

Flux-Map Based FEA Evaluation of Synchronous Machine Efficiency Maps

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(Article begins on next page)

1       **The elastic modulus variation during the shotcrete curing jointly investigated by the**  
2       **convergence-confinement and the hyperstatic reaction methods**

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11       **ABSTRACT**

12       Induced stresses in sprayed concrete (or shotcrete) are quite complex to evaluate and depend on  
13       many factors such as the size and depth of the tunnel, the geomechanical characteristics of the  
14       surrounding ground in which the tunnel is excavated, the type of shotcrete, the evolution of its  
15       mechanical parameters over time and the excavation face advance rate. In particular, the  
16       evolution of the mechanical properties of the shotcrete is crucial regarding the interaction with the  
17       tunnel wall and the development of the bending moments and the normal forces which occur  
18       along the circumference of the lining. In this research, a new calculation procedure based on the  
19       combined use of two calculation methods the Convergence Confinement Method (CCM) and the  
20       Hyperstatic Reaction Methods (HRM) is presented. Thanks to this procedure, it is possible to  
21       progressively apply the load acting on the lining as the curing phase of the concrete progresses  
22       and therefore with the evolution of its mechanical parameters. This procedure has been applied  
23       to several examples of calculation, obtaining useful considerations regarding the mechanical  
24       behavior of the shotcrete lining when some fundamental parameters of the calculation change. As  
25       it is possible to achieve bending moments and forces in the lining with the progress of the load  
26       steps. It is also possible to determine the trend of the lining safety factor over time and at the end

27 of the loading phase, allowing a proper design of the support, with particular attention to the type  
28 of shotcrete and the thickness of the lining.

29 **Keyword:** Hyperstatic reaction method; Convergence confinement method; lining; shotcrete;  
30 rock; curing

31 **NOTATION LIST**

32	$A$	Area of the lining section
33	$E_{rm}$	Elastic modulus of the rock mass
34	$E_{,mean}$	Mean value of the elastic modulus of shotcrete
35	$E_{,t}$	Elastic modulus of shotcrete at the time $t$
36	$E_{,0}$	Value of the asymptotic elastic modulus of the shotcrete, for $t = \infty$
37	$\{F\}$	Nodal forces applied to the numerical model
38	$J_z$	Moment of inertia of the lining section
39	$K$	Global stiffness matrix
40	$k_i$	Local stiffness matrix of the element $i$ ;
41	$K_n$	Normal stiffness of the interaction spring in the node of the model
42	$K_0$	Lateral earth pressure
43	$K_s$	Shear stiffness of the interaction spring in the node of the model
44	$l$	Length of the one-dimensional element
45	$M$	Bending moment
46	$N$	Normal force
47	$p$	Internal tunnel pressure
48	$p_{cr}$	Critical pressure at the limit between the elastic and the plastic behavior
49	$p_{fict}$	Fictitious internal tunnel pressure
50	$p_0$	Lithostatic pressure
51	$R$	Tunnel radius
52	$r$	Generic radial coordinate
53	$\{S\}$	Vector of nodal displacements
54	$T$	Shear force
55	$t_0$	Final installation time of the support
56	$u$	Tunnel wall radial displacement
57	$\nu$	Poisson's ratio
58	$\alpha$	Time constants ( $t^{-1}$ ) of the curing equation for the elastic modulus
59	$\alpha_i$	Angle of inclination of the element $i$ th with respect to the horizontal
60	$\phi$	Rotation of the element in correspondence to the nodes

61	$\delta$	Advance step
	$\delta n$	nodal normal displacement between the structure and the rock mass
	$\delta s$	shear displacement between the structure and the rock mass
62	$\sigma_{c,t}$	Unconfined compressive strength for the shotcrete at the time $t$ .
63		

## 64 INTRODUCTION

65 Sprayed concrete or shotcrete (SC) is pumped under pressure through a pneumatic hose and  
66 projected into place at high velocity (30 to 50 m/s), which is compacted and finally cures (DIN  
67 18551, 1992; Thomas, 2009; Hemphill, 2013), see Fig. 1.

68 Because SC compared with ordinary concrete has a shorter setting time and high early age  
69 mechanical properties (Wang et al., 2015), it is normally used for solving stability problems in  
70 tunnels and other underground constructions such as mines, hydropower projects and slope  
71 stabilization (e.g. Melby, 1994). SC can be employed for temporary and permanent supports.  
72 However, regarding the design and construction of modern tunnels, SC single layer lining is  
73 becoming the trend of future development (Franzen et al., 2001). With SC as permanent final  
74 lining, long-term performance requirements, such as good bonding, high final density,  
75 compressive strength and chemical resistance, have to improve (Melby, 1994).

76 SC mechanical properties are influenced by its components such as cement, microsilica,  
77 aggregates, plasticizers, accelerators and fibers (Melby, 1994; Thomas 2009). Accelerators are  
78 particularly important in their selection as the use of SC in underground constructions requires the  
79 compliance with early age strength and the possibility of being employed in thick layers without  
80 the risk of detachments and movements (Prudencio, 1998).

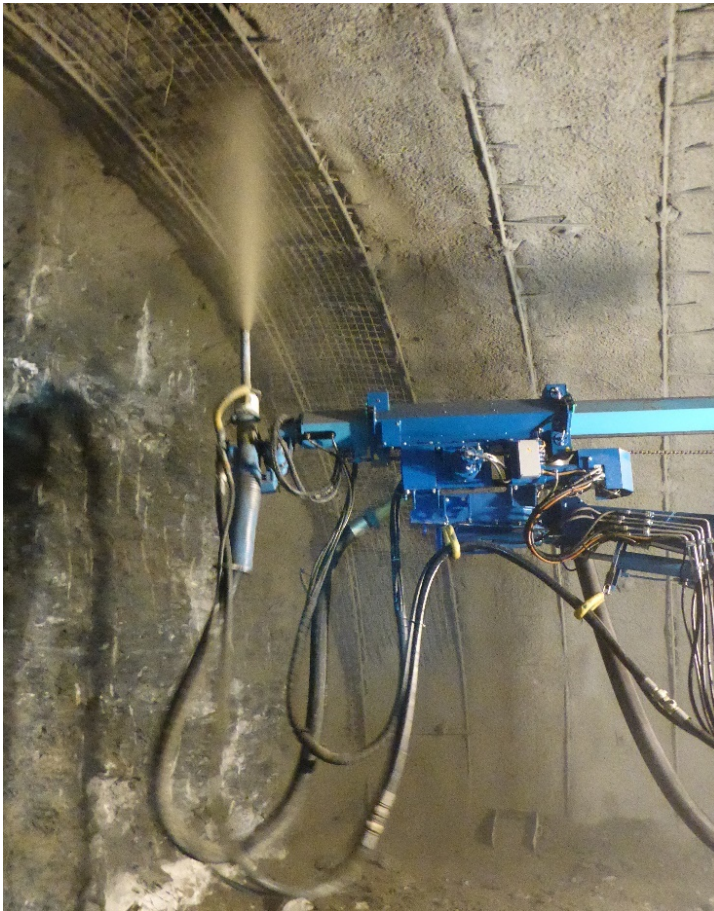
81 The early-age strength of SC is frequently more important than its ultimate strength. The advance  
82 speed of tunnel operations is strongly influenced by the rate of development of early-age  
83 strength, since it determines, both in soft ground and weak rock, when the excavation face can  
84 proceed again. As a matter of fact, re-entry is mainly influenced by the tunnel drive progression to  
85 ensure the safety of personnel to continue development (Mohajerani et al., 2015). Re-entry times  
86 range from 2 to 4 hours, where the Unconfined Compressive Strength (UCS) of the SC reaches  
87 1MPa (Clements, 2004; Concrete Institute of Australia, 2010), however, this value is not  
88 standardized and it can be also lower, if safety is ensured (see Rispin et al., 2009). Iwaki et al.  
89 (2001) empirically determined that an UCS of 0.5–1MPa should be an adequate strength for SC  
90 to protect against rock-fall, although the safe re-entry times, based on strength measurements, is  
91 still determined on project basis (Mohajerani et al., 2015).

92 Because coring should not take place until an UCS value of at least 5MPa (Clements, 2004), or  
93 between 8–10MPa, as Jolin and Beaupré (2003) suggest, the assessment of strength  
94 improvement is normally indirectly performed by means of the J-curves method for minimum  
95 strength (DIN EN 14487-1, 2006) by using the needle penetration method up to 1MPa strength  
96 (DIN EN 14488-2, 2006) and the stud driving method between 1 and 56 MPa strength (DIN EN  
97 14488-2, 2006; ÖVBB, 2006). Conventional compressive strength tests on cored samples are  
98 only performed from UCS from 5 to 100MPa according to the DIN EN 12504-1 (2009).

99 After the SC application, with the restart of the tunnel excavation, the lining load phase starts.  
100 This loading phase occurs during the curing of the SC when the mechanical characteristics  
101 (strength and stiffness) vary over time at a certain rate. Each load step, due to each excavation  
102 face advance, produces different effects on the lining, due to the different stiffness and strength of  
103 the SC. The final tensional state and, therefore, the final conditions of the lining are the ultimate  
104 result of this complex loading mechanism due to the excavation face advance (while the SC  
105 cures) and the corresponding variations in its mechanical characteristics (Oreste, 2003).

106 The Converge Confinement Method (CCM) and the Hyperstatic Reaction Method (HRM) have  
107 been used in this paper to study in detail the behavior of the tunnel support under external loads  
108 with increasing elastic modulus values of SC simulating the curing effect. CCM generally requires  
109 a mean stiffness of the SC lining to obtain the support reaction line (Oreste, 2003). In this  
110 research, the reaction line of the SC lining is considered as curve, in order to simulate the curing  
111 effect of the SC during the loading phase of the support. CCM was useful to evaluate the  
112 magnitude of the various loading steps developing over time during the excavation face advance.  
113 In the HRM the interaction between ground and support is represented by Winkler type springs.  
114 This method permits to determine the displacement of the lining and the developed bending  
115 moments and forces in order to design it (Oreste, 2007; Do et al. 2014a; 2014b). In the specific  
116 case, at the HRM model different loading steps, obtained with the CCM, have been applied,  
117 considering in each of these steps the effective stiffness value reached by the SC and hence by  
118 the support. Due to the results obtained with the combined analysis of the two calculation  
119 methods, it was possible to obtain a detailed evaluation of the stress state of the support, which

120 can consider both the effect of the characteristics of the SC employed (with the evolving curve of  
121 strength and stiffness with time) and the advance rate of the excavation face.



