The ogive, instead, is pushed mechanically by a rod. In the hydraulic expansion process, the size and shape of the final connection depends on the stiffness of the parts, tubes and fins; local variations due to, for example,

material variations or thickness variations are difficult to control and can give unpredictable results. On the contrary, the mechanical expansion process is strongly affected by interference, that is by the effective diameters of the parts; these geometrical parameters must be precisely controlled to avoid manufacturing uncertainties. In the mechanical expansion process, the method based on the insertion of the sphere is less controllable because the movement (speed) of the sphere depends on the resistance encountered during insertion. When using the ogive, pushed by a rod, the insertion speed is imposed; the system is simpler, but the ogives are more expensive due to their complex shape. In general, the mechanical expansion process is cheaper and more versatile. It is more interesting, especially for producing smaller heat-exchangers and small series or for individual production, where each single product is made on purpose and is unique. The hydraulic expansion method is more commonly used in petroleum production, while mechanical expansion is used in heat-exchanger production and energy absorption applications. The hydraulic expansion method was studied by Hwang and Altan [3] in the case of a circular tube expanded to a rectangular cross-section. The hydroforming process of aluminium tubes was investigated by Abrantes et al. [4], whereas the expansion of stainless-steel tubes using the hydroforming process was studied by Gao and Strano [5], and this process optimised the pre-bending phase using numerical simulations. In the same field, a control algorithm in combination with FE

models was developed by Ray and Mac Donald [6] to optimise the hydroforming process of the tubes.

Several works in the technical literature have dealt with the study of the mechanical expansion process of tubes for various applications with various materials and with different approaches: considering the energy absorption applications, a theoretical prediction supported by an experimental investigation was carried out by Tan et al. [7]. Theoretical analyses and models were also proposed by Wu et al. [8], Luo et al. [9] and Liu and Qiu [10]. The plastic energy absorption of the aluminium tubes when the expansion was performed with conical-cylindrical die was analysed by Jialing et al. [11].

The expansion of the tubes used in the petroleum industry was analytically investigated by Hwang and Chen [12] and by Pervez et al. [13, 14] working with FE models [13] and experimental tests [14]. The aluminium and steel tubes expanded for this application were also investigated by Seibi et al. [15], who carried out an experimental study designed for the mechanical expansion of the tubes. The same author proposed [16, 17] a mathematical model of the expanded tube.

Focusing on the production of fluid pipe circuits and heat-exchangers, the tube-to-tubesheet joints were discussed by Alves et al. [18], who presented a new deformation process, and by Bouzid and Zhu [19], who studied the effect of the residual contact pressure between the two parts. They also developed an analytical model where the

effects of strain-hardening [35] **Errore. L'origine riferimento non è stata trovata.** and of reverse yielding [36] **Errore. L'origine riferimento non è stata trovata.** were introduced and shown. The expansion of the tubes made of copper was analysed by Tang et al. in different works. In [22], they studied both from a numerical and an experimental viewpoint the deformation and contact between microgroove tube and aluminium fins. In [23], they investigated the influence of the groove shape of the tubes on the quality of the forming (expansion) process. In [24], they optimised the expansion process, developing a method based on numerical simulations and experimental tests. For example, they focused on the shape of the fin collar to increase the contact surface between the tube and the fin. The contact area between the tube and the fin was also studied with numerical simulations by Kwon et al. [25], whereas Kang et al. [26] developed three-dimensional groove tubes to increase further the efficiency of heat-exchangers.

As for other applications, in this field, numerical simulation by means of finite element models is a fundamental instrument to develop studies on the tube expansion process. Avalle et al. [2] designed an FE model, starting from experimental tests, to evaluate the effects of the process parameters. Scattina [27] used a three-dimensional FE model to study the effects of the tolerance errors of the tubes on the expansion process.

Numerical models are also often used to develop analytical models on the subject, as proposed by Karrech and Seibi [28], who developed a mathematical model to evaluate

the stress state of the deformed part and the drawing force of the process, or by Alves et al. [29], who conducted experimental tests on AA6060 aluminium alloy tubes, comparing the results with a numerical model and evidencing the importance of issues with modelling friction during the process. The same model was also used in [30] to study a related application, such as the hydroforming of carbon tubes. In [31], the formability of aluminium tubes and the effects of the process parameters using numerical simulations were investigated. The numerical models were also used to study the effects of several configurations (expansion method, alloy, pipe loading) on the mechanical properties of the steel subjected to tubular expansion, as proposed by Mack [32], or to investigate the effect of the process parameters, as proposed by Avalle et al. [2, 33] and Han et al. [34], who used the expansion force rate to define the amount of adhesion in the tube's inner grooves.

In this overview, the aim of the present work is to describe the procedure of designing the tube-expansion process for finned air heat-exchangers, starting from material characterisation to obtain a numerical model of the expansion process. This FE model will describe the influence of the process parameters and will thus guide the selection and definition of the optimal process parameters, depending on the materials and characteristics of the tubes and fins.

## **2. Experimental characterisation: Material properties and driving force**

### 2.1 Material properties

The mechanical properties of the tube materials were defined by performing a series of tensile tests. The experimental tests were carried out by means of an Instron 8801 testing machine. The setup of the tests was according to the standard ASTM E8M-16a. This standard deals with tube specimens. In this work, AISI 316 stainless steel tubes were studied. This material is mostly used to produce the type of heat-exchangers under consideration; therefore, an improvement in the analysis of the production process could satisfy industrial requirements. Other materials typically used to produce this type of heat-exchanger were studied by the authors in previous works: copper-nickel alloys by Avalor et al. [2] and titanium by Avalor and Scattina [33]. The tube samples for tensile tests had a length  $L$  of 208–210 mm and an external diameter  $D_e$  of 15.875 mm and 19.05 mm (non-expanded tube, see Table 1).

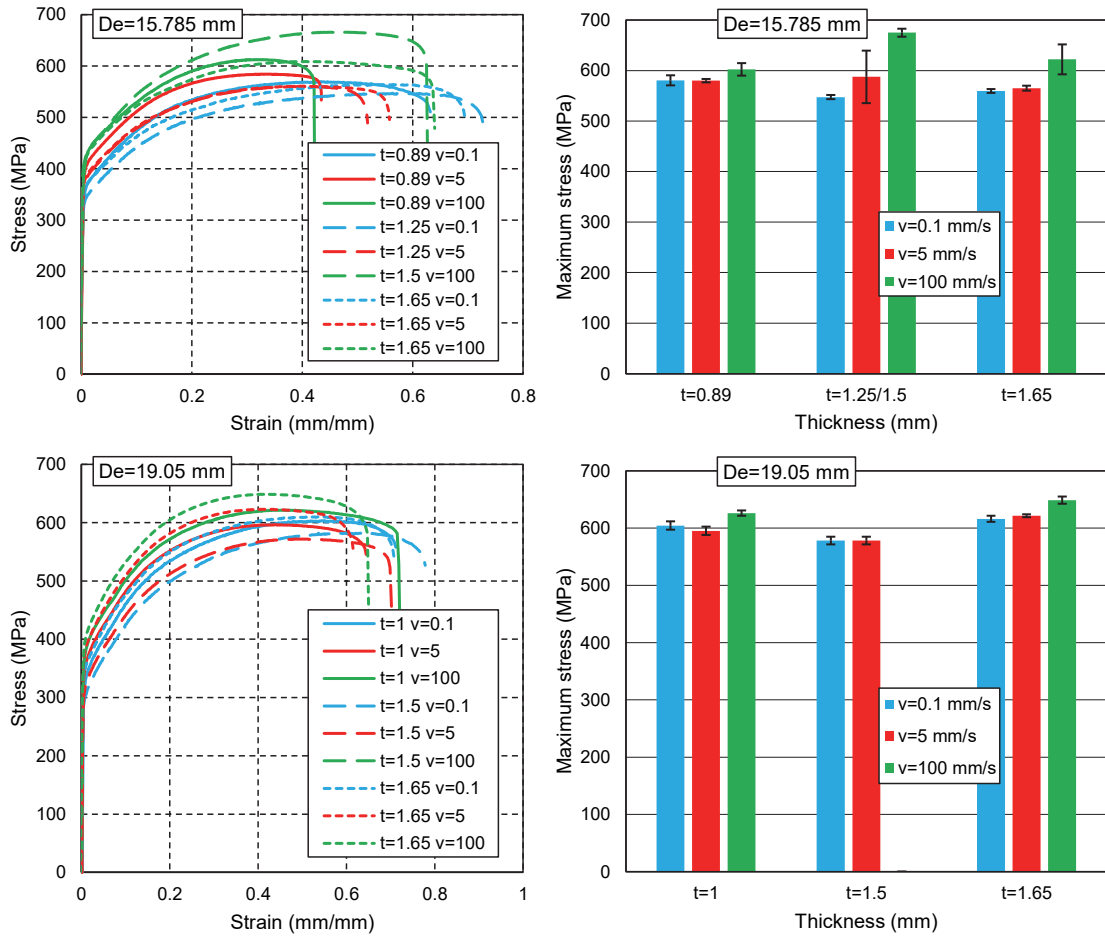
The tests were performed in stroke control until tensile failure occurred. Three loading speeds were examined to study the effects of the strain rate, namely  $v = 0.1, 5$  and  $100$  mm/s. To prevent the tubes collapse from the compression applied by the grips of the testing machine, a steel plug was introduced into both ends of the samples. This practice is suggested by the test standard ASTM E8M-16a.