122

123 **Fig. 1 Spraying the tunnel roof with the shotcrete spraying machine (picture courtesy**  
124 **Roland Mayr, BASF)**

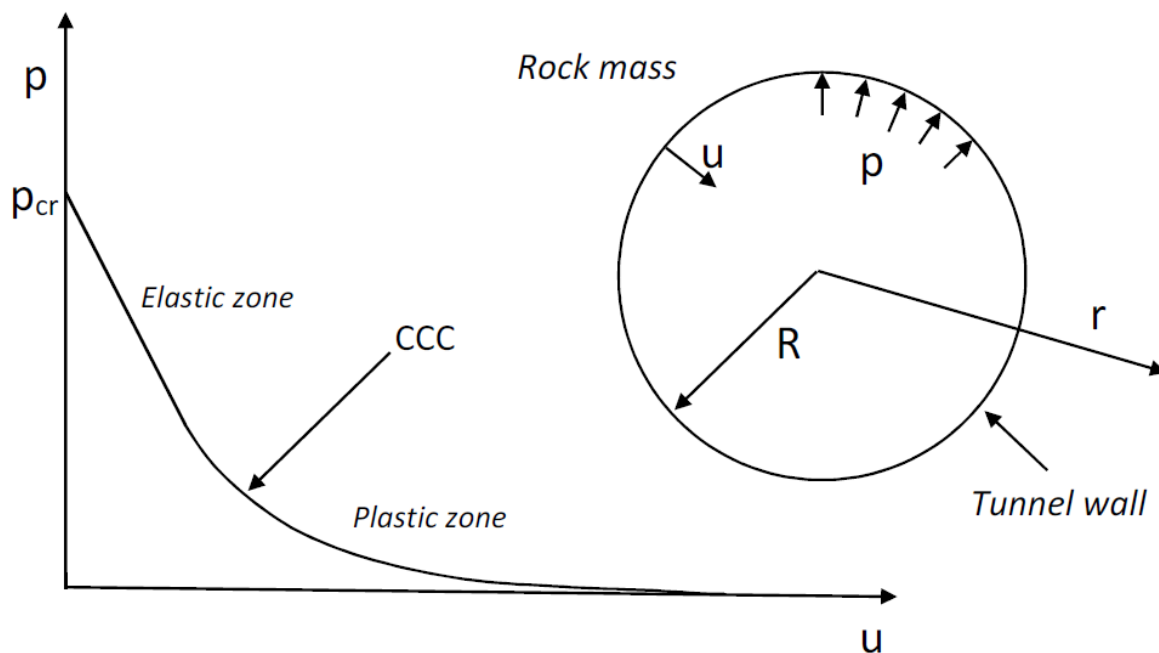
## 125 **NUMERICAL MODEL**

126 The numerical procedure developed to obtain a detailed analysis of the stress and strain state of  
127 a SC lining tunnel **presented in this paper can be studied easily by a combined analysis of CCM**  
128 **and HRM.** The necessary calculation parameters are as follows: mechanical parameters of the  
129 rock, tunnel radius, lithostatic stress state at the corresponding depth, lining thickness, evolving  
130 curve of the strength and stiffness of the SC over the time, the advance rate of the excavation  
131 face and the frequency and duration of the excavation operation stand still, to allow the support  
132 installation and other operations on the site.

133 The CCM is based on the analysis of the stress and strain state that develops in the rock around  
134 a tunnel. The simplicity of the method is due to the important hypotheses on which it is based  
135 (e.g. Oreste, 2009; 2014; Spagnoli et al., 2017):

- 136 • Circular and deep tunnels (boundary conditions of the problem to infinity);
- 137 • Lithostatic stresses of a hydrostatic type and constant in the surrounding medium of the  
138 tunnel (the variation of the stresses with depth due to the weight of the rock is neglected);
- 139 • Continuous, homogeneous and isotropic rock mass;
- 140 • Bi-dimensional problem and plane stress field.

141 CCM consists of the definition of the convergence-confinement curve (CCC), that is the  
142 relationship between the internal pressure and the radial displacement ( $p - |u|$ ) on the boundary  
143 of the tunnel represented by a circular void (Oreste, 2009), see Fig. 2.



144  
145 **Fig. 2: Convergence-confinement method: Geometry of the problem and example of a**  
146 **convergence-confinement curve. Key:  $p$ : Internal tunnel pressure,  $R$ : Tunnel radius,  $r$ :**  
147 **Radial coordinate,  $u$ : Radial displacement of the tunnel wall,  $p_{cr}$ : Critical pressure**  
148 **(modified by Oreste, 2009).**

149 Along with the CCC it is possible to draw on the same graph also the reaction line of the SC lining  
150 (RLSL). This reaction line starts from a point on the abscissa (where pressure is zero) but the  
151 displacement  $u^*$  is different from zero. The pressure  $p$  (the radial load on the lining,

152 corresponding also to the radial pressure applied by the lining on the tunnel wall) increases with  
 153 increasing displacement  $u$  (the radial displacement of the tunnel wall). At the lining installation  
 154 (initial point of the reaction line), the pressure applied at the extrados is zero, but a displacement  
 155 of the tunnel wall,  $u^*$ , already occurred (Oreste, 2003). The reaction line is concave because the  
 156 stiffness of the SC increases over the time, causing increased loads on the lining and reduced  
 157 radial displacement of the tunnel wall (Oreste, 2003), see Fig. 3. The pressure difference at a  
 158 certain displacement level  $u$  between the CCC and RLSL is called fictitious pressure ( $p_{fict}$ ) and it  
 159 is the static contribute of the excavation face on the investigated vertical section of the tunnel.  
 160 The fictitious pressure can be evaluated as a function of the (positive) distance  $x$  between the  
 161 investigated section and the excavation face, with the well-known equation of Panet and Guenot  
 162 (1982):

$$p_{fict} = a \cdot p_0 \cdot \frac{b}{x + b} \quad (1)$$

163 Where:  $a = 0.72$  and  $b = 0.845 \cdot R$ .

164 Starting from the initial point of the reaction line ( $p = 0; u = u^*$ ) and knowing the initial elastic  
 165 modulus of the SC after the re-entry, it is possible to obtain the initial slope of the reaction line,  $k$   
 166 (Oreste, 2009) based on the support geometry (tunnel radius and thickness), the elastic modulus  
 167 and the Poisson ratio,  $\nu$ , of the SC. Proceeding with a numerical approach, an initial segment of  
 168 the RLSL for a small increase  $\Delta u$  of  $u$  is drawn. At the end of this first segment,  $p_{fict}$  can be  
 169 evaluated as the difference between CCC and RLSL and from the fictitious pressure the distance  
 170  $x$  reached by the excavation face, using equation 1 (Fig. 3).

171 As excavation advance rate is known, and hence the relation linking  $x$  to the time,  $t$ , at each  
 172 distance  $x$  reached by the excavation face with respect to the investigated section, a time value  $t$   
 173 corresponding subsequent to the SC lining installation can be given. At first load step  $\Delta p$   
 174 (evaluated as the difference from the final value and the initial value of  $p$  in the first segment of  
 175 the RLSL) the reached time at the end of the first segment can be associated and therefore also  
 176 the mean elastic modulus of the SC in the period corresponding to the initial linear part of RLSL.  
 177 The method continues in the same way for successive small linear segments, until the  
 178 intersection between the CCC and the RLSL is obtained. The intersection point between the two

179 curves represents the final stage of the loading process when the excavation face is advanced at  
 180 a distance where static effects on the investigated vertical section of the tunnel are negligible  
 181 (Fig. 3).

182 The procedure for the generic calculation step  $j$  is the following:

- 183 • Evaluation of the pressure  $p$  reached by the RLSL in the final point of the previous  
 184 segment  $p_{lin,j-1}$  and by difference between CCC and RLSL in such a point, evaluation of  
 185 the fictitious pressure  $p_{fict,j-1} = p_{j-1} - p_{lin,j-1}$ ,  $p_{j-1}$  is the pressure read on CCC in  
 186 correspondence of the displacement  $u_{j-1}$ ;
- 187 • If the  $p_{fict,j-1}$  is known, the corresponding distance  $x_{j-1}$  of the excavation face is  
 188 calculated using equation 1;
- 189 • Knowing the face advance rate, the duration and frequency of still stands of the  
 190 excavation phase, i.e. the relation  $x = f(t)$ , it is possible to determine the time  $t_{j-1}$   
 191 subsequent to the installation of the SC in the investigated section;
- 192 • If the evolving trend of the elastic modulus of the SC over the time is known, it is possible  
 193 to determine the elastic modulus  $E_{j-1}$  and therefore the stiffness of the SC lining  $k_{j-1}$  in  
 194 function of the time  $t_{j-1}$ ;
- 195 • The knowledge of the stiffness  $k_{j-1}$  allows to draw the new straight line of the RLSL for  
 196 the step  $j$  for a predetermined amplitude of the radial displacement  $u$  equal to  $\Delta u$ ; at the  
 197 end of such a segment we obtain:  $p_{lin,j} = p_{lin,j-1} + k_{j-1} \cdot \Delta u$ ;
- 198 • The difference  $p_{lin,j} - p_{lin,j-1}$  is the loading step  $\Delta p_{lin,j}$  of the step  $j$ , linked to the mean  
 199 elastic modulus of the SC,  $E_{mean,j}$  in the step  $j$  where  $E_{mean,j} = 0.5(E_{j-1} + E_j)$ .

200 Therefore, in the detailed study of the stress state in the SC lining, the knowledge of the evolving  
 201 trend of the SC,  $E = f(t)$ , is fundamental. Generally, the variation of the UCS over the time,  
 202  $\sigma_c = f(t)$ , is evaluated. Then, the relation between the elastic modulus and UCS is considered  
 203 constant over time. This is given by the equation of Chang (1993):

$$\sigma_{c,t} = \left( \frac{E_{t}}{3.86} \right)^{1/0.6} \quad (2)$$

204 Where:

205  $E_{t}$  is the SC elastic modulus at the time  $t$ ;

206  $\sigma_{c,t}$  is the UCS for the SC at the time  $t$ .

207 A method to represent the variation of the elastic modulus over the time is given by Pottler  
208 (1990):

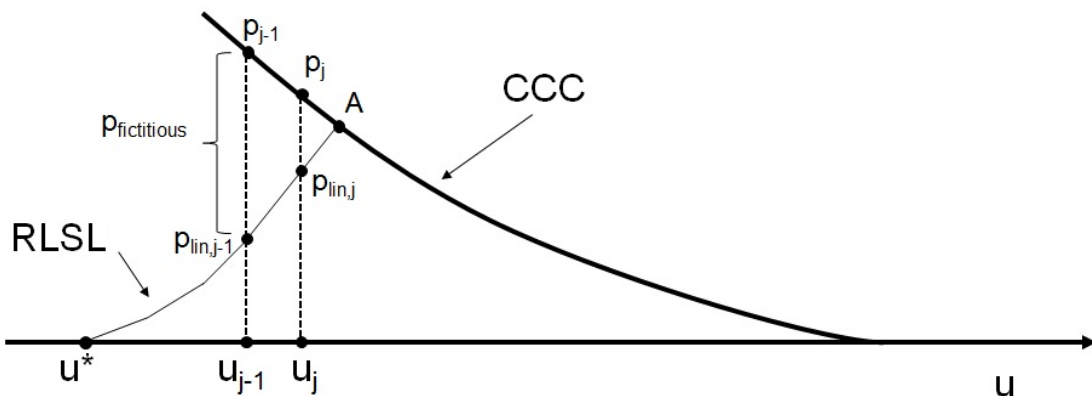
$$E_t = E_0 \cdot (1 - e^{-\alpha t}) \quad (3)$$

209 Where:

- 210 •  $E_t$  is the SC elastic modulus at the time  $t$ ;
- 211 •  $E_0$  is the value of the asymptotic elastic modulus of the SC, for  $t = \infty$ ;
- 212 •  $\alpha$  is a time constant ( $t^{-1}$ ).

213 From the practical point of view, UCS of SC is measured over the time subsequent to the lining  
214 installation and from these values, a series of elastic modulus values for different times is  
215 obtained.

216 Then the negative exponential curve, which best approximates these obtained points, i.e. the  
217 pairs of values of the elastic modulus and the associated time, is obtained. This curve will have a  
218 particular value of the asymptotic elastic modulus,  $E_0$ , and of the coefficient  $\alpha$  in equation 3.



219  
220 **Fig. 3 Convergence-confinement curve and reaction curve of the shotcrete lining with**  
221 **numerical integration of the reaction curve of the shotcrete lining and a calculation step. A**  
222 **is the interaction between reaction line and CCC to identify the final load process. Not to**  
223 **scale.**

224 The analysis with HRM permits to evaluate in detail the behavior of SC (Oreste, 2007). In more  
225 detail, it is possible to analyze the interaction between the SC lining and the surrounding rock  
226 mass, during the loading phase of the support. This loading phase can take place gradually,  
227 depending on the different load steps identified in the CCM analysis as outlined above. At each

228 load step, the stiffness value of SC lining is updated. HRM allows to obtain the exact course of  
 229 the bending moment ( $M$ ), the normal force ( $N$ ) and the shear force ( $T$ ) along the whole SC lining  
 230 at each load step and at the end of the loading stage of the lining (in the final state when the  
 231 excavation face is far from the investigated section). The knowledge of the values of  $M$ ,  $N$ , and  $T$   
 232 allows to evaluate at each point of the lining the normal and the shear stresses that are  
 233 developed, and thus also the safety factor against the SC failure. It is therefore possible to  
 234 determine the minimum safety factor present along the SC lining, for each load step and at the  
 235 end of the loading phase of the support. Very interesting is the determination of the safety factor  
 236 over time: in this way, it is possible to check whether the SC lining has transient conditions in  
 237 which the safety factor drops to lower values than the obtained final value. HRM is based on the  
 238 finite element method (FEM) and consists in dividing the SC lining of the tunnel into one-  
 239 dimensional elements. These elements have axial and flexural stiffness and are therefore able to  
 240 develop axial displacements, lateral displacements and rotations at their ends. The one-  
 241 dimensional elements are interconnected in succession through nodes. At each node, Winkler  
 242 springs are applied in both perpendicular and tangential direction to the lining. These springs  
 243 allow to simulate the interaction between the lining and the rock wall.

244 From the local stiffness matrix of each element it is possible to come to the definition of the  
 245 overall stiffness matrix of the lining. In this paper only half of the lining was considered, for  
 246 symmetry reasons with respect to the vertical axis passing through the center of the tunnel. The  
 247 elements considered are 36, therefore the total number of nodes is 37. The global stiffness matrix  
 248  $K$  is given by the following expression:

$$K = \begin{bmatrix} k_{1,a} & k_{1,b} & 0 & 0 & 0 & \dots & 0 \\ k_{1,c} & k_{1,d} + k_{2,a} & k_{2,b} & 0 & 0 & \dots & 0 \\ 0 & k_{2,c} & k_{2,d} + k_{3,a} & k_{3,b} & 0 & \dots & 0 \\ 0 & 0 & k_{3,c} & k_{3,d} + k_{4,a} & \ddots & \dots & 0 \\ 0 & 0 & 0 & \ddots & \ddots & \ddots & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \ddots & k_{i,b} \\ 0 & 0 & 0 & 0 & 0 & k_{i,c} & k_{i,d} \end{bmatrix} \quad (4)$$

249 where the terms  $k_{i,a}$ ,  $k_{i,b}$ ,  $k_{i,c}$ ,  $k_{i,d}$  represent the 3x3 sub-matrices of the local  $k_i$  stiffness matrix  
 250 of the  $i$ th one-dimensional element of the SC lining:

$$k_i = \begin{bmatrix} \frac{EA}{I}c^2 + \frac{12EJ}{I^3}zs^2 & \frac{EA}{I}c^2 - \frac{12EJ}{I^3}zs^2 & -\frac{6EJ}{I^2}zs & -\frac{EA}{I}c^2 - \frac{12EJ}{I^3}zs^2 & -\frac{EA}{I}c^2 + \frac{12EJ}{I^3}zs^2 & -\frac{6EJ}{I^2}zs \\ \frac{EA}{I}cs - \frac{12EJ}{I^3}zc^2 & \frac{EA}{I}s^2 + \frac{12EJ}{I^3}zc^2 & \frac{6EJ}{I^2}zc & -\frac{EA}{I}cs + \frac{12EJ}{I^3}zc^2 & -\frac{EA}{I}s^2 - \frac{12EJ}{I^3}zc^2 & \frac{6EJ}{I^2}zc \\ -\frac{6EJ}{I^2}zs & \frac{6EJ}{I^2}zc & \frac{4EJ}{I}z & \frac{6EJ}{I^2}zs & -\frac{6EJ}{I^2}zc & \frac{2EJ}{I}z \\ -\frac{EA}{I}c^2 - \frac{12EJ}{I^3}zs^2 & -\frac{EA}{I}cs + \frac{12EJ}{I^3}zc^2 & \frac{6EJ}{I^2}zs & \frac{EA}{I}c^2 + \frac{12EJ}{I^3}zs^2 & \frac{EA}{I}cs - \frac{12EJ}{I^3}zc^2 & \frac{6EJ}{I^2}zs \\ -\frac{EA}{I}cs + \frac{12EJ}{I^3}zc^2 & -\frac{EA}{I}s^2 - \frac{12EJ}{I^3}zc^2 & -\frac{6EJ}{I^2}zc & \frac{EA}{I}cs - \frac{12EJ}{I^3}zc^2 & \frac{EA}{I}s^2 + \frac{12EJ}{I^3}zc^2 & -\frac{6EJ}{I^2}zc \\ -\frac{6EJ}{I^2}zs & \frac{6EJ}{I^2}zc & \frac{2EJ}{I}z & \frac{6EJ}{I^2}zs & -\frac{6EJ}{I^2}zc & \frac{4EJ}{I}z \end{bmatrix} \quad (5)$$

$c = \cos \alpha_i \quad s = \sin \alpha_i$

251 where  $\alpha_i$  is the angle of inclination of the element  $i$ th with respect to the horizontal;  $E$  is the  
252 elastic modulus of SC lining,  $A$  the area of the lining section,  $J$  the moment of inertia of the lining  
253 section,  $l$  is the length of the one-dimensional element.

254  $[k_{i,a}], [k_{i,b}], [k_{i,c}], [k_{i,d}]$  are thus positioned within the local stiffness matrix  $k_i$ :

$$[k]_i = \begin{bmatrix} k_{i,a} & k_{i,b} \\ k_{i,c} & k_{i,d} \end{bmatrix} \quad (6)$$

255 The elements of a diagonal band of the global stiffness matrix (equation 4) are then modified to  
256 add the values of the normal and tangential stiffness of the springs simulating the interaction of  
257 the SC lining with the rock wall (Oreste, 2007).

258 Once the global stiffness matrix  $K$  is defined, and knowing the vector of the nodal forces  $\{F\}$   
259 applied to the numerical model (i.e. the external loads applied to the lining), it is possible to  
260 determine the vector of nodal displacements  $\{S\}$  from the following relation:

$$[K] \cdot \{S\} = \{F\} \quad (7)$$

261 From the vector of the nodal displacements, it is possible to obtain the radial displacements of the  
262 lining, which give indications of its global deformation and also of the interactions with the rock  
263 wall. From the nodal displacements, it is also possible to obtain the normal force  $N$ , the shear  
264 force  $T$  and the bending moment  $M$ . From these stress characteristics, it is possible to define in  
265 detail the existing stress state in the lining and, therefore, also the factor of safety that the lining  
266 reaches for each load step and over time.

267 For each load step of the lining, the global stiffness matrix as function of the elastic modulus of  
268 SC reached for the specific load step is evaluated. The load step is used in order to determine the

269 nodal forces for each step. The vector of the nodal displacements obtained for each load step will  
 270 update the total displacements achieved; the values of  $M$ ,  $N$ ,  $T$  and the normal tangential stresses  
 271 obtained for each load step update the corresponding overall values achieved. The final situation  
 272 is represented by the total displacements and total stresses, as the sum of the values obtained  
 273 for each step of loading.

## 274 **NUMERICAL RESULTS AND DISCUSSION**

275 The calculation procedure proposed in this article has been applied to some examples, in order to  
 276 verify which can be the effect on the stress state in the SC lining, by varying the characteristics of  
 277 the SC (in particular the curing rate and final elastic modulus) and the advance rate of the  
 278 excavation face.