The stress–strain curves, tensile strength of the material and strain-rate influence are shown in Fig. 1. The material has a moderate strain-rate sensitivity, although the

examined strain-rate levels were relatively low but sufficient for the examined application. In any case, the material model used in this work considers the strain-rate sensitivity.

**Table 1.** Test speed of the tensile tests for the examined stainless steel.

	<b>External diameter</b>			
<b>Thickness</b>	$D_e = 15.875$ mm		$D_e = 19.05$ mm	
$t = 0.89$ mm	0.1	mm/s	-	mm/s
	5		-	
$t = 1$ mm	-	mm/s	0.1	mm/s
	-		5	
$t = 1.25$ mm	0.1	mm/s	-	mm/s
	5			
$t = 1.5$ mm	-	mm/s	0.1	mm/s
			5	
$t = 1.65$ mm	0.1	mm/s	0.1	mm/s
	5		5	
	100		100	



**Fig. 1.** The experimental results of the tensile tests of the analysed stainless-steel tubes as a function of the thickness  $t$ , loading speed  $v$  and external diameter  $De$ . The charts on the left side show the stress–strain curve (one curve for each test configuration is shown), and the charts on the right side show the average values and the scatter of the tensile strength.

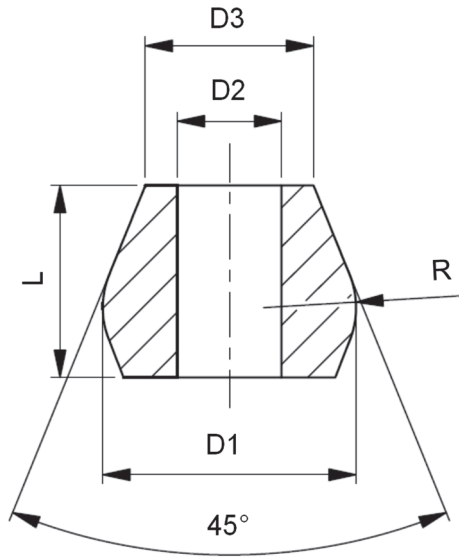
## 2.2. Driving force

To develop and validate the numerical model, a series of simplified components were considered and studied. Due to the practical impossibility of performing experimental measurements directly on the real components, simplified sub-components were

considered to measure the process parameters, particularly the force required to drive the ogive to achieve tube expansion.

Two different test setups were used, namely simple tubes laterally free (unconstrained, without fins, Fig. 3) and small-scale heat-exchanger models (Fig. 4). These latter models consisted of a pack of fins between simplified end plates. The pack of fins is crossed by seven tubes with the axis perpendicular to the plane of the fins. One tube is positioned in the centre of the fins, whereas the other six tubes are positioned according to a hexagonal pattern. The central tube was subjected to the ogive insertion, while the remaining six had only a supporting function. The distance between the tubes and their positions reflected the standard production proportions. The tubes had standard thicknesses of 1 and 1.5 mm.

The shape and size of the ogive are shown in Fig. 2 and Table 2, respectively. In the case of the tests on the simple, laterally free tubes, the ends were pre-formed to ease the ogive insertion at the beginning of the process (and during production). This pre-forming was applied for the first 10 mm of tube length. One of the ends was clamped in the testing machine, as in Fig. 3, while the other was used for the ogive insertion.



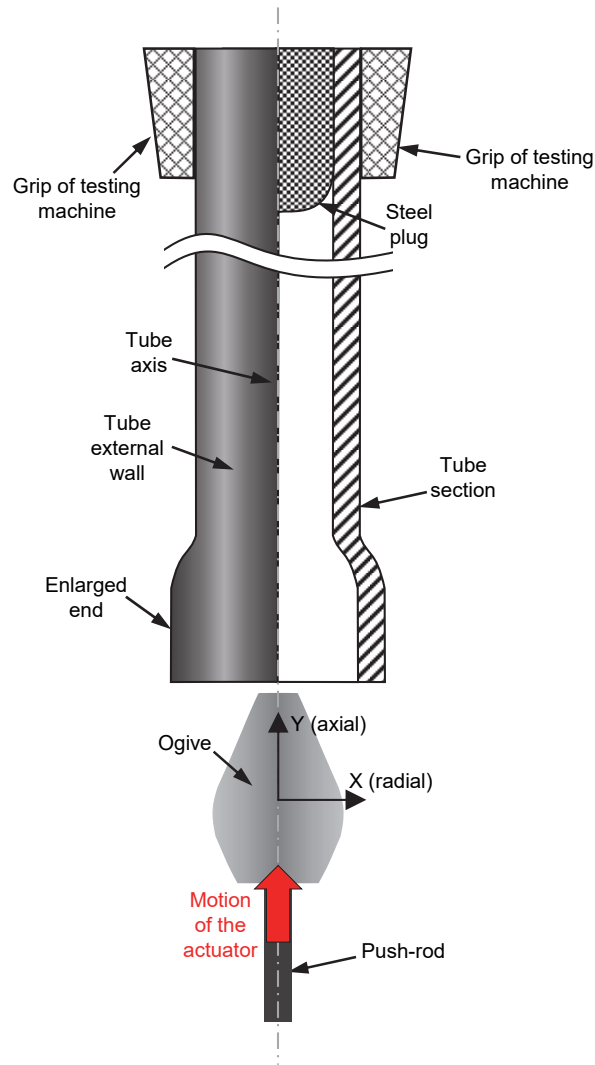
**Fig. 2.** Ogive shape and dimensions.

**Table 2.** Ogive dimensions with reference to Figure 2, all the dimensions are in mm.

<b>t</b>	<b>De</b>	<b>R</b>	<b>L</b>	<b>D1</b>	<b>D2</b>	<b>D3</b>
1	15.875	5	11	14.54	6.25	9.67
1.5	19.05	5	11	13.10	6.25	8.23
1	15.875	5	11	17.50	6.25	12.63
1.5	19.05	5	11	16.25	6.25	11.38

During the ogive insertion tests, the driving speed was chosen as 10 mm/s for the simple, laterally free tubes and 100 mm/s for the small-scale heat-exchanger models. This insertion speed value reproduces the typical speed adopted in the manufacturing process. Grease, equivalent to the real production process, was used for proper lubrication between the inner wall of the tube and the ogive. At least three repetitions of each test were conducted.

The experimental results will be shown in section §3.2. A comparison with the results of the numerical models will be also proposed and discussed.



**Fig. 3.** The configuration of the experimental expansion test adopted for the simple, laterally free tubes.

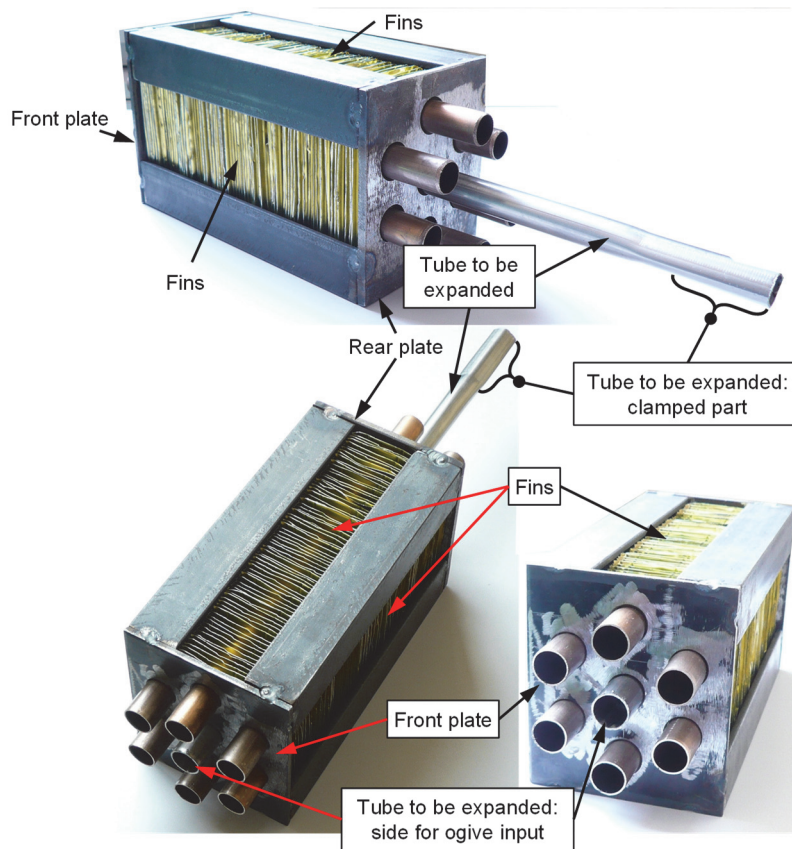


Fig. 4. Different views of the small-scale heat-exchanger model used for the expansion tests.