279 Different geometries of the tunnel were considered, along with various rock mass types. In  
 280 general, six main examples are presented, each of which has four cases. The cases considered  
 281 include the following assumptions, in accordance with the underlying hypotheses of the  
 282 calculation methods which were used in the procedure presented.

- 283 • a bi-dimensional stress state considering circular and deep tunnels;
- 284 • a continuous, homogeneous and isotropic rock mass.

285 The first example (example 1) refers to a tunnel of 2m radius excavated in a rock of poor quality.  
 286 The geomechanical parameters are shown in Tab. 1. The lithostatic stress  $p_0$  is 7MPa and the  
 287 fictitious internal pressure  $p_{fict}$  at the face is  $0.72 \cdot p_0$ , where the SC lining is installed. SC lining  
 288 has a thickness of 20cm. The horizontal stress in the lithostatic environment is  $\frac{1}{2}$  of the vertical  
 289 one ( $K_0 = 0.5$ ).

<b>Rock Mass Parameters</b>	
Elastic modulus [MPa]	3160
Poisson's ratio	0.30
Peak cohesion [MPa]	0.15
Residual cohesion [MPa]	0.12
Peak angle of friction [°]	20
Residual angle of friction [°]	16
Dilatancy [°]	16

290 **Table 1. Geomechanical parameters for the rock mass for example 1**

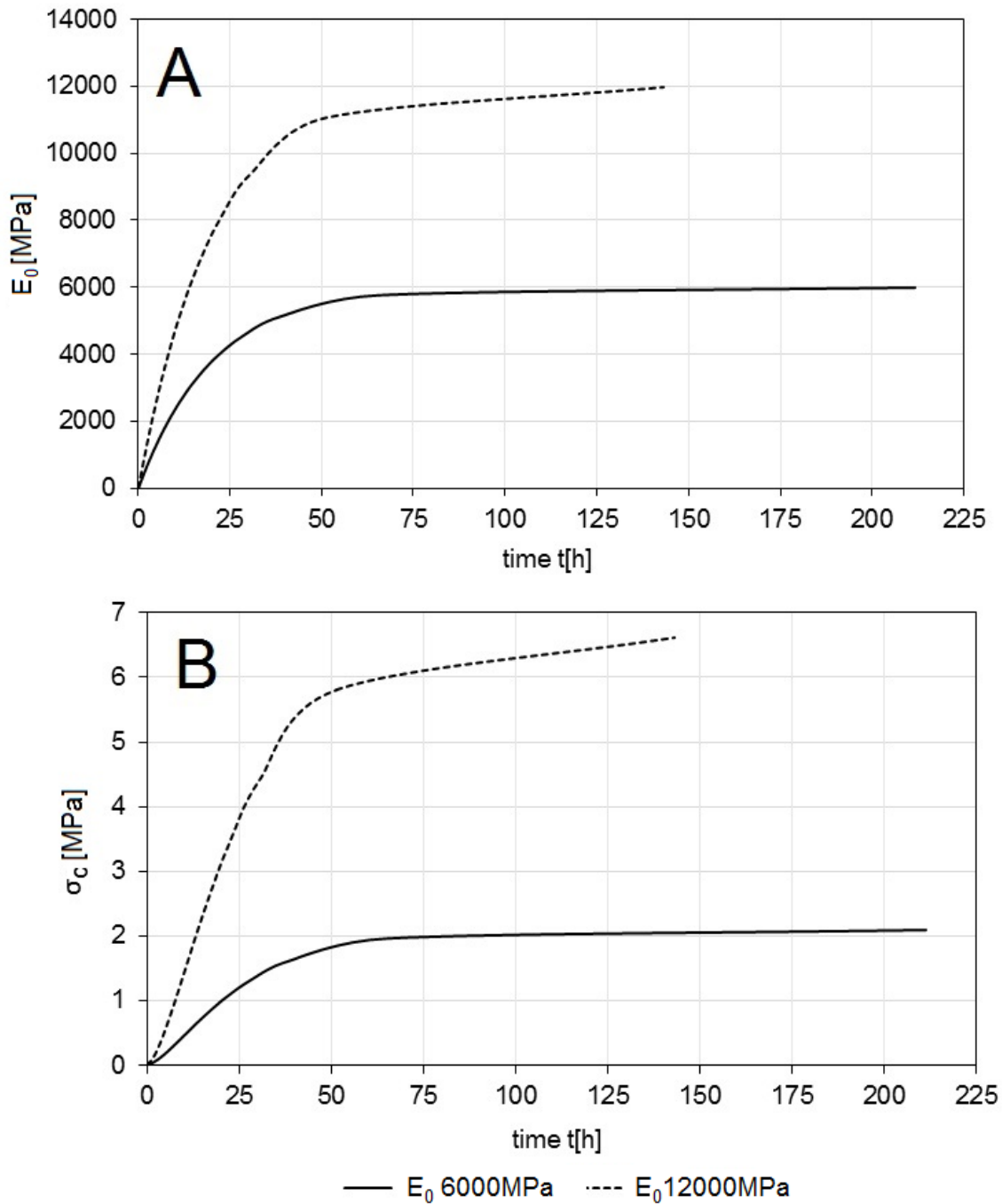
291 Since the calculation procedure uses HRM, the values of the stiffness of the interaction springs of  
292 the support with the ground are obtained by the following expressions:

$$293 \quad K_n = 2 \cdot \frac{E_{rm}}{R} \cdot b \quad (8)$$

$$294 \quad K_s = \frac{K_n}{2} \quad (9)$$

295 Where:  $b = 2 \cdot R \cdot \cos(2,5^\circ) \cdot \sin(2,5^\circ)$ ,  $R$  and  $E_{rm}$  is the elastic modulus of the rock mass.

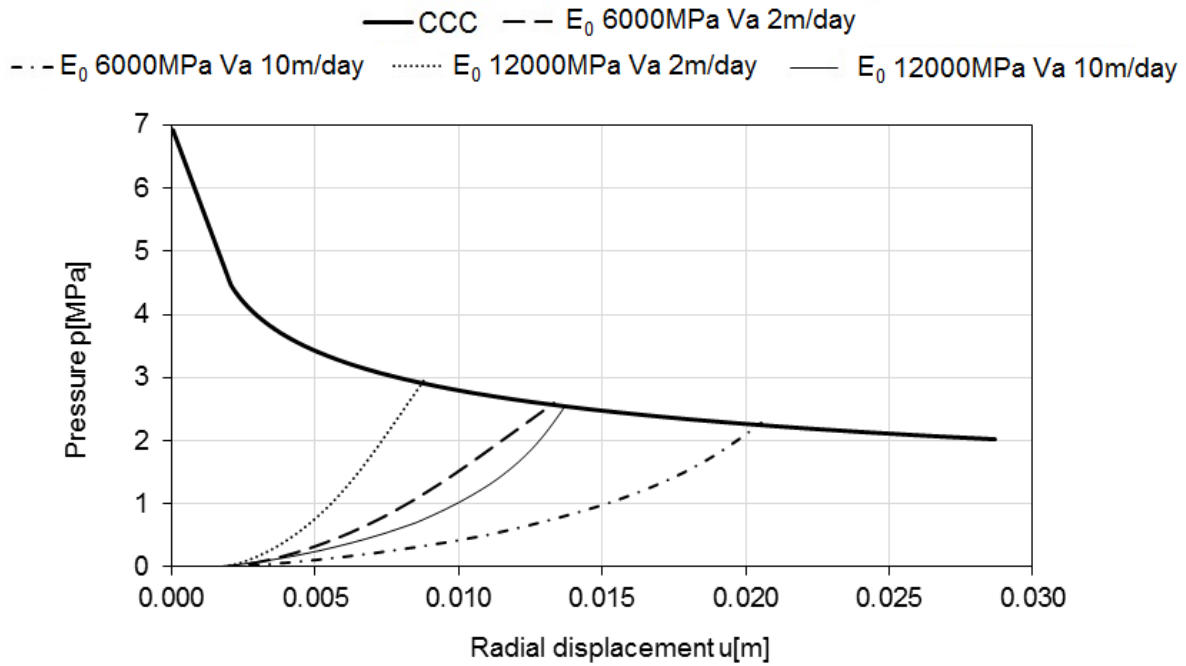
296 Two different types of SC were assumed with a final and asymptotic value of the elastic modulus  
297 ( $E_{,0}$ ) of 6000 and 12000MPa, both with a Poisson's ratio,  $\nu$ , 0.15. The time constant  $\alpha$  has a value  
298 of  $0.05 \text{ h}^{-1}$  in both cases (eq. 3). The diagrams relating the modulus of elasticity and UCS varying  
299 with time are shown in Fig. 4.



300  
 301 **Fig. 4 Progressive increase of the asymptotic elastic modulus (A) and UCS (B) of the**  
 302 **shotcrete with time for the two considered typologies in the example 1.**

303 The other parameter to be varied is the daily mean rate of tunnel advance (assumed as 2 m/day  
 304 and 10m/day), with support installation time  $t_0$  and the advance step  $\delta$  equal to 1h and 1.2m,  
 305 respectively.