### 3 Forming process simulation

#### 3.1 Modelling

A series of FE analyses was conducted using the LS-DYNA 971 software, version double precision, release 7, implicit solver option.

##### 3.1.1 Material modelling

The material properties of the tubes were identified by simulating the tensile tests described in section §2.1. Tensile tests on expanded tubes, that is tubes subject to

expansion in laterally free conditions, as in Fig. 3, were also performed to validate the model.

Several models for the materials from the collection of the used FE software [35] were considered and accurately selected. The most suitable model for this application was then considered the elastic visco-plastic material model (MAT\_106 of the LS-DYNA collection), as it considers thermal effects. This model is described in equation (1):

$$\sigma(\varepsilon_{eff}^p) = \sigma_0 + Q_{r1} [1 - \exp(-C_{r1} \varepsilon_{eff}^p)] + Q_{r2} [1 - \exp(-C_{r2} \varepsilon_{eff}^p)] + Q_{\chi1} [1 - \exp(-C_{\chi1} \varepsilon_{eff}^p)] + Q_{\chi2} [1 - \exp(-C_{\chi2} \varepsilon_{eff}^p)] \quad (1)$$

Where:

$\sigma_0$  yield stress

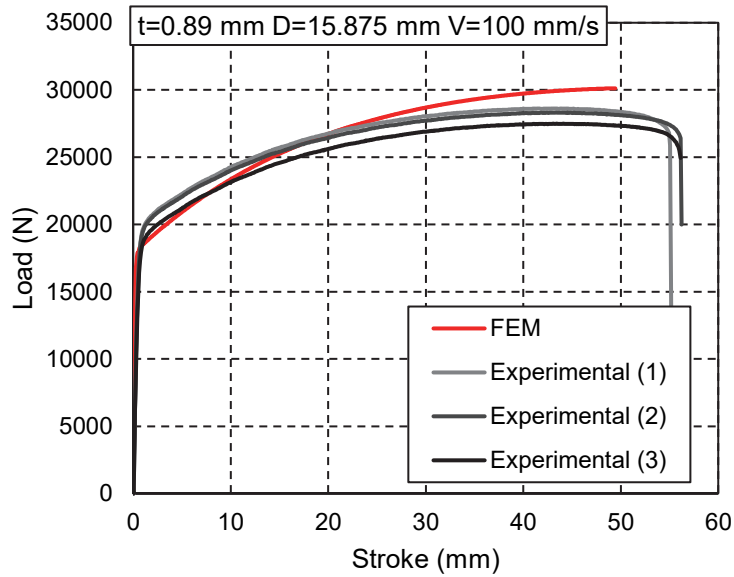
$\varepsilon_{eff}$  effective plastic strain

$Q_{r1,2}$  and  $C_{r1,2}$  parameters of isotropic hardening

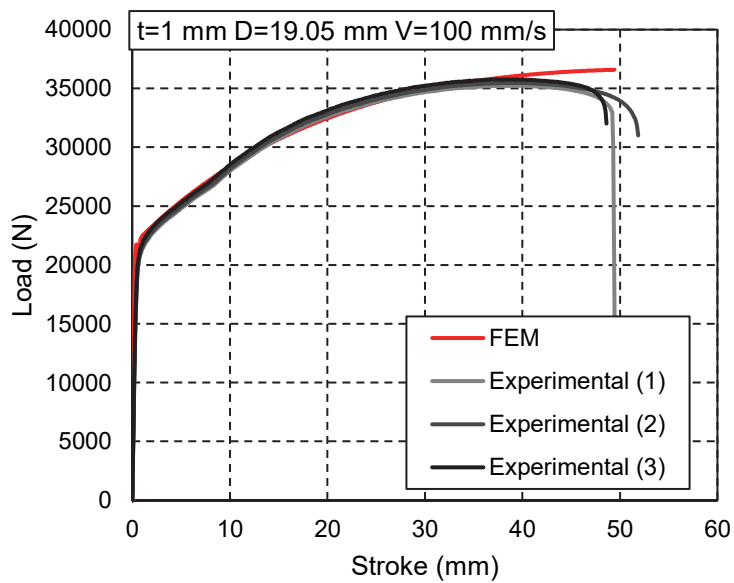
$Q_{\chi1,2}$  and  $C_{\chi1,2}$  parameters of kinematic hardening

The visco-plastic effect is accounted for with the lessandro–Symonds [36] model .

Simulations of the tensile tests were carried out for all thicknesses (1 or 1.5 mm) and speeds (0.1, 5 or 100 mm/s). The outcomes of the identification are shown in Fig. 5, where the experimental and numerical results are compared.



(a)



(b)

**Fig. 5.** Simulation results of the tensile tests: comparison between the experimental results (curves in different grey levels) and the numerical identified curves (in red colour) for specimens with external diameters: (a)  $D_e = 15.875$  mm; (b)  $D_e = 19.05$  mm.

### 3.1.2 Simulation of the laterally unconstrained simple tube expansion

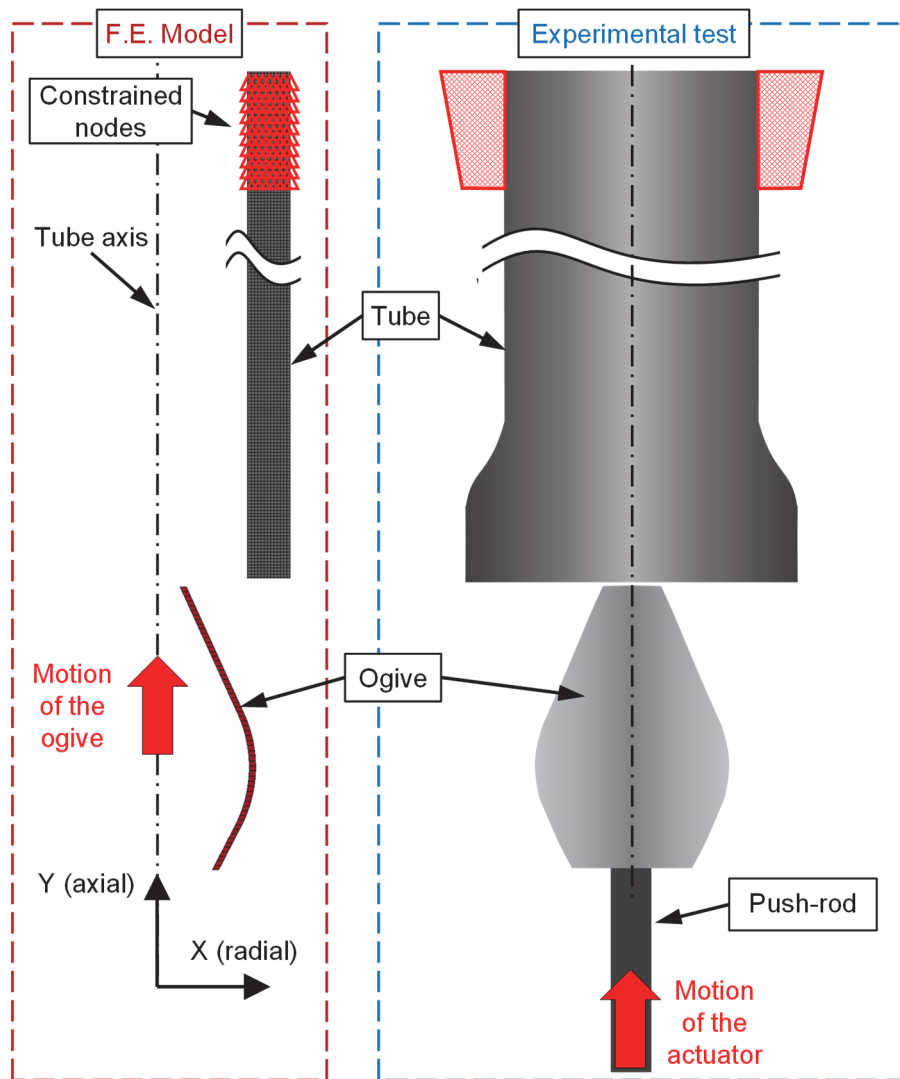
An axisymmetric model was created in LS-DYNA to simulate the expansion test on the tubes without lateral constraints (Fig. 3). This derives from the assumption of perfect axial symmetry of both the tube and the inserted ogive; it is a strong assumption not completely true for the real components but an adequate approximation at the current study level and for practical purposes. Such an analysis was carried out by Scattina [27]; errors include deviation from the ideal circular cylindrical shape of both the internal and external surfaces (in principle, the section shapes can be approximated by ellipses) and a lack of coaxiality between the two surfaces. The axisymmetric model has the great advantage of a dramatic simplification of the model and a huge reduction in calculation times.

The axisymmetric model consisted of three/four nodes plane axisymmetric elements. The average size of the elements was 0.125 mm. Therefore, the number of elements was between  $13 \times 10^3$  and  $20 \times 10^3$ , depending on thickness. The ogive was modelled with a rigid material and axisymmetric elements. The friction between the ogive and the tube was modelled with a simple sliding model, and the coefficient of friction was chosen as 0.15 from a previous analysis by Avalor et al. [2]. Boundary conditions (Fig. 6), to reproduce the real loading conditions, were applied to axial displacements of the first line of nodes of the tube, at the end opposite to that where the ogive was inserted. Then,

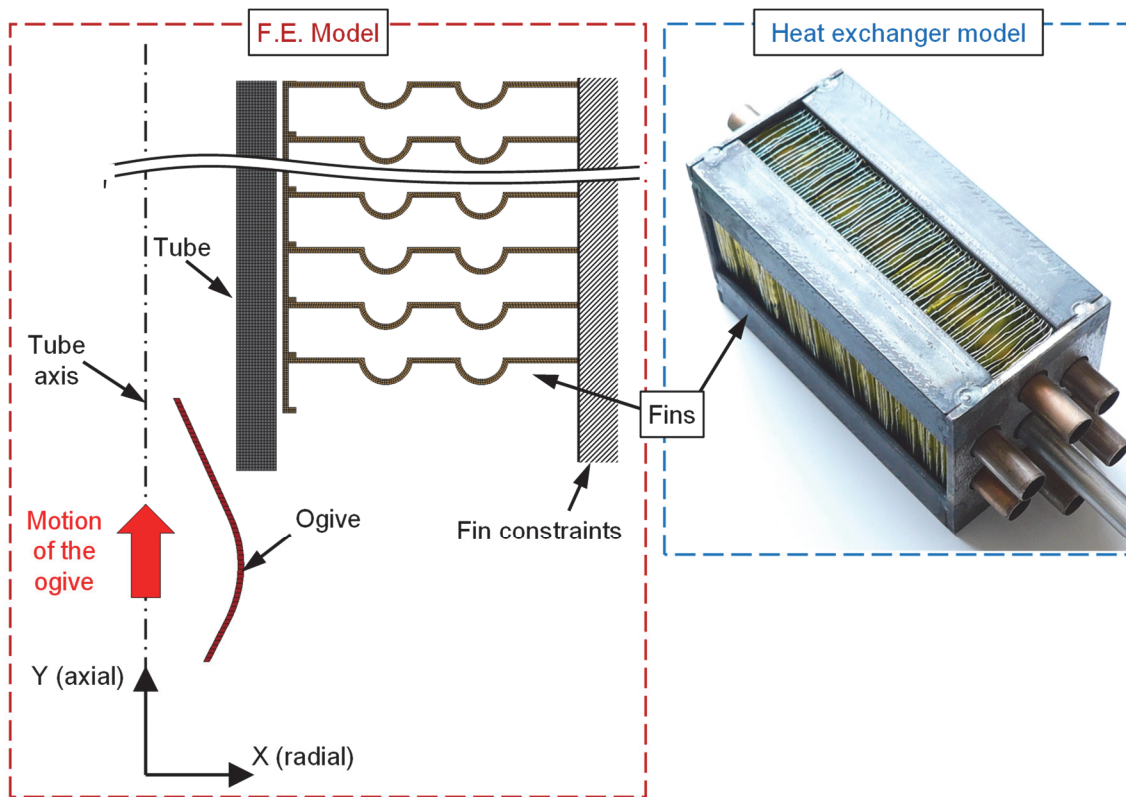
a constant axial insertion speed of 10 mm/s was applied to the ogive; a sliding interface was used to model the contact between the ogive surface and the internal tube surface.

### 3.1.3 Simulation of the small-scale heat-exchanger models

To consider the effect of the lateral constraint of the fins, the second model was developed to reproduce the small-scale heat-exchanger tests (Fig. 7). The model was similar to that of the simple tube, built with axisymmetric elements for the tube section and for the fin section (an average size of 0.075 mm was used for the fin element). The fins are non-axisymmetric, but they were modelled as simple axisymmetric plates exploiting the local nature of the expansion process. The fin plates had a diameter measured at a distance equal to half the tube's pitch. This diameter was then radially constrained in the model. A further contact algorithm was added between the fins. The aluminium alloy of the fins was modelled as simply bi-linear elasto-plastic material. The material parameters were obtained from previous tests of the authors [27]. The end clamped in the testing machine was constrained for a length of 45 mm, as in the experimental setup. The ogive was subjected to a constant axial insertion speed of 100 mm/s, as in the previous model.



**Fig. 6.** The numerical model (on the left-hand side of the figure) used to simulate the unconstrained tube subjected to the expansion test (right-hand side of the figure).

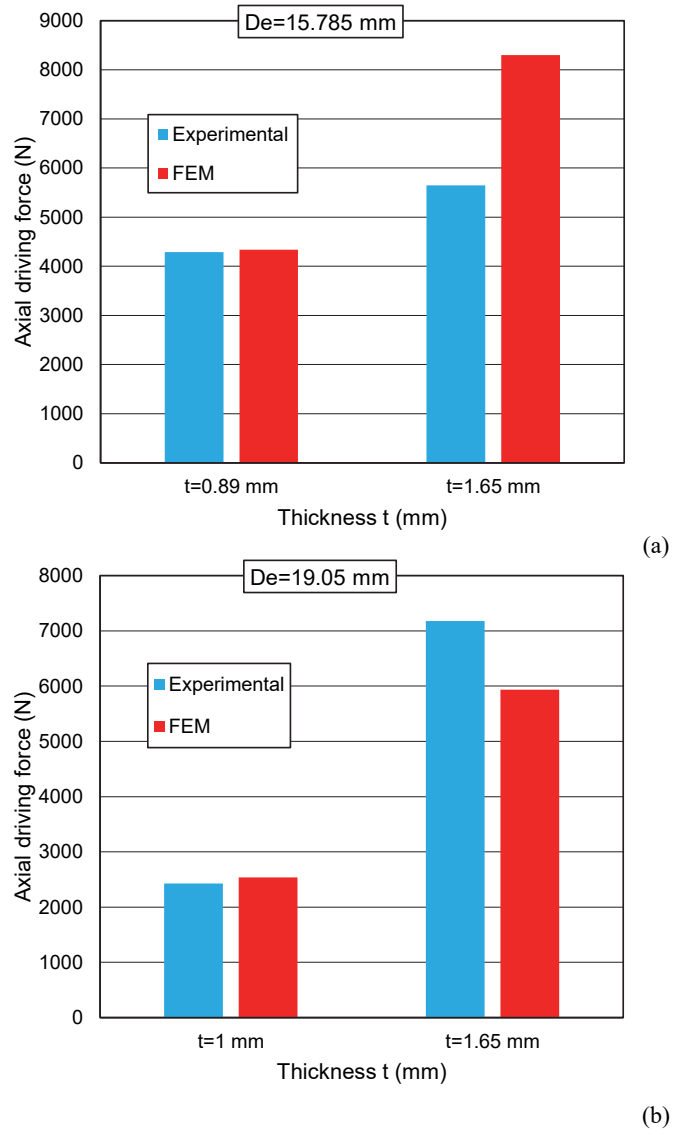


**Fig. 7.** Numerical model (on the left-hand side of the figure) for the simulation of the tube expansion for the heat-exchanger model.