306 The reaction lines of the SC linings are shown in Fig. 5 for the four analyzed cases.



307

308 **Fig. 5 Reaction curves of the SC lining as a function of the face advance rate (Va) and the**  
 309 **mechanical characteristics of the shotcrete for the example 1.**

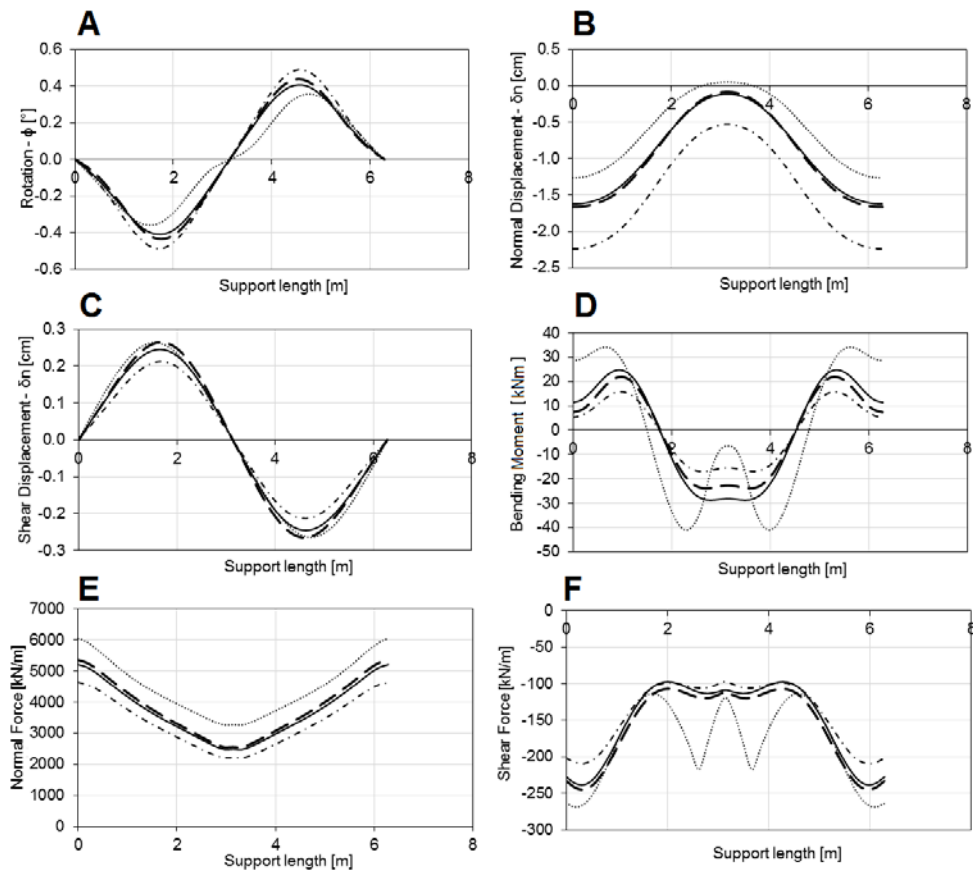
310 It is possible to see in Fig. 5 the change of the equilibrium point (intersection between the CCC  
 311 and the SCRL) for each of the cases. In addition, it can be observed that the reaction line is not  
 312 straight but curved. This is because the calculation model considers the curing time of the SC, i.e.  
 313 the progressive increase of the modulus of elasticity and UCS from the installation of the support  
 314 to the point at which the maximum asymptotic strength and stiffness of the SC has been  
 315 obtained.

316 The influence of the SC type and advance rate (Va) appears to be very important in the final  
 317 evaluation of the equilibrium point and, hence, of the final loading on the SC lining and the final  
 318 displacement of the tunnel wall.

319 The final load on the lining, as well as the final displacement of the tunnel wall, may vary  
 320 significantly depending on the type of SC used and the tunnel face advancing speed. The highest  
 321 final stress values are found for the most rigid type of SC and the lowest advance rate.

322 Also the stress and displacement characteristics of the lining can vary significantly. In the  
 323 following the values referring to the final condition (at the equilibrium point) for example 1 are  
 324 shown (Fig. 6).

—  $E_0$  6000MPa  $V_a$  2m/day    ···  $E_0$  6000MPa  $V_a$  10m/day    ·····  $E_0$  12000MPa  $V_a$  2m/day    - -  $E_0$  12000MPa  $V_a$  10m/day



325

326 **Fig. 6 Variation of the rotation (A), normal displacement (B), shear displacement (C),**  
 327 **bending moment (D), normal force (E) and shear force (F) for the two considered type of**  
 328 **SC and two assumed advance rates ( $V_a$ ) of the tunnel face, with reference to the final**  
 329 **equilibrium point (example 1).**

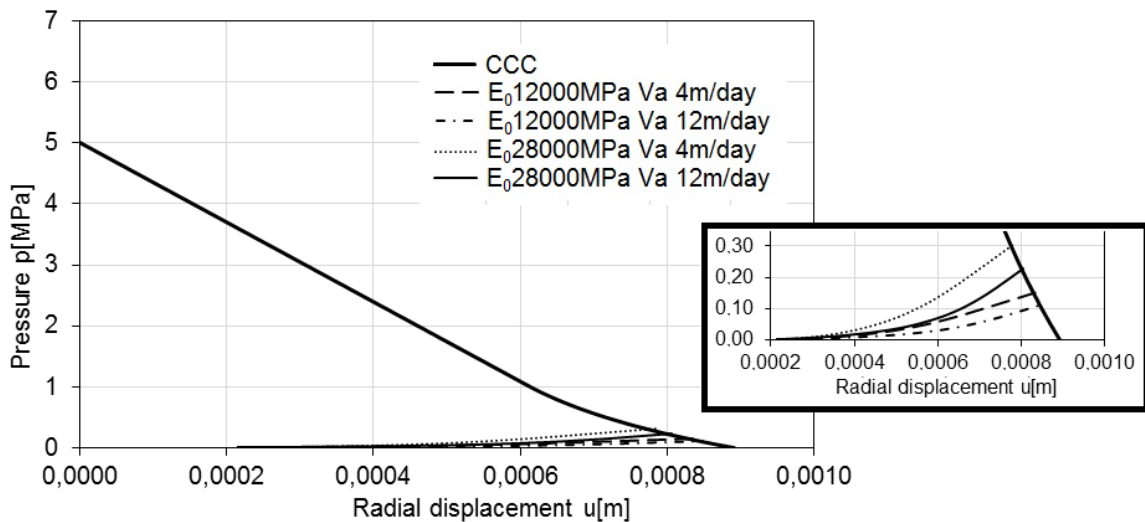
330 Of particular interest is the trend of normal displacements, bending moments, normal and shear  
 331 forces along the lining (*i.e. length of the beam elements considered for the calculation*). Lower  
 332 stiffness during the concrete setting period and faster advance speed provide larger normal  
 333 displacements. Conversely, higher stiffness and lower advance rate produce lower normal  
 334 displacements. The highest peak moments are detected in the lining when using high stiffness  
 335 SC and low advance speed. The opposite is for lower stiffness and higher advance speed. Same  
 336 considerations can be made for normal and shear forces.

337 In the example 2 a tunnel with a radius  $R$  of 2.5m, excavated in a rock with poor mechanical  
 338 properties (RMR=40, see Tab. 2), is considered. The lithostatic pressure  $p_0$  is 5MPa. Also in this  
 339 example, the lining thickness is 20cm and  $K_0$  is 0.5.

Rock Mass Parameters	
Elastic modulus [MPa]	21170
Poisson's ratio	0.30
Peak cohesion [MPa]	1.5
Residual cohesion [MPa]	1.5
Peak angle of friction [°]	33
Residual angle of friction [°]	33
Dilatancy [°]	16

340 **Table 2. Geomechanical parameters for the rock mass in the example 2**

341 Four different cases were analyzed in which higher final elastic modulus values of the support  
342 ( $E_0$ ) were taken as 12000 and 28000MPa. The  $\alpha$  time constant has a value of  $0.05 \text{ h}^{-1}$  and the  
343 Poisson's ratio  $\nu$  of 0.15. The tunnel advance daily rates were arbitrary assumed to be 4 m/day  
344 and 12 m/day, with support installation time  $t_0$  and the advance step  $\delta$  of 1 h and 1.2 m  
345 respectively. The different reaction lines of the SC lining in conjunction with the CCCs are  
346 presented in Fig. 7, where it is possible to identify the equilibrium point corresponding to each  
347 analyzed case.

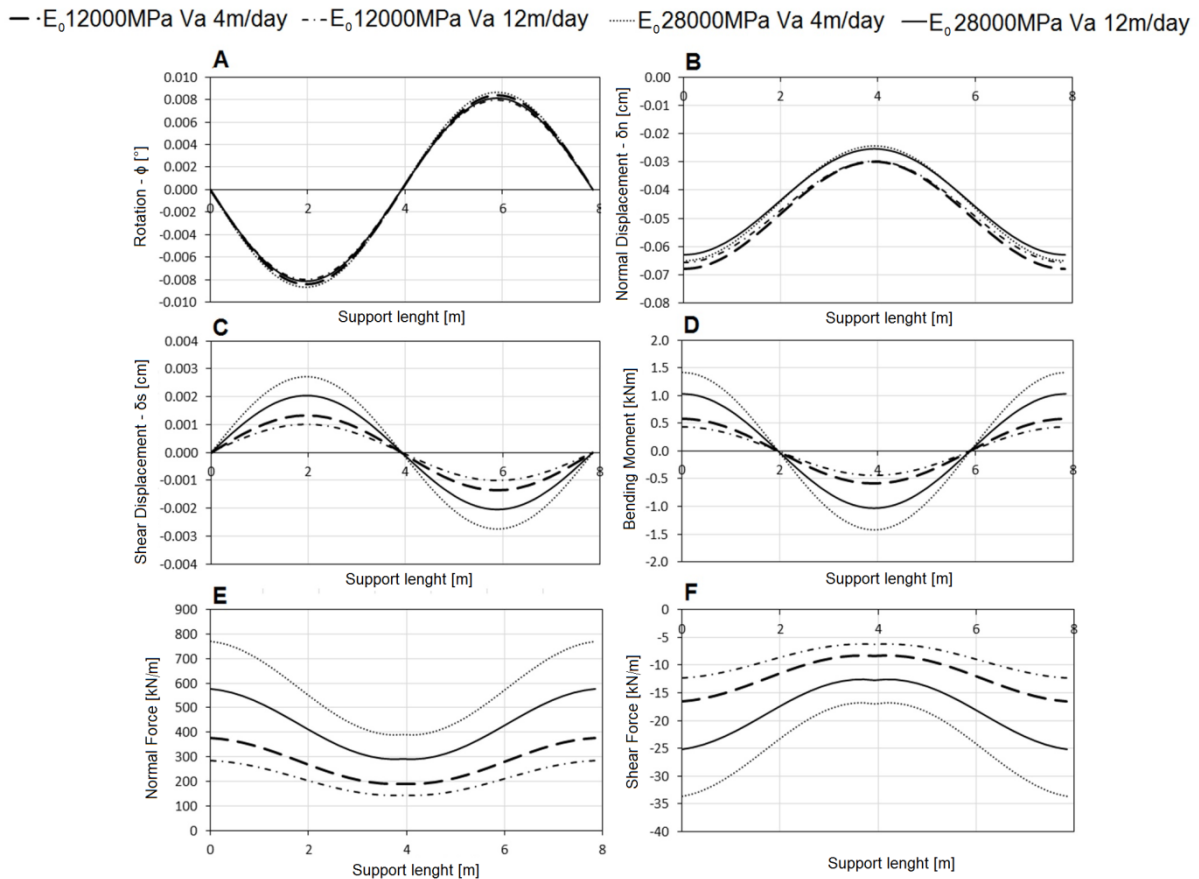


348

349 **Fig. 7 Reaction curve of the shotcrete lining (with enlargement on the right side) as a**  
350 **function of the face advance rate (Va) and the shotcrete type considered in the example 2.**

351 In this second example, lower final pressures are observed on the lining, but the differences  
352 between the 4 cases considered are in very high percentages. Higher final pressures have a  
353 higher final elastic modulus and a lower advance rate.