### 3.2 Validation of the numerical models

To validate the FE models used for the simulation of the experimental test of the simplified expansion process, the results are compared, as shown in Fig. 8, in terms of the axial driving force of the ogive and, in Table 3, in terms of the tube's dimensions after expansion. The comparison is excellent for thicknesses of a smaller value, while it is less satisfactory for thicker tubes. From various analyses performed by the authors [2] and from what can be found in the literature [9], the critical role of the friction value can

be shown. A slight change in the friction coefficient value between the ogive and the inner wall of the tube could change the value of the axial driving force. This could explain the difference obtained with thicker tubes of a smaller diameter. Moreover, to obtain simple synthetic models of the tube expansion, the approximation was considered sufficient to describe the problem.



**Fig. 8.** The comparison of the axial driving force of the ogive between the numerical and experimental results for the specimens with external diameter: (a)  $D_e = 15.875$  mm; (b)  $D_e = 19.05$  mm.

**Table 3.** Size analysis of tube specimens: comparison between numerical and experimental results after the expansion tests. All dimensions are in mm.

External Diameter $D_e$	Thickness $t$	External diameter after expansion			Internal diameter after expansion		
		Experimental (averaged value)	FEM	Difference	Experimental (averaged value)	FEM	Difference
15.875	1	16.64	16.65	-0.01	14.66	14.70	-0.04
15.875	1.65	16.33	16.46	-0.13	13.15	13.23	-0.07
19.05	1	19.57	19.57	0.00	17.59	17.60	-0.01
19.05	1.65	19.60	19.62	-0.02	16.35	16.38	-0.03

#### 4 Investigation of the process parameters

To obtain a synthetic model of the expansion process, parametric simulations were performed by varying the values of some mostly significant variables. Processing parameters are countless, but only a few can be considered important and measurable in terms of input/output. Among the process parameters, the following were considered for the synthetic model, based on previous experiences of both the authors and the manufacturers:

- the friction coefficient  $f$  between the internal surface of the tube and the ogive;
- the initial thickness  $t_0$  of the tube;
- the insertion speed  $v$  of the ogive.

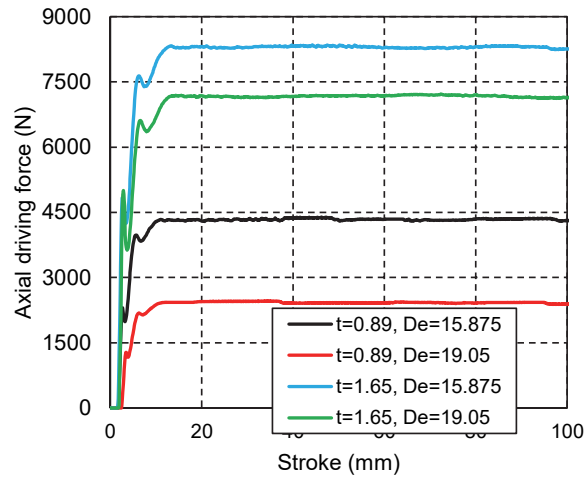
A multilevel factorial design was used to change the three variables according to Table 4; two variables, tube thickness and insertion speed, were considered at three levels, whereas friction was varied at four different levels. Then, the 24 combinations of the three variables were numerically simulated.

**Table 4.** The variation in factor levels.

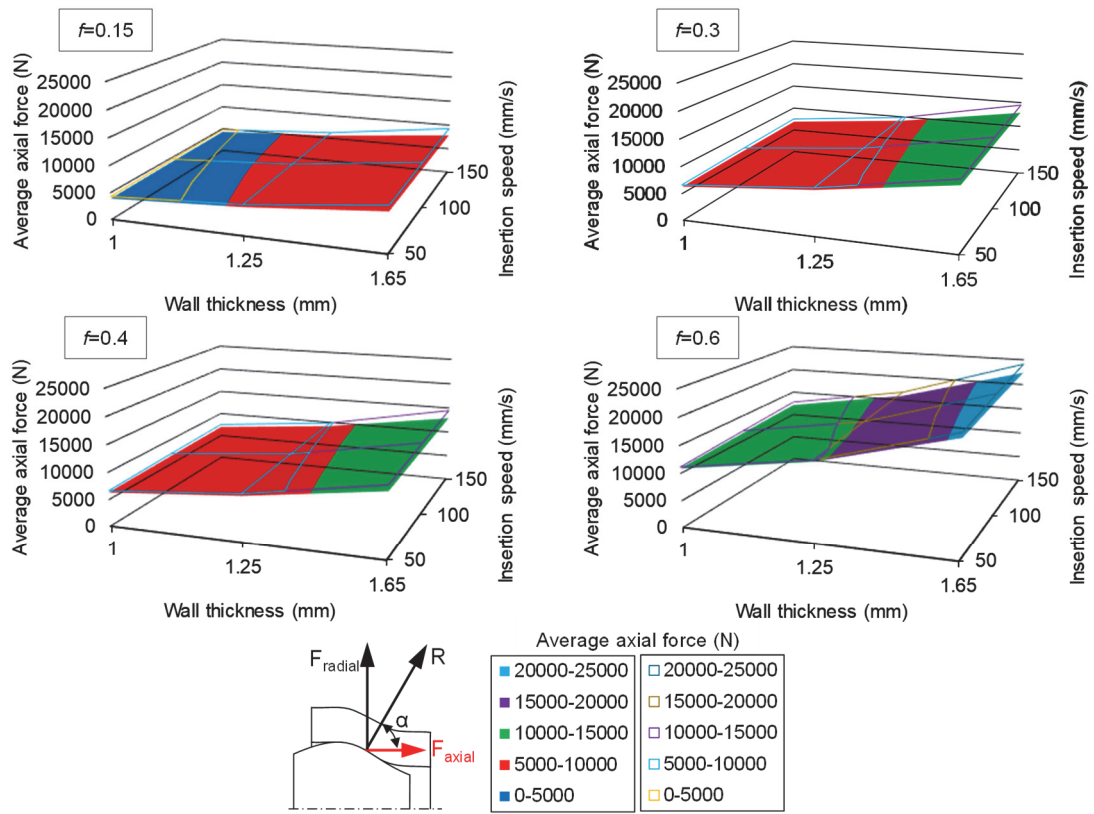
<b>Factor</b>	<b>Levels</b>
Friction coefficient, $f$	0.15–0.30–0.40–0.60
Insertion speed, $v$ (mm/s)	50–100–150
Tube thickness, $t_0$ (mm)	1.0–1.25–1.65

For each simulation, the radial and axial components of the driving force of the ogive were obtained as a function of the ogive position. As shown in Fig. 9, the axial driving forces increase then stabilise with small variations (less than 2%) in what can be considered a steady-state region, which was conventionally defined for an ogive stroke greater than 20 mm. The mean radial and axial driving forces of the ogive were then calculated as the average in the steady-state region.

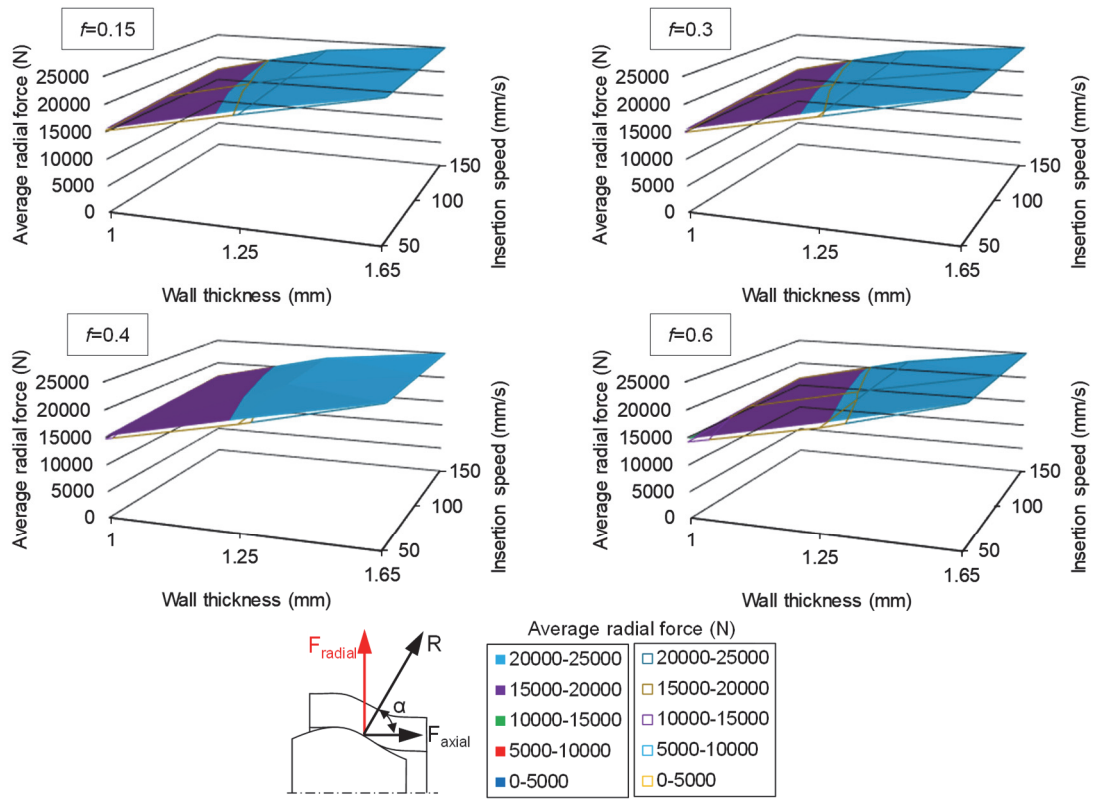
The ratio of the mean radial and the axial components of the ogive driving force does not remain constant but depends on the process parameters. In Fig. 10, the value of the mean radial and axial forces are reported as a function of the wall thickness and the insertion speed. The four values of the friction coefficient are also considered. Of course, the mean driving force can also be represented as the value of the mean resultant  $R$  and of its angle  $\alpha$  measured clockwise with respect to the radial axis, as shown in Fig. 11.



**Fig. 9.** Examples of the axial driving force as a function of the ogive's stroke obtained in the numerical simulations.

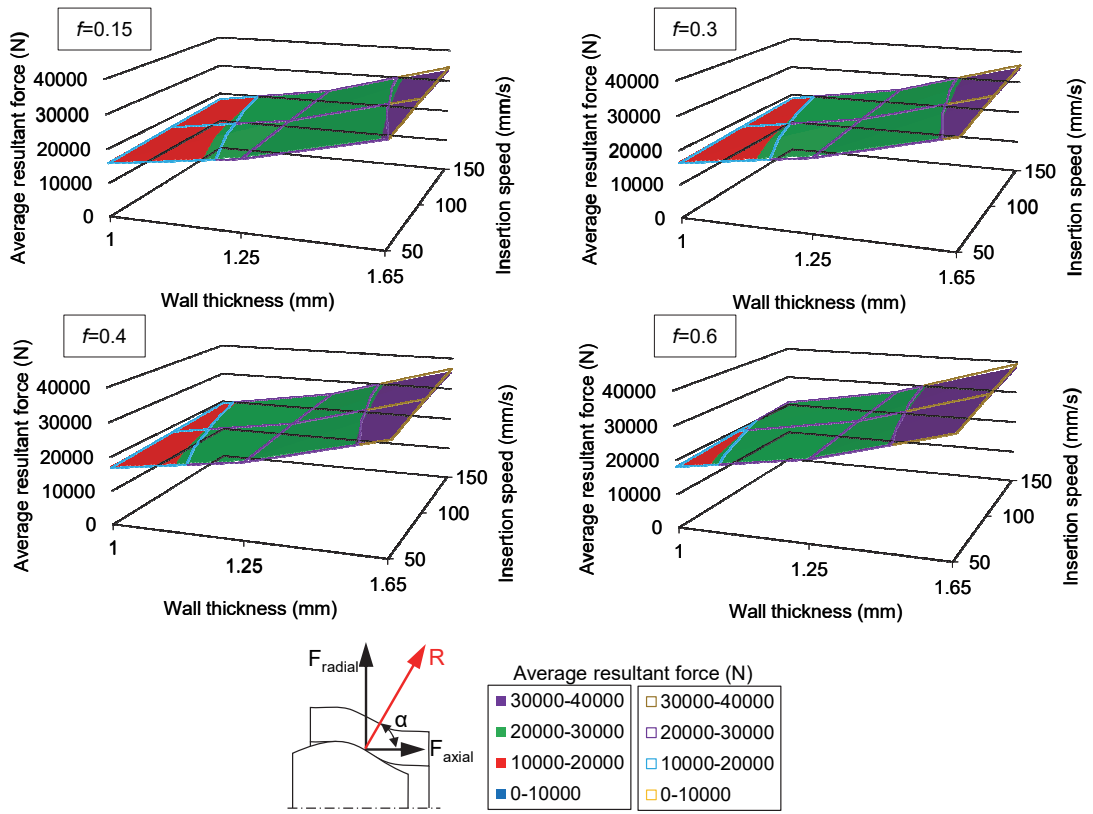


(a)

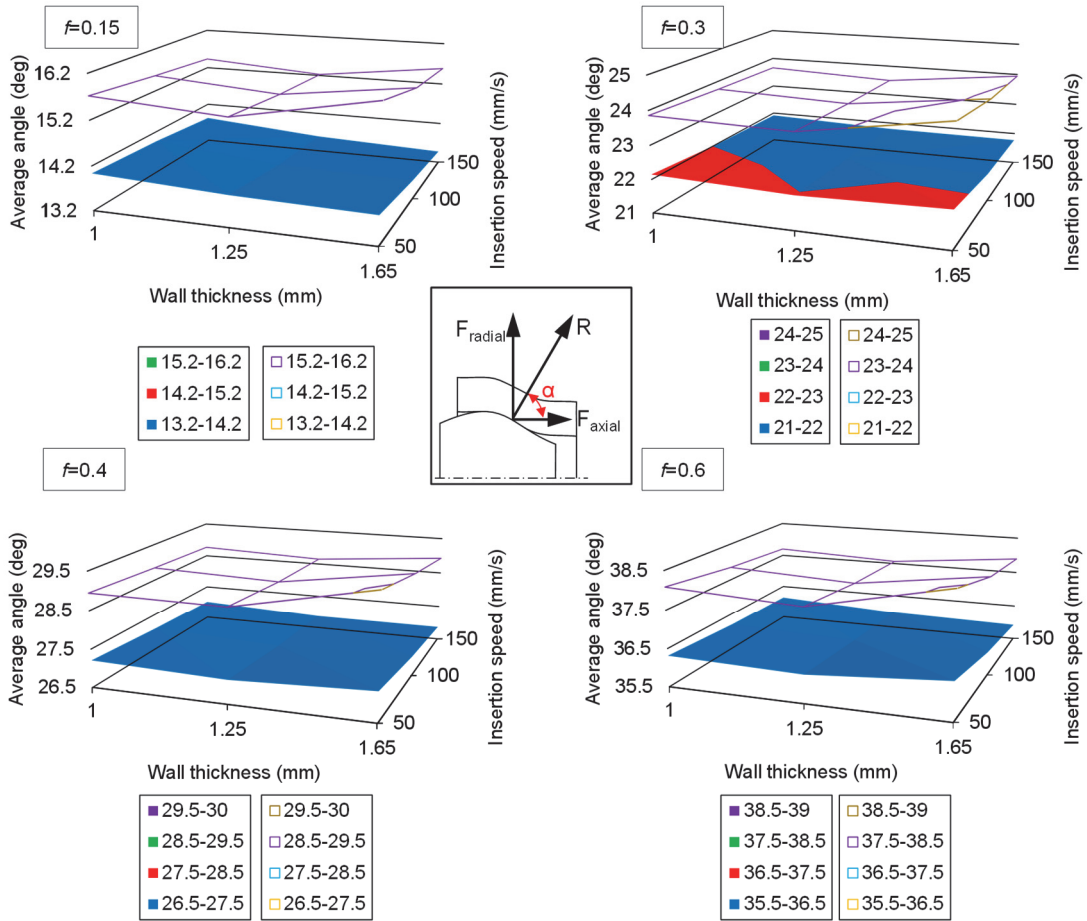


(b)

**Fig. 10.** The results for the driving force: (a) axial and (b) radial average components as a function of the process parameters. Transparent surface (top) for diameter  $D_e = 15.875$  mm, shaded (bottom) for diameter  $D_e = 19.05$  mm.