354 The results in terms of displacements and stress characteristics along the lining circumference for  
 355 the four cases presented in this example, when the final condition is reached, are shown in Fig. 8.



356  
 357 **Fig. 8 Variation of the rotation (A), normal displacement (B), shear displacement (C),**  
 358 **bending moment (D), normal force (E) and shear force (F) for the two considered types of**  
 359 **SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the**  
 360 **final equilibrium point (example 2).**

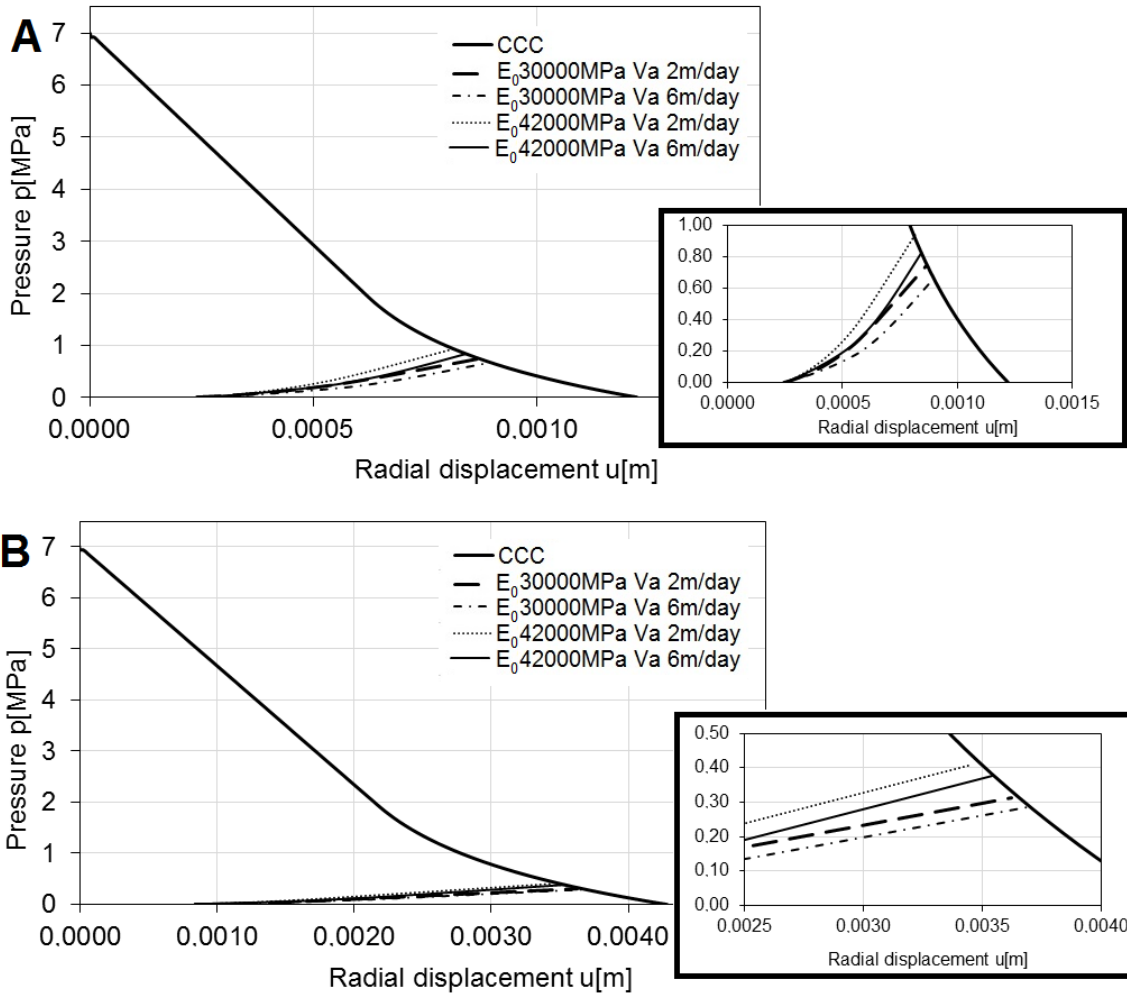
361 Examples 3 and 4 refer to two tunnels built on rock with the same characteristics, differing from  
 362 one another only in size. Examples three and four were analyzed in four different cases, in which  
 363 the elastic modulus values of SC were obtained by the UCS values given in Melbye (1994). The  
 364 first proposed SC installation was implemented in the tunnel of Blisadona (Austria) where a final  
 365 value of elastic modulus of 30000MPa was calculated based on equation 2. The second is a SC  
 366 installed in a tunnel located at Quarry Bay Station (Hong Kong) where a final value of elastic  
 367 modulus of 42000MPa was calculated. The time constant  $\alpha$  (equation 3) and the Poisson's ratio  $\nu$   
 368 of the SC were assumed to be  $0.05 \text{ h}^{-1}$  and 0.15 respectively. The mechanical properties of the  
 369 rock mass arbitrary assumed for these examples are shown in Tab. 3. For the example 3 a radius  
 370 of 2m has been assumed, while for the example 4 a larger dimension with a radius of 7m has

371 been hypothesized. The in situ hydrostatic stress  $p_0$  was assumed as 7MPa, with a SC lining  
 372 thickness of 20cm and  $K_0$  value of 0.5. The daily advance rates were arbitrary assumed for both  
 373 examples 2m/day and 6m/day, with installation time of the support  $t_0$  equal to 6h and the  
 374 advance step  $\delta$  of 3.5m.

<b>Rock Mass Parameters</b>	
Elastic modulus [MPa]	21170
Poisson's ratio	0.30
Peak cohesion [MPa]	1.5
Residual cohesion [MPa]	1.5
Peak angle of friction [°]	33
Residual angle of friction [°]	33
Dilatancy [°]	16

375 **Table 3. Geomechanical parameters for the rock mass for example 3 and 4**

376 In Fig. 9 the reaction lines of the SC lining for the four considered cases are shown. It is worth  
 377 noticing as for the example of the smallest tunnel (example 3), considering all the other  
 378 parameters being equal in the calculation, the differences in terms of final load on the lining and  
 379 final tunnel wall displacement are more pronounced. In the case of a large tunnel (example 4),  
 380 the differences between the 4 cases examined are smaller.  
 381 However, even in these two calculation examples it is noted that the major final pressures are  
 382 observed for the lining with a higher stiffness and with lower face advance rate.

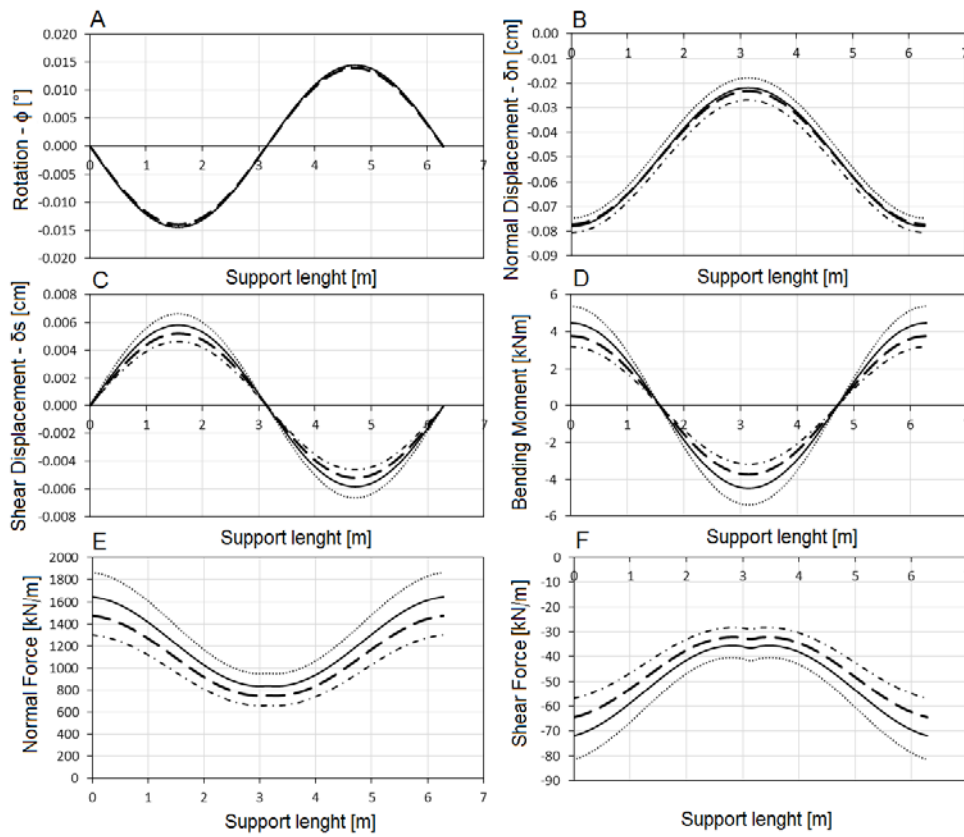


383

384 **Fig. 9 CCCs and reaction curve of the shotcrete lining (with enlargement on the right side)**  
 385 **as a function of the velocity of advance (Va) and the final elastic modulus of the shotcrete,**  
 386 **for example 3 (A) and example 4 (B).**

387 Displacements and stress characteristics along the lining are shown in Figs. 10 and 11.

—  $E_0$ 30000MPa  $V_a$  2m/day    - - -  $E_0$ 30000MPa  $V_a$  6m/day    .....  $E_0$ 42000MPa  $V_a$  2m/day    —  $E_0$ 42000MPa  $V_a$  6m/day