(a)

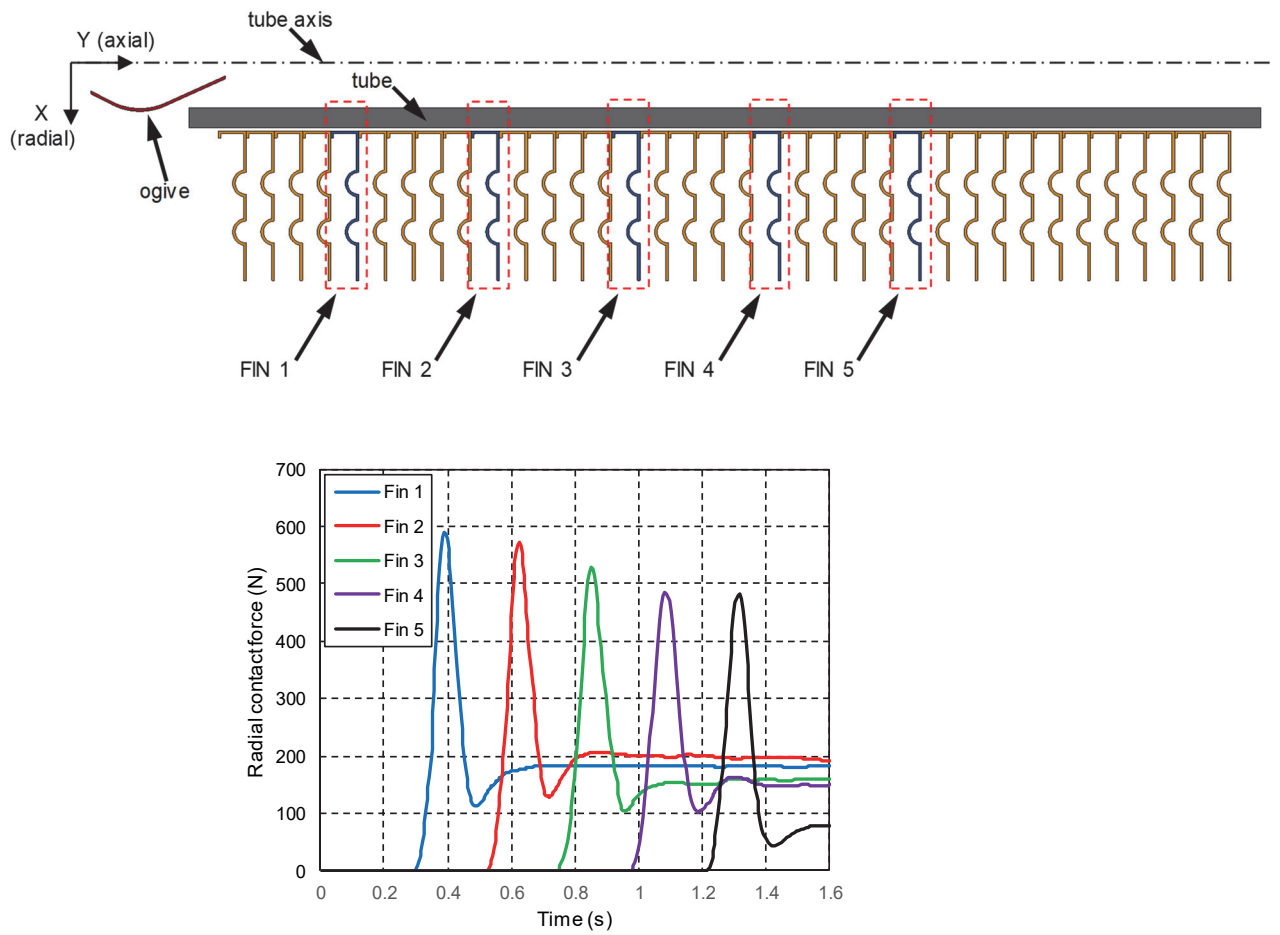


(b)

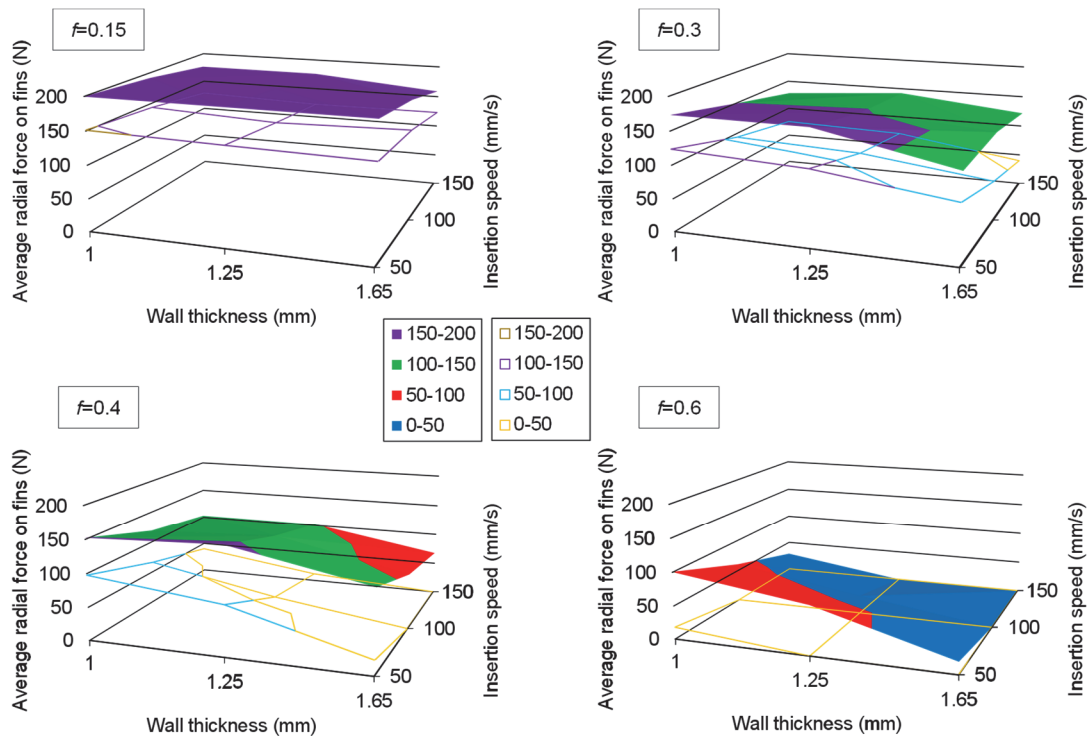
**Fig. 11.** Numerical results for the driving force: (a) average resultant and (b) angle as a function of the process parameters. Transparent surface (top) for diameter  $D_e = 15.875$  mm, shaded (bottom) for diameter  $D_e = 19.05$  mm.

Another important result from the numerical model is the radial force developed in the contact between each single fin and the tube. In Fig. 12, the radial force in the contact is shown. Its variability with the ogive stroke is considered. Five different trends are considered for fins equally spaced along the axis tube. For each fin, the radial force

reaches a maximum — when the ogive expands the tube closest to that fin — then, after a small springback due to the bending of the thin wall, it becomes stable at a constant value. This force is due to the residual stresses caused by the plastic deformation of the tube. The radial force remaining on the different fins is not constant; this is due to end effects because in the small-scale heat-exchanger models, the tube length is relatively short with respect to the tube diameter. In longer tubes, as in the real production components, end effects will vanish after a sufficient tube length, and a constant value of the force is expected. However, the variation, measured by the standard deviation of the final remaining radial force, is poor (around 10%), so the average can be considered a good estimate of the force exerted by the tubes on the fins. This average value is examined as follows in Fig. 13. In this figure, the values of the average radial force exchanged with the fins are also reported. Variabilities in wall thickness and insertion speed are considered, and the evaluation is repeated for the different friction coefficient values.



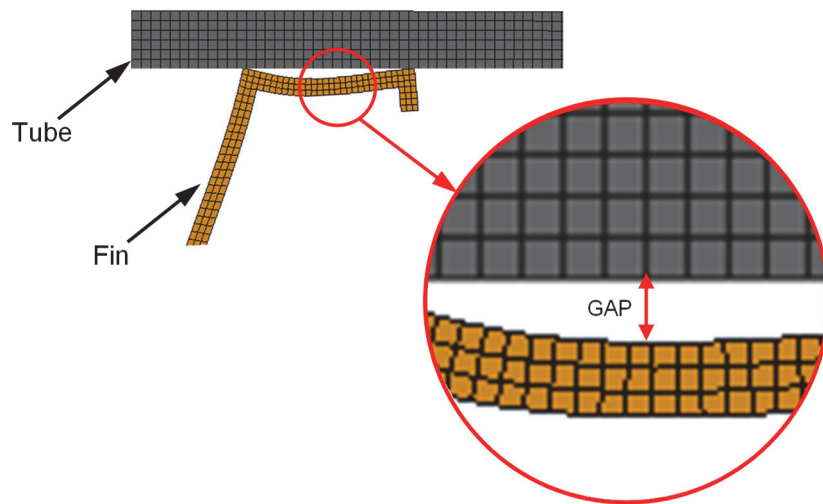
**Fig. 12.** An example showing the variation in radial forces developed in the contact between the tube and the fins. Five different positions in the tube's axial direction are considered.