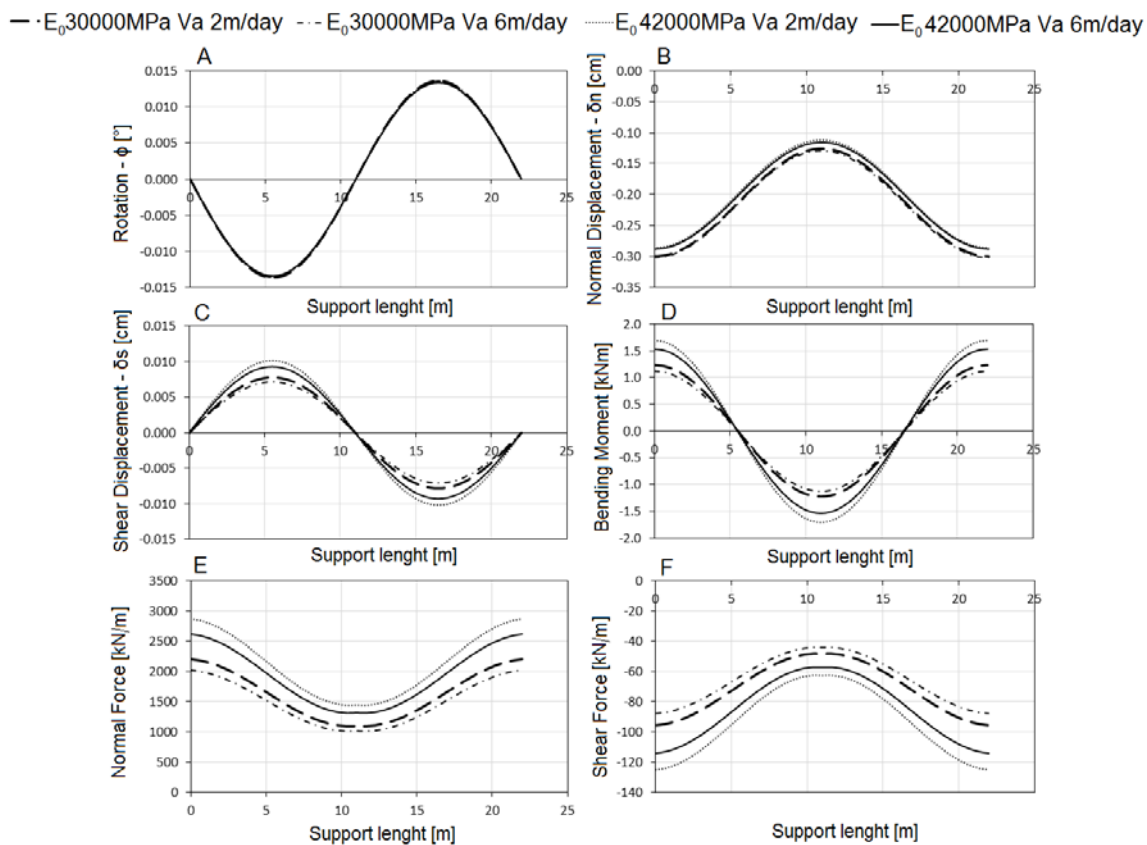


388

389 **Fig. 10** Variation of the rotation (A), normal displacement (B), shear displacement (C),  
 390 bending moment (D), normal force (E) and shear force (F) for two considered types of SC  
 391 and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the final  
 392 equilibrium point (example 3).

393  $\phi$

394  $\delta$



395  
 396 **Fig. 11 Variation of the rotation (A), normal displacement (B), shear displacement (C),**  
 397 **bending moment (D), normal force (E) and shear force (F) for the two considered types of**  
 398 **SC and two assumed velocities of advance (Va) of the tunnel face, with reference to the**  
 399 **final equilibrium point (example 4).**

400 Even for these two examples, higher stress characteristics are observed for SC with higher  
 401 stiffness during the concrete setting time and lower face advance rates. Major changes in terms  
 402 of percentage occur among the four cases analyzed for the smaller tunnel, compared to the  
 403 larger tunnel example.

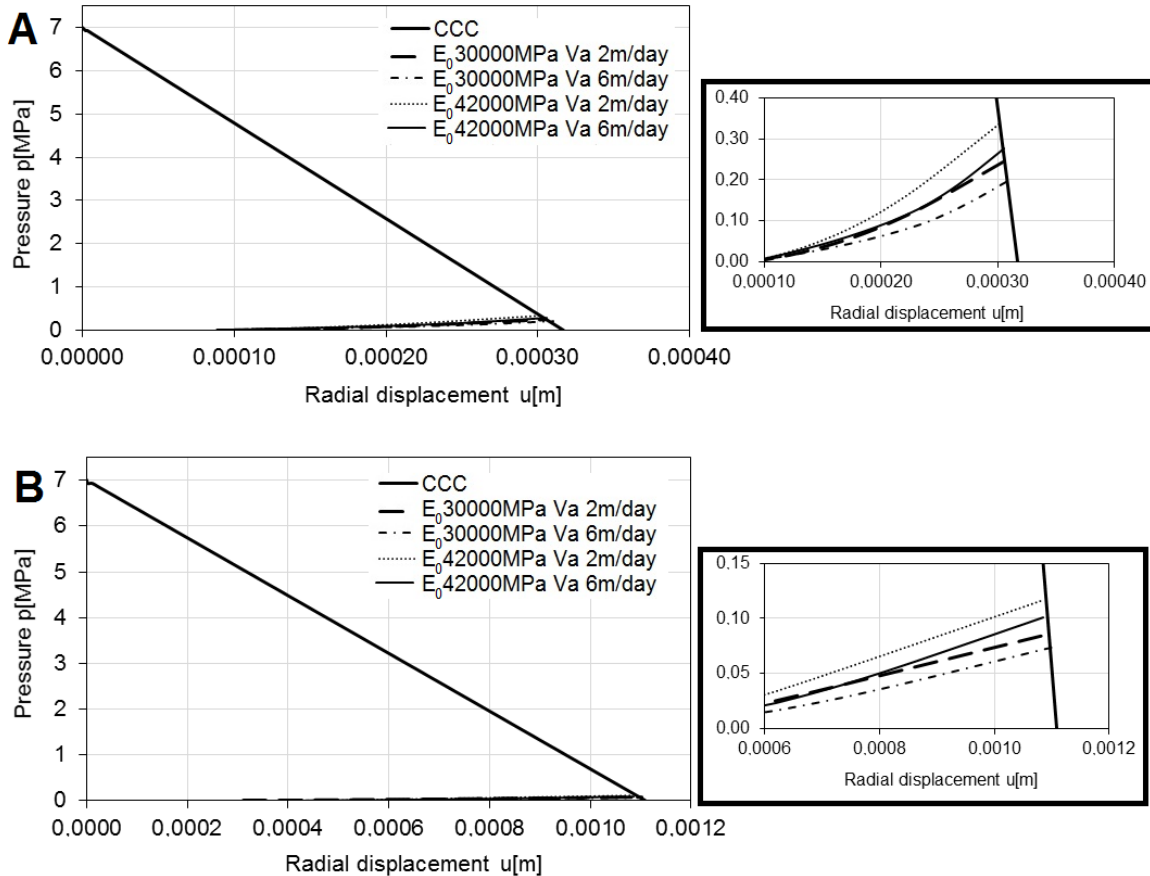
404 Examples 5 and 6 refer to two tunnels of radius 2m and 7m, respectively, excavated in a rock  
 405 mass with the same characteristics. The rock in these two examples, unlike the previous two, is a  
 406 rock mass of good mechanical properties corresponding to **RMR = 80**. The geomechanical  
 407 parameters are listed in Tab. 4.

408 The lithostatic pressure  $p_0$  is assumed to be 7MPa, the SC lining has a thickness of 20cm and  $K_0$   
 409 is equal to 0.5 for both examples. The daily advance rates and the SC types implemented in the  
 410 support of these two examples are assumed to be the same types as in examples 3 and 4. The  
 411 reaction lines of the SC lining in conjunction with the CCCs are shown in Fig. 12.

Rock Mass Parameters	
Elastic modulus [MPa]	57500
Poisson's ratio	0.30
Peak cohesion [MPa]	3.75
Residual cohesion [MPa]	3.75
Peak angle of friction [°]	42
Residual angle of friction [°]	42
Dilatancy [°]	16

412  
413

**Table 4. Geomechanical parameters of the rock mass in the example 5 and 6.**

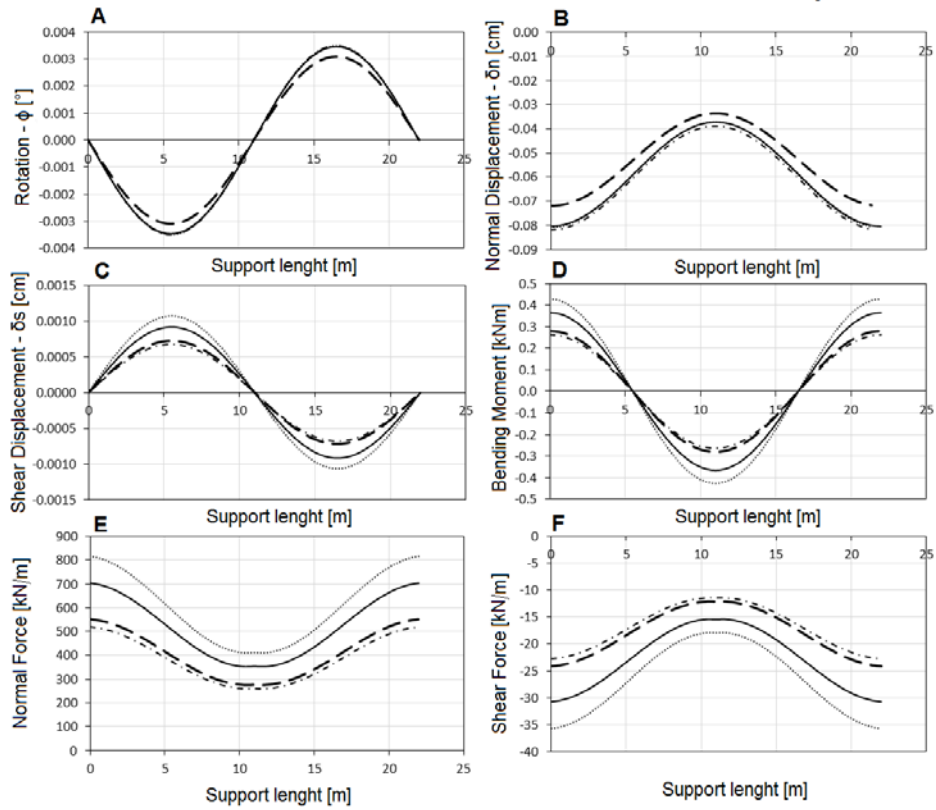


414

415 **Fig. 12 CCCs of the tunnel and reaction lines of the shotcrete lining (with enlargement on**  
416 **the right side) as a function of the face velocity of advance ( $V_a$ ) and the shotcrete types for**  
417 **the example 5 (A) and 6 (B).**

418 The stress characteristics ( $M$ ,  $N$  and  $F$ ) to determine the stress state in the lining and the more  
419 important displacements of the SC lining are shown in the Figs. 13 and 14.

—  $E_0=30000\text{MPa}$   $V_a$  2m/day    - - -  $E_0=30000\text{MPa}$   $V_a$  6m/day    .....  $E_0=42000\text{MPa}$   $V_a$  2m/day    —  $E_0=42000\text{MPa}$   $V_a$  6m/day

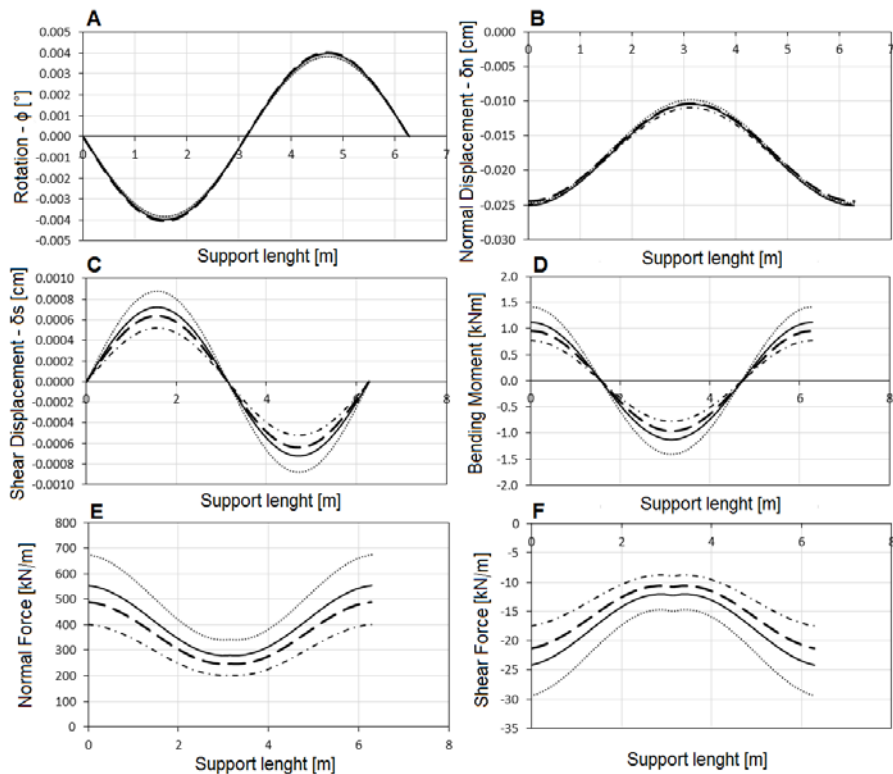


420

421 **Fig. 13** Variation of the rotation (A), normal displacement (B), shear displacement (C),  
 422 bending moment (D), normal force (E) and shear force (F) for the two considered types of  
 423 SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the  
 424 final equilibrium point (example 5).

425

—  $E_0$  30000MPa  $V_a$  2m/day    - - -  $E_0$  30000MPa  $V_a$  6m/day    .....  $E_0$  42000MPa  $V_a$  2m/day    —  $E_0$  42000MPa  $V_a$  6m/day



426

427 **Fig. 14 Variation of the rotation (A), normal displacement (B), shear displacement (C),**  
 428 **bending moment (D), normal force (E) and shear force (F) for the two considered types of**  
 429 **SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the**  
 430 **final equilibrium point (example 6).**

431 In high-quality rock masses, such as those for example 5 and 6, the final load on the lining is of  
 432 low magnitude. In fact, the intersection between the CCC and the RLSL is for low pressure  
 433 values. In the example 6 ( $R = 7m$ ) there are no noticeable differences in the RLSL performance  
 434 for the four examined cases, but there are some differences in example 5 ( $R = 2m$ ).

435 On the other hand, the differences between the bending moments and the forces that develop  
 436 inside the lining are more pronounced. The same considerations done previously are also here  
 437 valid. In percentage terms, the variations found in the four examined cases are higher for  
 438 example 5 ( $R = 2m$ ) than for example 6 ( $R = 7m$ ). In addition, for  $R = 7m$  and final elastic  
 439 modulus of SC of 30GPa (lower stiffness between the two types of concrete used), the advance  
 440 rate appears to have a minor influence on the trend of bending moments, normal and shear  
 441 forces developed in the lining.

442 **CONCLUSIONS**

443 The sprayed concrete (shotcrete) linings represent one of the most popular tunnel supporting  
444 works. Its operating mechanism is quite complex due to the installation method, the particular  
445 load application phase and the SC curing with the consequent modification of the mechanical  
446 properties of the SC over time. Precisely because of the complexity of the operation of this  
447 support work, it is difficult to analyze the behavior and to evaluate its static conditions. The three-  
448 dimensional numerical analysis, able to consider all the complex aspects of the operating  
449 mechanism, requires very long calculation times.

450 In this article, after highlighting the fundamental characteristics of the SC, a new calculation  
451 procedure based on the combined use of two widely used calculation methods for tunnel linings  
452 was introduced: the Convergence-Confinement Method (CCM) and the Hyperstatic Reaction  
453 Method (HRM).

454 The former, thanks to the evaluation of the sprayed concrete reaction line (RLSL) and the  
455 intersection of the Convergence Containment Curve (CCC), allows obtaining the final load on the  
456 support and the evolution of the load with the progress of the curing phase of the SC. The latter,  
457 based on the results obtained with the former, allows determining the mechanical behavior of the  
458 lining and the interaction with the tunnel wall with the progress of the applied load and the  
459 development of mechanical parameters of the SC over time.

460 The interesting result is the trend of bending moments, normal and shear forces, and  
461 displacement along the lining circumference during the transient loading phase and in the final  
462 load condition.

463 From the stress characteristics, it is possible to assess the stress state in the SC and the safety  
464 factors of the lining against compression or traction failure in the SC. Note that the safety factors  
465 allow to correctly design the lining, defining in particular the average of the tunnel lining thickness.

466 The calculation procedure was then applied to examples, differentiated by the tunnel geometry  
467 and the geomechanical quality of the surrounding rock mass. For each example, four different  
468 cases were considered, taking into account two different types of SC and two different advance  
469 rates of the tunnel excavation face. From the results, it was possible to develop useful  
470 considerations on the parameters that mostly influence the mechanical behavior of the lining.

471 Thanks to the fact that the model is able to appropriately consider the evolution of the mechanical  
472 properties of SC over time and the advance rate of the excavation face, it is a useful tool for  
473 selecting two key parameters in a tunnel design, as the type of SC and the thickness of the lining.

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539

540 **FIGURE CAPTION**

541 **Fig. 1 Spraying the tunnel roof with the shotcrete spraying machine (picture courtesy**  
542 **Roland Mayr, BASF)**

543 **Fig. 2: Convergence-confinement method: Geometry of the problem and example of a**  
544 **convergence-confinement curve. Key:  $p$ : Internal tunnel pressure,  $R$ : Tunnel radius,  $r$ :**  
545 **Radial coordinate,  $u$ : Radial displacement of the tunnel wall,  $p_{cr}$ : Critical pressure**  
546 **(modified by Oreste, 2009).**

547 **Fig. 3 Convergence-confinement curve and reaction curve of the shotcrete lining with**  
548 **numerical integration of the reaction curve of the shotcrete lining and a calculation step. **A****  
549 **is the interaction between reaction line and CCC to identify the final load process. Not to**  
550 **scale.**

551 **Fig. 4 Progressive increase of the asymptotic elastic modulus (A) and UCS (B) of the**  
552 **shotcrete with time for the two considered typologies in the example 1.**

553 **Fig. 5 Reaction curves of the SC lining as a function of the face advance rate ( $V_a$ ) and the**  
554 **mechanical characteristics of the shotcrete for the example 1.**

555 **Fig. 6 Variation of the rotation (A), normal displacement (B), shear displacement (C),**  
556 **bending moment (D), normal force (E) and shear force (F) for the two considered type of**  
557 **SC and two assumed advance rates ( $V_a$ ) of the tunnel face, with reference to the final**  
558 **equilibrium point (example 1).**

559 **Fig. 7 Reaction curve of the shotcrete lining (with enlargement on the right side) as a**  
560 **function of the face advance rate ( $V_a$ ) and the shotcrete type considered in the example 2.**

561 **Fig. 8 Variation of the rotation (A), normal displacement (B), shear displacement (C),**  
562 **bending moment (D), normal force (E) and shear force (F) for the two considered types of**  
563 **SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the**  
564 **final equilibrium point (example 2).**

565 **Fig. 9 CCCs and reaction curve of the shotcrete lining (with enlargement on the right side)**  
566 **as a function of the velocity of advance ( $V_a$ ) and the final elastic modulus of the shotcrete,**  
567 **for example 3 (A) and example 4 (B).**

568 **Fig. 10** Variation of the rotation (A), normal displacement (B), shear displacement (C),  
569 bending moment (D), normal force (E) and shear force (F) for two considered types of SC  
570 and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the final  
571 equilibrium point (example 3).

572 **Fig. 11** Variation of the rotation (A), normal displacement (B), shear displacement (C),  
573 bending moment (D), normal force (E) and shear force (F) for the two considered types of  
574 SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the  
575 final equilibrium point (example 4).

576 **Fig. 12** CCCs of the tunnel and reaction lines of the shotcrete lining (with enlargement on  
577 the right side) as a function of the face velocity of advance ( $V_a$ ) and the shotcrete types for  
578 the example 5 (A) and 6 (B).

579 **Fig. 13** Variation of the rotation (A), normal displacement (B), shear displacement (C),  
580 bending moment (D), normal force (E) and shear force (F) for the two considered types of  
581 SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the  
582 final equilibrium point (example 5).

583 **Fig. 14** Variation of the rotation (A), normal displacement (B), shear displacement (C),  
584 bending moment (D), normal force (E) and shear force (F) for the two considered types of  
585 SC and two assumed velocities of advance ( $V_a$ ) of the tunnel face, with reference to the  
586 final equilibrium point (example 6).