**Fig. 13.** Radial force on the fins: transparent surface (top) for diameter  $D_e = 15.875$  mm, shaded (bottom) for diameter  $D_e = 19.05$  mm.

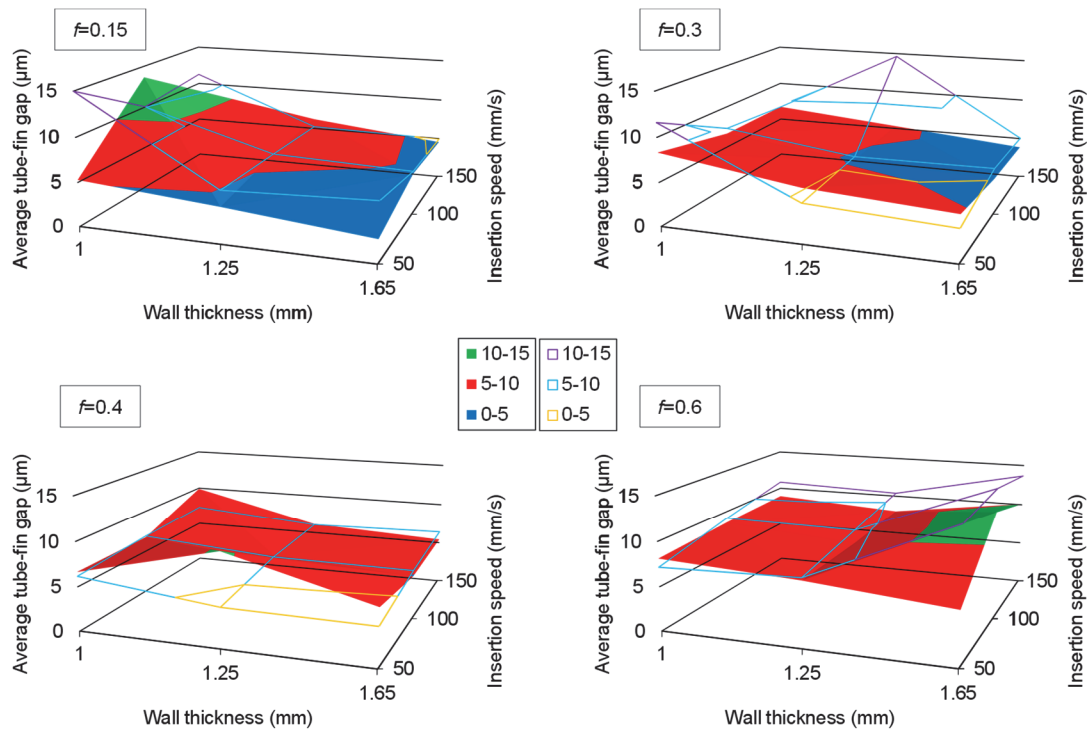
The final contact area between the tubes and the fins is then the last important outcome of this analysis; the contact is essential for the heat exchange between the (usually warmer) fluid in the tubes and the (usually colder) air passing over the fins. It was observed that — unexpectedly — the contact is incomplete and remains in a highly limited area only, as shown in Fig. 14. The fact that the contact area is reduced, at least within reasonable and measurable limits, does not seem to significantly influence the heat exchange from experimental observations; even a small contact area between two

materials with high thermal transmissivity generates thermal bridges largely sufficient for heat transmission. The average remaining gap (Fig. 15) was then calculated by measuring its value for five fins along the tube and taking the maximum distance between the fin and the tube. The measure was repeated for each fin.



**Fig. 14.** Detail of the contact zone between the tube and the fin after the expansion (the deformation of the fin is enlarged 50 times in the figure) and criterion for the evaluation of the gap measure.

The average values, calculated as a function of the wall thickness and insertion speed, are reported in Fig. 15. The evaluation is repeated for the considered values of friction.



**Fig. 15.** Analysis of the maximum tube–fin gap: transparent surface (top) for diameter  $D_e = 15.875$  mm, shaded (bottom) for diameter  $D_e = 19.05$  mm.

## 5 Discussion: Analysis of the influence of the process parameters

In the following sections, the influence of the three factors considered in the analysis is discussed based on the numerical model results.

### 5.1 Friction coefficient

From the analysis of the effect of the friction coefficient  $f$  (Fig. 10), a strong influence on the driving force in the axial direction  $F_{d,a}$  is apparent, whereas the radial force  $F_{d,r}$  is only slightly affected. This confirms the result obtained from CuNi tubes, as reported by

Hwang and Altan [3]. Consequently, because the radial force is higher than the axial force, the friction coefficient  $f$  produces only a slight increase of the resultant  $R$  (Fig. 11). Increasing the friction coefficient  $f$  increases the angle  $\alpha$ , and this effect is explained by an increase in the friction force that is backward-oriented in the direction of the ogive motion. Moreover, the expansion of the tube is lower for higher friction, and this effect is explained by an increment of the energy dissipated by the friction forces. Consequently, the outer diameter of the tube  $D_e (= D_i + 2 t)$  is subjected to a lower expansion, and the force in the contact between the fins and the tube (Fig. 13) is affected as well. Finally, an increase in the maximum gap  $g_{max}$  is observed (Fig. 15, on the left) with higher friction.

## 5.2 Insertion speed

The insertion speed  $v$  also influences the ogive driving force, but much less than the friction coefficient. The two components (axial and radial) of the driving force (from Fig. 10) and the resultant force  $R$  (in Fig. 11) both increase with the insertion speed, so the angle  $\alpha$  remains almost constant. In terms of tube expansion, the insertion speed does not significantly affect the diameter and thickness variations. With higher friction coefficient values, however, a slight decrease in the contact force between the tubes and fins with the insertion speed  $v$  is noticeable, independent of the thickness. Instead, the insertion speed  $v$  has no significant influence on the gap (Fig. 15).

### 5.3 Tube thickness

The numerical model demonstrated that the tube thickness linearly influences the magnitude of both components of the driving force (Figs. 10 and 11) and the resultant  $R$ , whereas, again, the effect of the angle  $\alpha$  is negligible (Fig. 11b). The average radial force in the contact between the fins and the tube is slightly higher for  $t = 1.5$  mm considering the lowest friction coefficient value ( $f = 0.15$ ). At higher friction coefficient values (Fig. 10), the opposite trend is noticed. The component of force in the radial direction due to friction becomes more important. However, the variation is so small that further investigation seemed unnecessary; analysis of the interactions revealed a negligible correlation between these parameters. Finally, the maximum gap between the tube and fin is reduced by increasing the thickness (Fig. 15).

## 6. Conclusions

A detailed analysis of the mechanical process of stainless-steel tube expansion was performed. This process is used to produce air heat-exchangers with finned tubes. The analysis was based on the results of experimental tests on the material and on the process, as well as of subsequent simulations. First, the parameters of a suitable material model were obtained using the experimental results. The same data were then used to validate a numerical model of the tube expansion process. The models were based on the assumptions of axial symmetry, allowing for reduced 2D FE analyses. Such a simplified model was, however, adequate for a correct description of the analysed

problem. A good agreement between the numerical results — in terms of driving forces in the radial and axial directions — and the experimental data was revealed. The evaluation of the axial driving force is the main process parameter, as it is related to the power required for the process and therefore to the manufacturing costs.

A main outcome obtained concerns the effect of the main manufacturing and process parameters, namely tube geometry, insertion speed and friction, on the driving force. In addition, the model can give indications of the characteristics of the contact between the tubes and the fins. From the reported analysis, it appears that friction is the main influencing factor; to reduce the driving force, it is necessary to reduce friction.

Lubrication is essential to reduce the power and energy required for tube expansion, as well as to, as it appeared, improve the contact between the tubes and the fins by reducing the gap between these two parts.

Therefore, the model can be considered an important tool to predict the process and product performance of finned tube air heat-exchangers and could be a useful basis for the optimisation of the production process.

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The authors declare that no conflict of interest is present.

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